# Summary

December 6, 2024

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# 0.1 Loaded Graphs

### $0.1.1 g_{0}$

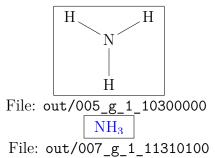
N C H

File: out/001\_g\_0\_10300000

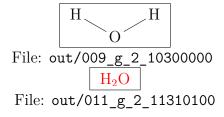
N CH

File: out/003\_g\_0\_11310100

0.1.2 g\_{1}

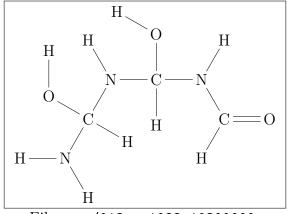


 $0.1.3 g_{2}$ 

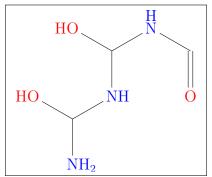


# 0.2 Product Graphs

## $0.2.1 p_{0,56}$



File: out/013\_g\_1088\_10300000

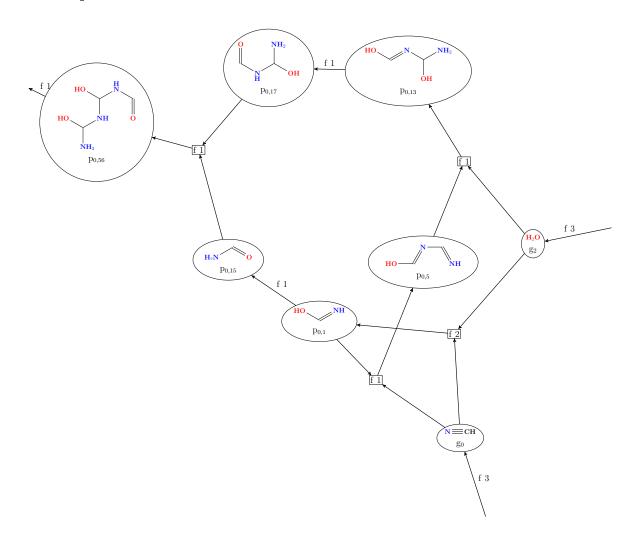


File: out/015\_g\_1088\_11310100

# 0.3 Enumerated Flows

### 0.3.1 Solution 0

Objective value (non-integral): -0.121564					
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	1.000000	33
p_{0,15}	0	0	-10.625174	-1.010180	32
p_{0,17}	0	0	-21.248887	1.000000	34
p_{0,1}	0	0	-10.610101	1.000000	31
p_{0,56}	0	1	-31.869324	-3.000000	67
p_{0,5}	0	0	-16.158998	-3.000000	32



 $File: \ \mathtt{out/031\_dg\_0\_11100\_f\_0\_0\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	31
$p_{0,5}$	0	0	-42425.44262	-3.0	-42435.419975	32
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	33
$p_{0,15}$	0	0	-27896.389963	-1.01018	-27899.749605	32
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	34
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

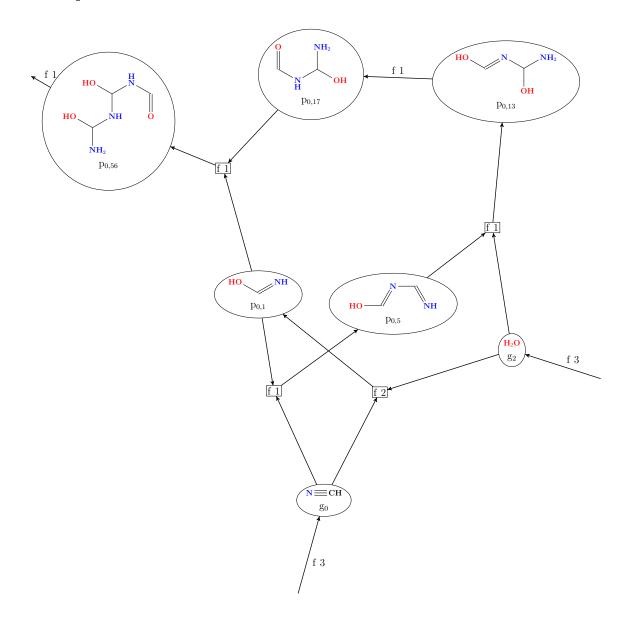
Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-95.803747	-95.803747
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-130.386145	-130.386145
36	$p_{0,1},$	$p_{0,15},$	1	-47.929692	-47.929692
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-23.331853	-23.331853
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
250	$p_{0,13},$	$p_{0,17},$	1	-21.553186	-21.553186
Sum					-319.1652844935788

```
\begin{split} \Delta G &= \text{-}41.48022495830054\\ \Delta E &= \text{-}0.12156363676240757\\ |\mathbf{E}| &= 7\\ |\mathbf{U}| &= 6 \end{split}
```

#### **0.3.2** Solution 1

#### Overall Data

Objective value (non-integral): -0.121564 Vertex/Graph In Out G logK t\_order -5.507152 1.000000 g\_{0} 3 3 g\_{2} 0 -5.068043 1.000000  $p_{0,13}$ 0 0 -21.240678 1.000000 3  $p_{0,17}$ 0 0 -21.248887 1.000000 34 p\_{0,1} 0 0 -10.610101 1.000000 1 p\_{0,56} 0 1 -31.869324 -3.000000 67  $p_{0,5}$ -16.158998 1.000000 2 0 0



 $File: \ \mathtt{out/040\_dg\_0\_11100\_f\_0\_1\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	3
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	34
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	2	-95.803747	-95.803747
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-113.75722	-113.75722
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-39.960779	-39.960779
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-47.923579	-47.923579
250	$p_{0,13}$ ,	$p_{0,17},$	1	-21.553186	-21.553186
Sum					-319.1652844935773

 $\Delta G = -41.48022495830054$ 

 $\Delta E = -0.12156363676240702$ 

|E| = 6

 $|\mathbf{U}| = 5$ 

#### 0.3.3 Solution 2

#### Overall Data

Objective value (non-integral): -0.121564 Vertex/Graph In Out G logK t order g\_{0} 3 0 -5.507141 1.000000 0 g\_{2} 3 0 -5.068043 -3.000000 0 p\_{0,13} -21.240678 1.000000 0  $p_{0,15}$ -10.625174 -3.000000 63 0 0  $p_{0,1}$ 0 0 -10.610080 1.000000 1  $p_{0,56}$ 0 1 -31.869324 0.194685 p\_{0,5} 0 0 -16.158998 -3.000000 2



 $File: \ \mathtt{out/049\_dg\_0\_11100\_f\_0\_2\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14458.99666	1.0	-14455.670875	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,5}$	0	0	-42425.44262	-3.0	-42435.419975	2
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	3
$p_{0,15}$	0	0	-27896.389963	-3.0	-27906.367318	63
$p_{0,56}$	0	1	-83672.898792	0.194685	-83672.251312	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-79.148026	-79.148026
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-130.470776	-130.470776
36	$p_{0,1},$	$p_{0,15},$	1	-56.257547	-56.257547
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-6.702928	-6.702928
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-319.1652844935726

 $\Delta G = -35.17211892164696$ 

 $\Delta E = -0.12156363676240522$ 

|E| = 6

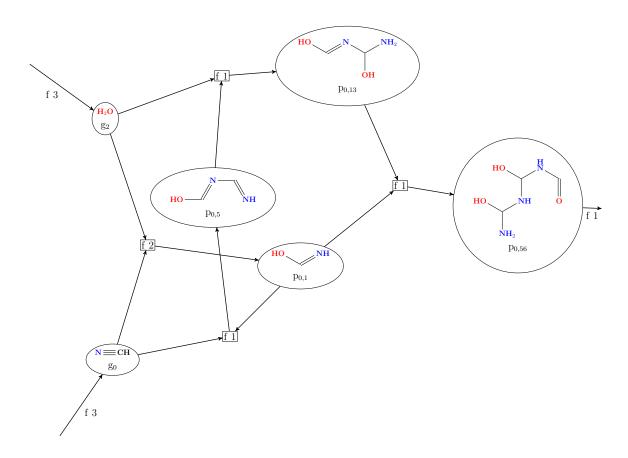
 $|\mathbf{U}| = 5$ 

### 0.3.4 Solution 3

#### Overall Data

Objective value (non-integral): -0.121564

Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	-3.000000	3
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67
p_{0,5}	0	0	-16.158998	1.000000	2



 $File: \verb|out/058_dg_0_11100_f_0_3_filt|$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	3
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	2	-95.803747	-95.803747
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-113.75722	-113.75722
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-56.589704	-56.589704
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-52.84784	-52.84784
Sum					-319.1652844935805

 $\Delta G = \text{-}41.48022522085051$ 

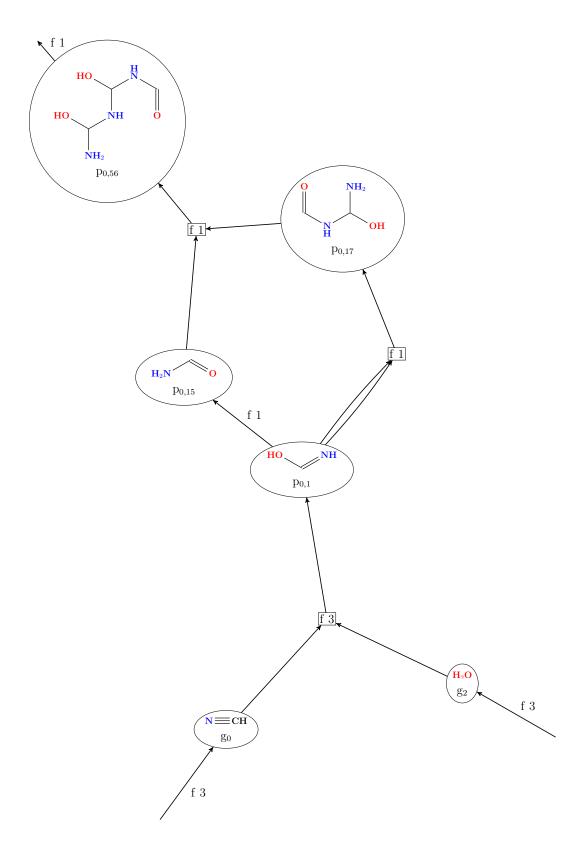
 $\Delta E = \text{-}0.12156363676240822$ 

|E| = 5

|U| = 4

# 0.3.5 Solution 4

Objective val	Lue	(non-integral): -0.085074			
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	-3.00000	0
p_{0,15}	0	0	-10.625195	-0.996759	2
p_{0,17}	0	0	-21.248887	1.000000	64
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67



File: out/067\_dg\_0\_11100\_f\_0\_4\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.445756	-0.996759	-27899.760763	2
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	64
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-79.174822	-79.174822
36	$p_{0,1},$	$p_{0,15},$	1	-47.929692	-47.929692
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-79.467437	-79.467437
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-223.3617209372962

 $\Delta G = -36.491547224819904$ 

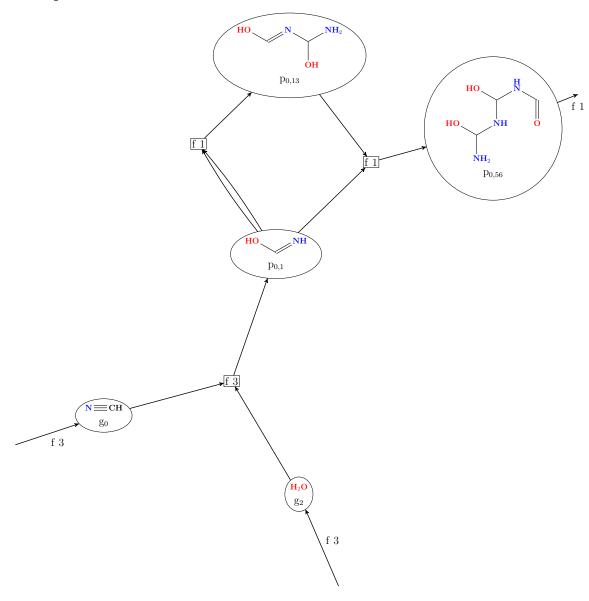
 $\Delta E = \text{-}0.08507398651996566$ 

|E| = 6

|U| = 4

### 0.3.6 Solution 5

Objective val	Lue	(non-integral): -0.085074				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-3.000000	0	
p_{0,13}	0	0	-21.240635	1.000000	65	
p_{0,1}	0	0	-10.610080	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \verb"out/076_dg_0_11100_f_0_5_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-79.119108	-79.119108
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-57.914144	-57.914144
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-69.644013	-69.644013
Sum					-223.36172093729473

 $\begin{array}{l} \Delta G = \text{-}36.491547224819904 \\ \Delta E = \text{-}0.08507398651996509 \end{array}$ 

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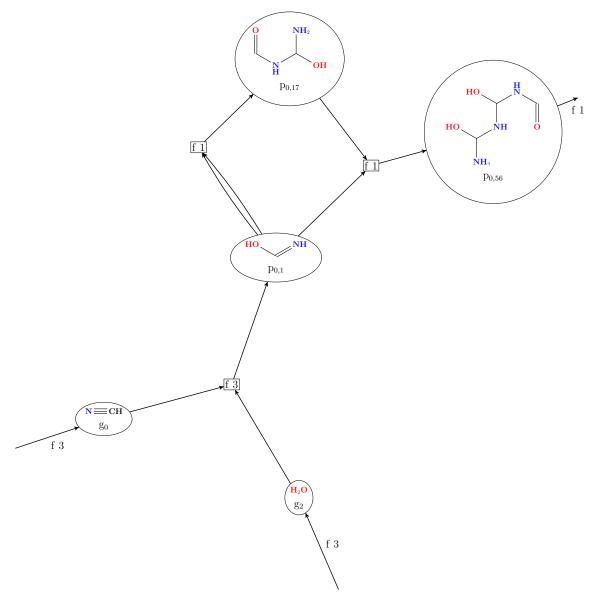
```
\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}
```

#### 0.3.7 Solution 6

#### Overall Data

Objective value (non-integral): -0.085074 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 1.000000  $p_{0,17}$ 0 0 -21.248844 1.000000 65  $p_{0,1}$ 0 0 -10.610080 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -3.000000 67

### Filtered Graph



File: out/085\_dg\_0\_11100\_f\_0\_6\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-95.748033	-95.748033
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-79.467287	-79.467287
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-48.090871	-48.090871
Sum					-223.36172093729473

 $\Delta G = -41.48022495830054$ 

 $\Delta E = \text{-}0.08507398651996509$ 

|E| = 5

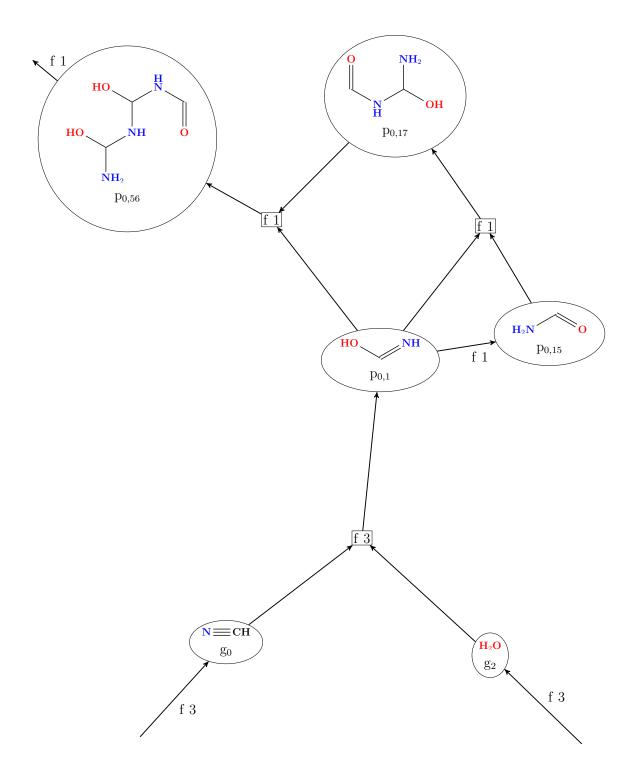
|U| = 3

### 0.3.8 Solution 7

#### Overall Data

Objective value (non-integral): -0.085074

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57
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 $File: \ \mathtt{out/094\_dg\_0\_11100\_f\_0\_7\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	4
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-95.748033	-95.748033
36	$p_{0,1},$	$p_{0,15},$	1	-56.31334	-56.31334
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-23.153947	-23.153947
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-48.090871	-48.090871
Sum					-223.36172093729627

 $\Delta G = \text{-}41.48022469575057$ 

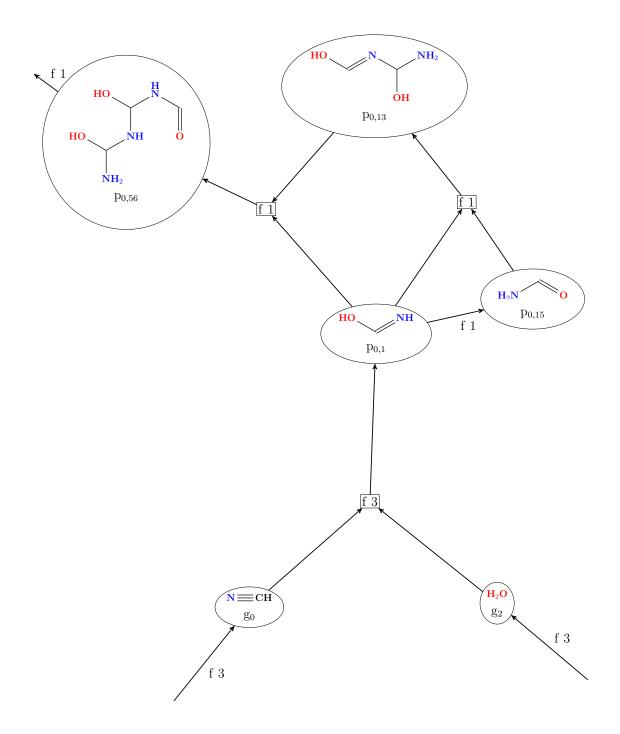
 $\Delta E = \text{-}0.08507398651996567$ 

|E| = 6

|U| = 4

### 0.3.9 Solution 8

Objective val	Lue	(non-integral): -0.085074				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	-3.000000	44	
p_{0,15}	0	0	-10.625195	-3.000000	42	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ {\tt out/103\_dg\_0\_11100\_f\_0\_8\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	44
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	42
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-95.803747	-95.803747
36	$p_{0,1},$	$p_{0,15},$	1	-56.257627	-56.257627
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-18.28555	-18.28555
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-52.84784	-52.84784
Sum					-223.36172093729326

 $\Delta G = -41.48022548340047$ 

 $\Delta E = \text{-}0.08507398651996453$ 

|E| = 6

|U| = 4

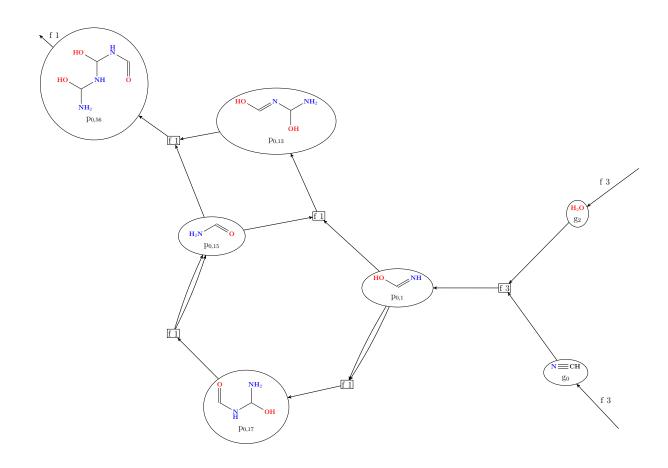
### 0.3.10 Solution 9

### Overall Data

Objective value (non-integral): -0.085074

Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507141	1.000000	0
g_{2}	3	0	-5.068033	1.000000	10
p_{0,13}	0	0	-21.240678	-3.000000	39
p_{0,15}	0	0	-10.625174	0.961318	27
p_{0,17}	0	0	-21.248887	1.000000	26
p_{0,1}	0	0	-10.610080	1.000000	11
p_{0,56}	0	1	-31.869324	-3.000000	67

### Filtered Graph



File: out/112\_dg\_0\_11100\_f\_0\_9\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14458.99666	1.0	-14455.670875	0
$g_2$	3	0	-13306.118349	1.0	-13302.792564	10
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	11
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	39
$p_{0,15}$	0	0	-27896.389963	0.961318	-27893.192826	27
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	26
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-95.803564	-95.803564
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-79.578865	-79.578865
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	-13.114121	-13.114121
192	$p_{0,1}, p_{0,15},$	$p_{0,13}$ ,	1	-34.865172	-34.865172
237	$p_{0,17},$	$p_{0,15}, p_{0,15},$	1	0.0	0.0
Sum					-223.36172093729323

 $\Delta G = -41.496884016063$ 

 $\Delta E = -0.08507398651996452$ 

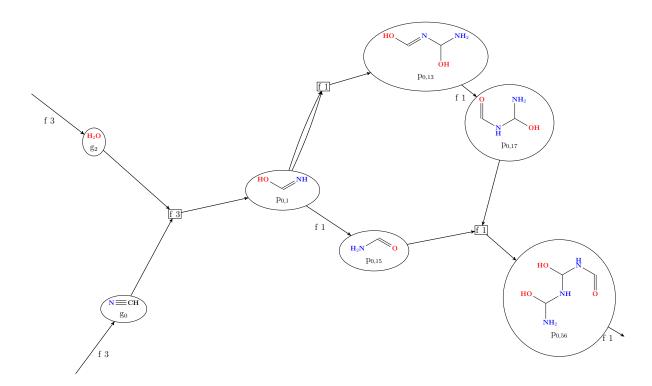
|E| = 7

 $|\mathbf{U}| = 5$ 

#### 0.3.11 Solution 10

#### Overall Data

Objective value (non-integral): -0.085074 Vertex/Graph In Out G t\_order logK g\_{0} 3 0 -5.507152 1.000000 g\_{2} 3 0 -5.068043 -3.000000 0  $p_{0,13}$ 0 0 -21.240635 1.000000 p\_{0,15} 0 0 -10.625174 1.000000  $p_{0,17}$ -21.248844 1.000000 64 0 0  $p_{0,1}$ 0 0 -10.610101 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -3.000000 67



File: out/121\_dg\_0\_11100\_f\_0\_10\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	3
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	64
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-79.174822	-79.174822
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-57.802717	-57.802717
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	-8.462249	-8.462249
250	$p_{0,13},$	$p_{0,17},$	1	-21.553143	-21.553143
Sum					-223.36172093729306

 $\Delta G = \text{-}36.49154696226994$ 

 $\Delta E = \text{-}0.08507398651996445$ 

|E| = 7

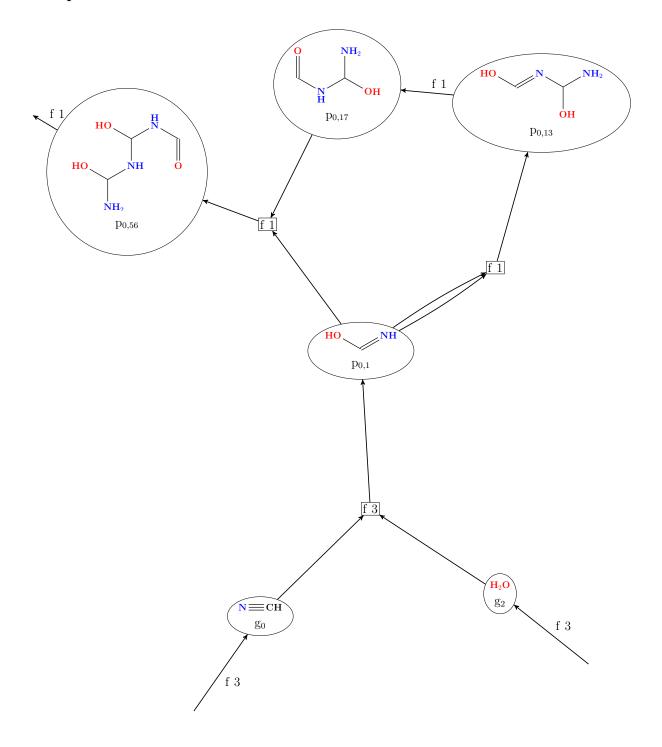
|U| = 5

### 0.3.12 Solution 11

#### Overall Data

Objective value (non-integral): -0.085074

```
Vertex/Graph In Out G
                              logK
                                        t_order
g_{0}
            3 0
                   -5.507152 1.000000
g_{2}
            3 0
                   -5.068043 -3.000000 0
p<sub>{0,13}</sub>
            0 0 -21.240635 1.000000
p_{0,17}
            0 0 -21.248844 1.000000
                                        65
p_{0,1}
            0 0
                  -10.610080 1.000000
p_{0,56}
                  -31.869324 -3.000000 67
            0 1
```



 $File: \ \mathtt{out/130\_dg\_0\_11100\_f\_0\_11\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	3
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-79.119108	-79.119108
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-57.914144	-57.914144
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-48.090871	-48.090871
250	$p_{0,13},$	$p_{0,17},$	1	-21.553143	-21.553143
Sum					-223.36172093729155

 $\Delta G = -36.491547224819904$ 

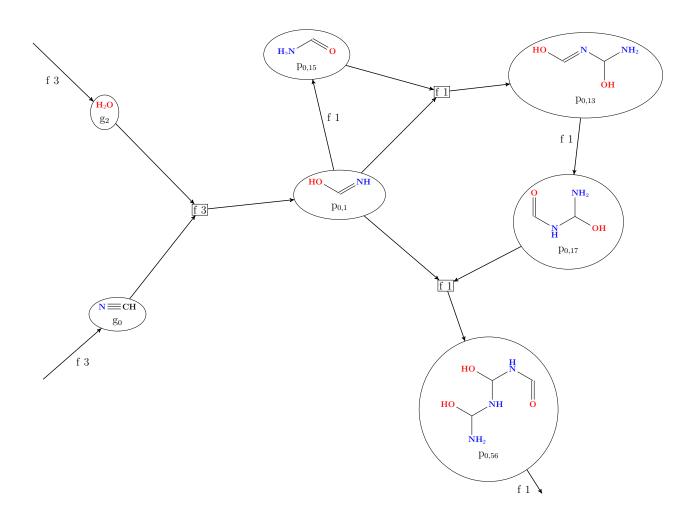
 $\Delta E = \text{-}0.08507398651996388$ 

|E| = 6

|U| = 4

### 0.3.13 Solution 12

Objective val	lue	n-integral)	: -0.085074	1	
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240635	1.000000	4
p_{0,15}	0	0	-10.625195	-3.000000	2
p_{0,17}	0	0	-21.248844	1.000000	5
p_{0,1}	0	0	-10.610080	1.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67



File: out/139\_dg\_0\_11100\_f\_0\_12\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	4
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	5
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-95.748033	-95.748033
36	$p_{0,1},$	$p_{0,15},$	1	-56.31334	-56.31334
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-1.600804	-1.600804
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-48.090871	-48.090871
250	$p_{0,13},$	$p_{0,17},$	1	-21.553143	-21.553143
Sum					-223.3617209372901

 $\Delta G = \text{-}41.48022443320061$ 

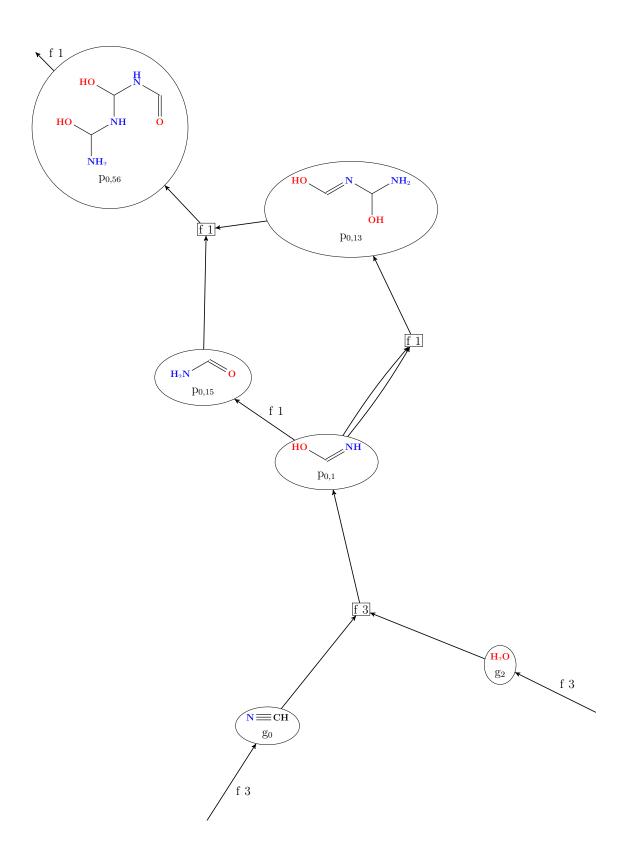
 $\Delta E = \text{-}0.08507398651996333$ 

 $\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}$ 

### 0.3.14 Solution 13

#### Overall Data

Objective value (non-integral): -0.085074 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 -3.000000 0 g\_{2} 3 0 -5.068043 -3.000000 0 p\_{0,13} 0 0 -21.240678 -2.181264 64 p\_{0,15} 0 0 -10.625195 -3.000000 2 p\_{0,1} 0 0 -10.610101 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -3.000000 67



 $File: \ {\tt out/148\_dg\_0\_11100\_f\_0\_13\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-3.0	-14469.002933	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.391129	-2.181264	-55774.645545	64
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	2
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-62.545896	-62.545896
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-71.139503	-71.139503
36	$p_{0,1},$	$p_{0,15},$	1	-56.257627	-56.257627
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-223.3617209372869

 $\Delta G = -31.502869753889232$ 

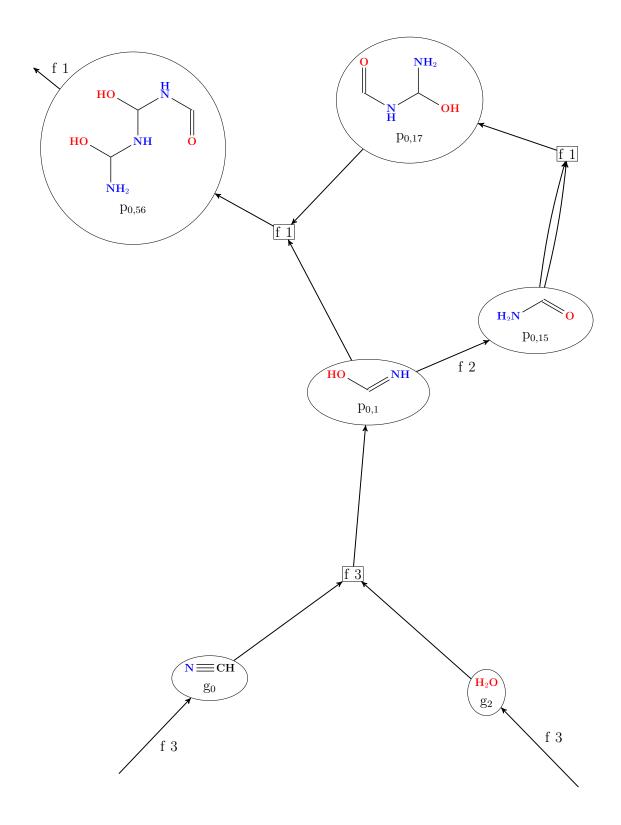
 $\Delta E = \text{-}0.0850739865199621$ 

|E| = 6

|U| = 4

### 0.3.15 Solution 14

Objective val	Lue	(non-integral): -0.0699802			
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,15}	0	0	-10.625174	0.974002	32
p_{0,17}	0	0	-21.248844	1.000000	65
p_{0,1}	0	0	-10.610080	1.000000	1
p {0,56}	0	1	-31.869324	-3.000000	67



 $File: \ {\tt out/157\_dg\_0\_11100\_f\_0\_14\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.389963	0.974002	-27893.15064	32
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-95.748033	-95.748033
36	$p_{0,1},$	$p_{0,15},$	2	-39.7367	-39.7367
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.006113	0.006113
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-48.090871	-48.090871
Sum					-183.73309883350115

 $\Delta G = -41.48022469575057$ 

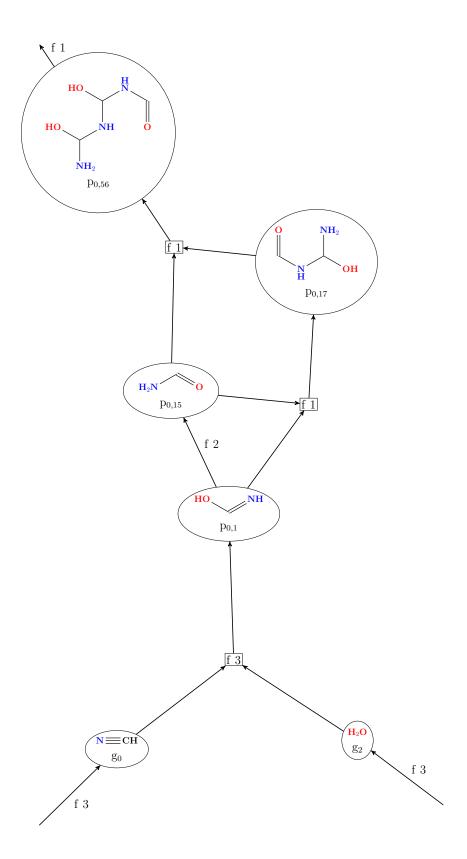
 $\Delta E = \text{-}0.06998024150172455}$ 

|E| = 7

|U| = 4

### 0.3.16 Solution 15

Objective val	lue	(non-integral): -0.0699802				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-3.000000	0	
p_{0,15}	0	0	-10.625195	-0.996759	2	
p_{0,17}	0	0	-21.248887	1.000000	4	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ \mathtt{out/166\_dg\_0\_11100\_f\_0\_15\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.445756	-0.996759	-27899.760763	2
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	4
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-79.174822	-79.174822
36	$p_{0,1},$	$p_{0,15},$	2	-47.929692	-47.929692
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-31.537745	-31.537745
Sum					-183.73309883350115

 $\Delta G = -36.49154696226994$ 

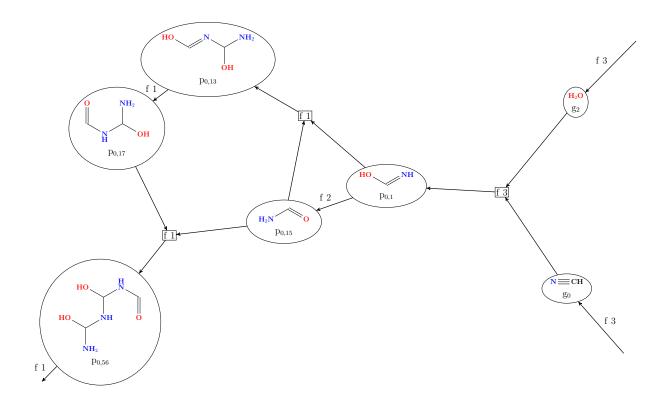
 $\Delta E = \text{-}0.06998024150172455}$ 

|E| = 7

|U| = 4

### 0.3.17 Solution 16

Objective val	Lue	(non-integral): -0.0699802				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240635	1.000000	4	
p_{0,15}	0	0	-10.625174	1.000000	2	
p_{0,17}	0	0	-21.248887	-1.008710	64	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ {\tt out/175\_dg\_0\_11100\_f\_0\_16\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	4
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.944315	-1.00871	-55792.299066	64
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-95.803747	-95.803747
36	$p_{0,1},$	$p_{0,15},$	2	-39.572909	-39.572909
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-18.229808	-18.229808
250	$p_{0,13}$ ,	$p_{0,17}$	1	-30.015391	-30.015391
Sum					-183.73309883349495

 $\Delta G = \text{-}41.48022495830054$ 

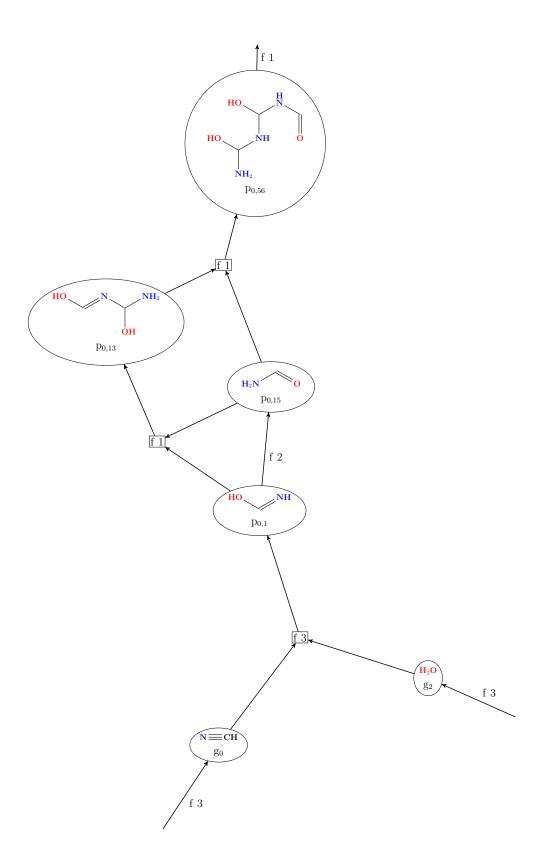
 $\Delta E = -0.06998024150172219$ 

|E| = 8

|U| = 5

### 0.3.18 Solution 17

Objective value (non-integral): -0.0699802						
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	-3.000000	44	
p_{0,15}	0	0	-10.625174	1.000000	22	
p_{0,1}	0	0	-10.610080	1.000000	21	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ \mathtt{out/184\_dg\_0\_11100\_f\_0\_17\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	44
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	22
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-95.748033	-95.748033
36	$p_{0,1},$	$p_{0,15},$	2	-39.628622	-39.628622
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	-13.274931	-13.274931
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-35.025982	-35.025982
Sum					-183.73309883348878

 $\Delta G = \text{-}41.48022469575057$ 

 $\Delta E = \text{-}0.06998024150171984$ 

 $\begin{aligned} |E| &= 7 \\ |U| &= 4 \end{aligned}$