# Summary

December 7, 2024

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# 0.1 Loaded Graphs

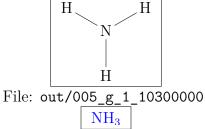
# $0.1.1 g_{0}$

N C H
File: out/001\_g\_0\_10300000

N CH
File: out/003\_g\_0\_11310100

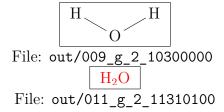
The. 00t/005\_g\_0\_1151010

# 0.1.2 g\_{1}



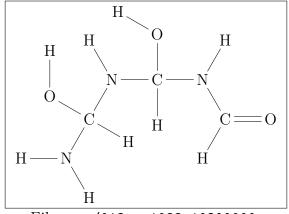
File: out/007\_g\_1\_11310100

## $0.1.3 g_{2}$

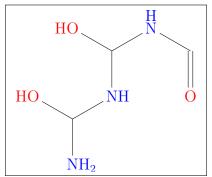


# 0.2 Product Graphs

# 0.2.1 p\_{0,56}



File: out/013\_g\_1088\_10300000

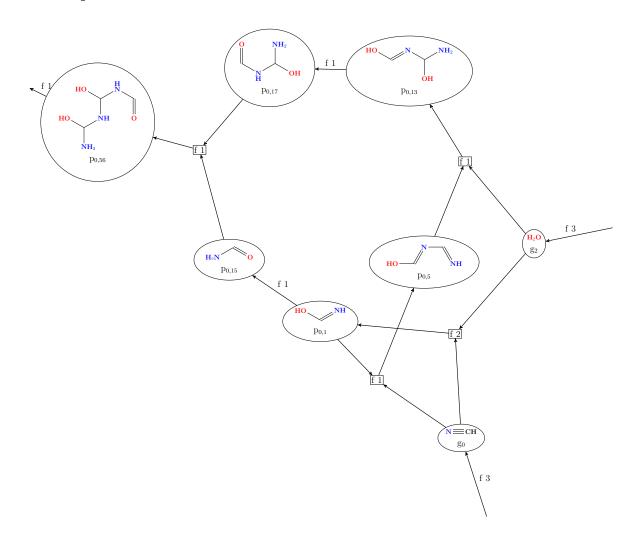


File: out/015\_g\_1088\_11310100

# 0.3 Enumerated Flows

# 0.3.1 Solution 0

Objective val	lue	(nor	(non-integral): -0.12189				
Vertex/Graph	In	Out	G	logK	$t\_order$		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	1.000000	0		
p_{0,13}	0	0	-21.240678	-5.951710	3		
p_{0,15}	0	0	-10.625174	-2.938239	2		
p_{0,17}	0	0	-21.248887	1.000000	4		
p_{0,1}	0	0	-10.610101	1.000000	1		
p_{0,56}	0	1	-31.869260	-6.000000	67		
p_{0,5}	0	0	-16.158998	-6.000000	2		



 $File: \verb"out/033_dg_0_11100_f_0_0_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	-6.0	-42445.397331	2
$p_{0,13}$	0	0	-55767.391129	-5.95171	-55787.185236	3
$p_{0,15}$	0	0	-27896.389963	-2.938239	-27906.161913	2
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	4
$p_{0,56}$	0	1	-83672.731446	-6.0	-83692.686157	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	2	-94.74781	-94.74781
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-134.410345	-134.410345
36	$p_{0,1},$	$p_{0,15},$	1	-51.786547	-51.786547
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.755079	-38.755079
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
250	$p_{0,13}$ ,	$p_{0,17},$	1	0.006113	0.006113
Sum					-320.02167414324634

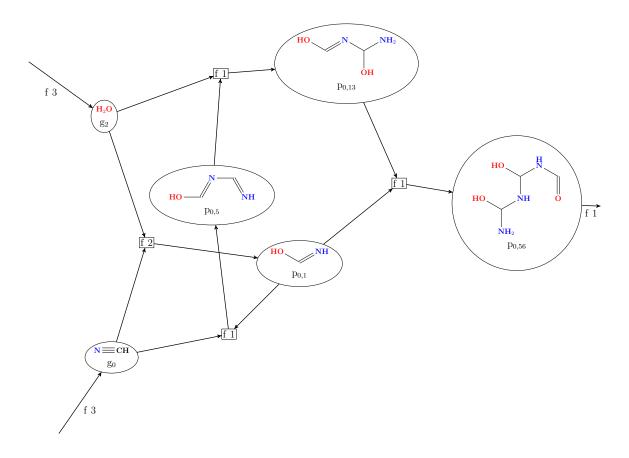
```
\begin{split} \Delta G &= \text{-}41.443535701238524\\ \Delta E &= \text{-}0.12188981835344265\\ |\mathbf{E}| &= 7\\ |\mathbf{U}| &= 6 \end{split}
```

#### 0.3.2 Solution 1

#### Overall Data

Objective value (non-integral): -0.12189 Vertex/Graph In Out G logK t\_order -5.507152 1.000000 g\_{0} 3 0 g\_{2} -5.068043 1.000000  $p_{0,13}$ 0 0 -21.240678 1.000000 45  $p_{0,1}$ 0 0 -10.610101 1.000000 21  $p_{0,56}$ 0 1 -31.869324 -6.000000 67  $p_{0,5}$ 0 0 -16.158998 1.000000 22

## Filtered Graph



File: out/042\_dg\_0\_11100\_f\_0\_1\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	21
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	22
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-94.74781	-94.74781
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-112.701283	-112.701283
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.904842	-38.904842
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-73.500965	-73.500965
Sum					-320.0216741432485

 $\Delta G = \text{-}41.46027011084064$ 

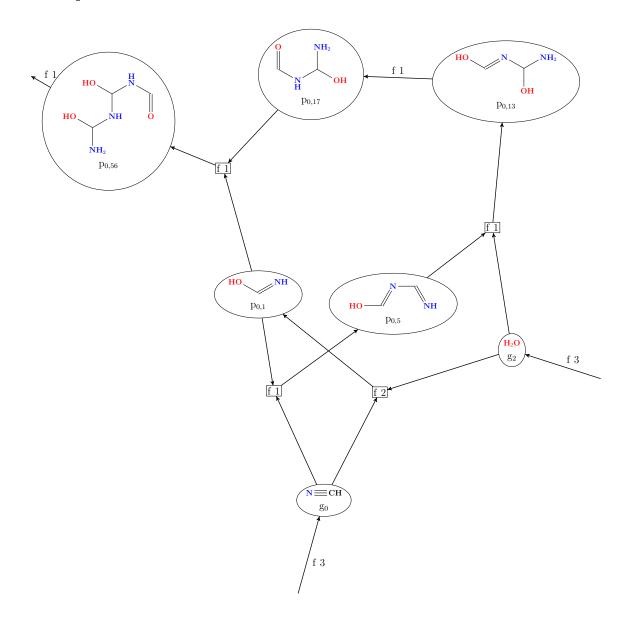
 $\Delta E = \text{-}0.12188981835344345$ 

|E| = 5

|U| = 4

# 0.3.3 Solution 2

Objective val	lue	(non-integral): -0.12189				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	-5.951710	43	
p_{0,17}	0	0	-21.248887	1.000000	45	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	
p_{0,5}	0	0	-16.158998	1.000000	2	



 $File: \ \mathtt{out/051\_dg\_0\_11100\_f\_0\_2\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	-5.95171	-55787.185236	43
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-94.74781	-94.74781
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-112.701283	-112.701283
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-60.464141	-60.464141
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-51.947779	-51.947779
250	$p_{0,13}$ ,	$p_{0,17},$	1	0.006113	0.006113
Sum					-320.0216741432451

 $\Delta G = -41.4602703733906$ 

 $\Delta E = -0.12188981835344216$ 

|E| = 6

 $|\mathbf{U}| = 5$ 

#### **0.3.4** Solution 3

#### Overall Data

Objective value (non-integral): -0.12189 Vertex/Graph In Out G logK t order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} -5.068043 -6.000000 0 3 0 p\_{0,13} -21.240678 -6.000000 3 0  $p_{0,15}$ 0 0 -10.625195 1.000000  $p_{0,1}$ 0 0 -10.610101 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -6.000000 67 p\_{0,5} 0 0 -16.158998 1.000000 2



 $File: \ \mathtt{out/060\_dg\_0\_11100\_f\_0\_3\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	3
$p_{0,15}$	0	0	-27896.445756	1.0	-27893.119971	2
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-73.038748	-73.038748
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-112.701283	-112.701283
36	$p_{0,1},$	$p_{0,15},$	1	-39.628701	-39.628701
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.904842	-38.904842
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	-12.163202	-12.163202
Sum					-320.02167414324043

 $\Delta G = -34.947551273333424$ 

 $\Delta E = -0.1218898183534404$ 

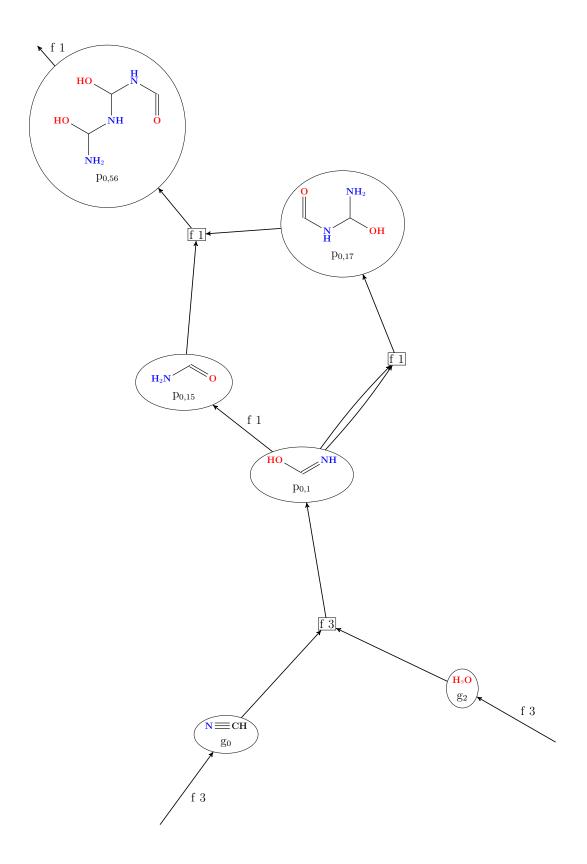
|E| = 6

|U| = 5

#### 0.3.5 Solution 4

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G logK t\_order 3 g\_{0} 0 -5.507152 -6.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,15} 0 0 -10.625195 -3.010186 2 p\_{0,17} -21.248844 1.000000 3 0 0 p\_{0,1} -10.610101 1.000000 1 0 0 p\_{0,56} -31.869324 -6.000000 67



 $File: \ \mathtt{out/069\_dg\_0\_11100\_f\_0\_4\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.445756	-3.010186	-27906.456988	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	3
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-51.329686	-51.329686
36	$p_{0,1},$	$p_{0,15},$	1	-52.06547	-52.06547
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.299923	-78.299923
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-225.27404733946997

 $\Delta G = -28.434833748576036$ 

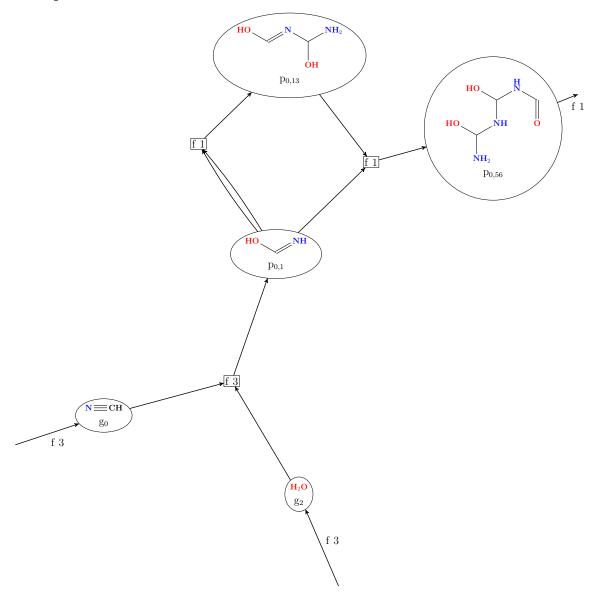
 $\Delta E = -0.08580235317955984$ 

|E| = 6

|U| = 4

# 0.3.6 Solution 5

Objective val	(nor	(non-integral): -0.0858024			
Vertex/Graph	In	Out	G	logK	$t\_order$
g_{0}	3	0	-5.507152	-6.000000	0
g_{2}	3	0	-5.068043	-6.000000	0
p_{0,13}	0	0	-21.240635	1.000000	65
p_{0,1}	0	0	-10.610080	1.000000	1
p_{0,56}	0	1	-31.869324	-6.000000	67



 $File: \verb"out/078_dg_0_11100_f_0_5_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-51.273973	-51.273973
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.858207	-56.858207
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$ ,	1	-73.668213	-73.668213
Sum					-225.27404733946875

 $\Delta G = -28.434832960926144$ 

 $\Delta E = \text{-}0.08580235317955937$ 

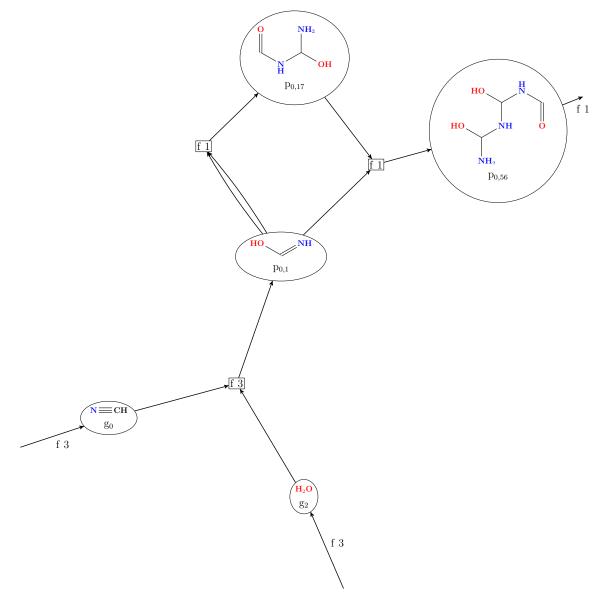
```
\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}
```

## 0.3.7 Solution 6

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 1.000000  $p_{0,17}$ 0 0 -21.248844 1.000000  $p_{0,1}$ 0 0 -10.610080 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -6.000000 67

## Filtered Graph



File:  $out/087_dg_0_11100_f_0_6_filt$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	3
$p_{0.56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.692097	-94.692097
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.41135	-78.41135
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-52.115071	-52.115071
Sum					-225.27404733946875

 $\Delta G = -41.46027011084064$ 

 $\Delta E = \text{-}0.08580235317955937$ 

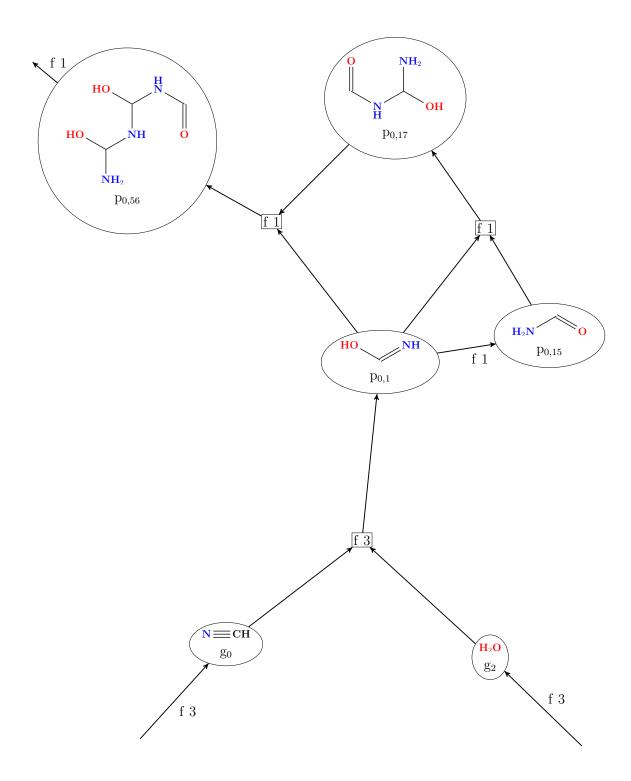
|E| = 5

|U| = 3

#### 0.3.8 Solution 7

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G  $t_{order}$ logK g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 20  $p_{0,15}$ -10.625195 -6.000000 22 -21.248844 1.000000 44  $p_{0,17}$ 0 0 p\_{0,1} 0 0 -10.610080 1.000000 21  $p_{0,56}$ 0 1 -31.869324 -6.000000 67



 $File: \ \mathtt{out/096\_dg\_0\_11100\_f\_0\_7\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	20
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	22
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	44
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-72.983035	-72.983035
36	$p_{0,1},$	$p_{0,15},$	1	-61.393477	-61.393477
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-17.017873	-17.017873
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-52.115071	-52.115071
Sum					-225.27404733946997

 $\Delta G = -34.94755153588339$ 

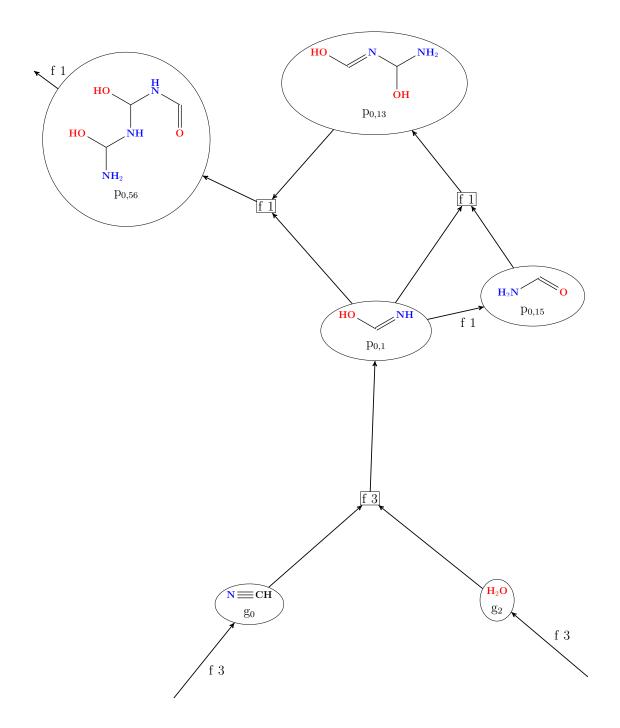
 $\Delta E = -0.08580235317955984$ 

|E| = 6

|U| = 4

# 0.3.9 Solution 8

Objective val	lue	(non-integral): -0.0858024				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-6.000000	0	
p_{0,13}	0	0	-21.240678	-6.000000	43	
p_{0,15}	0	0	-10.625195	-6.000000	22	
p_{0,1}	0	0	-10.610101	-4.557591	20	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ {\tt out/105\_dg\_0\_11100\_f\_0\_8\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-4.557591	-27871.974622	20
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	43
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	22
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-90.274474	-90.274474
36	$p_{0,1},$	$p_{0,15},$	1	-44.102037	-44.102037
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	0.006113	0.006113
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$ ,	1	-34.556177	-34.556177
Sum					-225.27404733946744

 $\Delta G = -34.94755179843335$ 

 $\Delta E = -0.08580235317955887$ 

|E| = 6

|U| = 4

### 0.3.10 Solution 9

#### Overall Data

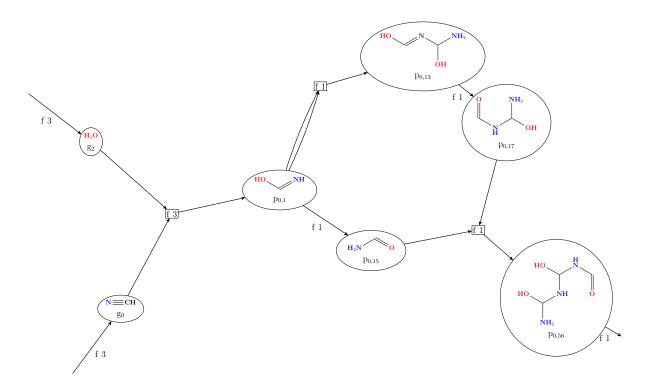
Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,13} 0 0 -21.240635 1.000000 3

p\_{0,15} 0 0 -10.625174 1.000000 2 p\_{0,17} 0 0 -21.248844 -3.026205 64

Objective value (non-integral): -0.0858024

p\_{0,1} 0 0 -10.610101 1.000000 1 p\_{0,56} 0 1 -31.869324 -6.000000 67

#### Filtered Graph



File: out/114\_dg\_0\_11100\_f\_0\_9\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	3
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.832737	-3.026205	-55798.897245	64
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-73.038748	-73.038748
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.74678	-56.74678
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
250	$p_{0,13},$	$p_{0,17},$	1	-34.039591	-34.039591
Sum					-225.2740473394666

 $\Delta G = -34.947551273333424$ 

 $\Delta E = -0.08580235317955855$ 

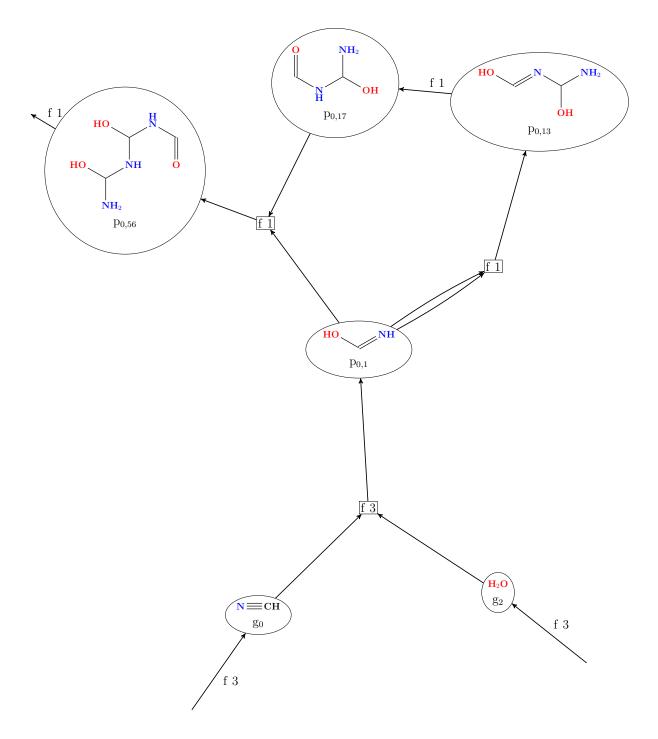
|E| = 7

|U| = 5

#### 0.3.11 Solution 10

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 1.000000 p\_{0,13} 0 0 -21.240635 1.000000 p\_{0,17} -21.248844 -6.000000 65 0 0 p\_{0,1} -10.610080 1.000000 1 0 0 -31.869324 -6.000000 67  $p_{0,56}$ 



 $File: \ \mathtt{out/123\_dg\_0\_11100\_f\_0\_10\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	3
$p_{0,17}$	0	0	-55788.832737	-6.0	-55808.787447	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-94.692097	-94.692097
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.858207	-56.858207
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-30.406009	-30.406009
250	$p_{0,13},$	$p_{0,17},$	1	-43.262205	-43.262205
Sum					-225.27404733946537

 $\Delta G = -41.46027011084064$ 

 $\Delta E = \text{-}0.08580235317955807$ 

|E| = 6

|U| = 4

## 0.3.12 Solution 11

0 0

0 1

## Overall Data

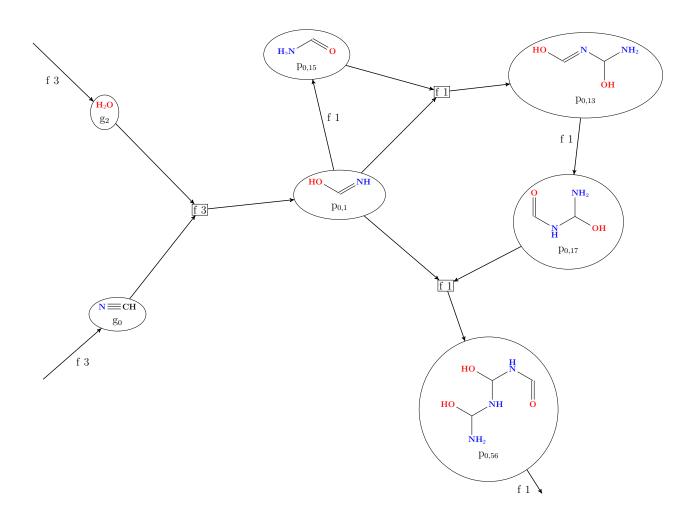
 $p_{0,1}$ 

 $p_{0,56}$ 

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G t order logK g\_{0} 3 0 -5.507152 -6.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,13} 0 0 -21.240635 1.000000 44 -10.625195 -4.539592 22  $p_{0,15}$ 0 0  $p_{0,17}$ -21.248844 -6.000000 45 0 0

-10.610080 1.000000 21

-31.869324 -6.000000 67



File: out/132\_dg\_0\_11100\_f\_0\_11\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	44
$p_{0,15}$	0	0	-27896.445756	-4.539592	-27911.543462	22
$p_{0,17}$	0	0	-55788.832737	-6.0	-55808.787447	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-51.273973	-51.273973
36	$p_{0,1},$	$p_{0,15},$	1	-56.86432	-56.86432
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	0.006113	0.006113
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-30.406009	-30.406009
250	$p_{0,13},$	$p_{0,17},$	1	-43.262205	-43.262205
Sum					-225.27404733946406

 $\Delta G = \text{-}28.434832960926144$ 

 $\Delta E = \text{-}0.08580235317955758}$ 

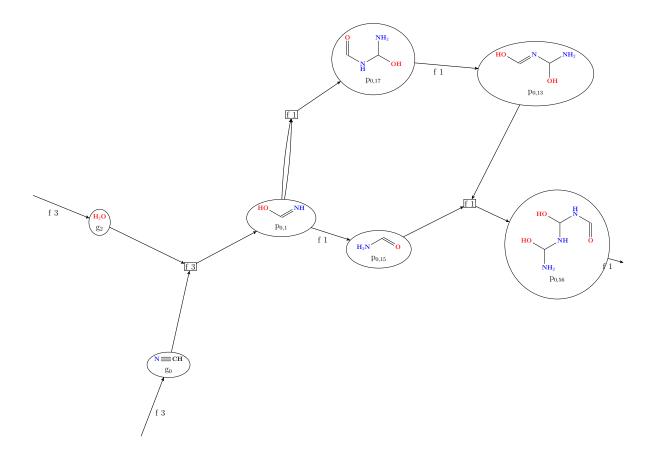
```
\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}
```

#### 0.3.13 Solution 12

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G t\_order logK g\_{0} 3 0 -5.507152 1.000000 0 3 0 g\_{2} -5.068043 1.000000 20 p\_{0,13} 0 0 -21.240678 -5.911790 44  $p_{0,15}$ -10.625174 -3.030147 22 0 0  $p_{0,17}$ 0 0 -21.248844 1.000000 43  $p_{0,1}$ 0 0 -10.610101 1.000000 21  $p_{0,56}$ 0 1 -31.869324 -6.000000 67

#### Filtered Graph



File: out/141\_dg\_0\_11100\_f\_0\_12\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	20
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	21
$p_{0,13}$	0	0	-55767.391129	-5.91179	-55787.05247	44
$p_{0,15}$	0	0	-27896.389963	-3.030147	-27906.467582	22
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	43
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-94.74781	-94.74781
36	$p_{0,1},$	$p_{0,15},$	1	-52.071583	-52.071583
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.299923	-78.299923
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
253	$p_{0,17},$	$p_{0,13},$	1	0.006113	0.006113
Sum					-225.27404733946406

 $\Delta G = -41.46027011084064$ 

 $\Delta E = -0.08580235317955758$ 

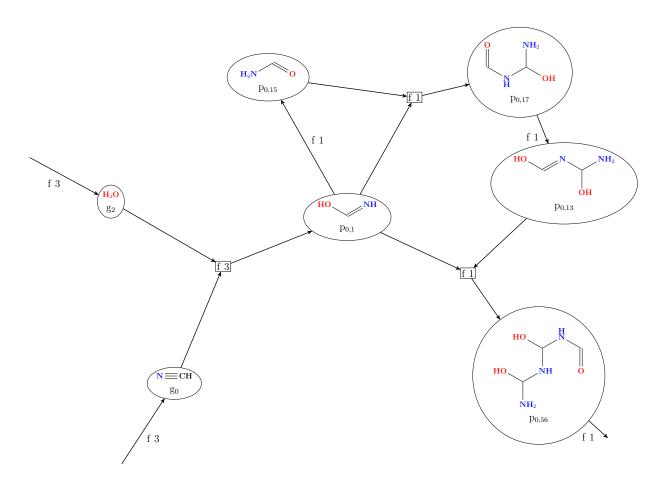
|E| = 7

|U| = 5

#### 0.3.14 Solution 13

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 1.000000 0 p\_{0,13} 0 0 -21.240678 -6.000000 65 p\_{0,15} -10.625195 1.000000 21 0 0 p\_{0,17} 0 0 -21.248844 1.000000 23 -10.610080 1.000000 1  $p_{0,1}$ 0  $p_{0,56}$ -31.869324 -6.000000 67



 $File: \ {\tt out/150\_dg\_0\_11100\_f\_0\_13\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	65
$p_{0,15}$	0	0	-27896.445756	1.0	-27893.119971	21
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	23
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-94.692097	-94.692097
36	$p_{0,1},$	$p_{0,15},$	1	-39.684415	-39.684415
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-38.726935	-38.726935
253	$p_{0,17},$	$p_{0,13},$	1	-0.267454	-0.267454
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$ ,	1	-51.847617	-51.847617
Sum					-225.2740473394734

 $\Delta G = \text{-}41.46026984829067$ 

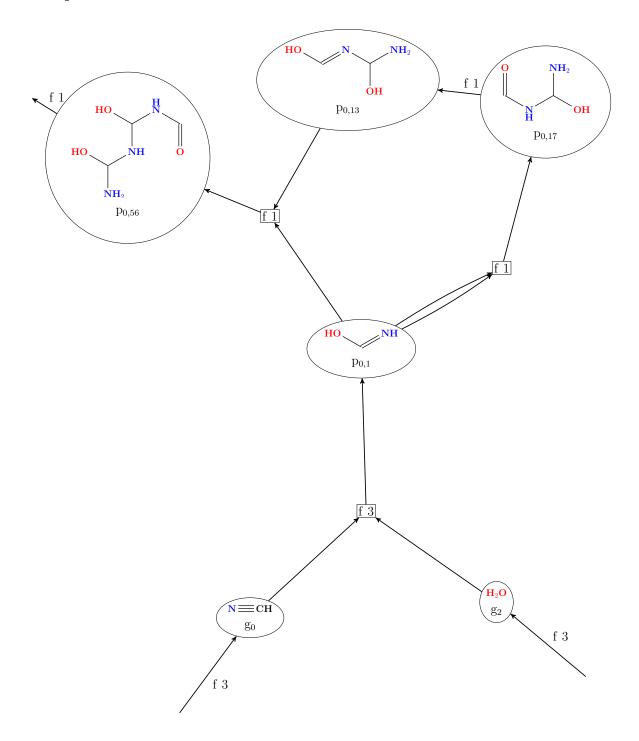
 $\Delta E = -0.08580235317956114$ 

|E| = 7

|U| = 5

# 0.3.15 Solution 14

Objective value (non-integral): -0.0858024						
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	-6.000000	4	
p_{0,17}	0	0	-21.248844	1.000000	3	
p_{0,1}	0	0	-10.610080	1.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ {\tt out/159\_dg\_0\_11100\_f\_0\_14\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	4
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	3
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.692097	-94.692097
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.41135	-78.41135
253	$p_{0,17},$	$p_{0,13},$	1	-0.267454	-0.267454
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-51.847617	-51.847617
Sum					-225.2740473394721

 $\Delta G = -41.46026984829067$ 

 $\Delta E = -0.08580235317956064$ 

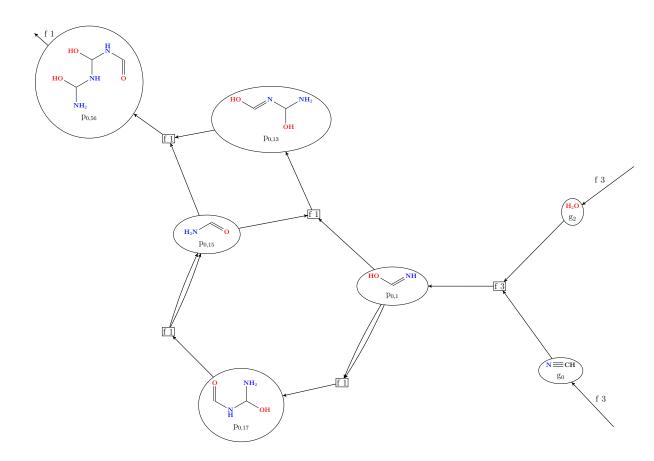
|E| = 6

|U| = 4

#### 0.3.16 Solution 15

#### Overall Data

Objective value (non-integral): -0.0858024 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 g\_{2} 3 0 -5.068043 1.000000 0  $p_{0,13}$ 0 0 -21.240678 -6.000000 34 p<sub>{0,15}</sub> 0 0 -10.625174 -2.380626 32 p\_{0,17} 0 0 -21.248887 -6.000000 31 p\_{0,1} 0 0 -10.610080 1.000000 1 -31.869324 -6.000000 67  $p_{0,56}$ 1



 $File: \ \mathtt{out/168\_dg\_0\_11100\_f\_0\_15\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	34
$p_{0,15}$	0	0	-27896.389963	-2.380626	-27904.307412	32
$p_{0,17}$	0	0	-55788.944315	-6.0	-55808.899025	31
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.692097	-94.692097
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-100.23199	-100.23199
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	-1.734678	-1.734678
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-28.565865	-28.565865
237	$p_{0,17},$	$p_{0,15}, p_{0,15},$	1	0.006113	0.006113
Sum					-225.2740473394615

 $\Delta G = -41.46027011084064$ 

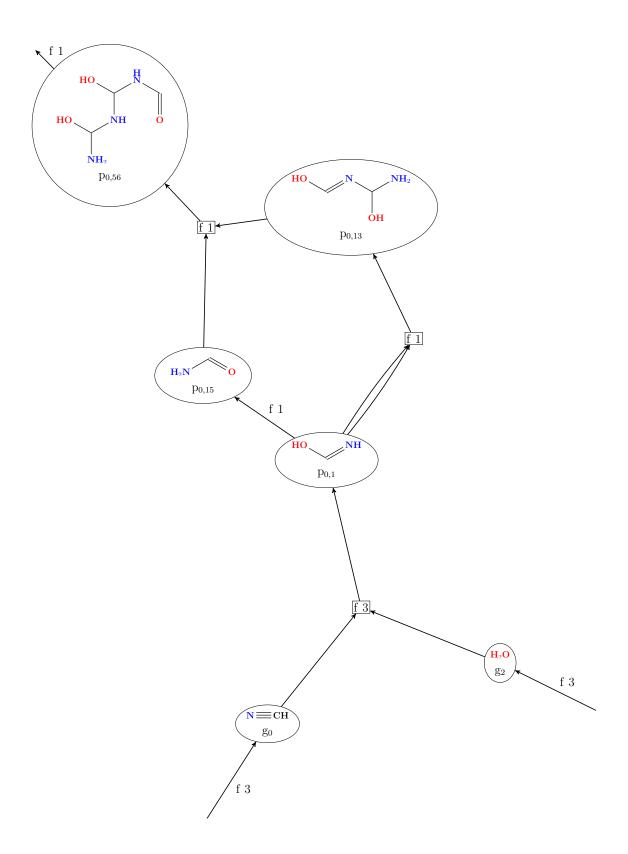
 $\Delta E = \text{-}0.0858023531795566$ 

|E| = 7

|U| = 5

# 0.3.17 Solution 16

Objective val	Lue	(nor	n-integral):	: -0.085802	24
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	-6.000000	0
g_{2}	3	0	-5.068043	-6.000000	0
p_{0,13}	0	0	-21.240678	-2.923947	3
p_{0,15}	0	0	-10.625195	-6.000000	2
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-6.000000	67



 $File: \ {\tt out/177\_dg\_0\_11100\_f\_0\_16\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.391129	-2.923947	-55777.115547	3
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	2
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-51.329686	-51.329686
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-69.02763	-69.02763
36	$p_{0,1},$	$p_{0,15},$	1	-61.337763	-61.337763
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-225.27404733946065

 $\Delta G = -28.434833748576036$ 

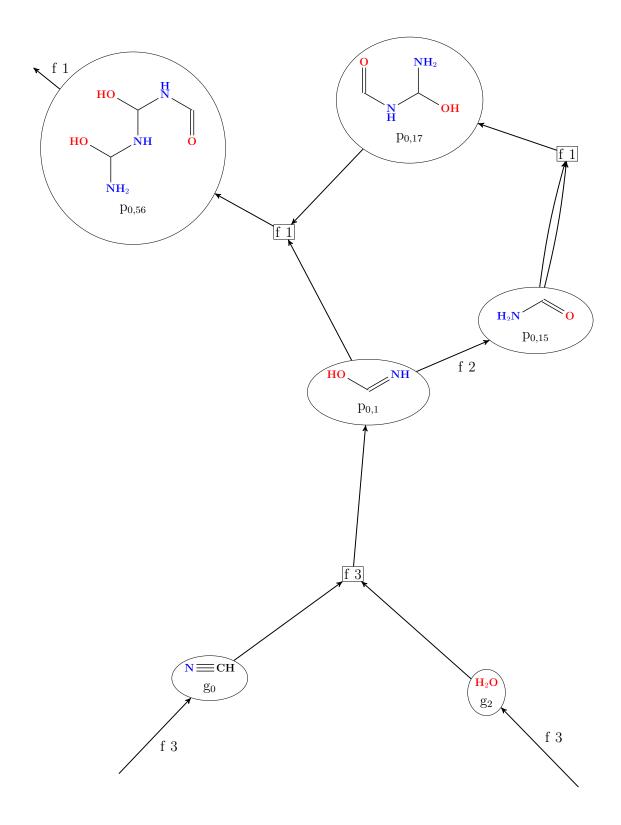
 $\Delta E = \text{-}0.08580235317955628$ 

|E| = 6

|U| = 4

# 0.3.18 Solution 17

Objective val	Lue	(nor	(non-integral): -0.0707086				
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	-6.000000	0		
p_{0,15}	0	0	-10.625174	1.000000	2		
p_{0,17}	0	0	-21.248844	0.727245	5		
p_{0,1}	0	0	-10.610080	1.000000	1		
p_{0,56}	0	1	-31.869324	-6.000000	67		



 $File: \ \mathtt{out/186\_dg\_0\_11100\_f\_0\_17\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.832737	0.727245	-55786.414077	5
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-72.983035	-72.983035
36	$p_{0,1},$	$p_{0,15},$	2	-39.628622	-39.628622
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.0	0.0
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-51.269176	-51.269176
Sum					-185.6454252356783

 $\Delta G = -34.94755153588339$ 

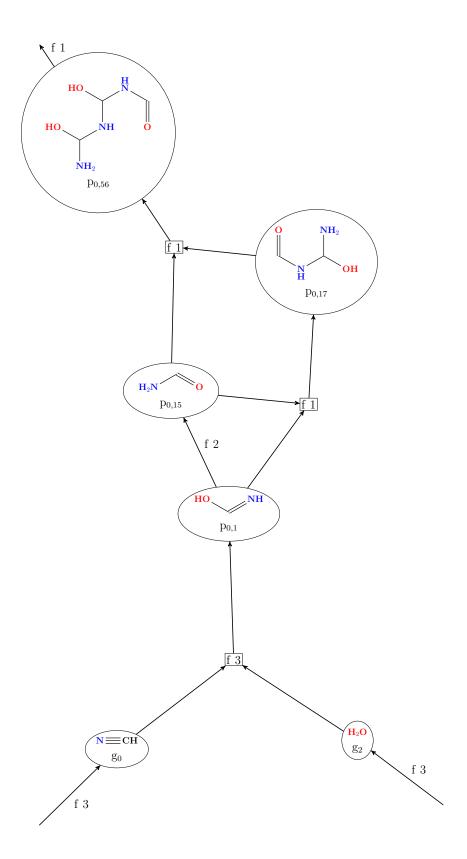
 $\Delta E = \text{-}0.07070860816132002$ 

|E| = 7

|U| = 4

# 0.3.19 Solution 18

Objective val	Lue	(nor	(non-integral): -0.0707086				
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	1.000000	0		
p_{0,15}	0	0	-10.625195	1.000000	32		
p_{0,17}	0	0	-21.248887	-2.974208	34		
p_{0,1}	0	0	-10.610101	1.000000	1		
p_{0,56}	0	1	-31.869324	-6.000000	67		



 $File: \ {\tt out/195\_dg\_0\_11100\_f\_0\_18\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.445756	1.0	-27893.119971	32
$p_{0,17}$	0	0	-55788.944315	-2.974208	-55798.835893	34
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.74781	-94.74781
36	$p_{0,1},$	$p_{0,15},$	2	-39.628701	-39.628701
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-51.10799	-51.10799
Sum					-185.6454252356749

 $\Delta G = -41.46027011084064$ 

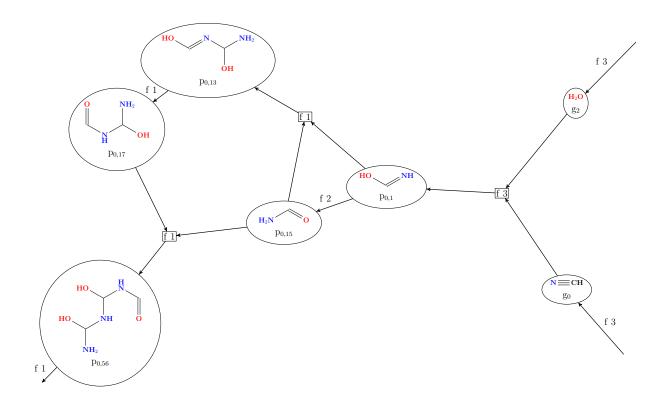
 $\Delta E = \text{-}0.07070860816131873$ 

|E| = 7

|U| = 4

# 0.3.20 Solution 19

Objective val	lue	(nor	(non-integral): -0.0707086				
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	-6.000000	0		
p_{0,13}	0	0	-21.240635	1.000000	4		
p_{0,15}	0	0	-10.625174	1.000000	2		
p_{0,17}	0	0	-21.248887	-2.990227	64		
p_{0,1}	0	0	-10.610101	-4.539617	1		
p_{0,56}	0	1	-31.869324	-6.000000	67		



 $File: \ \mathtt{out/204\_dg\_0\_11100\_f\_0\_19\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-4.539617	-27871.914845	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	4
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.944315	-2.990227	-55798.889169	64
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-90.218733	-90.218733
36	$p_{0,1},$	$p_{0,15},$	2	-22.392924	-22.392924
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	0.006113	0.006113
250	$p_{0,13}$ ,	$p_{0,17}$	1	-34.039591	-34.039591
Sum					-185.64542523566897

 $\Delta G = -34.94755179843335$ 

 $\Delta E = \text{-}0.07070860816131647$ 

|E| = 8

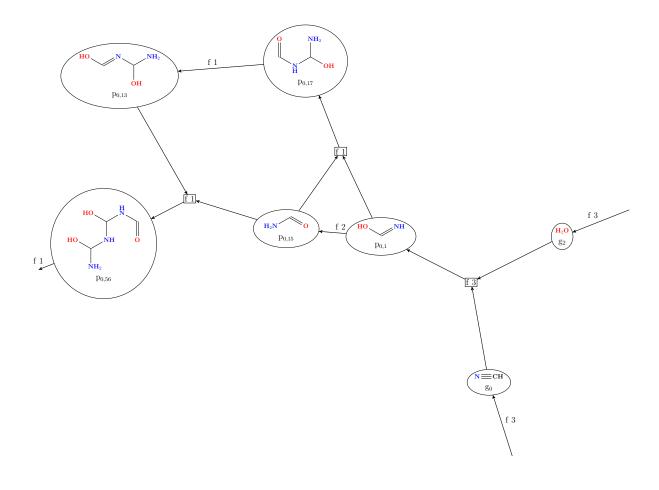
|U| = 5

# 0.3.21 Solution 20

### Overall Data

Objective val	lue	(non-integral): -0.0707086				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-6.000000	19	
p_{0,13}	0	0	-21.240678	-6.000000	44	
p_{0,15}	0	0	-10.625195	-2.923947	22	
p_{0,17}	0	0	-21.248844	1.000000	43	
p_{0,1}	0	0	-10.610101	1.000000	20	
p_{0,56}	0	1	-31.869324	-6.000000	67	

# Filtered Graph



File: out/213\_dg\_0\_11100\_f\_0\_20\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	19
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	20
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	44
$p_{0,15}$	0	0	-27896.445756	-2.923947	-27906.170174	22
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	43
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-73.038748	-73.038748
36	$p_{0,1},$	$p_{0,15},$	2	-51.798016	-51.798016
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-26.501907	-26.501907
253	$p_{0,17},$	$p_{0,13},$	1	-0.267454	-0.267454
Sum					-185.64542523566897

 $\Delta G = -34.947551273333424$ 

 $\Delta E = -0.07070860816131647$ 

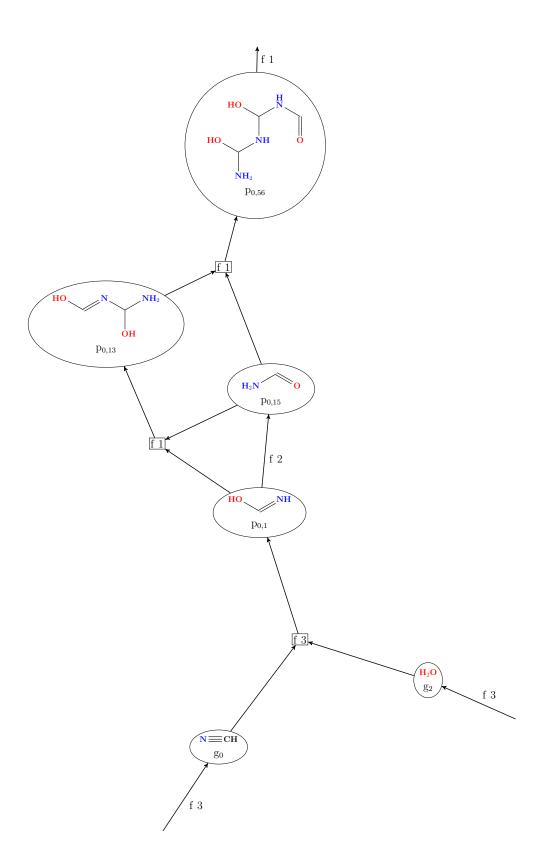
|E| = 8

|U| = 5

#### 0.3.22 Solution 21

#### Overall Data

Objective value (non-integral): -0.0707086 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,13} 0 0 -21.240678 -6.000000 4 p\_{0,15} 0 0 -10.625174 1.000000 2 p\_{0,1} -10.610080 1.000000 1 0 0 -31.869324 -6.000000 67  $p_{0,56}$ 0 1



 $File: \ \mathtt{out/222\_dg\_0\_11100\_f\_0\_21\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	4
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-72.983035	-72.983035
36	$p_{0,1},$	$p_{0,15}$ ,	2	-39.628622	-39.628622
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	-12.218995	-12.218995
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-39.050182	-39.050182
Sum					-185.64542523566303

 $\Delta G = -34.94755153588339$ 

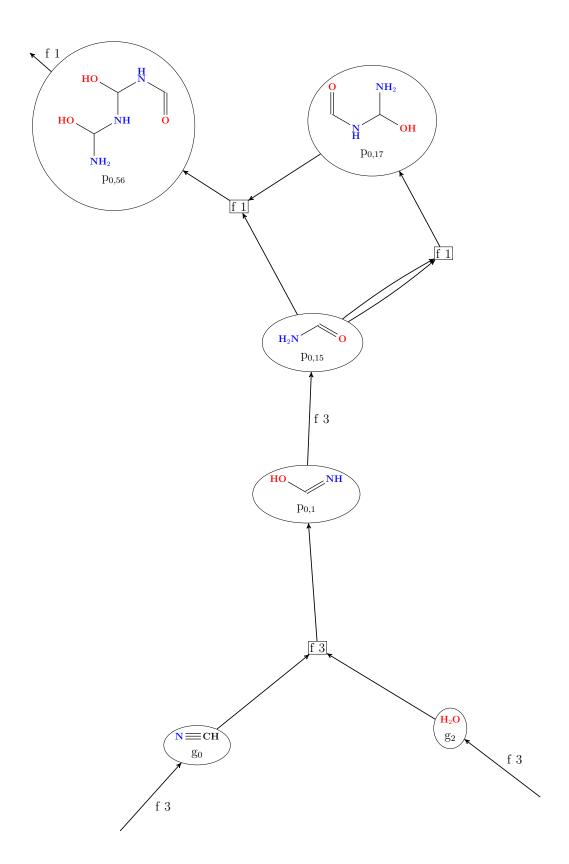
 $\Delta E = \text{-}0.0707086081613142$ 

|E| = 7

|U| = 4

# 0.3.23 Solution 22

Objective val	Lue	(non-integral): -0.0556149				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	-6.000000	0	
g_{2}	3	0	-5.068043	-6.000000	0	
p_{0,15}	0	0	-10.625174	-0.252464	21	
p_{0,17}	0	0	-21.248887	-1.739734	45	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ {\tt out/231\_dg\_0\_11100\_f\_0\_22\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.389963	-0.252464	-27897.229604	21
$p_{0,17}$	0	0	-55788.944315	-1.739734	-55794.730298	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-51.329686	-51.329686
36	$p_{0,1},$	$p_{0,15},$	3	-43.457169	-43.457169
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.006113	0.006113
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-146.01680313188317

 $\Delta G = \text{-}28.434833748576036$ 

 $\Delta E = \text{-}0.05561486314307889$ 

 $\begin{aligned} |E| &= 8 \\ |U| &= 4 \end{aligned}$