# Summary

December 6, 2024

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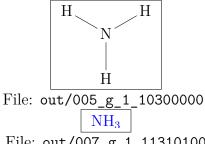
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#### 0.1 Loaded Graphs

#### 0.1.1g\_{0}

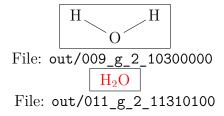
 $N \equiv C - H$ File: out/001\_g\_0\_10300000  $N \equiv CH$ File: out/003\_g\_0\_11310100

0.1.2 g\_{1}



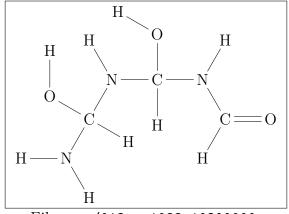
File: out/007\_g\_1\_11310100

0.1.3g\_{2}

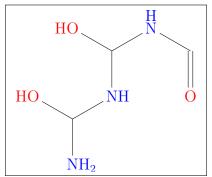


#### **Product Graphs** 0.2

#### 0.2.1p\_{0,56}



File: out/013\_g\_1088\_10300000

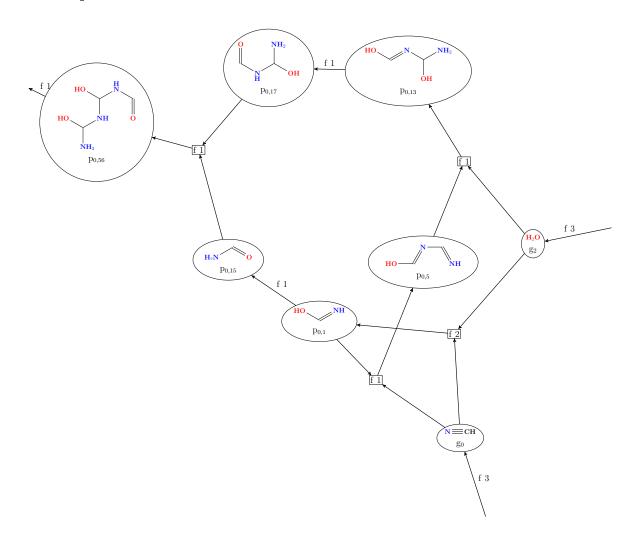


File: out/015\_g\_1088\_11310100

# 0.3 Enumerated Flows

# 0.3.1 Solution 0

Objective value (non-integral): -0.118581						
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	1.000000	10	
p_{0,15}	0	0	-10.625174	1.000000	55	
p_{0,17}	0	0	-21.248887	-1.622626	11	
p_{0,1}	0	0	-10.610080	1.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	
p_{0,5}	0	0	-16.158998	-6.000000	9	



 $File: \ \mathtt{out/031\_dg\_0\_11100\_f\_0\_0\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,5}$	0	0	-42425.44262	-6.0	-42445.397331	9
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	10
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	55
$p_{0,17}$	0	0	-55788.944315	-1.622626	-55794.340821	11
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

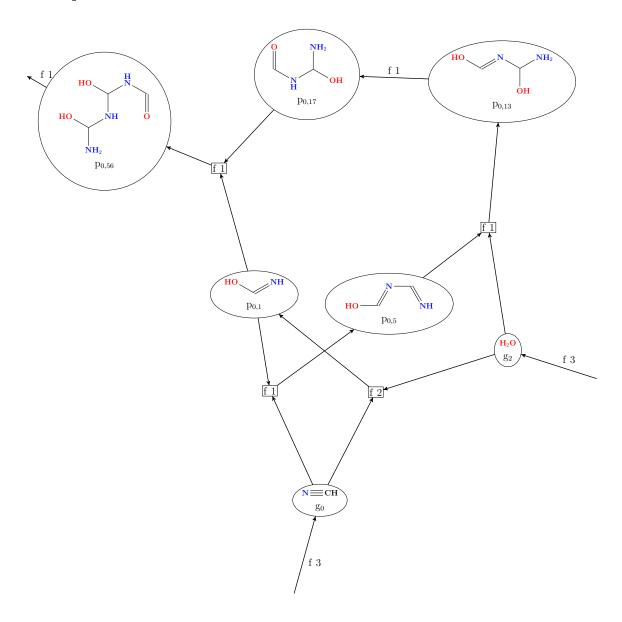
Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-93.902223	-93.902223
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-128.147067	-128.147067
36	$p_{0,1},$	$p_{0,15},$	1	-39.628622	-39.628622
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-21.935024	-21.935024
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
250	$p_{0,13}$ ,	$p_{0,17},$	1	-27.615178	-27.615178
Sum					-311.3330607073006

```
\begin{split} \Delta G &= \text{-}40.5124214202443\\ \Delta E &= \text{-}0.11858050026964104\\ |\mathbf{E}| &= 7\\ |\mathbf{U}| &= 6 \end{split}
```

#### 0.3.2 Solution 1

#### Overall Data

Objective value (non-integral): -0.118581 Vertex/Graph In Out G logK t\_order -5.507152 1.000000 g\_{0} 3 3 0 g\_{2} -5.068043 1.000000  $p_{0,13}$ 0 0 -21.240678 1.000000 64  $p_{0,17}$ 0 0 -21.248887 -6.000000 65 p\_{0,1} 0 0 -10.610101 1.000000 1 p\_{0,56} 0 1 -31.869324 -6.000000 67 p\_{0,5} -16.158998 1.000000 2 0 0



 $File: \ \mathtt{out/040\_dg\_0\_11100\_f\_0\_1\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	64
$p_{0,17}$	0	0	-55788.944315	-6.0	-55808.899025	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	2	-93.957936	-93.957936
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-111.911409	-111.911409
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.114968	-38.114968
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-29.448843	-29.448843
250	$p_{0,13},$	$p_{0,17},$	1	-37.73313	-37.73313
Sum					-311.33306070730197

 $\Delta G = -40.5124214202443$ 

 $\Delta E = -0.11858050026964156$ 

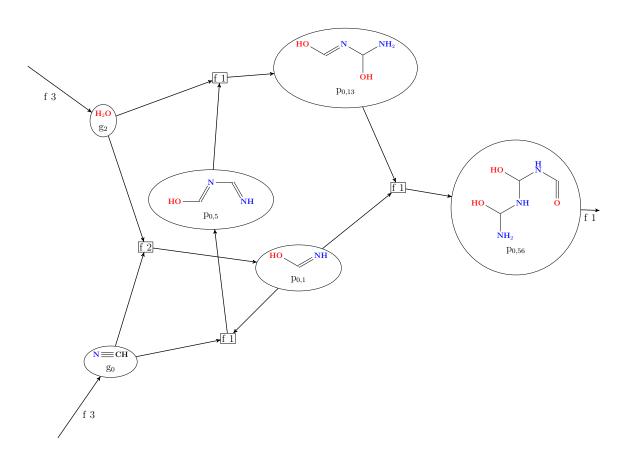
|E| = 6

|U| = 5

#### 0.3.3 Solution 2

#### Overall Data

Objective value (non-integral): -0.118581 Vertex/Graph In Out G logK t order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,13} -21.240678 -6.000000 24 0  $p_{0,1}$ 0 0 -10.610101 -6.000000 22  $p_{0,56}$ -31.869260 1.000000 67 0 1 p\_{0,5} 0 0 -16.158998 1.000000 23



 $File: \ \mathtt{out/049\_dg\_0\_11100\_f\_0\_2\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-6.0	-27876.771765	22
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	23
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	24
$p_{0,56}$	0	1	-83672.731446	1.0	-83669.405661	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-93.957936	-93.957936
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-95.731465	-95.731465
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.114968	-38.114968
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-18.474795	-18.474795
Sum					-311.33306070729867

 $\Delta G = \text{-}34.02370910124065$ 

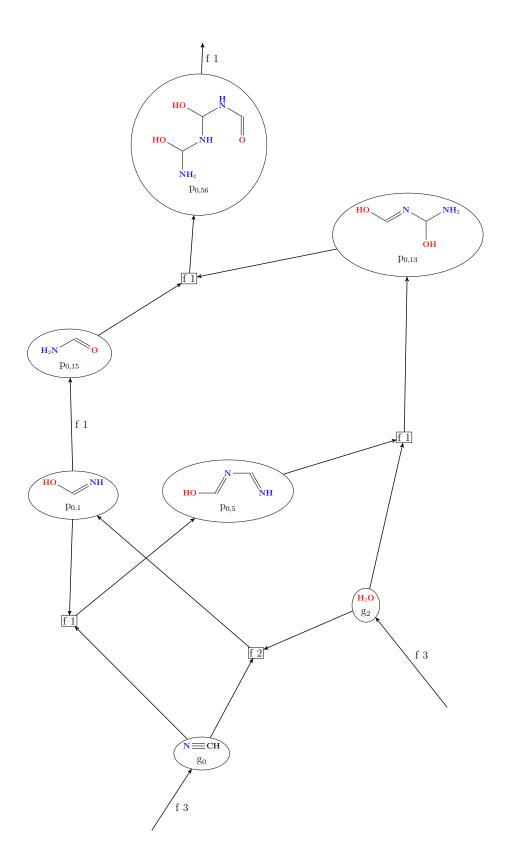
 $\Delta E = \text{-}0.11858050026964032$ 

|E| = 5

|U| = 4

# **0.3.4** Solution 3

Objective val	lue	(non-integral): -0.118581			
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	-6.000000	3
p_{0,15}	0	0	-10.625195	1.000000	2
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-1.076863	67
p_{0,5}	0	0	-16.158998	-6.000000	2



 $File: \ \mathtt{out/058\_dg\_0\_11100\_f\_0\_3\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	-6.0	-42445.397331	2
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	3
$p_{0,15}$	0	0	-27896.445756	1.0	-27893.119971	2
$p_{0,56}$	0	1	-83672.898792	-1.076863	-83676.480206	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	2	-93.957936	-93.957936
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-128.091353	-128.091353
36	$p_{0,1},$	$p_{0,15},$	1	-39.628701	-39.628701
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.114968	-38.114968
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-311.3330607072973

 $\Delta G = -39.374477366500884$ 

 $\Delta E = -0.11858050026963979$ 

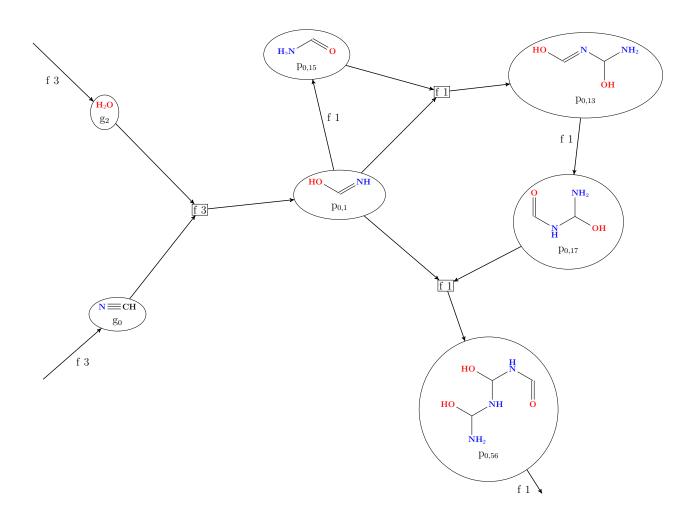
|E| = 6

|U| = 5

#### 0.3.5 Solution 4

#### Overall Data

Objective value (non-integral): -0.0827939 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 0 p\_{0,13} 0 0 -21.240635 1.000000 4  $p_{0,15}$ -10.625195 -6.000000 2 0 0 p\_{0,17} 0 0 -21.248844 -6.000000 65 -10.610080 1.000000 1  $p_{0,1}$ 0  $p_{0,56}$ -31.869324 -6.000000 67



 $File: \verb"out/067_dg_0_11100_f_0_4_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	4
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	2
$p_{0,17}$	0	0	-55788.832737	-6.0	-55808.787447	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-77.722278	-77.722278
36	$p_{0,1},$	$p_{0,15},$	1	-55.864359	-55.864359
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-0.203974	-0.203974
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-29.616135	-29.616135
250	$p_{0,13}$ ,	$p_{0,17},$	1	-37.733087	-37.733087
Sum					-217.37530785222552

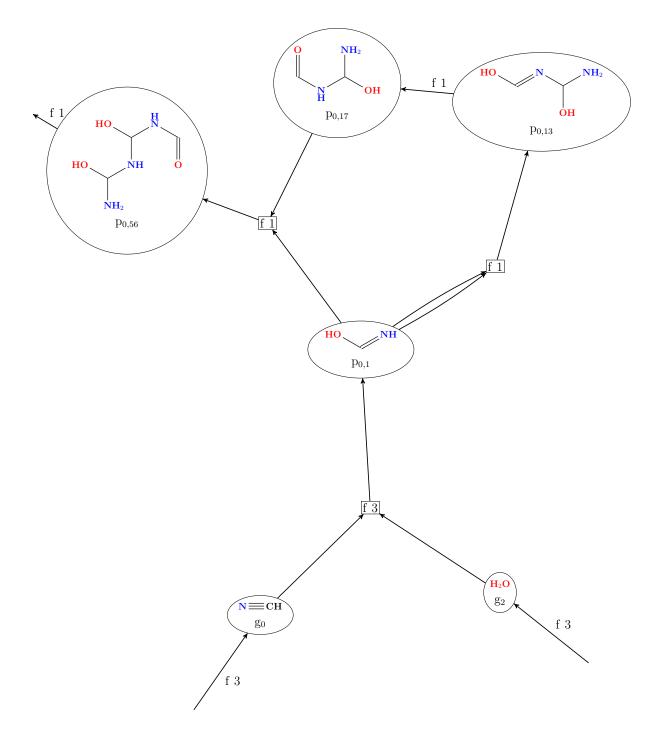
 $\Delta G = \text{-}35.65843785691816$ 

 $\Delta E = \text{-}0.08279388219427763}$ 

 $\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}$ 

# 0.3.6 Solution 5

Objective val	Lue	(non-integral): -0.0827939					
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	1.000000	0		
p_{0,13}	0	0	-21.240635	1.000000	64		
p_{0,17}	0	0	-21.248887	1.000000	65		
p_{0,1}	0	0	-10.610080	1.000000	1		
p_{0,56}	0	1	-31.869324	-6.000000	67		



 $File: \verb"out/076_dg_0_11100_f_0_5_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	64
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-93.902223	-93.902223
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.068333	-56.068333
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$ ,	1	-45.684501	-45.684501
250	$p_{0,13}$ ,	$p_{0,17},$	1	-21.664721	-21.664721
Sum					-217.37530785222415

 $\Delta G = -40.5124214202443$ 

 $\Delta E = \text{-}0.08279388219427711}$ 

|E| = 6

|U| = 4

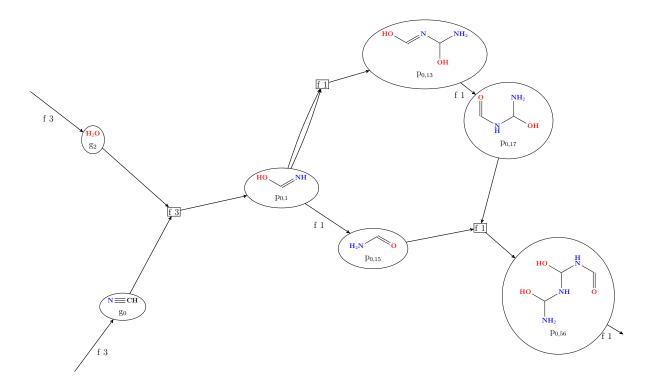
## 0.3.7 Solution 6

### Overall Data

Objective value (non-integral): -0.0827939

Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	20
p_{0,13}	0	0	-21.240635	1.000000	43
p_{0,15}	0	0	-10.625174	1.000000	22
p_{0,17}	0	0	-21.248887	1.000000	44
p_{0,1}	0	0	-10.610101	1.000000	21
p_{0,56}	0	1	-31.869324	-6.000000	67

### Filtered Graph



File: out/085\_dg\_0\_11100\_f\_0\_6\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	20
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	21
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	43
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	22
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	44
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.957936	-93.957936
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-55.956906	-55.956906
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	-6.055879	-6.055879
250	$p_{0,13}$ ,	$p_{0,17},$	1	-21.664721	-21.664721
Sum					-217.37530785222276

 $\Delta G = -40.51242089514438$ 

 $\Delta E = -0.08279388219427658$ 

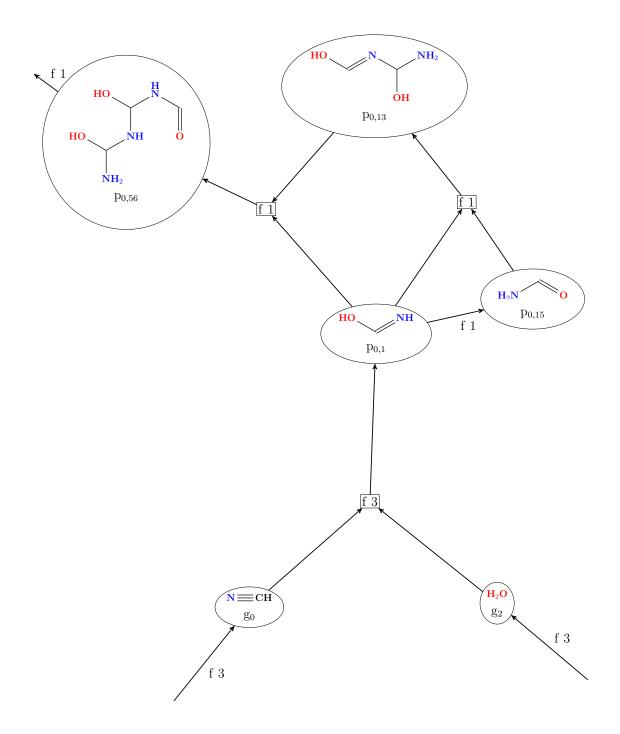
|E| = 7

|U| = 5

#### 0.3.8 Solution 7

#### Overall Data

Objective value (non-integral): -0.0827939 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 g\_{2} 3 0 -5.068043 1.000000 0 p\_{0,13} 0 0 -21.240678 -6.000000 45 p\_{0,15} -10.625174 1.000000 22 0 0 p\_{0,1} -10.610101 1.000000 0 21 -31.869324 -6.000000 67  $p_{0,56}$ 1



 $File: \verb"out/094_dg_0_11100_f_0_7_filt"$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	21
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	45
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	22
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-93.957936	-93.957936
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-32.675476	-32.675476
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-51.002029	-51.002029
Sum					-217.37530785222225

 $\Delta G = -40.51242115769434$ 

 $\Delta E = -0.08279388219427639$ 

|E| = 6

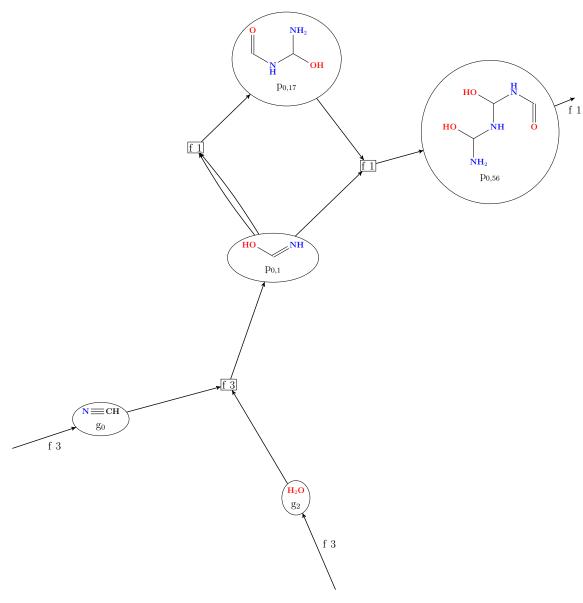
|U| = 4

# 0.3.9 Solution 8

## Overall Data

Objective value (non-integral): -0.0827939

Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	20
p_{0,17}	0	0	-21.248844	1.000000	43
p_{0,1}	0	0	-10.610080	1.000000	21
p_{0,56}	0	1	-31.869324	-6.000000	67



 $File: \ \mathtt{out/103\_dg\_0\_11100\_f\_0\_8\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	20
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	43
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.902223	-93.902223
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-77.621476	-77.621476
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-45.796079	-45.796079
Sum					-217.37530785222086

 $\Delta G = \text{-}40.5124214202443$ 

 $\Delta E = \text{-}0.08279388219427586$ 

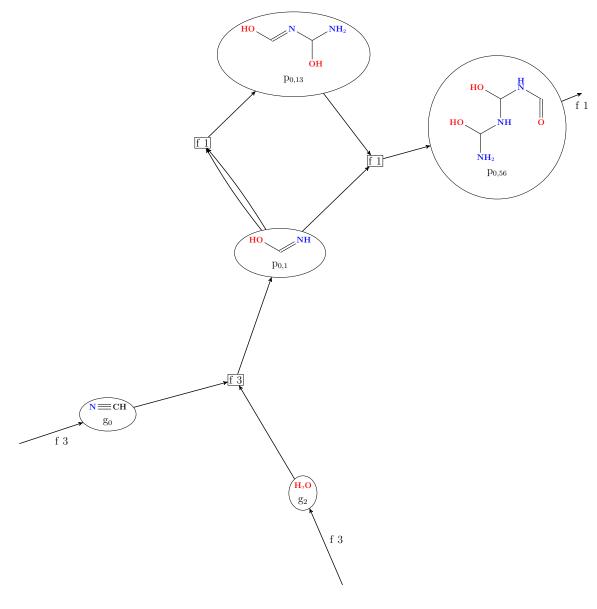
```
\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}
```

## 0.3.10 Solution 9

#### Overall Data

Objective value (non-integral): -0.0827939 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 1.000000  $p_{0,13}$ 0 0 -21.240635 1.000000 65  $p_{0,1}$ 0 0 -10.610080 1.000000 1  $p_{0,56}$ 0 1 -31.869324 -6.000000 67

### Filtered Graph



File: out/112\_dg\_0\_11100\_f\_0\_9\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	65
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-93.902223	-93.902223
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.068333	-56.068333
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$ ,	1	-67.349222	-67.349222
Sum					-217.37530785222086

 $\Delta G = -40.5124214202443$ 

 $\Delta E = \text{-}0.08279388219427586$ 

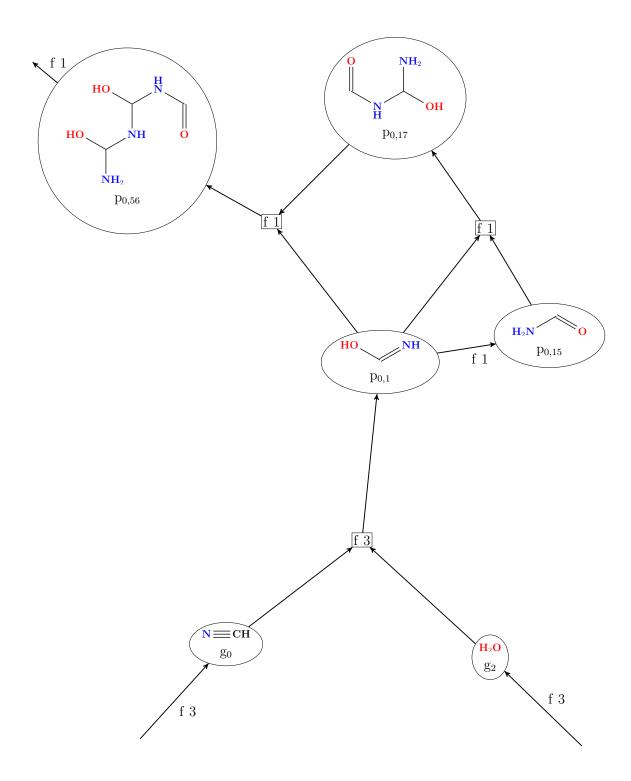
|E| = 5

|U| = 3

### 0.3.11 Solution 10

#### Overall Data

Objective value (non-integral): -0.0827939 Vertex/Graph In Out G logK t\_order g\_{0} 3 0 -5.507152 1.000000 0 g\_{2} 3 0 -5.068043 -6.000000 20 p\_{0,15} 0 0 -10.625195 -6.000000 23 -21.248844 1.000000 45  $p_{0,17}$ 0 0 p\_{0,1} 0 0 -10.610080 1.000000 21  $p_{0,56}$ 0 1 -31.869324 -6.000000 67



 ${\rm File:} \ {\tt out/121\_dg\_0\_11100\_f\_0\_10\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	20
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	23
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-77.722278	-77.722278
36	$p_{0,1},$	$p_{0,15},$	1	-55.864359	-55.864359
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-21.757117	-21.757117
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-45.796079	-45.796079
Sum					-217.37530785222881

 $\Delta G = -35.6584383820181$ 

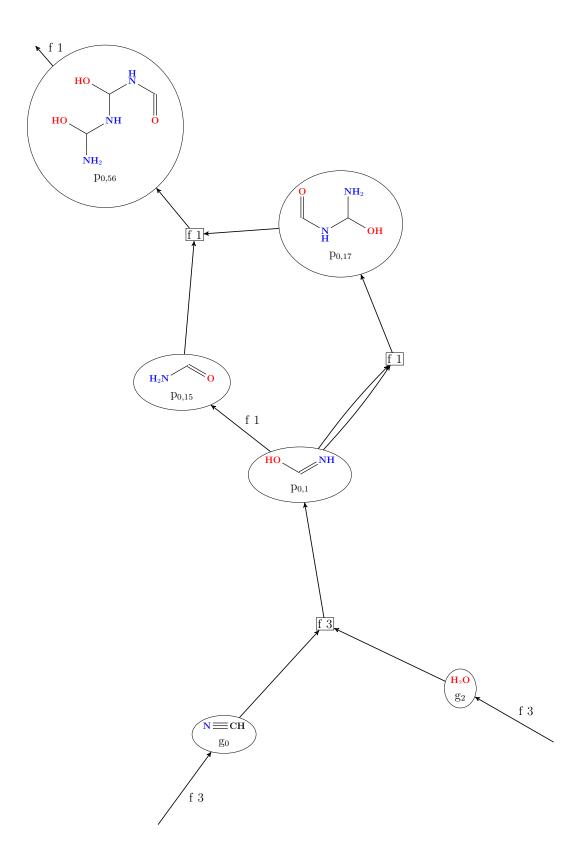
 $\Delta E = \text{-}0.08279388219427888}$ 

|E| = 6

|U| = 4

# 0.3.12 Solution 11

Objective val	Lue	(non-integral): -0.0827939				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-6.000000	0	
p_{0,15}	0	0	-10.625195	-1.598488	22	
p_{0,17}	0	0	-21.248887	1.000000	44	
p_{0,1}	0	0	-10.610101	1.000000	21	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ \mathtt{out/130\_dg\_0\_11100\_f\_0\_11\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	21
$p_{0,15}$	0	0	-27896.445756	-1.598488	-27901.761984	22
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	44
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-77.777992	-77.777992
36	$p_{0,1},$	$p_{0,15},$	1	-45.634901	-45.634901
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-77.621627	-77.621627
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-217.37530785221946

 $\Delta G = -35.6584383820181$ 

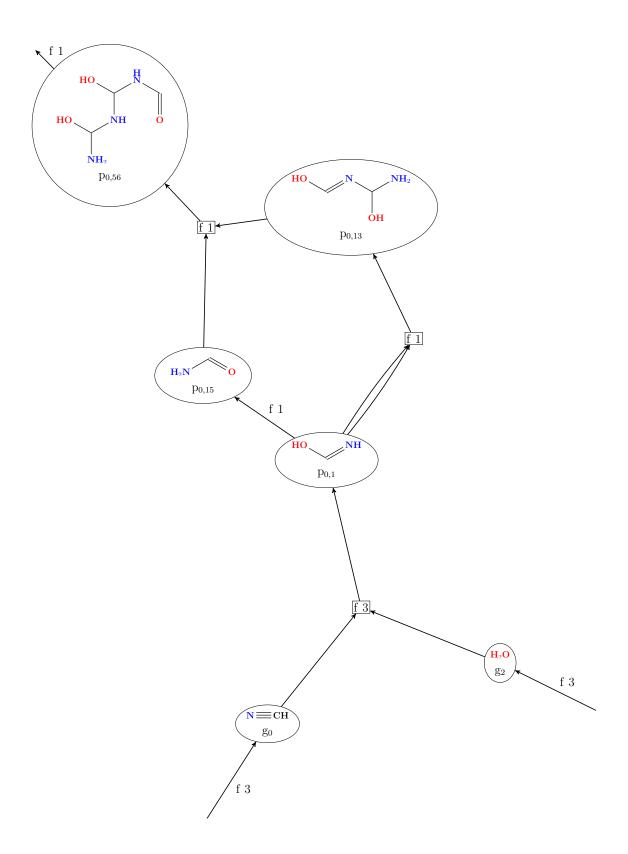
 $\Delta E = -0.08279388219427533$ 

|E| = 6

|U| = 4

# 0.3.13 Solution 12

Objective val	lue	(non-integral): -0.0827939				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,13}	0	0	-21.240678	-3.923137	3	
p_{0,15}	0	0	-10.625195	-6.000000	2	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ \mathtt{out/139\_dg\_0\_11100\_f\_0\_12\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.391129	-3.923137	-55780.43864	3
$p_{0,15}$	0	0	-27896.445756	-6.0	-27916.400466	2
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.957936	-93.957936
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-67.447882	-67.447882
36	$p_{0,1},$	$p_{0,15},$	1	-55.808646	-55.808646
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-217.37530785221946

 $\Delta G = \text{-}40.5124214202443$ 

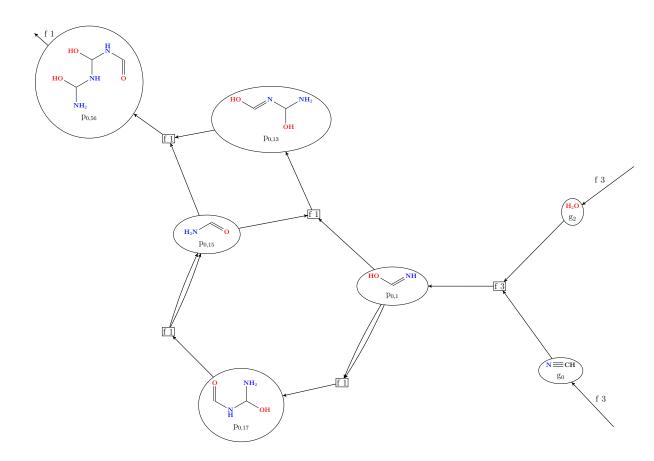
 $\Delta E = -0.08279388219427533$ 

|E| = 6

|U| = 4

# 0.3.14 Solution 13

Objective val	lue	(non-integral): -0.0827939				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-6.000000	0	
p_{0,13}	0	0	-21.240678	-4.904048	34	
p_{0,15}	0	0	-10.625195	-5.019089	32	
p_{0,17}	0	0	-21.248887	-6.000000	31	
p_{0,1}	0	0	-10.610101	-6.000000	1	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ \mathtt{out/148\_dg\_0\_11100\_f\_0\_13\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-6.0	-27876.771765	1
$p_{0,13}$	0	0	-55767.391129	-4.904048	-55783.700939	34
$p_{0,15}$	0	0	-27896.445756	-5.019089	-27913.138167	32
$p_{0,17}$	0	0	-55788.944315	-6.0	-55808.899025	31
$p_{0.56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.957936	-93.957936
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-61.441682	-61.441682
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	0.006113	0.006113
192	$p_{0,1}, p_{0,15},$	$p_{0,13}$ ,	1	0.006113	0.006113
237	$p_{0,17},$	$p_{0,15}, p_{0,15},$	1	-13.281125	-13.281125
Sum					-217.37530785221895

 $\Delta G = -35.65843811946813$ 

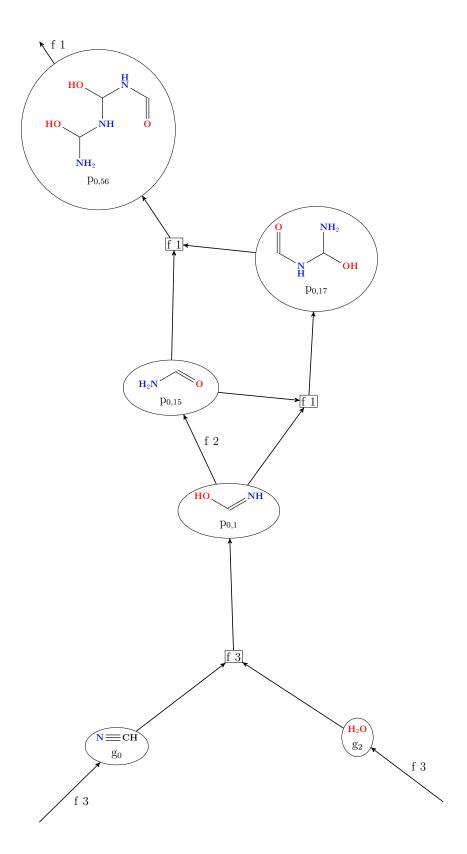
 $\Delta E = \text{-}0.08279388219427514$ 

|E| = 7

|U| = 5

# 0.3.15 Solution 14

Objective value (non-integral): -0.0677001					
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	-6.000000	0
g_{2}	3	0	-5.068043	-6.000000	0
p_{0,15}	0	0	-10.625195	-1.646761	2
p_{0,17}	0	0	-21.248844	1.000000	4
p_{0,1}	0	0	-10.610101	-6.000000	1
p_{0,56}	0	1	-31.869324	-6.000000	67



 $File: \ {\tt out/157\_dg\_0\_11100\_f\_0\_14\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	-6.0	-14478.980288	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-6.0	-27876.771765	1
$p_{0,15}$	0	0	-27896.445756	-1.646761	-27901.922528	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	4
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-77.777992	-77.777992
36	$p_{0,1},$	$p_{0,15},$	2	-29.566534	-29.566534
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-15.583626	-15.583626
Sum					-177.7466857484337

 $\Delta G = -30.80445508124192$ 

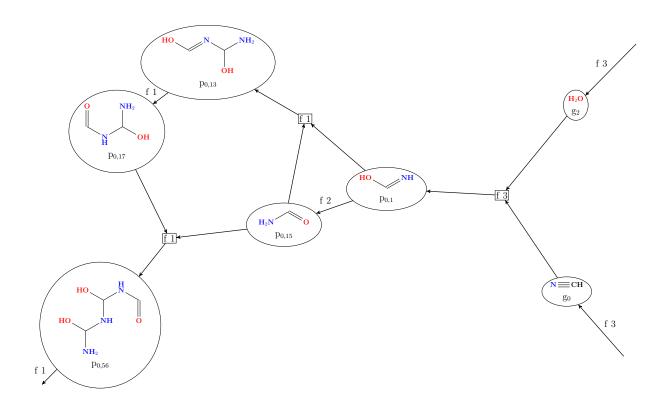
 $\Delta E = \text{-}0.06770013717603776$ 

|E| = 7

|U| = 4

# 0.3.16 Solution 15

Objective val	lue	(non-integral): -0.0677001				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-6.000000	0	
p_{0,13}	0	0	-21.240635	1.000000	42	
p_{0,15}	0	0	-10.625174	1.000000	21	
p_{0,17}	0	0	-21.248887	-1.619981	45	
p_{0,1}	0	0	-10.610101	-6.000000	20	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ \mathtt{out/166\_dg\_0\_11100\_f\_0\_15\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.817054	-6.0	-27876.771765	20
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	42
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	21
$p_{0,17}$	0	0	-55788.944315	-1.619981	-55794.332025	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.957936	-93.957936
36	$p_{0,1},$	$p_{0,15},$	2	-23.392964	-23.392964
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-0.204053	-0.204053
250	$p_{0,13}$ ,	$p_{0,17},$	1	-27.7206	-27.7206
Sum					-177.74668574843042

 $\Delta G = -35.6584375943682$ 

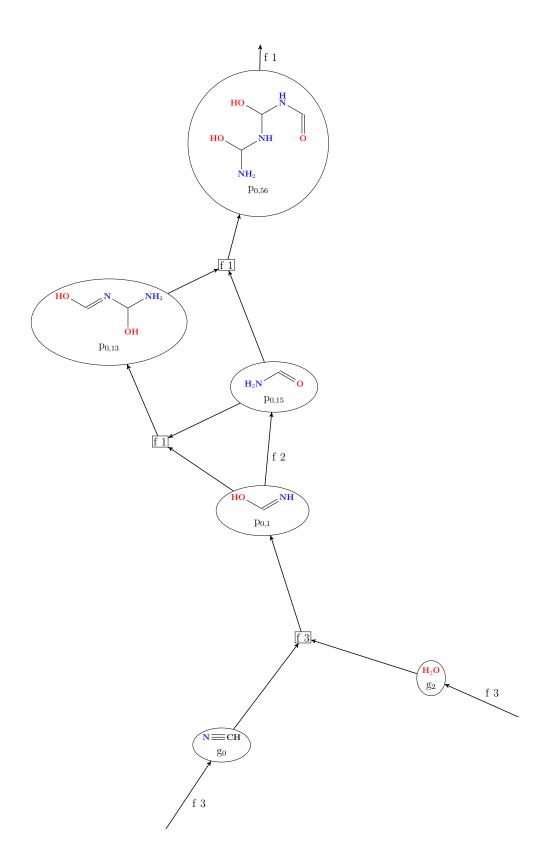
 $\Delta E = \text{-}0.06770013717603651$ 

|E| = 8

|U| = 5

# 0.3.17 Solution 16

Objective value (non-integral): -0.0677001							
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	1.000000	0		
p_{0,13}	0	0	-21.240678	-6.000000	64		
p_{0,15}	0	0	-10.625174	1.000000	2		
p_{0,1}	0	0	-10.610080	1.000000	1		
p_{0,56}	0	1	-31.869324	-6.000000	67		



 $File: \ out/175\_dg\_0\_11100\_f\_0\_16\_filt$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-6.0	-55787.345839	64
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.902223	-93.902223
36	$p_{0,1},$	$p_{0,15}$ ,	2	-39.628622	-39.628622
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$ ,	1	-11.429121	-11.429121
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-32.73119	-32.73119
Sum					-177.74668574842713

 $\Delta G = -40.5124214202443$ 

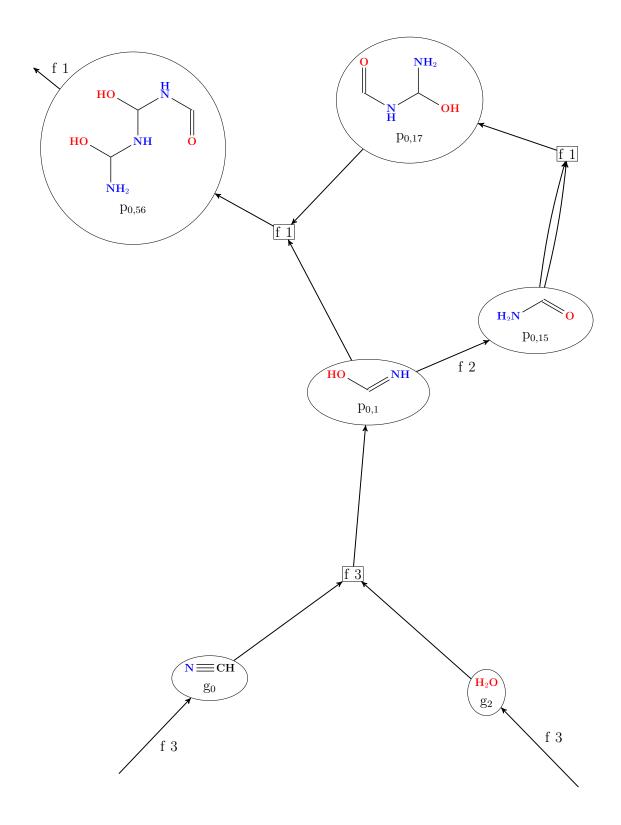
 $\Delta E = \text{-}0.06770013717603526$ 

|E| = 7

|U| = 4

# 0.3.18 Solution 17

Objective val	Lue	(non-integral): -0.0677001				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	1.000000	0	
p_{0,15}	0	0	-10.625174	1.000000	22	
p_{0,17}	0	0	-21.248844	0.292310	45	
p_{0,1}	0	0	-10.610080	1.000000	21	
p_{0,56}	0	1	-31.869324	-6.000000	67	



 $File: \ \mathtt{out/184\_dg\_0\_11100\_f\_0\_17\_filt}$ 

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	22
$p_{0,17}$	0	0	-55788.832737	0.29231	-55787.860575	45
$p_{0,56}$	0	1	-83672.898792	-6.0	-83692.853502	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-93.902223	-93.902223
36	$p_{0,1},$	$p_{0,15},$	2	-39.628622	-39.628622
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.0	0.0
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-44.160311	-44.160311
Sum					-177.74668574842107

 $\Delta G = -40.51242168279427$ 

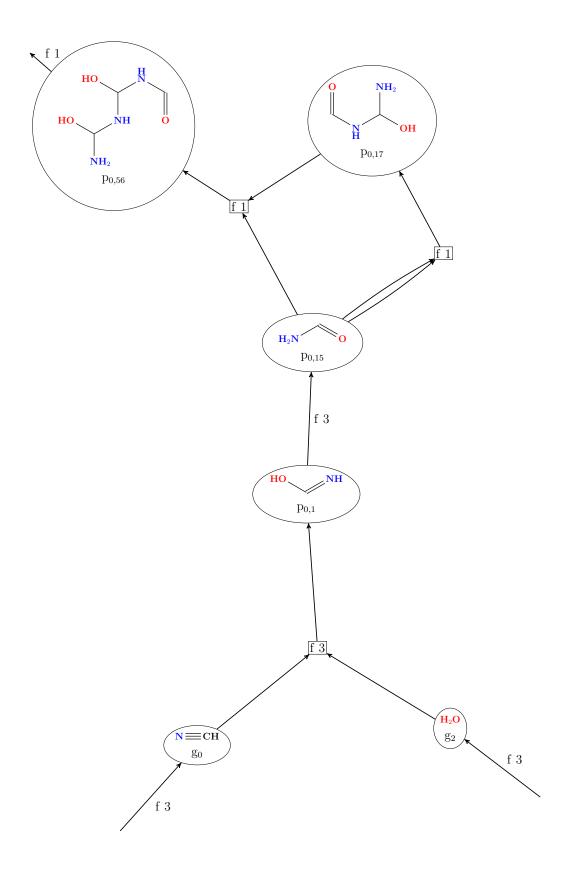
 $\Delta E = \text{-}0.06770013717603296$ 

|E| = 7

|U| = 4

# 0.3.19 Solution 18

Objective val	(non-integral): -0.0526064				
Vertex/Graph In		Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	-6.000000	0
p_{0,15}	0	0	-10.625174	1.000000	21
p_{0,17}	0	0	-21.248887	0.343228	45
p_{0,1}	0	0	-10.610080	1.000000	1
p_{0,56}	0	1	-31.869260	-4.106546	67



File: out/193\_dg\_0\_11100\_f\_0\_18\_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	$x_v^K$	$x_v^{\Delta G}$	$t_v$
$g_0$	3	0	-14459.025578	1.0	-14455.699793	0
$g_2$	3	0	-13306.144961	-6.0	-13326.099672	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	21
$p_{0,17}$	0	0	-55788.944315	0.343228	-55787.802814	45
$p_{0,56}$	0	1	-83672.731446	-4.106546	-83686.388935	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$ ,	3	-77.722278	-77.722278
36	$p_{0,1},$	$p_{0,15},$	3	-39.628622	-39.628622
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.006113	0.006113
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-138.11806364462598

 $\Delta G = \text{-}35.20404736021271$ 

 $\Delta E = \text{-}0.05260639215779184$ 

 $\begin{aligned} |E| &= 8 \\ |U| &= 4 \end{aligned}$