

15 Bubble Sort

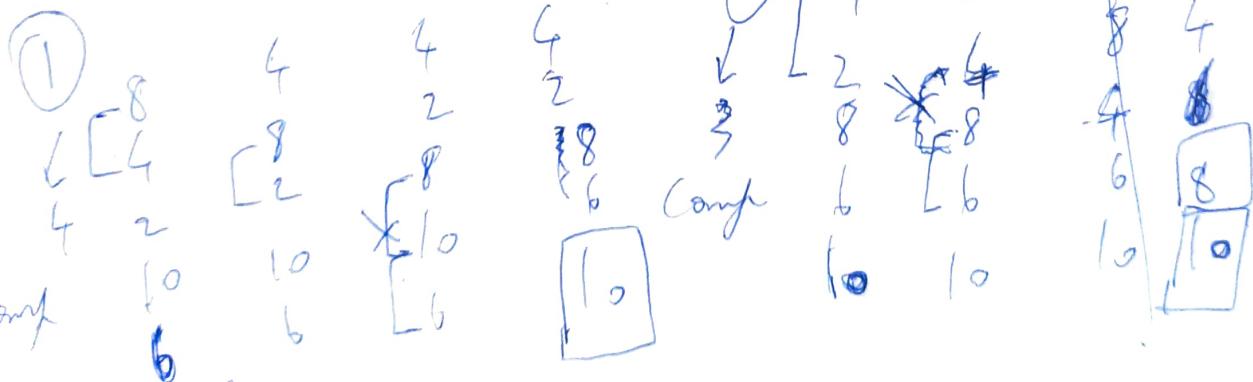
①

→ Popular Sorting Technique based on Brute Force Technique (Simplest)

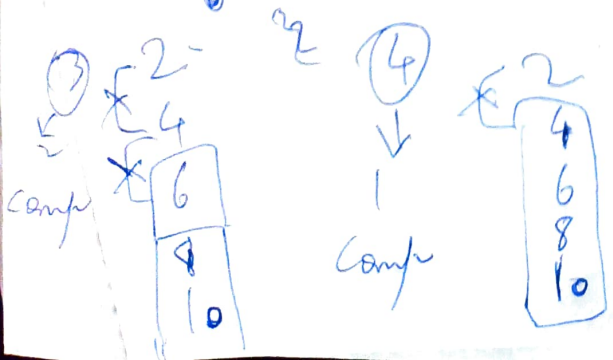
→ Brute Force is a straight forward approach to solve a problem. It is ~~usually~~ based on the problem statement and the definitions of the concept involved.

→ In Bubble Sort, we compare the adjacent elements of the list and exchange them (if required). By doing it repeatedly, we end up ~~the~~ bubbling up the largest element to the last position. In the next iteration, the second largest element bubbles up & so on ~~the~~ until, after $n-1$ iterations, the list is sorted.

8 4 2 10 6 ($n=5$)



For 5 elements,
 $4 + 3 + 2 + 1 = 10$



Algorithm BubbleSort($A[0 \dots n-1]$)

// Sorts a given array by bubble sort

// Input: An array $A[0 \dots n-1]$

// Output: Sorted array $A[0 \dots n-1]$ in ascending order

for $i \leftarrow 0$ to $n-2$ do // no. of iteration

for $j \leftarrow 0$ to $n-2-i$ do

if $(A[j] > A[j+1])$

swap($A[j]$ and $A[j+1]$)

Time complexity

Basic operation \rightarrow Comparison

Let $C(n)$ denotes the Total no. of comparison made for an input size n

$$C(n) = \sum_{i=0}^{n-2} \sum_{j=0}^{n-2-i} 1 = \sum_{i=0}^{n-2} (n-2-i+1)$$

$$= \sum_{i=0}^{n-2} (n-i-1) = (n-1) + (n-2) + \dots + 1$$

$$= \frac{n(n-1)}{2} = n^2 - n = \boxed{n^2}$$

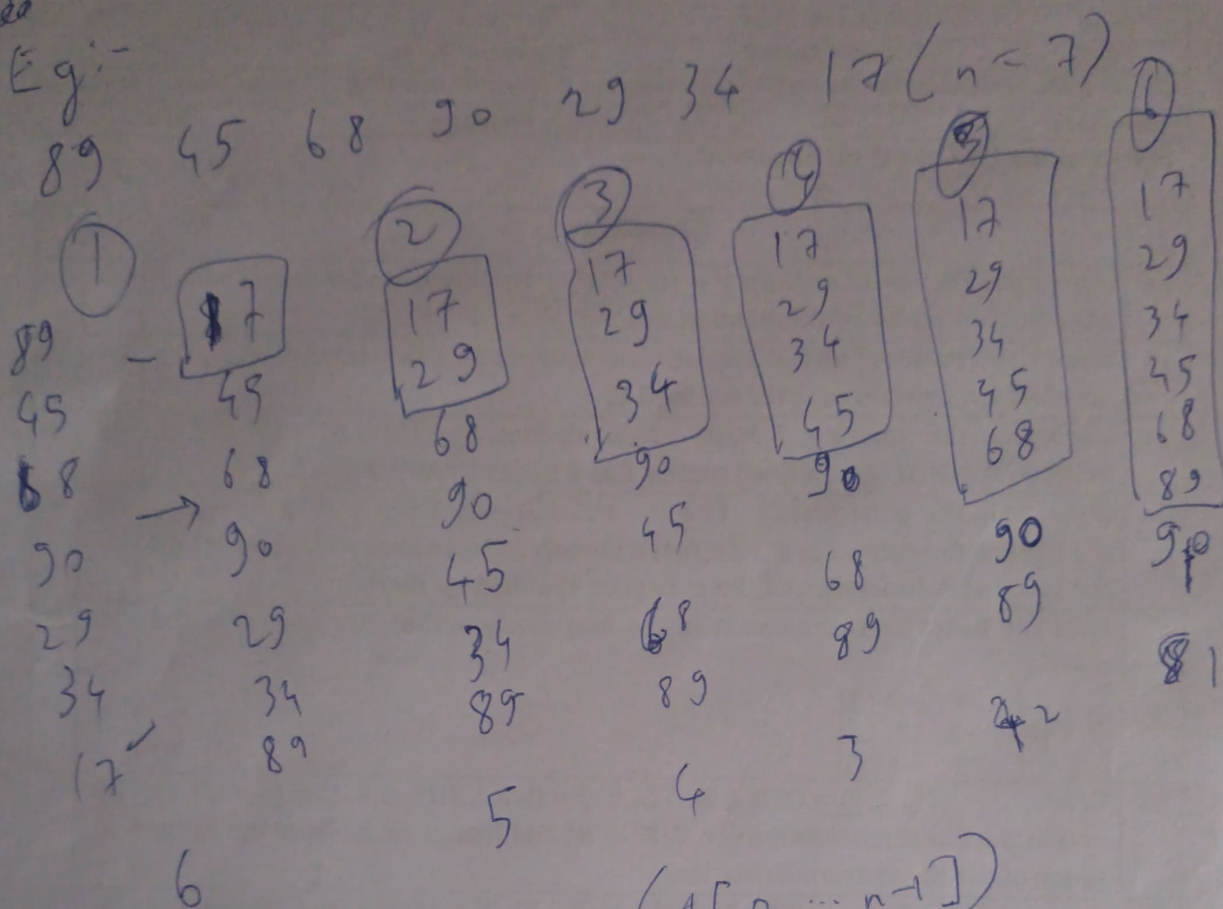
1b) Selection Sort

\rightarrow Selection sort is also based on Brute-Force

\rightarrow In Selection Sort, we scan the entire list to find the smallest element & exchange it with the first element. In the next iteration, we scan the list again from second element to find the smallest among $n-1$ elements and exchange it with second element and so on until

we are left with only one element.
 → For n elements, the no. of iterations is $n-1$. (3)

Eg:-



Algorithm Selection Sort ($A[0 \dots n-1]$)
 // Sorts a given array by selection sort
 // Input: an array $A[0 \dots n-1]$
 // Output: A sorted array $A[0 \dots n-1]$
 for $i \leftarrow 0$ to $n-2$ do // no. of iterations
 ~~min~~ $\min \leftarrow i$
 for $j \leftarrow i+1$ to $n-1$ do
 if $A[j] < A[\min]$
 $\min \leftarrow j$
 swap($A[i]$ and $A[\min]$)

Time complexity
 Input size = n

Basic operation = Comparison

(4)

Let $C(n)$ denotes the total no. of comparisons

$$C(n) = \sum_{i=0}^{n-2} \sum_{j=i+1}^{n-1} 1$$

$$= \sum_{i=0}^{n-2} n-1-i$$

$$= \sum_{i=0}^{n-2} n-1-i = \frac{n(n-1)}{2} = \frac{n^2 - n}{2} = \frac{n(n-1)}{2}$$