Clustering Techniques

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Earning is in Learning
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Agenda

R Setup
Clustering Overview
Hierarchical Clustering
Non-Hierarchical Clustering

Python Setup for Clustering

- Python 3.2.3 or higher version should be installed
- Following Libraries are installed. Check by running the below command ## it is okay if you get Warning Message, but you should not get Error Message
 sklearn

seaborn

matplotlib



Intro: Data – Information – Knowledge – Wisdom (DIKW)

Where is the Life... we have lost in Living?
Where is the wisdom... we have lost in Knowledge?
Where is the Knowledge...we have lost in Information?
- T.S. Eliot

Where is the Information... we have lost in Data?

In order to go from

Data to Information to Knowledge and to Wisdom

We need to simplify Data

How do we simplify data

- Simplify data equals to eliminating data complexity
 - too many variables to a few variables
 - too many records to a few records

- Dimension Reduction
 - Reduce number of variable by using techniques like Principal Component Analysis, Collinearity Check, Business Rule Based, etc

Clustering / Segmentation

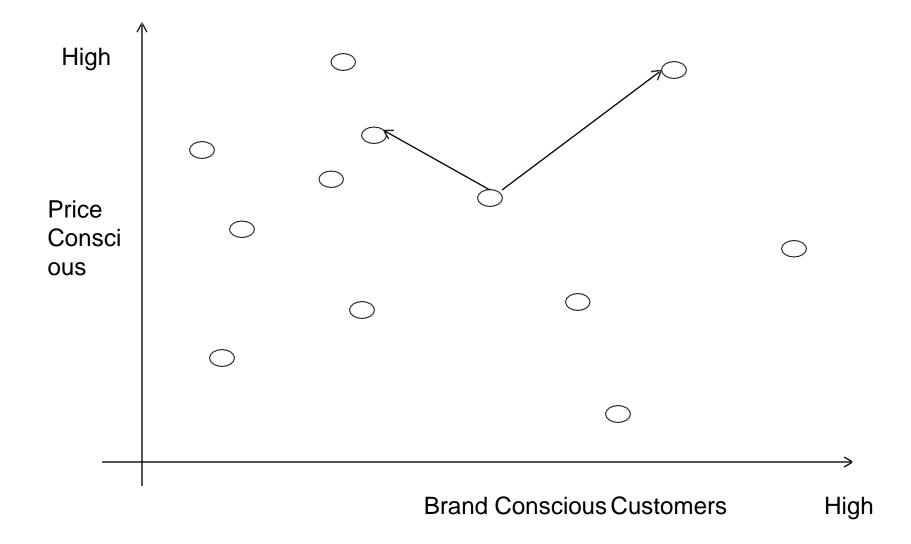
- Case reduction
- Reduce the number of records by identifying similar groups and representing them as a cluster

Our focus area in this presentation

Clustering

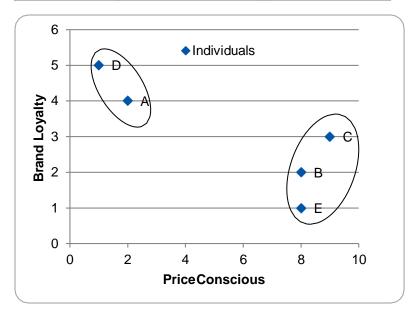
- Clustering is a technique for finding similar groups in data, called clusters.
- It groups data instances that are similar to (near) each other in one cluster and data instances that are very different (far away) from each other into different clusters.
- A cluster is therefore a collection of objects which are "similar" between them and are "dissimilar" to the objects belonging to other clusters
- How do we define "Similar" in clustering?

Note: Clustering is an unsupervised learning technique



Simple Clustering e.g.

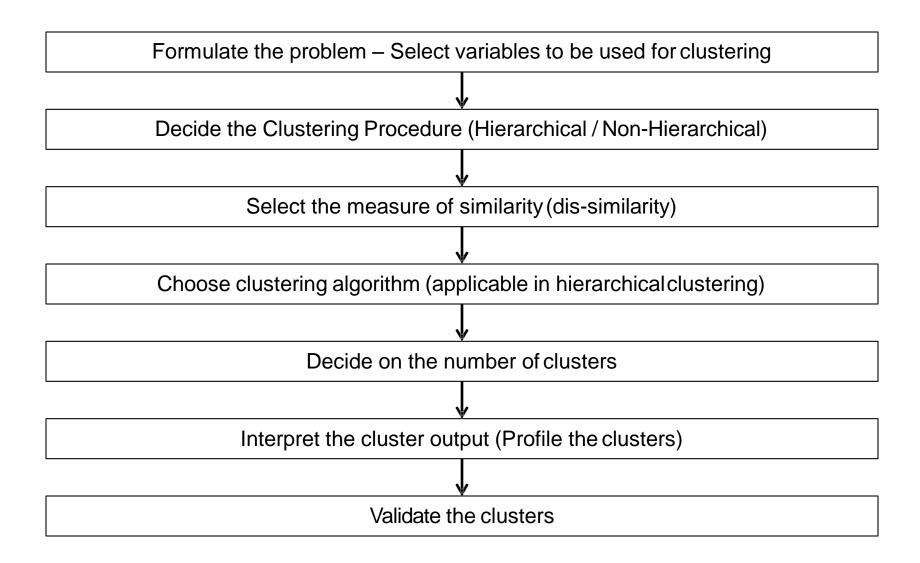
Individuals	Price Conscious	Brand Loyalty
Α	2	4
В	8	2
С	9	3
D	1	5
E	8	1



- From Scatter Plot we can see that
 - A & D form one segment of customers who are very high on Brand Loyalty
 - B, C, & E is another segment which is very Price Conscious

Note: The above e.g. is just an hypothetical data to introduce the subject of clustering. It is not related to the below url: http://globalbizresearch.org/chennai_conference/pdf/pdf/ID_C405_Formatted.pdf

Steps involved in Clustering Analysis



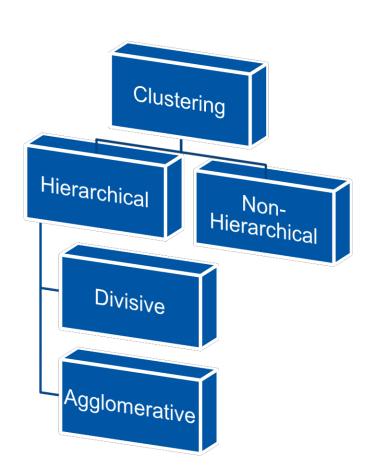
Formulate the clustering problem

- Formulate the problem
 - understand the business problem
 - hypothesize variables that will help solve the clustering problem at hand

- Applications of Clustering Technique
 - Store Clustering
 - Customer Clustering
 - Village Affluency Categorization

Note: It is preferable to do Factor Analysis / Principal Component Analysis before clustering

Decide the clustering procedure



- Types of Clustering Procedures
 - Hierarchical Clustering
 - Non-Hierarchical Clustering
- Hierarchical clustering is characterized by a tree like structure and uses distance as a measure of (dis)similarity

 Non-hierarchical clustering techniques uses partitioning methods and within cluster variance as a measure to form homogeneous groups

Hierarchical Vs. Non-Hierarchical clustering

Hierarchical Clustering

- Relatively very slower
- Agglomerative clustering is most used algorithm
- Uses distance as a measure for (dis)similarity
- Helps suggest optimal numbers of clusters in data.
- Object assigned to a cluster remains in that cluster

Non-Hierarchical Clustering

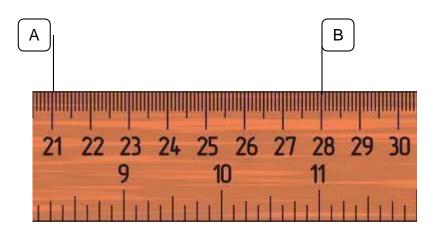
- Fast and preferable to use with large datasets
- K-means is a very popular nonhierarchical clustering technique
- Uses within cluster variance as a measure of similarity
- Non-hierarchical clustering require number of clusters as an input parameter for starting
- Objects can be reassigned to other clusters during the clusteringprocess



Hierarchical Clustering - (dis)similarity measure

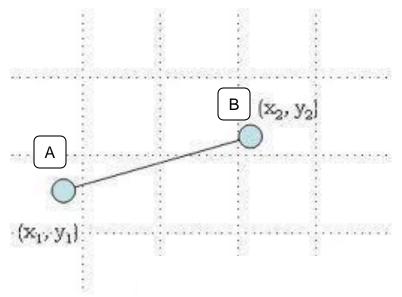
- Hierarchical Clustering is based on dis(similarity)
 measure
- Most software package calculate a measure of dissimilarity by estimating the distance between pair of objects
- Objects with shorter distance are considered similar, whereas objects with larger distance are dissimilar
- Measures of similarity
 - Euclidean distance (most commonly used)
 - City Block or Manhattan distance
 - Chebyshev distance

Distance Computation



What is the distance between Point A and B?

Ans: 7

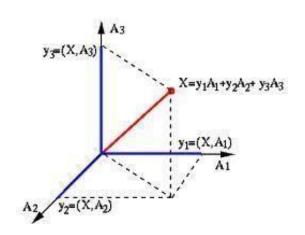


What is the distance between Point A and B?

Ans:
$$\sqrt{[(x^2-x^1)^2+(y^2-y^1)^2]}$$

(Remember the Pythagoras Theorem)

Distance Computation Contd...



What is the distance between Point A and B in n-Dimension Space?

- If A (a₁, a₂, ... a_n) and B (b₁, b₂, ... b_n) are cartesian coordinates
- By using Euclidean Distance (which is an extension of Pythagoras Theorem), we get Distance AB as
- $D_{AB} = \sqrt{[(a_1-b_1)^2 + (a_2-b_2)^2 + + (a_n-b_n)^2]}$

Chebyshev Distance

- In mathematics, Chebyshev distance is a metric defined on a vector space where the distance between two vectors is the greatest of their differences along any coordinate dimension
- Assume two vectors: A $(a_1, a_2, ... a_n)$ & B $(b_1, b_2, ... b_n)$
- Chebyshev Distance

$$= Max (|a_1 - b_1|, |a_2 - b_2|, |a_n - b_n|)$$

 Application: Survey / Research Data where the responses are Ordinal

Manhattan Distance

- Manhattan Distance also called City Block Distance
- Assume two vectors: A (x1, x2, ...xn) & B (y1, y2,...yn)
- Manhattan Distance

$$= |a_1 - b_1| + |a_2 - b_2| + \dots |a_n - b_n|$$



Block

Manhattan Distance = 8 + 4 = 12

Block

Chebyshev Distance = Max(8, 4) = 8

Block

Eucledian Distance = $sqrt(8^2 + 4^2) = 8.94$

Block

Block

Block

Block

Block

Block

Block

Block

В

Hierarchical Clustering | Agglomerative Clustering

Step

Step

 Starts with each record as a cluster of one record each

 Sequentially merges 2 closest records by distance as a measure of (dis)similarity to form a cluster. This reduces the number of records by 1

0 1 2 3 4

a b c de

c d e

d d e

Step

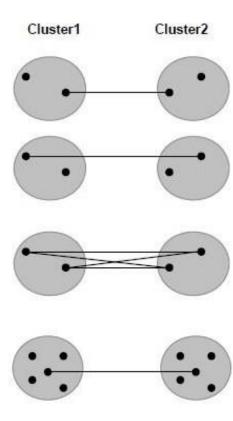
Step

Step

 Repeat the above step with new cluster and all remaining clusters till we have one big cluster How do you measure the distance between cluster (a,b) and (c) or the cluster (a,b) and (d,e) ????

Agglomerative Clustering Procedures

- Single linkage Minimum distance or Nearest neighbour rule
- Complete linkage Maximum distance or Farthest distance
- Average linkage Average of the distances between all pairs
- Centroid method combine cluster with minimum distance between the centroids of the two clusters
- Ward's method Combineclusters with which the increase in within cluster variance is to the smallest degree







http://sites.stat.psu.edu/~ajw13/stat505/fa06/19_cluster/09_cluster_wards.html

Clustering e.g. 1 : Clustering for Retail Customers

Let us find the clusters in given Retail Customer Spends data

We will use Hierarchical Clustering technique

Let us first set the working directory path and import the data

RCDF <- pd.read_csv("datafiles/Cust_Spend_Data.csv", header=TRUE) View(RCDF)

Cust_ID [‡]	Name [‡]	Avg_Mthly_Spend [‡]	No_Of_Visits $^{\diamondsuit}$	Apparel_Items [‡]	FnV_Items [‡]	Staples_Items †
1	Α	10000	2	1	1	0
2	В	7000	3	0	10	9
3	С	7000	7	1	3	4
4	D	6500	5	1	1	4
5	E	6000	6	0	12	3
6	F	4000	3	0	1	8
7	G	2500	5	0	11	2
8	н	2500	3	0	1	1
9	I	2000	2	0	2	2
10	J	1000	4	0	1	7

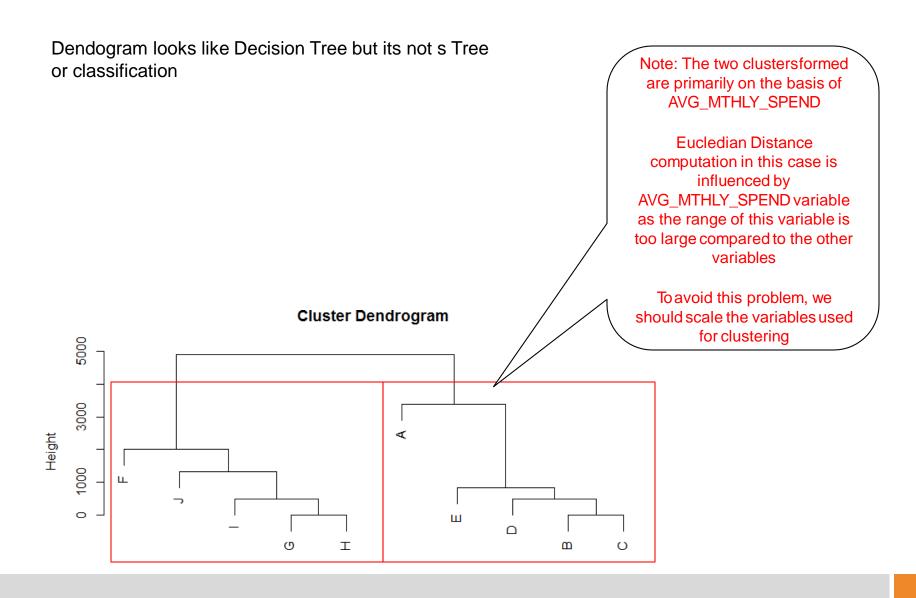
<u>HyperMarket Customer Spend</u> <u>Data - Metatdata</u>

AVG_Mthly_Spend: The average monthly amount spent by customer

No_of_Visits: The number of times a customer visited the HyperMarketi

Count of **Apparel**, **Fruits and Vegetable**, **Staple Items** purchased in a month

Building the hierarchical clusters (without variable scaling)

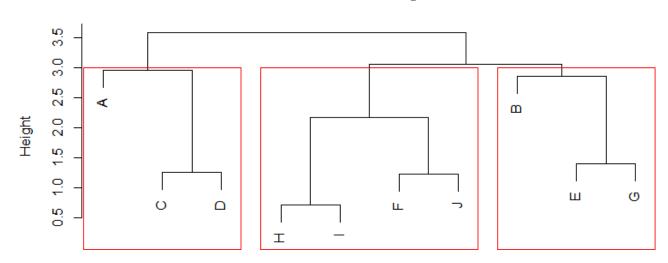


Building the hierarchical clusters (with variable scaling)

scale function standardizes the values

Scaling of features can change the shape and sizes of the clusters. It can even generate various numbers of clusters.

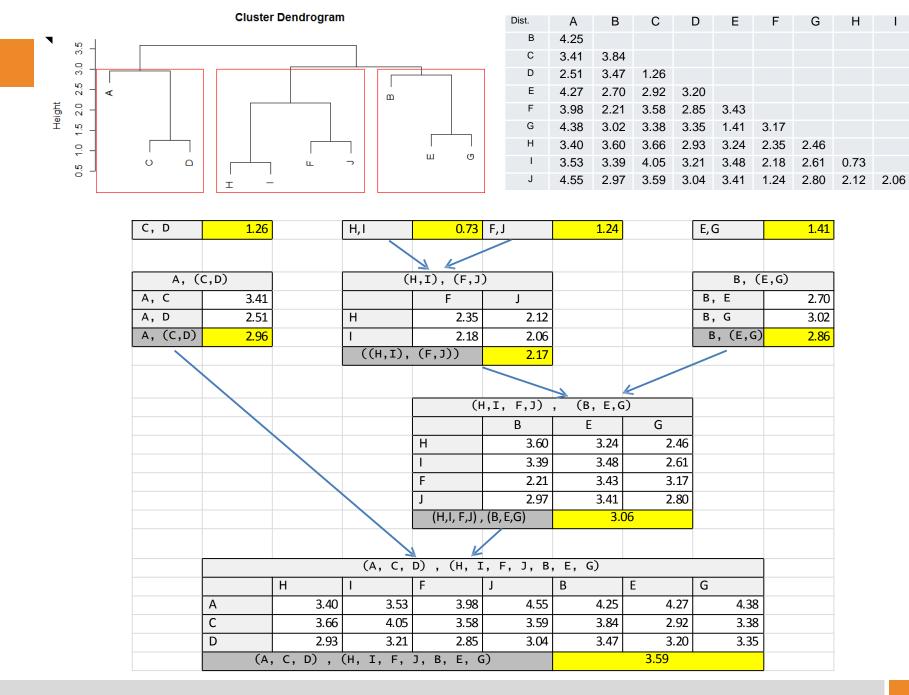
Cluster Dendrogram



Understanding the Height Calculation in Clustering

Let us see the distance matrix

Dist.	Α	В	С	D	E	F	G	Н	1
В	4.25								
С	3.41	3.84							
D	2.51	3.47	1.26						
Е	4.27	2.70	2.92	3.20					
F	3.98	2.21	3.58	2.85	3.43				
G	4.38	3.02	3.38	3.35	1.41	3.17			
Н	3.40	3.60	3.66	2.93	3.24	2.35	2.46		
I	3.53	3.39	4.05	3.21	3.48	2.18	2.61	0.73	
J	4.55	2.97	3.59	3.04	3.41	1.24	2.80	2.12	2.06



Profiling the clusters

profiling the clusters

Profiling of clusters means the aggregation of the patterns identified within the each cluster.

Also, The characteristics of the clusters

Cluster [‡]	Freq	÷	Avg_Mthly_Spend $^{\diamondsuit}$	No_Of_Visits $^{\Diamond}$	Apparel_Items $^{\oplus}$	FnV_Items [‡]	Staples_Items
1		3	7833.333	4.666667	1	1.666667	2.666667
2		3	5166.667	4.666667	0	11.000000	4.666667
3		4	2375.000	3.000000	0	1.250000	4.500000

Non-Hierarchical Clustering (K Means)

K Means Clustering

 K-Means is the most used, non-hierarchical clustering technique

It is not based on Distance...

It is based on within cluster Variation, in other words
 Squared Distance from the Centre of the Cluster

 The algorithm aims at segmenting data such that within cluster variation is reduced

K Means Algorithm

Input Required : No of Clusters to be formed. (Say K)

Steps

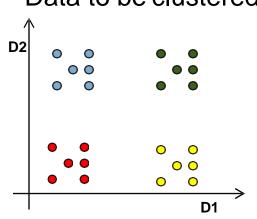
- Assume K Centroids (for K Clusters)
- 2. Compute Eucledian distance of each objects with these Centroids.
- 3. Assign the objects to clusters with shortest distance
- 4. Compute the new centroid (mean) of each cluster based on the objects assigned to each clusters. The K number of means obtained will become the new centroids for each cluster
- 5. Repeat step 2 to 4 till there is convergence
 - i.e. there is no movement of objects from one cluster to another
 - Or threshold number of iterations have occurred

K-means advantages

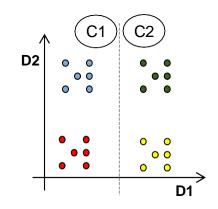
- K-means is superior technique compared to Hierarchical technique as it is less impacted by outliers
- Computationally it is more faster compared to Hierarchical
- Preferable to use on interval or ratio-scaled data as it uses Eucledian distance... desirable to avoid using on ordinal data
- Challenge Number of clusters are to be pre-defined and to be provided as input to the process

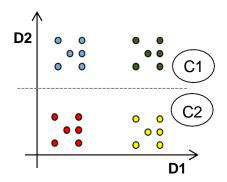
Why find optimal No. of Clusters?

Data to be clustered

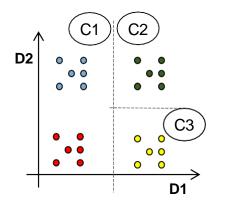


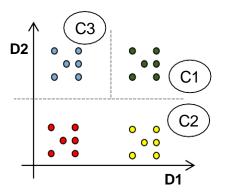
■ Two Clusters – 2 possible solution

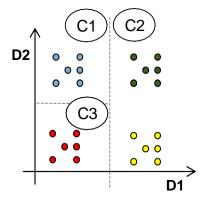


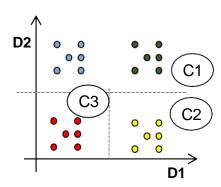


Three Clusters – Multiple possible solution







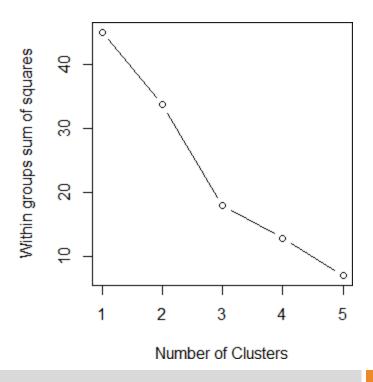


Optimal No. of Clusters

WSS Plot or Within Sum of Square Error Plot is used to identify the optimal number of clusters.

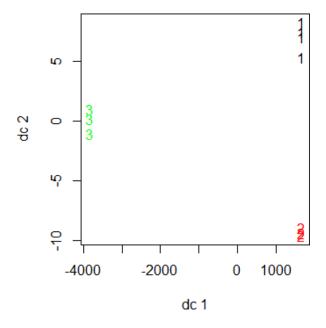
WSS plot is also called as Scree Plot or Elbow Curve within the Analytics Industry.

Elbow in the graph represents the optimal value of the clusters.



Plotting the clusters

plotting the clusters



More better plot

CLUSPLOT(scaled.RCDF)

Profiling the clusters

Cluster [‡]	Freq	#	Avg_Mthly_Spend $^{\diamondsuit}$	No_Of_Visits	Apparel_Items $^{\circ}$	FnV_Items [‡]	Staples_Items $^{\scriptsize \oplus}$
1		4	2375.000	3.000000	0	1.250000	4.500000
2		3	7833.333	4.666667	1	1.666667	2.666667
3		3	5166.667	4.666667	0	11.000000	4.666667

Next steps after clustering

- Clustering provides you with clusters in the given dataset
- Clustering does not provide you rules to classify future records
- To be able to classify future records you may do the following
 - Build Discriminant Model on Clustered Data
 - Build Classification Tree Model on Clustered Data

References

- Chapter 9 : Cluster Analysis (http://www.springer.com)
 - Google search: "www.springer.com_cluster analysis chapter 9"

Questions???

Thank you

Contact Us <u>kul.utkarsh1205@gmail.com</u>