Summary

December 6, 2024

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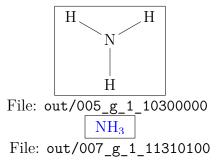
0.1 Loaded Graphs

$0.1.1 g_{0}$

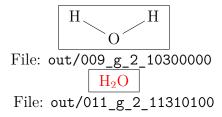
N C H
File: out/001_g_0_10300000

N CH
File: out/003_g_0_11310100

0.1.2 g_{1}

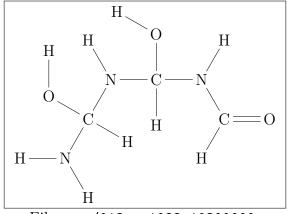


0.1.3 g_{2}

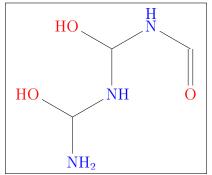


0.2 Product Graphs

0.2.1 p_{0,56}



File: out/013_g_1088_10300000



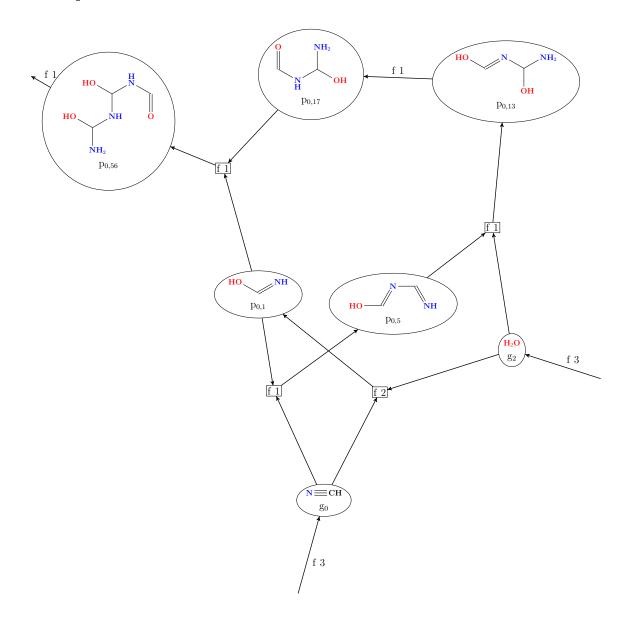
File: out/015_g_1088_11310100

0.3 Enumerated Flows

0.3.1 Solution 0

Overall Data

| Objective val | Lue | (non-integral): -0.113219 | | | | |
|---------------|-----|---------------------------|------------|----------|---------|--|
| Vertex/Graph | In | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | 1.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | 1.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | 0.000000 | 64 | |
| p_{0,17} | 0 | 0 | -21.248844 | 0.000000 | 65 | |
| p_{0,1} | 0 | 0 | -10.610080 | 1.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869324 | 0.000000 | 67 | |
| p_{0,5} | 0 | 0 | -16.158998 | 0.000000 | 63 | |



 $File: \ \mathtt{out/029_dg_0_11100_f_0_0_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | 0.0 | -42425.44262 | 63 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 0.0 | -55767.391129 | 64 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | 0.0 | -55788.832737 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 2 | -93.86065 | -93.86065 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -114.195398 | -114.195398 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -38.073396 | -38.073396 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56}$, | 1 | -29.574562 | -29.574562 |
| 250 | $p_{0,13}$, | $p_{0,17},$ | 1 | -21.441608 | -21.441608 |
| Sum | | | | | -297.25667549475185 |

 $\Delta G = -39.10062567680478$

 $\Delta E = -0.11321908829270522$

|E| = 6

 $|\mathbf{U}| = 5$

0.3.2 Solution 1

Overall Data

Objective value (non-integral): -0.113219 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068043 0.000000 0 p_{0,13} -21.240635 1.000000 3 0 0 0 $p_{0,15}$ -10.625174 0.000000 2 -10.610101 0.000000 1 $p_{0,1}$ 0 0 $p_{0,56}$ 0 1 -31.869324 0.000000 67 p_{0,5} 0 0 -16.158998 0.000000 2



 $File: \ \mathtt{out/040_dg_0_11100_f_0_1_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 0.0 | -13306.144961 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | 0.0 | -27856.817054 | 1 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | 0.0 | -42425.44262 | 2 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | 1.0 | -55763.953809 | 3 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 0.0 | -27896.389963 | 2 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 2 | -93.916364 | -93.916364 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -111.869837 | -111.869837 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -39.572909 | -39.572909 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -33.422164 | -33.422164 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56},$ | 1 | -11.499083 | -11.499083 |
| Sum | | | | | -297.2566754947565 |

 $\Delta G = -38.41967110185993$

 $\Delta E = -0.11321908829270699$

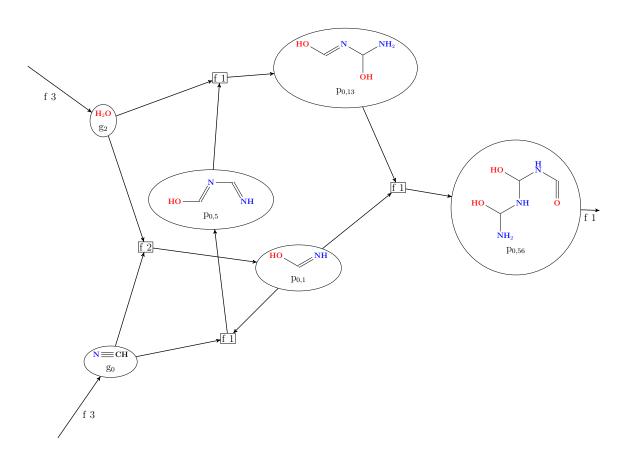
|E| = 6

|U| = 5

0.3.3 Solution 2

Overall Data

Objective value (non-integral): -0.113219 t_order Vertex/Graph In Out G logK 3 0 g_{0} -5.507152 1.000000 0 g_{2} 3 0 -5.068043 0.000000 0 p_{0,13} -21.240678 0.000000 65 0 0 p_{0,1} 0 0 -10.610101 1.000000 1 p_{0,56} -31.869324 0.000000 67 0 1 p_{0,5} -16.158998 1.000000 64 0 0



 $File: \verb"out/049_dg_0_11100_f_0_2_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 0.0 | -13306.144961 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | 1.0 | -27853.491269 | 1 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | 1.0 | -42422.116835 | 64 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 0.0 | -55767.391129 | 65 |
| $p_{0.56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 2 | -91.646516 | -91.646516 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -111.869837 | -111.869837 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -38.073396 | -38.073396 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56}$, | 1 | -50.960457 | -50.960457 |
| Sum | | | | | -297.25667549475463 |

 $\Delta G = -38.41967136440989$

 $\Delta E = \text{-}0.11321908829270627$

|E| = 5

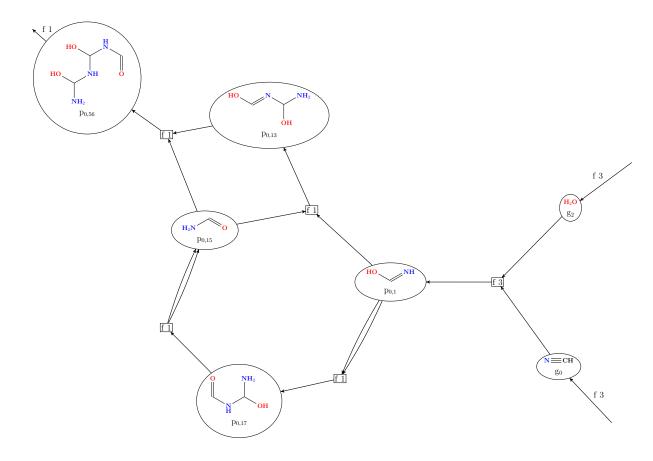
|U| = 4

0.3.4 Solution 3

Overall Data

| Objective val | Lue | (non-integral): -0.0774483 | | | | |
|---------------|-----|----------------------------|------------|----------|---------|--|
| Vertex/Graph | In | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | 1.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | 1.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | 1.000000 | 35 | |
| p_{0,15} | 0 | 0 | -10.625174 | 1.000000 | 31 | |
| p_{0,17} | 0 | 0 | -21.248887 | 0.307497 | 30 | |
| p_{0,1} | 0 | 0 | -10.610101 | 1.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869324 | 0.000000 | 67 | |

Filtered Graph



 $File: \ \mathtt{out/058_dg_0_11100_f_0_3_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|----------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | 1.0 | -27853.491269 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 1.0 | -55764.065344 | 35 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 1.0 | -27893.064178 | 31 |
| $p_{0,17}$ | 0 | 0 | -55788.944315 | 0.307497 | -55787.921644 | 30 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-----------------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -93.916364 | -93.916364 |
| 40 | $p_{0,1}, p_{0,1},$ | $p_{0,17},$ | 1 | -79.15193 | -79.15193 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56}$, | 1 | -13.657397 | -13.657397 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13}$, | 1 | -16.45396 | -16.45396 |
| 237 | $p_{0,17},$ | $p_{0,15}, p_{0,15},$ | 1 | 0.006113 | 0.006113 |
| Sum | | | | | -203.34049495278154 |

 $\Delta G = -39.100625414254814$

 $\Delta E = -0.07744830427516443$

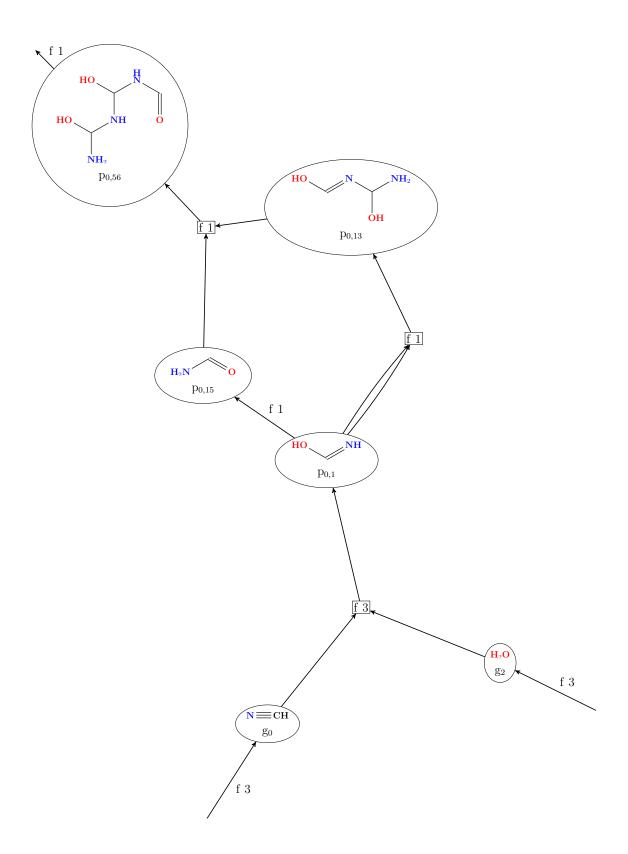
|E| = 7

 $|\mathbf{U}| = 5$

0.3.5 Solution 4

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G logK t order 3 0 g_{0} -5.507152 0.000000 0 g_{2} -5.068033 0.000000 0 3 0 p_{0,13} 0 0 -21.240678 0.000000 3 p_{0,15} 0 0 -10.625174 0.000000 2 $p_{0,1}$ -10.610101 1.000000 1 0 0 $p_{0,56}$ 0 1 -31.869260 1.000000 67



 $File: \ \mathtt{out/067_dg_0_11100_f_0_4_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | 0.0 | -14459.025578 | 0 |
| g_2 | 3 | 0 | -13306.118349 | 0.0 | -13306.118349 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | 1.0 | -27853.491269 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 0.0 | -55767.391129 | 3 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 0.0 | -27896.389963 | 2 |
| $p_{0,56}$ | 0 | 1 | -83672.731446 | 1.0 | -83669.405661 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -89.40328 | -89.40328 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -58.296717 | -58.296717 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -41.842757 | -41.842757 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56}$, | 1 | -6.680506 | -6.680506 |
| Sum | | | | | -203.34049495277878 |

 $\Delta G = \text{-}37.502980790785095$

 $\Delta E = \text{-}0.07744830427516337$

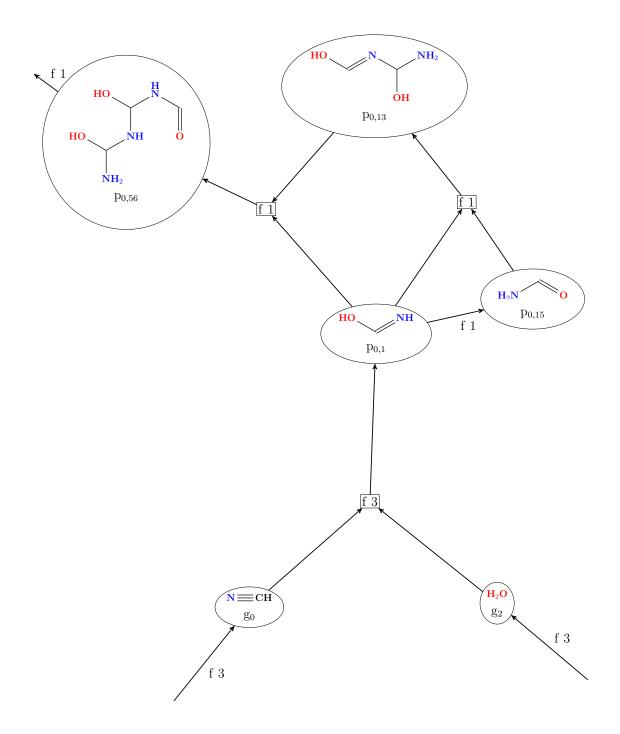
|E| = 6

|U| = 4

0.3.6 Solution 5

Overall Data

| Objective val | Lue | (nor | (non-integral): -0.0774483 | | | |
|---------------|-----|------|----------------------------|----------|---------|--|
| Vertex/Graph | In | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | 1.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | 1.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | 0.000000 | 35 | |
| p_{0,15} | 0 | 0 | -10.625174 | 0.000000 | 32 | |
| p_{0,1} | 0 | 0 | -10.610101 | 0.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869260 | 1.000000 | 67 | |



 $File: \verb"out/076_dg_0_11100_f_0_5_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | 0.0 | -27856.817054 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 0.0 | -55767.391129 | 35 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 0.0 | -27896.389963 | 32 |
| $p_{0,56}$ | 0 | 1 | -83672.731446 | 1.0 | -83669.405661 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -96.186212 | -96.186212 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -39.572909 | -39.572909 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | -14.184112 | -14.184112 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56}$, | 1 | -46.253415 | -46.253415 |
| Sum | | | | | -203.34049495277685 |

 $\Delta G = -38.856906321371056$

 $\Delta E = \text{-}0.07744830427516264$

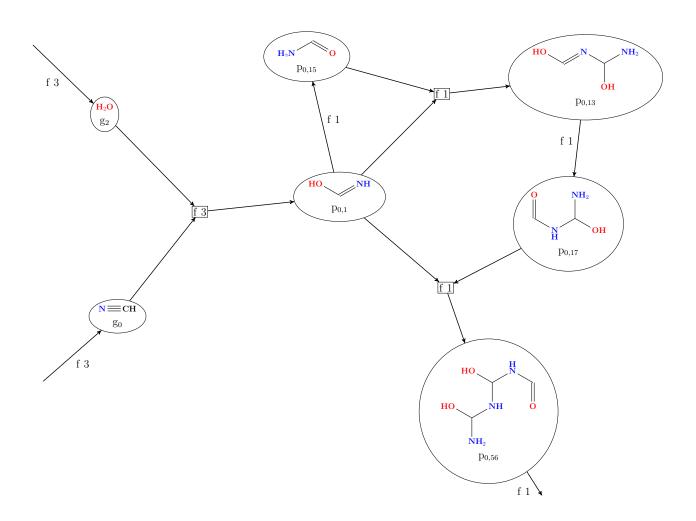
|E| = 6

|U| = 4

0.3.7 Solution 6

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068043 1.000000 20 $p_{0,13}$ 0 0 -21.240635 1.000000 44 -10.625195 0.000000 22 $p_{0,15}$ 0 0 $p_{0,17}$ -21.248887 1.000000 45 0 0 -10.610080 1.000000 21 $p_{0,1}$ 0 0 $p_{0,56}$ 0 1 -31.869324 0.000000 67



 $File: \verb"out/085_dg_0_11100_f_0_6_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 20 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 21 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | 1.0 | -55763.953809 | 44 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | 0.0 | -27896.445756 | 22 |
| $p_{0,17}$ | 0 | 0 | -55788.944315 | 1.0 | -55785.61853 | 45 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -93.86065 | -93.86065 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -41.954263 | -41.954263 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | -14.072498 | -14.072498 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56}$, | 1 | -31.732833 | -31.732833 |
| 250 | $p_{0,13},$ | $p_{0,17},$ | 1 | -21.664721 | -21.664721 |
| Sum | | | | | -203.34049495277685 |

 $\Delta G = \text{-}39.100625414254814$

 $\Delta E = \text{-}0.07744830427516264$

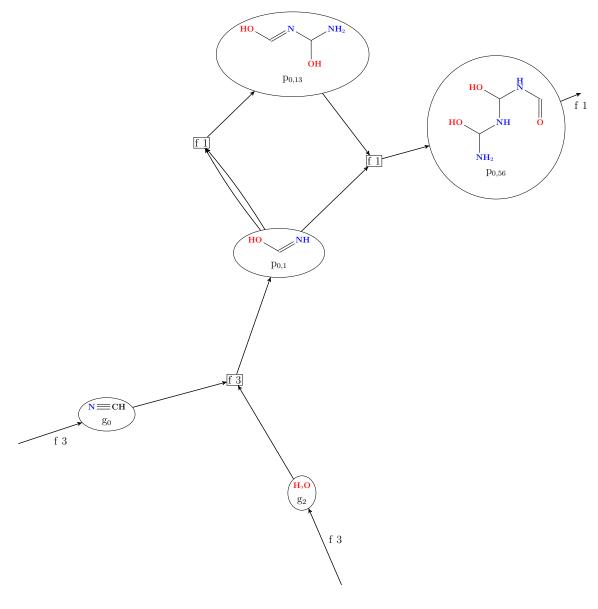
```
\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}
```

0.3.8 Solution 7

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 0.000000 0 g_{2} 3 0 -5.068033 0.000000 0 $p_{0,13}$ 0 0 -21.240635 1.000000 3 p_{0,1} 0 0 -10.610080 1.000000 1 0 1 -31.869324 0.000000 67 $p_{0,56}$

Filtered Graph



 $File: \verb"out/094_dg_0_11100_f_0_7_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | 0.0 | -14459.025578 | 0 |
| g_2 | 3 | 0 | -13306.118349 | 0.0 | -13306.118349 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | 1.0 | -55763.953809 | 3 |
| $p_{0.56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -89.347566 | -89.347566 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -56.026761 | -56.026761 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56},$ | 1 | -53.397553 | -53.397553 |
| Sum | | | | | -203.34049495277685 |

 $\Delta G = -37.74670067131874$

 $\Delta E = -0.07744830427516264$

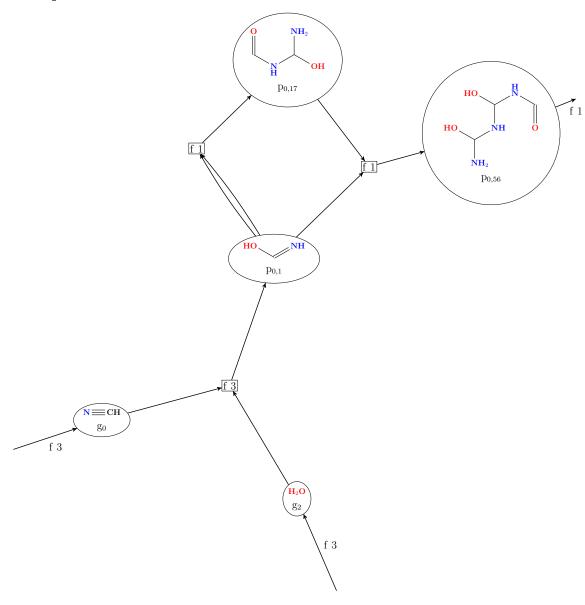
|E| = 5

|U| = 3

0.3.9 Solution 8

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068033 1.000000 0 p_{0,17} 0 0 -21.248844 1.000000 65 p_{0,1} 0 0 -10.610080 1.000000 1 0 1 -31.869324 0.000000 67 $p_{0,56}$



 $File: \ \mathtt{out/103_dg_0_11100_f_0_8_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.118349 | 1.0 | -13302.792564 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | 1.0 | -55785.506952 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -93.887263 | -93.887263 |
| 40 | $p_{0,1}, p_{0,1},$ | $p_{0,17},$ | 1 | -77.579904 | -77.579904 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -31.844411 | -31.844411 |
| Sum | | | | | -203.34049495277685 |

 $\Delta G = -39.10860929610851$

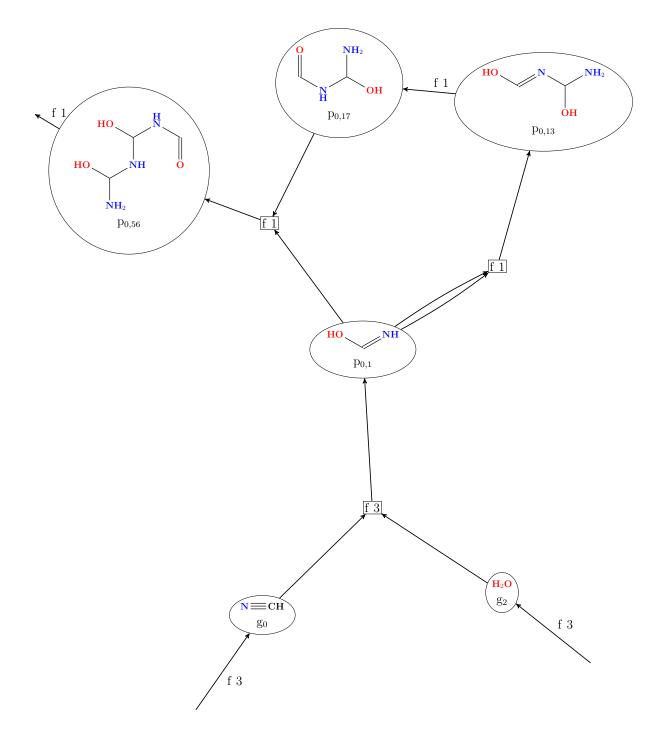
 $\Delta E = \text{-}0.07744830427516264$

 $\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}$

0.3.10 Solution 9

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068033 0.000000 0 -21.240635 1.000000 64 $p_{0,13}$ 0 0 0 0 -21.248844 1.000000 65 p_{0,17} p_{0,1} 0 0 -10.610080 1.000000 1 $p_{0,56}$ 0 1 -31.869324 0.000000 67



 $File: \verb"out/112_dg_0_11100_f_0_9_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.118349 | 0.0 | -13306.118349 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | 1.0 | -55763.953809 | 64 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | 1.0 | -55785.506952 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -91.617414 | -91.617414 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -56.026761 | -56.026761 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -31.844411 | -31.844411 |
| 250 | $p_{0,13},$ | $p_{0,17},$ | 1 | -21.553143 | -21.553143 |
| Sum | | | | | -203.34049495277685 |

 $\Delta G = -38.42765524626359$

 $\Delta E = -0.07744830427516264$

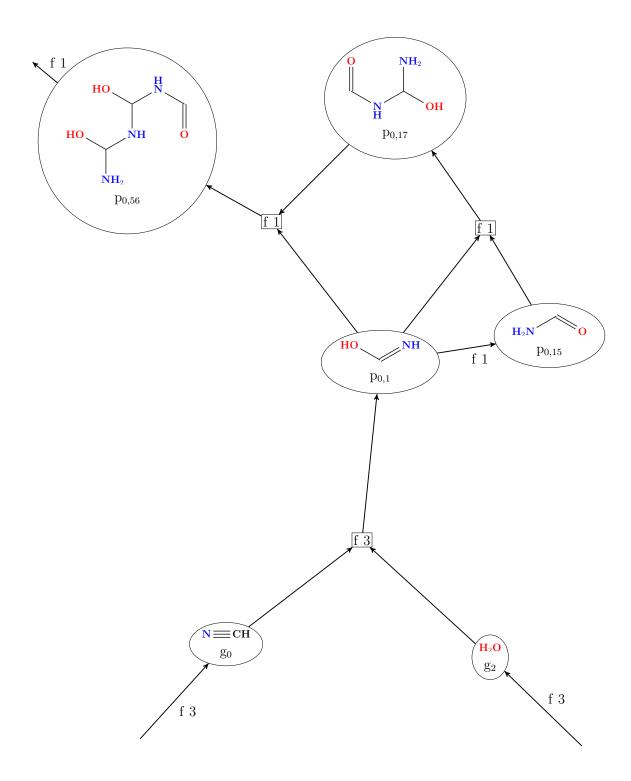
|E| = 6

|U| = 4

0.3.11 Solution 10

Overall Data

Objective value (non-integral): -0.0774483 Vertex/Graph In Out G t order logK g_{0} 3 0 -5.507152 1.000000 0 3 0 g_{2} -5.068043 0.000000 0 $p_{0,15}$ 0 0 -10.625195 0.000000 2 0 0 -21.248844 1.000000 4 $p_{0,17}$ p_{0,1} 0 0 -10.610080 1.000000 1 -31.869324 0.000000 67 $p_{0,56}$ 0 1



 ${\rm File:} \ {\tt out/121_dg_0_11100_f_0_10_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 0.0 | -13306.144961 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | 0.0 | -27896.445756 | 2 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | 1.0 | -55785.506952 | 4 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|--------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -91.590802 | -91.590802 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -41.954263 | -41.954263 |
| 183 | $p_{0,1}, p_{0,15},$ | $p_{0,17},$ | 1 | -35.625641 | -35.625641 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56}$, | 1 | -31.844411 | -31.844411 |
| Sum | | | | | -203.3404949527722 |

 $\Delta G = -38.41967136440989$

 $\Delta E = \text{-}0.07744830427516086$

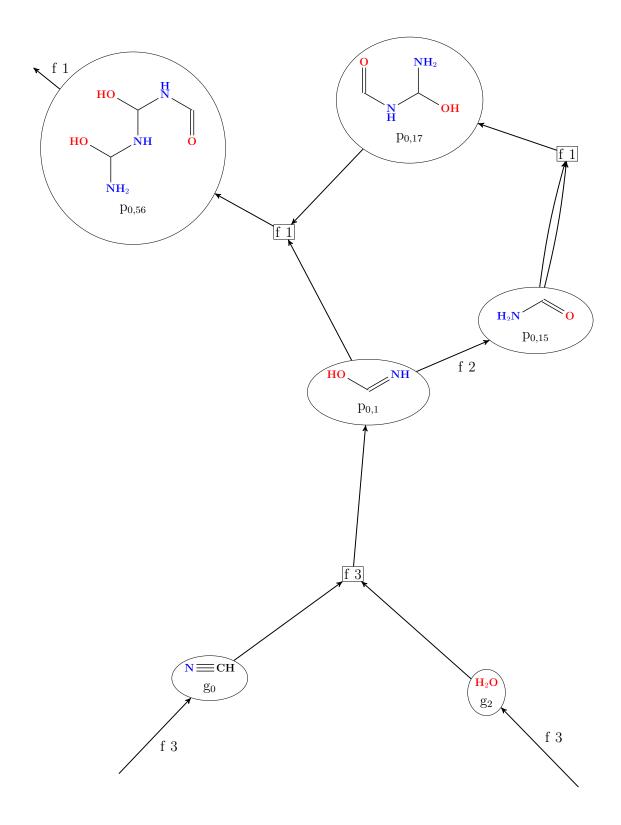
|E| = 6

|U| = 4

0.3.12 Solution 11

Overall Data

| Objective val | lue | (non-integral): -0.0623546 | | | | |
|-----------------|-----|----------------------------|------------|----------|---------|--|
| Vertex/Graph In | | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | 1.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | 1.000000 | 0 | |
| p_{0,15} | 0 | 0 | -10.625174 | 1.000000 | 32 | |
| p_{0,17} | 0 | 0 | -21.248844 | 0.261034 | 65 | |
| p_{0,1} | 0 | 0 | -10.610080 | 1.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869324 | 0.000000 | 67 | |



 $File: \ \mathtt{out/130_dg_0_11100_f_0_11_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|----------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 1.0 | -27893.064178 | 32 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | 0.261034 | -55787.964594 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -93.86065 | -93.86065 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 2 | -39.628622 | -39.628622 |
| 180 | $p_{0,15}, p_{0,15},$ | $p_{0,17},$ | 1 | 0.0 | 0.0 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -30.16707 | -30.16707 |
| Sum | | | | | -163.71187284898366 |

 $\Delta G = \text{-}39.10062593935474$

 $\Delta E = \text{-}0.06235455925692225$

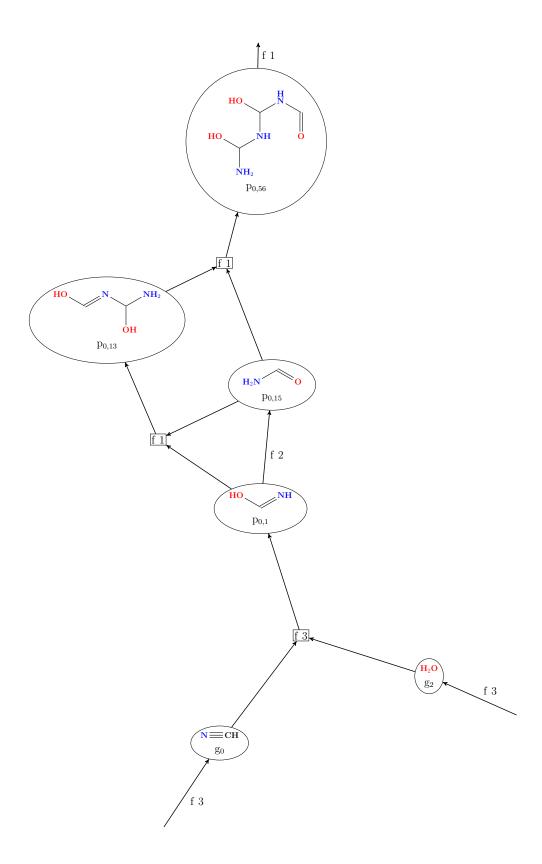
|E| = 7

|U| = 4

0.3.13 Solution 12

Overall Data

| Objective val | Lue | (non-integral): -0.0623546 | | | | |
|-----------------|-----|----------------------------|------------|----------|---------|--|
| Vertex/Graph In | | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | 1.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | 1.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | 0.000000 | 4 | |
| p_{0,15} | 0 | 0 | -10.625174 | 1.000000 | 2 | |
| p_{0,1} | 0 | 0 | -10.610080 | 1.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869324 | 0.000000 | 67 | |



 $File: \ \mathtt{out/139_dg_0_11100_f_0_12_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | 1.0 | -14455.699793 | 0 |
| g_2 | 3 | 0 | -13306.144961 | 1.0 | -13302.819176 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | 1.0 | -27853.435556 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | 0.0 | -55767.391129 | 4 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | 1.0 | -27893.064178 | 2 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | 0.0 | -83672.898792 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -93.86065 | -93.86065 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 2 | -39.628622 | -39.628622 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56},$ | 1 | -11.387548 | -11.387548 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | -18.779522 | -18.779522 |
| Sum | | | | | -163.71187284898176 |

 $\Delta G = -39.10062593935474$

 $\Delta E = \text{-}0.06235455925692152$

 $\begin{aligned} |E| &= 7 \\ |U| &= 4 \end{aligned}$