Summary

December 6, 2024

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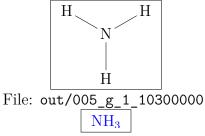
0.1 Loaded Graphs

$0.1.1 g_{0}$

N C H
File: out/001_g_0_10300000

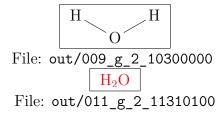
N CH
File: out/003_g_0_11310100

0.1.2 g_{1}



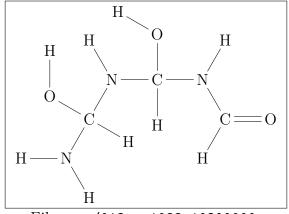
File: out/007_g_1_11310100

0.1.3 g_{2}

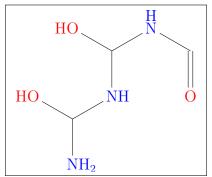


0.2 Product Graphs

0.2.1 p_{0,56}



File: out/013_g_1088_10300000



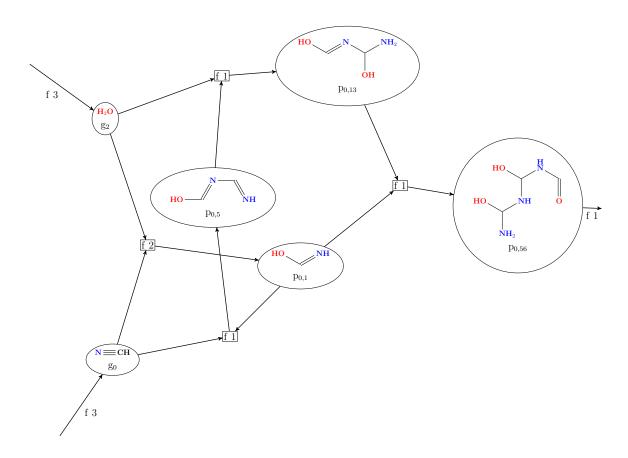
File: out/015_g_1088_11310100

0.3 Enumerated Flows

0.3.1 Solution 0

Overall Data

| Objective val | Lue | (non-integral): -0.103196 | | | |
|---------------|-----|---------------------------|------------|-----------|---------|
| Vertex/Graph | In | Out | G | logK | t_order |
| g_{0} | 3 | 0 | -5.507152 | -3.000000 | 0 |
| g_{2} | 3 | 0 | -5.068033 | -3.000000 | 0 |
| p_{0,13} | 0 | 0 | -21.240635 | -3.000000 | 65 |
| p_{0,1} | 0 | 0 | -10.610080 | -3.000000 | 1 |
| p_{0,56} | 0 | 1 | -31.869324 | -9.000000 | 67 |
| p_{0,5} | 0 | 0 | -16.158998 | -9.000000 | 64 |



 $File: \verb"out/027_dg_0_11100_f_0_0_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.118349 | -3.0 | -13316.095704 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 1 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | -9.0 | -42455.374686 | 64 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | -3.0 | -55777.256949 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 2 | -84.134398 | -84.134398 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -117.138718 | -117.138718 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -13.269576 | -13.269576 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56},$ | 1 | -56.340873 | -56.340873 |
| Sum | | | | | -270.941401308286 |

 $\Delta G = \text{-}35.501795559977474$

 $\Delta E = \text{-}0.10319612969436476$

|E| = 5

|U| = 4

0.3.2 Solution 1

Overall Data

| Objective val | lue | (nor | (non-integral): -0.103196 | | | |
|---------------|-----|------|---------------------------|-----------|------------|--|
| Vertex/Graph | In | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | -3.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | -3.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | -3.635441 | 33 | |
| p_{0,15} | 0 | 0 | -10.625195 | -9.000000 | 33 | |
| p_{0,1} | 0 | 0 | -10.610101 | -3.000000 | 31 | |
| p_{0,56} | 0 | 1 | -31.869324 | -9.000000 | 67 | |
| p_{0,5} | 0 | 0 | -16.158998 | -9.000000 | 32 | |



 $File: \ \mathtt{out/038_dg_0_11100_f_0_1_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|-----------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -3.0 | -13316.122316 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | -3.0 | -27866.79441 | 31 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | -9.0 | -42455.374686 | 32 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -3.635441 | -55779.481823 | 33 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | -9.0 | -27926.377821 | 33 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 2 | -84.163499 | -84.163499 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -117.083005 | -117.083005 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -54.594734 | -54.594734 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -14.939502 | -14.939502 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56},$ | 1 | 0.006113 | 0.006113 |
| Sum | | | | | -270.941401308287 |

 $\Delta G = -35.493811940673744$

 $\Delta E = -0.10319612969436516$

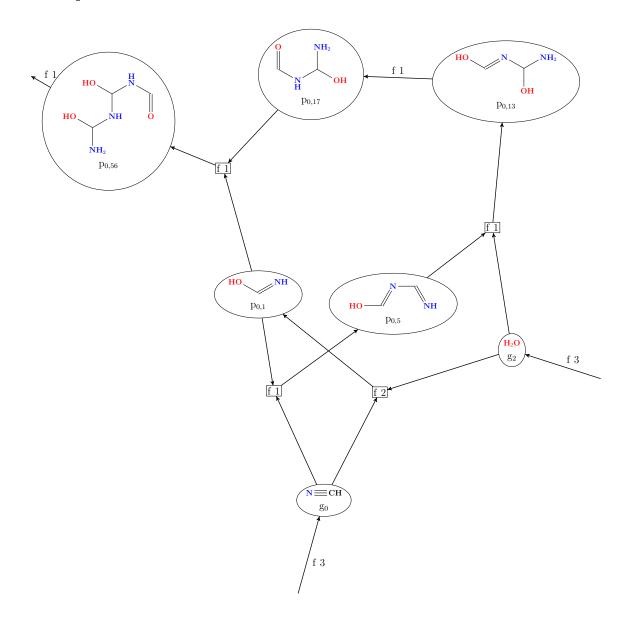
|E| = 6

|U| = 5

0.3.3 Solution 2

Overall Data

Objective value (non-integral): -0.103196 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 -3.000000 0 g_{2} 3 0 -5.068033 -9.000000 0 $p_{0,13}$ 0 0 -21.240678 -9.000000 3 $p_{0,17}$ -21.248887 -9.000000 65 0 0 -10.610101 -3.000000 1 $p_{0,1}$ 0 0 -31.869324 -9.000000 67 $p_{0,56}$ 0 1 -16.158998 -9.000000 2 $p_{0,5}$



 $File: \ \mathtt{out/049_dg_0_11100_f_0_2_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.118349 | -9.0 | -13336.050414 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | -3.0 | -27866.79441 | 1 |
| $p_{0,5}$ | 0 | 0 | -42425.44262 | -9.0 | -42455.374686 | 2 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -9.0 | -55797.323194 | 3 |
| $p_{0,17}$ | 0 | 0 | -55788.944315 | -9.0 | -55818.87638 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 2 | -69.224079 | -69.224079 |
| 14 | $g_0, p_{0,1},$ | $p_{0,5},$ | 1 | -117.083005 | -117.083005 |
| 123 | $g_2, p_{0,5},$ | $p_{0,13},$ | 1 | -13.381111 | -13.381111 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -19.654406 | -19.654406 |
| 250 | $p_{0,13},$ | $p_{0,17},$ | 1 | -21.553186 | -21.553186 |
| Sum | | | | | -270.94140130828237 |

 $\Delta G = \text{-}31.011985862394866$

 $\Delta E = -0.10319612969436338$

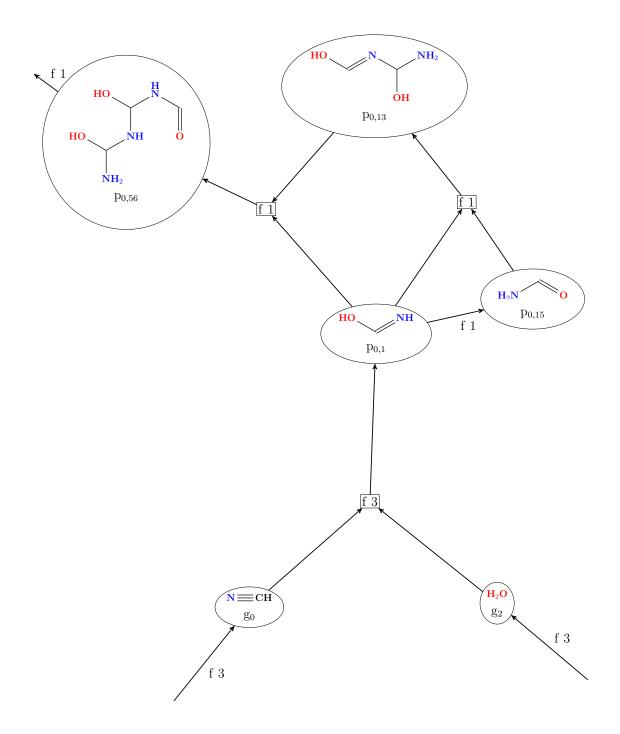
|E| = 6

 $|\mathbf{U}| = 5$

0.3.4 Solution 3

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 -9.000000 0 g_{2} 3 0 -5.068043 -9.000000 0 p_{0,13} 0 0 -21.240678 -9.000000 65 p_{0,15} 0 0 -10.625174 -9.000000 32 -10.610101 -5.688972 1 $p_{0,1}$ 0 0 p_{0,56} 0 1 -31.869260 -3.000000 67



 $File: \verb"out/058_dg_0_11100_f_0_3_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|-----------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -9.0 | -13336.077027 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | -5.688972 | -27875.737354 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -9.0 | -55797.323194 | 65 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | -9.0 | -27926.322028 | 32 |
| $p_{0,56}$ | 0 | 1 | -83672.731446 | -3.0 | -83682.708802 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -60.938642 | -60.938642 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -47.831733 | -47.831733 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | 0.006113 | 0.006113 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56},$ | 1 | -19.367006 | -19.367006 |
| Sum | | | | | -186.77808541741052 |

 $\Delta G = \text{-}25.000854028212327$

 $\Delta E = -0.07114001564075756$

|E| = 6

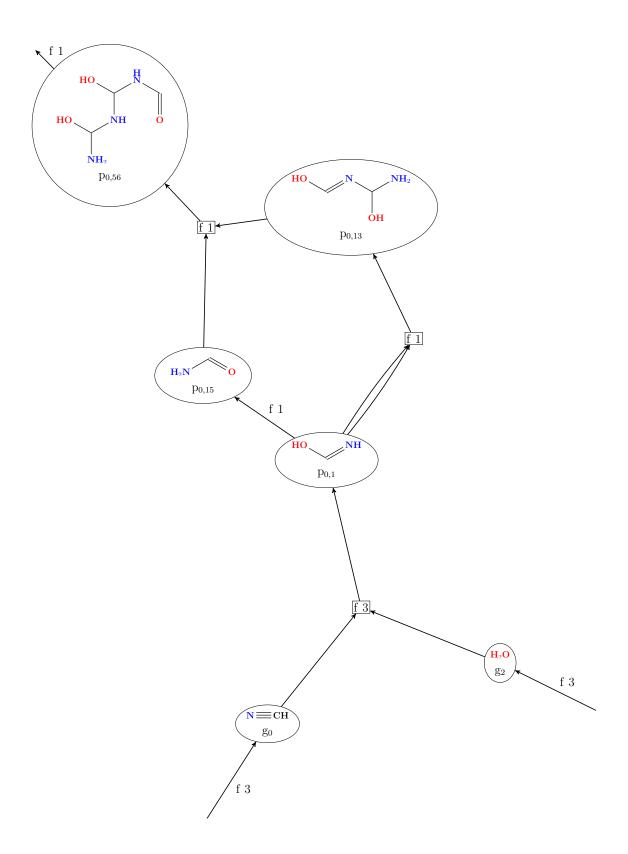
|U| = 4

0.3.5 Solution 4

Overall Data

Objective value (non-integral): -0.07114

| Vertex/Graph | In | Out | G | logK | t_order |
|--------------|----|-----|------------|-----------|---------|
| g_{0} | 3 | 0 | -5.507152 | -9.000000 | 0 |
| g_{2} | 3 | 0 | -5.068033 | -9.000000 | 0 |
| p_{0,13} | 0 | 0 | -21.240678 | -9.000000 | 3 |
| p_{0,15} | 0 | 0 | -10.625195 | -3.000000 | 63 |
| p_{0,1} | 0 | 0 | -10.610101 | -3.000000 | 1 |
| p_{0,56} | 0 | 1 | -31.869324 | -8.364559 | 67 |



 $File: \ \mathtt{out/067_dg_0_11100_f_0_4_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|-----------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.118349 | -9.0 | -13336.050414 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.817054 | -3.0 | -27866.79441 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -9.0 | -55797.323194 | 3 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | -3.0 | -27906.423111 | 63 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -8.364559 | -83700.717519 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -54.258046 | -54.258046 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -61.240036 | -61.240036 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -39.628701 | -39.628701 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56},$ | 1 | 0.006113 | 0.006113 |
| Sum | | | | | -186.77808541740794 |

 $\Delta G = \text{-}26.363676064326672$

 $\Delta E = \text{-}0.07114001564075657$

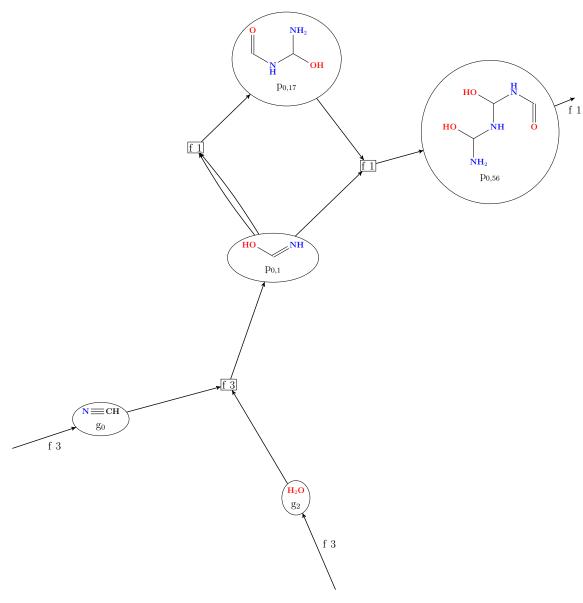
|E| = 6

|U| = 4

0.3.6 Solution 5

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G t_order logK g_{0} 3 -5.507152 -3.000000 0 3 g_{2} 0 -5.068043 -9.000000 0 $p_{0,17}$ 0 0 -21.248844 -3.000000 45 $p_{0,1}$ 0 0 -10.610080 -3.000000 21 p_{0,56} -31.869324 -9.000000 67 0 1



 $File: \ \mathtt{out/076_dg_0_11100_f_0_5_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -9.0 | -13336.077027 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 21 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | -3.0 | -55798.810092 | 45 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -69.141753 | -69.141753 |
| 40 | $p_{0,1}, p_{0,1},$ | $p_{0,17},$ | 1 | -67.827039 | -67.827039 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -34.78773 | -34.78773 |
| Sum | | | | | -186.77808541740694 |

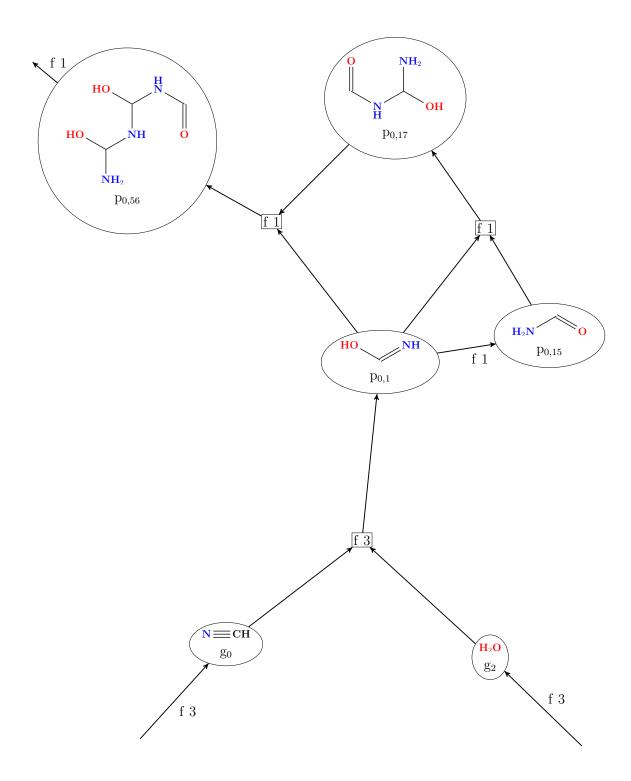
$$\begin{split} \Delta G &= \text{-}31.00400171799121 \\ \Delta E &= \text{-}0.07114001564075619 \end{split}$$

 $\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}$

0.3.7 Solution 6

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 -9.000000 0 g_{2} 3 0 -5.068043 -9.000000 0 p_{0,15} 0 0 -10.625195 -3.000000 22 0 0 -21.248844 -3.000000 44 p_{0,17} p_{0,1} 0 0 -10.610080 -3.000000 21 $p_{0,56}$ 0 1 -31.869324 -9.000000 67



 $File: \ \mathtt{out/085_dg_0_11100_f_0_6_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -9.0 | -13336.077027 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 21 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | -3.0 | -27906.423111 | 22 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | -3.0 | -55798.810092 | 44 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -54.17572 | -54.17572 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -39.684415 | -39.684415 |
| 183 | $p_{0,1}, p_{0,15},$ | $p_{0,17},$ | 1 | -28.142624 | -28.142624 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -34.78773 | -34.78773 |
| Sum | | | | | -186.77808541740794 |

 $\Delta G = -26.51419254550853$

 $\Delta E = \text{-}0.07114001564075657$

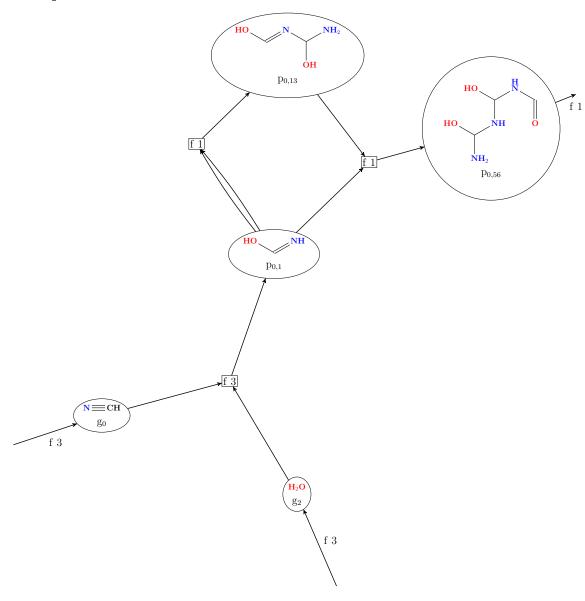
|E| = 6

|U| = 4

0.3.8 Solution 7

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G t_order logK g_{0} -5.507152 -9.000000 0 3 3 g_{2} 0 -5.068033 -9.000000 0 $p_{0,13}$ 0 0 -21.240635 -3.000000 3 $p_{0,1}$ 0 0 -10.610080 -3.000000 1 p_{0,56} -31.869324 -9.000000 67 0 1



 $File: \verb"out/094_dg_0_11100_f_0_7_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.118349 | -9.0 | -13336.050414 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | -3.0 | -55777.256949 | 3 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -54.202332 | -54.202332 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -46.273896 | -46.273896 |
| 263 | $p_{0,1}, p_{0,13},$ | $p_{0,56},$ | 1 | -56.340873 | -56.340873 |
| Sum | | | | | -186.77808541740688 |

 $\Delta G = \text{-}26.522176427362222$

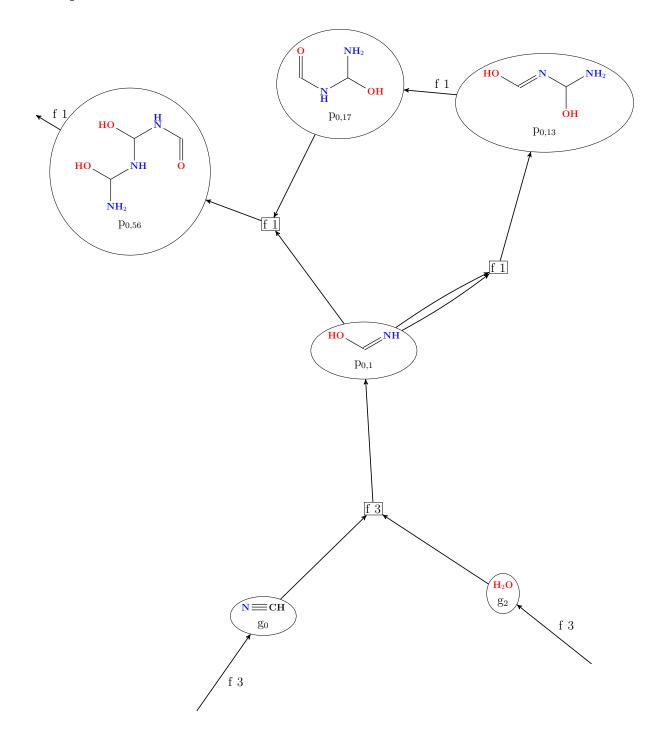
 $\Delta E = \text{-}0.07114001564075617$

 $\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}$

0.3.9 Solution 8

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 -9.000000 0 g_{2} 3 0 -5.068033 -9.000000 20 $p_{0,13}$ 0 0 -21.240635 -3.000000 43 p_{0,17} 0 0 -21.248844 -3.000000 45 p_{0,1} 0 0 -10.610080 -3.000000 21 $p_{0,56}$ 0 1 -31.869324 -9.000000 67



 $File: \verb"out/103_dg_0_11100_f_0_8_filt"$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|---------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.118349 | -9.0 | -13336.050414 | 20 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 21 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | -3.0 | -55777.256949 | 43 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | -3.0 | -55798.810092 | 45 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -54.202332 | -54.202332 |
| 30 | $p_{0,1}, p_{0,1},$ | $p_{0,13},$ | 1 | -46.273896 | -46.273896 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -34.78773 | -34.78773 |
| 250 | $p_{0,13},$ | $p_{0,17},$ | 1 | -21.553143 | -21.553143 |
| Sum | | | | | -186.77808541740532 |

 $\Delta G = -26.522176164812258$

 $\Delta E = \text{-}0.07114001564075557$

|E| = 6

|U| = 4

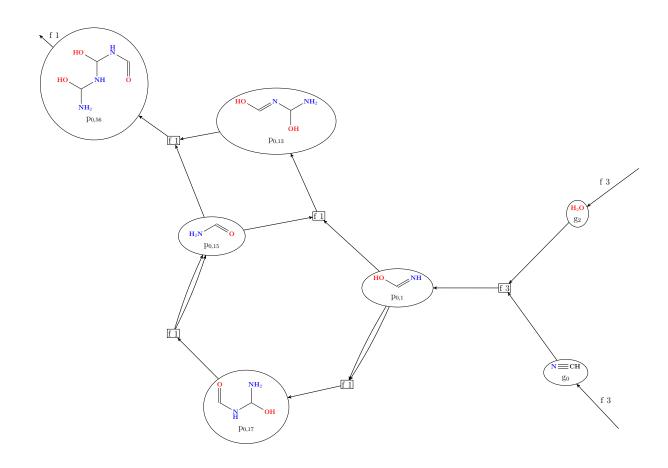
0.3.10 Solution 9

Overall Data

Objective value (non-integral): -0.07114

| In | Out | G | logK | t_order |
|----|------------------|---------------------------------|---------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 3 | 0 | -5.507152 | -3.000000 | 0 |
| 3 | 0 | -5.068043 | -3.000000 | 0 |
| 0 | 0 | -21.240678 | -4.973250 | 40 |
| 0 | 0 | -10.625174 | -7.684558 | 26 |
| 0 | 0 | -21.248887 | -9.000000 | 25 |
| 0 | 0 | -10.610080 | -3.000000 | 12 |
| 0 | 1 | -31.869324 | -9.000000 | 67 |
| | 3 0 0 0 | 3 0 3 0 0 0 0 0 0 0 | 3 0 -5.068043 0 0 -21.240678 0 0 -10.625174 0 0 -21.248887 0 0 -10.610080 | 3 0 -5.507152 -3.000000 3 0 -5.068043 -3.000000 0 0 -21.240678 -4.973250 0 0 -10.625174 -7.684558 0 0 -21.248887 -9.000000 0 0 -10.610080 -3.000000 |

Filtered Graph



File: out/112_dg_0_11100_f_0_9_filt

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|-----------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -3.0 | -13316.122316 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 12 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -4.97325 | -55783.931089 | 40 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | -7.684558 | -27921.947152 | 26 |
| $p_{0,17}$ | 0 | 0 | -55788.944315 | -9.0 | -55818.87638 | 25 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-----------------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -84.107786 | -84.107786 |
| 40 | $p_{0,1}, p_{0,1},$ | $p_{0,17},$ | 1 | -82.90465 | -82.90465 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56}$, | 1 | 0.006113 | 0.006113 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | 0.006113 | 0.006113 |
| 237 | $p_{0,17},$ | $p_{0,15}, p_{0,15},$ | 1 | -19.722346 | -19.722346 |
| Sum | | | | | -186.7780854174049 |

 $\Delta G = -35.493811940673744$

 $\Delta E = -0.07114001564075541$

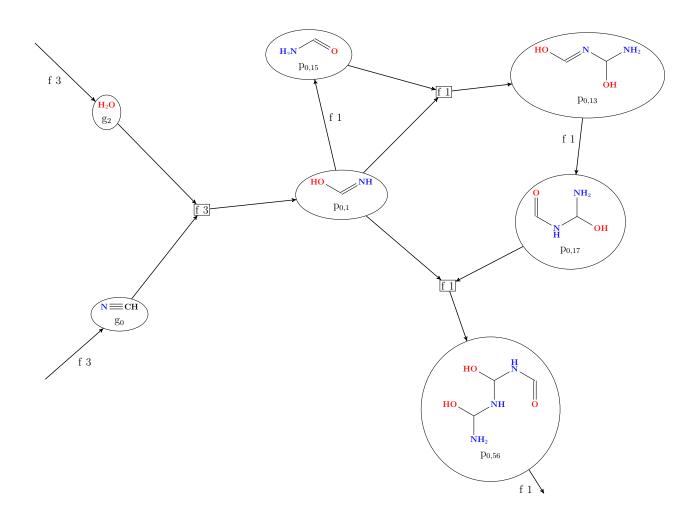
|E| = 7

|U| = 5

0.3.11 Solution 10

Overall Data

Objective value (non-integral): -0.07114 Vertex/Graph In Out G t_order logK g_{0} 3 0 -5.507152 -9.000000 0 g_{2} 3 0 -5.068043 -9.000000 0 $p_{0,13}$ 0 0 -21.240635 -3.000000 64 p_{0,15} 0 0 -10.625195 -3.000000 62 $p_{0,17}$ -21.248887 -3.000000 65 0 0 $p_{0,1}$ 0 0 -10.610080 -3.000000 1 $p_{0,56}$ 0 1 -31.869324 -9.000000 67



File: out/121_dg_0_11100_f_0_10_filt

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | -9.0 | -14488.957643 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -9.0 | -13336.077027 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.279594 | -3.0 | -55777.256949 | 64 |
| $p_{0,15}$ | 0 | 0 | -27896.445756 | -3.0 | -27906.423111 | 62 |
| $p_{0,17}$ | 0 | 0 | -55788.944315 | -3.0 | -55798.92167 | 65 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -54.17572 | -54.17572 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 1 | -39.684415 | -39.684415 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | -6.589481 | -6.589481 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -34.676153 | -34.676153 |
| 250 | $p_{0,13},$ | $p_{0,17},$ | 1 | -21.664721 | -21.664721 |
| Sum | | | | | -186.77808541740225 |

 $\Delta G = -26.51419254550853$

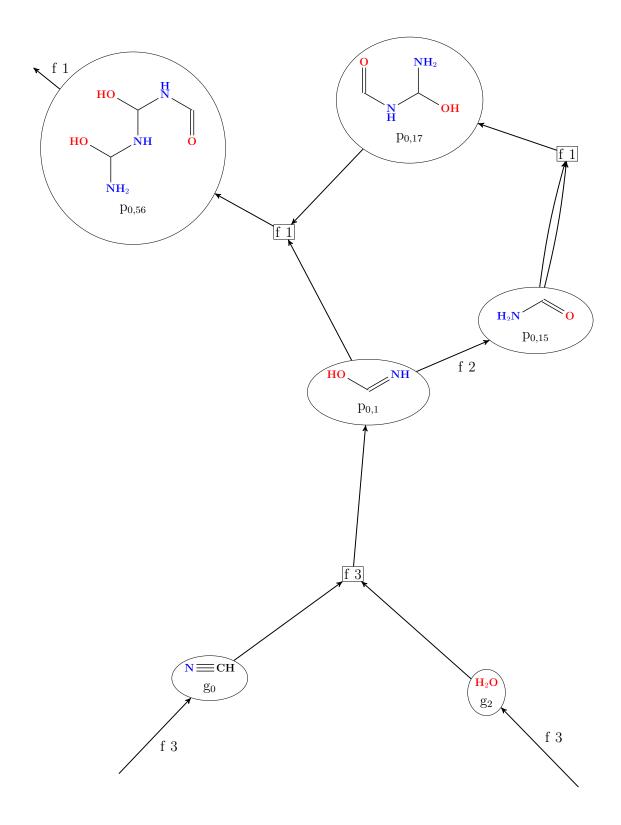
 $\Delta E = \text{-}0.07114001564075441}$

 $\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}$

0.3.12 Solution 11

Overall Data

Objective value (non-integral): -0.0560463 Vertex/Graph In Out G logK t_{order} g_{0} 3 0 -5.507152 -3.000000 0 g_{2} 3 0 -5.068043 -3.000000 0 p_{0,15} 0 0 -10.625174 -3.000000 2 p_{0,17} 0 0 -21.248844 -7.582459 5 p_{0,1} 0 0 -10.610080 -3.000000 1 $p_{0,56}$ 0 1 -31.869324 -9.000000 67



 $File: \ \mathtt{out/130_dg_0_11100_f_0_11_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------|--------|---------|--------------------|-----------|------------------|-------|
| g_0 | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -3.0 | -13316.122316 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 1 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | -3.0 | -27906.367318 | 2 |
| $p_{0,17}$ | 0 | 0 | -55788.832737 | -7.582459 | -55814.050366 | 5 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1},$ | 3 | -84.107786 | -84.107786 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 2 | -39.628622 | -39.628622 |
| 180 | $p_{0,15}, p_{0,15},$ | $p_{0,17},$ | 1 | 0.0 | 0.0 |
| 196 | $p_{0,1}, p_{0,17},$ | $p_{0,56},$ | 1 | -23.357525 | -23.357525 |
| Sum | | | | | -147.14946331361645 |

 $\Delta G = -35.493811940673744$

 $\Delta E = \text{-}0.05604627062251683$

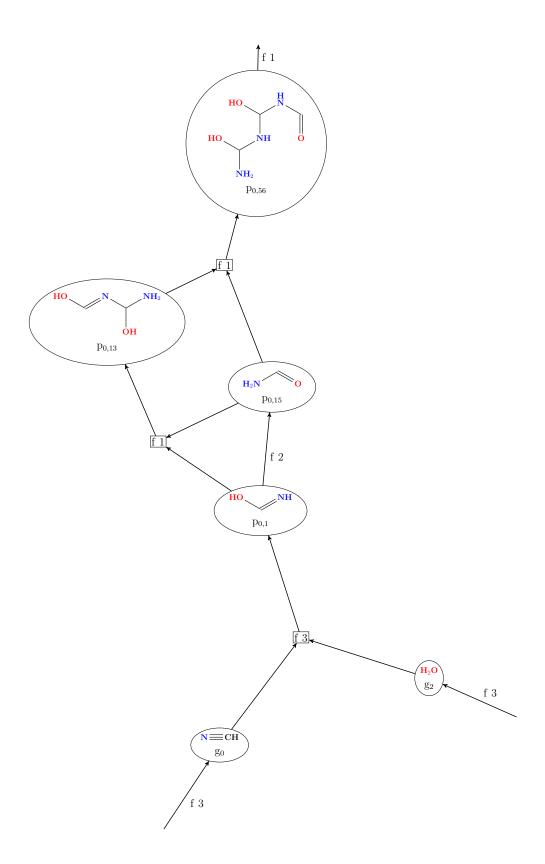
|E| = 7

|U| = 4

0.3.13 Solution 12

Overall Data

| Objective val | lue | (non-integral): -0.0560463 | | | | |
|---------------|-----|----------------------------|------------|-----------|---------|--|
| Vertex/Graph | In | Out | G | logK | t_order | |
| g_{0} | 3 | 0 | -5.507152 | -3.000000 | 0 | |
| g_{2} | 3 | 0 | -5.068043 | -3.000000 | 0 | |
| p_{0,13} | 0 | 0 | -21.240678 | -9.000000 | 64 | |
| p_{0,15} | 0 | 0 | -10.625174 | -3.000000 | 2 | |
| p_{0,1} | 0 | 0 | -10.610080 | -3.000000 | 1 | |
| p_{0,56} | 0 | 1 | -31.869324 | -9.000000 | 67 | |



 $File: \ \mathtt{out/139_dg_0_11100_f_0_12_filt}$

| Vertex | InFlow | OutFlow | $x_v^{\Delta G^0}$ | x_v^K | $x_v^{\Delta G}$ | t_v |
|------------------|--------|---------|--------------------|---------|------------------|-------|
| $\overline{g_0}$ | 3 | 0 | -14459.025578 | -3.0 | -14469.002933 | 0 |
| g_2 | 3 | 0 | -13306.144961 | -3.0 | -13316.122316 | 0 |
| $p_{0,1}$ | 0 | 0 | -27856.761341 | -3.0 | -27866.738696 | 1 |
| $p_{0,13}$ | 0 | 0 | -55767.391129 | -9.0 | -55797.323194 | 64 |
| $p_{0,15}$ | 0 | 0 | -27896.389963 | -3.0 | -27906.367318 | 2 |
| $p_{0,56}$ | 0 | 1 | -83672.898792 | -9.0 | -83702.830857 | 67 |

| Hyperedge | Source | Target | Flow | $x_e^{\Delta G}$ | $\overline{x}_e^{\Delta G}$ |
|-----------|-----------------------|-------------|------|------------------|-----------------------------|
| 6 | $g_0, g_2,$ | $p_{0,1}$, | 3 | -84.107786 | -84.107786 |
| 36 | $p_{0,1},$ | $p_{0,15},$ | 2 | -39.628622 | -39.628622 |
| 169 | $p_{0,13}, p_{0,15},$ | $p_{0,56},$ | 1 | -1.634684 | -1.634684 |
| 192 | $p_{0,1}, p_{0,15},$ | $p_{0,13},$ | 1 | -21.722842 | -21.722842 |
| Sum | | | | | -147.14946331361077 |

 $\Delta G = \text{-}35.493811940673744}$

 $\Delta E = \text{-}0.05604627062251467$

 $\begin{aligned} |E| &= 7 \\ |U| &= 4 \end{aligned}$