Summary

December 6, 2024

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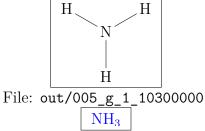
0.1 Loaded Graphs

$0.1.1 g_{0}$

N = C — H File: out/001_g_0_10300000 N = CH

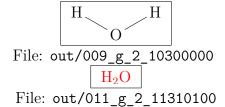
File: out/003_g_0_11310100

0.1.2 g_{1}



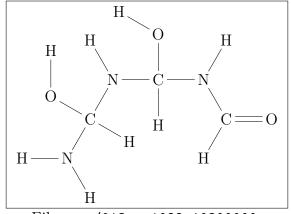
File: out/007_g_1_11310100

0.1.3 g_{2}

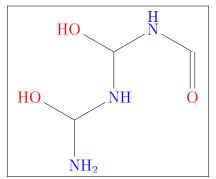


0.2 Product Graphs

0.2.1 p_{0,56}



File: out/013_g_1088_10300000

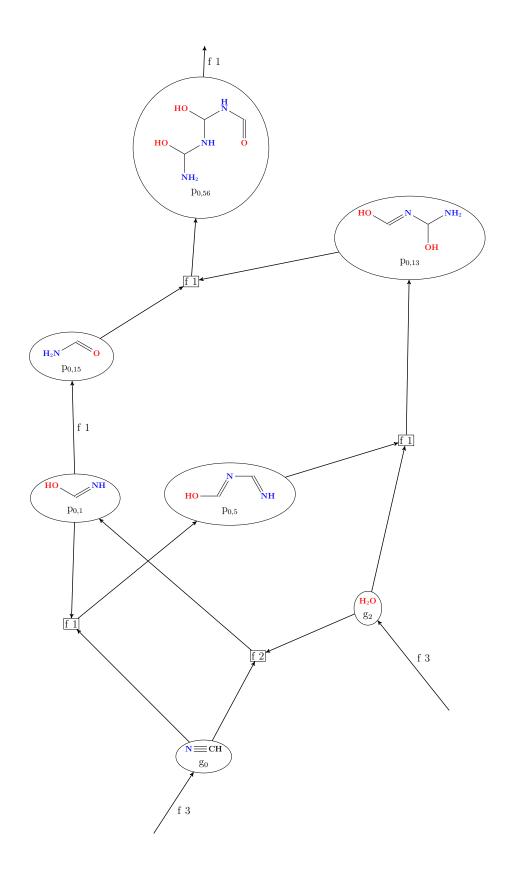


File: out/015_g_1088_11310100

0.3 Enumerated Flows

0.3.1 Solution 0

Objective val	(non-integral): -0.118346				
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	-2.941937	17
p_{0,15}	0	0	-10.625174	-3.000000	49
p_{0,1}	0	0	-10.610101	-3.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67
p_{0,5}	0	0	-16.158998	1.000000	16



 $File: \ \mathtt{out/029_dg_0_11100_f_0_0_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	-3.0	-27866.79441	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	16
$p_{0,13}$	0	0	-55767.391129	-2.941937	-55777.175379	17
$p_{0,15}$	0	0	-27896.389963	-3.0	-27906.367318	49
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	2	-107.152988	-107.152988
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-100.296105	-100.296105
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-51.12995	-51.12995
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-310.71779047352663

 $\Delta G = -40.529881780496744$

 $\Delta E = -0.11834615621393367$

|E| = 6

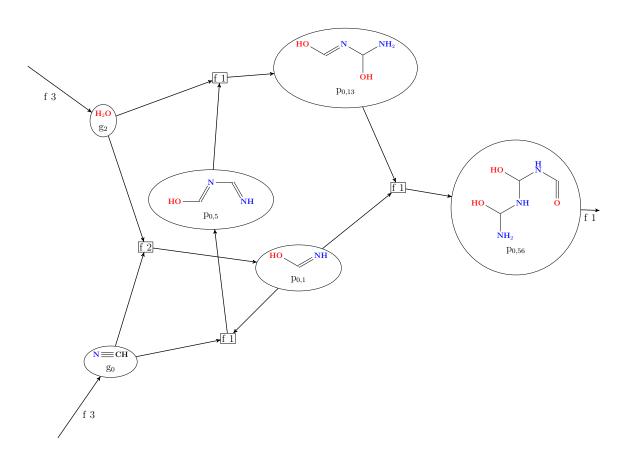
|U| = 5

0.3.2 Solution 1

Overall Data

Objective value (non-integral): -0.118346

Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	-3.000000	65
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67
p_{0,5}	0	0	-16.158998	1.000000	2



 $File: \ \mathtt{out/038_dg_0_11100_f_0_1_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	2	-94.74781	-94.74781
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-112.701283	-112.701283
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-51.31002	-51.31002
263	$p_{0,1}, p_{0,13},$	$p_{0,56},$	1	-51.791903	-51.791903
Sum					-310.71779047353465

 $\Delta G = \text{-}40.529881780496744$

 $\Delta E = -0.11834615621393674$

|E| = 5

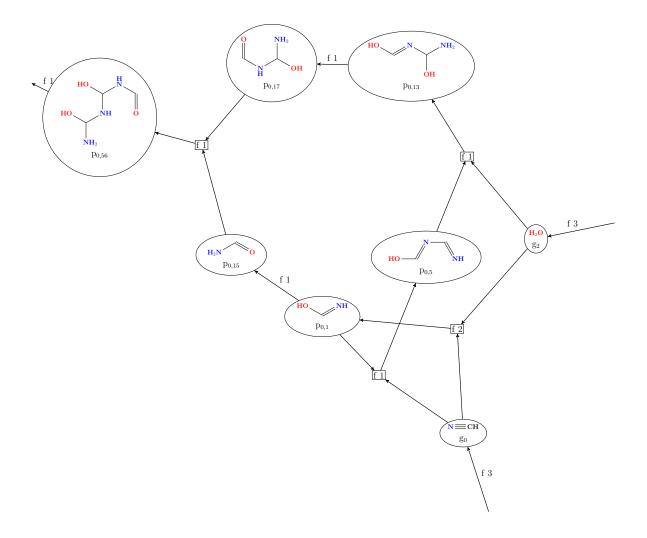
|U| = 4

0.3.3 Solution 2

Overall Data

Objective val	Lue	(non-integral): -0.118346			
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	-3.000000	0
p_{0,13}	0	0	-21.240678	1.000000	3
p_{0,15}	0	0	-10.625174	-0.028176	32
p_{0,17}	0	0	-21.248844	1.000000	34
p_{0,1}	0	0	-10.610101	-3.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67
p_{0,5}	0	0	-16.158998	1.000000	2

Filtered Graph



 $File: \ \mathtt{out/049_dg_0_11100_f_0_2_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	-3.0	-27866.79441	1
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	2
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	3
$p_{0,15}$	0	0	-27896.389963	-0.028176	-27896.483671	32
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	34
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	2	-94.74781	-94.74781
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-100.296105	-100.296105
36	$p_{0,1},$	$p_{0,15},$	1	-30.356408	-30.356408
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-26.499664	-26.499664
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
250	$p_{0,13}$,	$p_{0,17},$	1	-21.441608	-21.441608
Sum					-310.71779047353255

 $\Delta E = \text{-}0.11834615621393593$

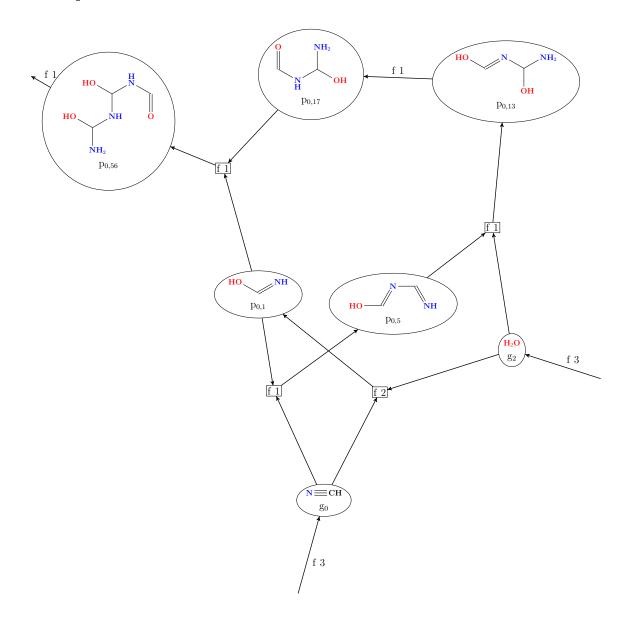
|E| = 7

|U| = 6

0.3.4 Solution 3

Overall Data

Objective value (non-integral): -0.118346 Vertex/Graph In Out G t order logK g_{0} 3 0 -5.507152 1.000000 g_{2} 3 0 -5.068043 -3.000000 0 $p_{0,13}$ 0 0 -21.240678 -3.000000 33 $p_{0,17}$ 0 0 -21.248887 -3.000000 35 -10.610101 1.000000 31 $p_{0,1}$ 0 0 $p_{0,56}$ 0 1 -31.869324 -3.000000 67 p_{0,5} 0 -16.158998 1.000000 32



 $File: \verb"out/058_dg_0_11100_f_0_3_filt"$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	31
$p_{0,5}$	0	0	-42425.44262	1.0	-42422.116835	32
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	33
$p_{0,17}$	0	0	-55788.944315	-3.0	-55798.92167	35
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	2	-82.342632	-82.342632
14	$g_0, p_{0,1},$	$p_{0,5},$	1	-112.701283	-112.701283
123	$g_2, p_{0,5},$	$p_{0,13},$	1	-38.904842	-38.904842
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$,	1	-30.238717	-30.238717
250	$p_{0,13},$	$p_{0,17},$	1	-21.553186	-21.553186
Sum					-310.7177904735313

 $\Delta E = \text{-}0.11834615621393545$

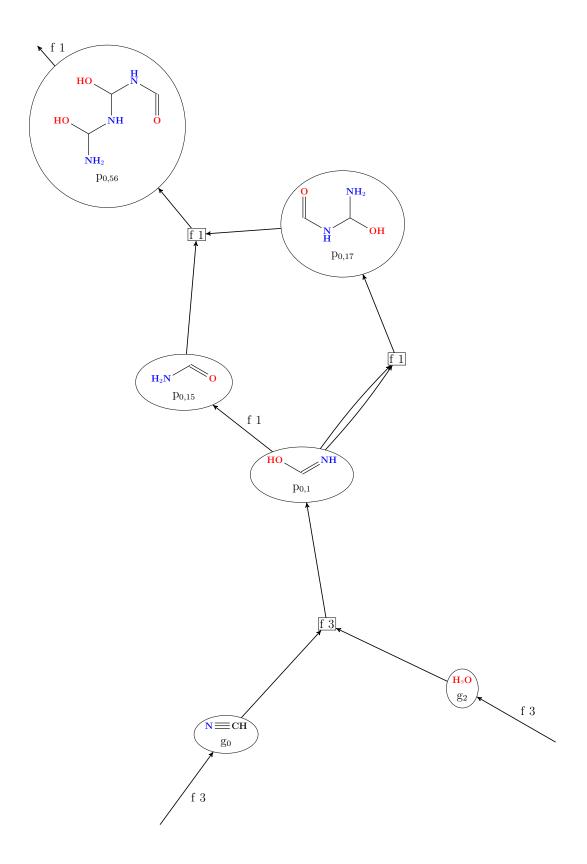
|E| = 6

 $|\mathbf{U}| = 5$

0.3.5 Solution 4

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G logK t order g_{0} 3 0 -5.507152 1.000000 0 g_{2} -5.068043 -3.000000 0 3 0 p_{0,15} 0 0 -10.625195 0.025792 $p_{0,17}$ 0 0 -21.248887 1.000000 64 $p_{0,1}$ -10.610101 -3.000000 1 0 0 p_{0,56} 0 1 -31.869324 -3.000000 67



 $File: \ \mathtt{out/067_dg_0_11100_f_0_4_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	-3.0	-27866.79441	1
$p_{0,15}$	0	0	-27896.445756	0.025792	-27896.359978	2
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	64
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.74781	-94.74781
36	$p_{0,1},$	$p_{0,15},$	1	-30.24483	-30.24483
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-53.601144	-53.601144
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-215.97016366975618

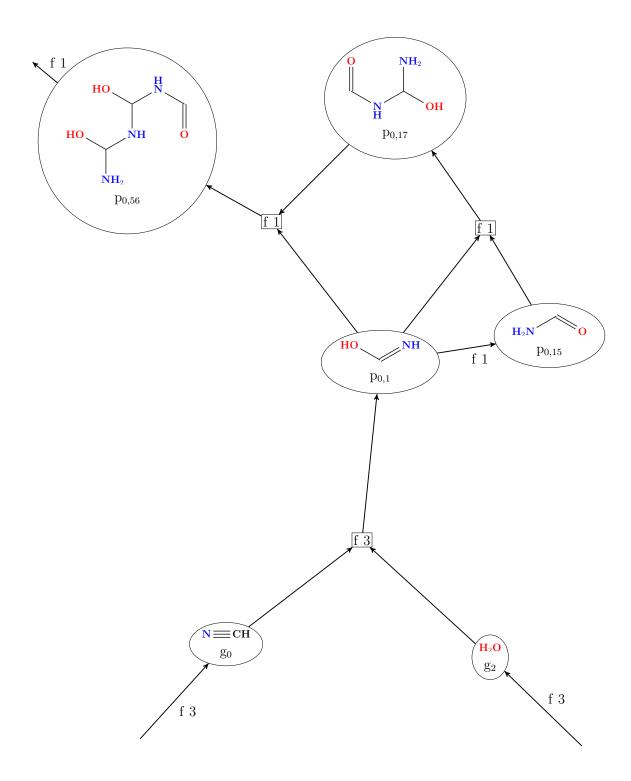
 $\Delta E = \text{-}0.08225869104005312}$

|E| = 6

|U| = 4

0.3.6 Solution 5

Objective val	Lue	(nor	(non-integral): -0.0822587				
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	1.000000	0		
g_{2}	3	0	-5.068043	-3.000000	0		
p_{0,15}	0	0	-10.625174	-3.000000	2		
p_{0,17}	0	0	-21.248844	1.000000	4		
p_{0,1}	0	0	-10.610080	1.000000	1		
p_{0,56}	0	1	-31.869324	-3.000000	67		



 $File: \ \mathtt{out/076_dg_0_11100_f_0_5_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.389963	-3.0	-27906.367318	2
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	4
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.286918	-82.286918
36	$p_{0,1},$	$p_{0,15},$	1	-52.0338	-52.0338
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-26.37755	-26.37755
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-42.811187	-42.811187
Sum					-215.97016366975618

 $\Delta G = \text{-}36.80832793402122$

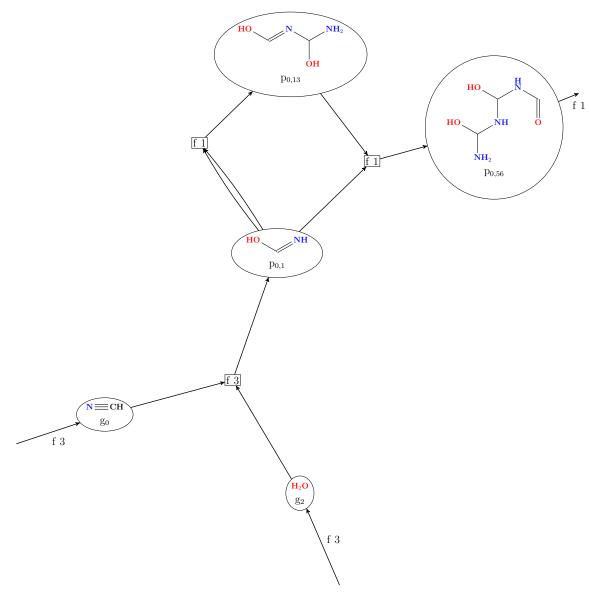
 $\Delta E = \text{-}0.08225869104005312$

|E| = 6

|U| = 4

0.3.7 Solution 6

Objective val	lue	(nor	(non-integral): -0.0822587				
Vertex/Graph	In	Out	G	logK	t_order		
g_{0}	3	0	-5.507152	-3.000000	0		
g_{2}	3	0	-5.068043	-3.000000	0		
p_{0,13}	0	0	-21.240635	1.000000	65		
p_{0,1}	0	0	-10.610080	1.000000	1		
p_{0,56}	0	1	-31.869324	-3.000000	67		



 $File: \ \mathtt{out/085_dg_0_11100_f_0_6_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
$\overline{g_0}$	3	0	-14459.025578	-3.0	-14469.002933	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-69.88174	-69.88174
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.858207	-56.858207
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$,	1	-64.36433	-64.36433
Sum					-215.9701636697549

 $\Delta G = \text{-}33.08677540029552$

 $\Delta E = \text{-}0.08225869104005264$

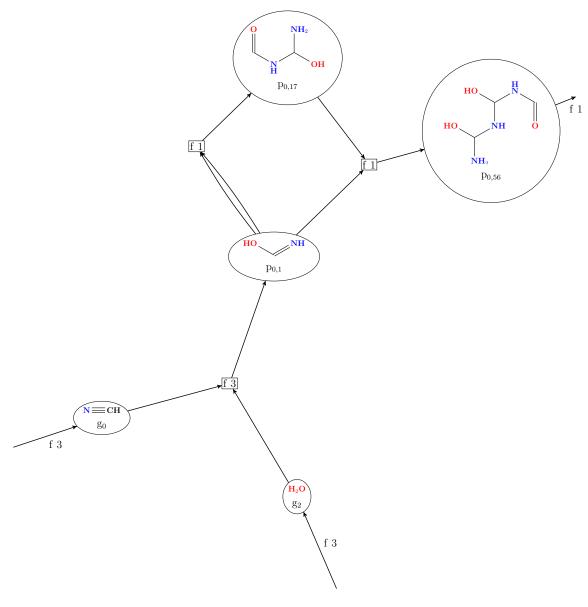
```
\begin{aligned} |E| &= 5\\ |U| &= 3 \end{aligned}
```

0.3.8 Solution 7

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068043 -3.000000 0 $p_{0,17}$ 0 0 -21.248844 1.000000 45 p_{0,1} 0 0 -10.610080 1.000000 21 $p_{0,56}$ 0 1 -31.869324 -3.000000 67

Filtered Graph



File: out/094_dg_0_11100_f_0_7_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,17}$	0	0	-55788.832737	1.0	-55785.506952	45
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.286918	-82.286918
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.41135	-78.41135
196	$p_{0,1}, p_{0,17},$	$p_{0,56}$,	1	-42.811187	-42.811187
Sum					-215.9701636697549

 $\Delta E = \text{-}0.08225869104005264$

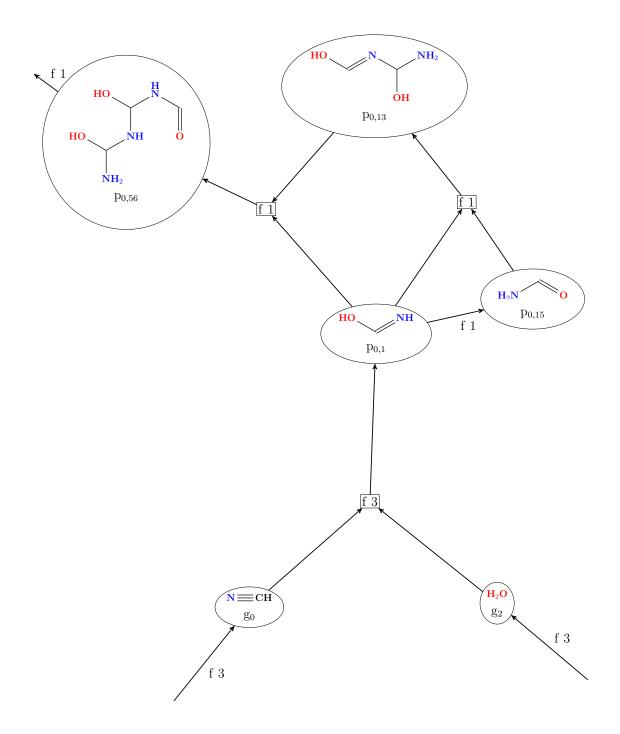
|E| = 5

|U| = 3

0.3.9 Solution 8

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068043 -3.000000 0 $p_{0,13}$ -21.240678 -1.442409 65 -10.625195 -3.000000 2 $p_{0,15}$ 0 0 p_{0,1} 0 0 -10.610101 -3.000000 1 $p_{0,56}$ 0 1 -31.869324 -3.000000 67



 $File: \verb"out/103_dg_0_11100_f_0_8_filt"$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	-3.0	-27866.79441	1
$p_{0,13}$	0	0	-55767.391129	-1.442409	-55772.188272	65
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	2
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	3	-94.74781	-94.74781
36	$p_{0,1},$	$p_{0,15},$	1	-39.628701	-39.628701
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	0.006113	0.006113
263	$p_{0,1}, p_{0,13},$	$p_{0,56}$,	1	-44.217273	-44.217273
Sum					-215.97016366975365

 $\Delta E = \text{-}0.08225869104005215$

|E| = 6

|U| = 4

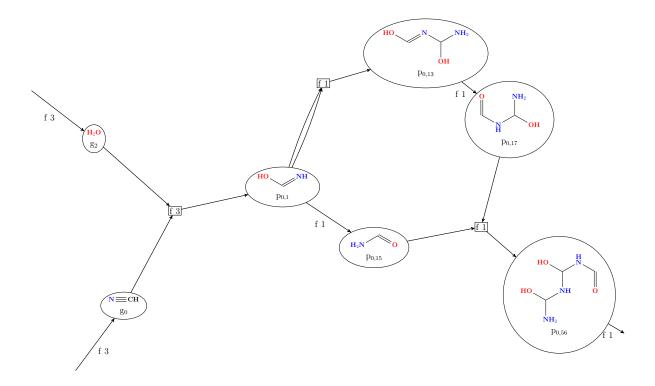
0.3.10 Solution 9

Overall Data

Objective value (non-integral): -0.0822587

In	Out	G	logK	t_order
3	0	-5.507152	1.000000	0
3	0	-5.068043	-3.00000	0
0	0	-21.240635	1.000000	3
0	0	-10.625174	1.000000	2
0	0	-21.248844	-0.026205	4
0	0	-10.610101	1.000000	1
0	1	-31.869324	-3.000000	67
	3 0 0 0	3 0 3 0 0 0 0 0 0 0 0 0	3 0 -5.068043 0 0 -21.240635 0 0 -10.625174 0 0 -21.248844 0 0 -10.610101	3 0 -5.507152 1.000000 3 0 -5.068043 -3.000000 0 0 -21.240635 1.000000 0 0 -10.625174 1.000000 0 0 -21.248844 -0.026205 0 0 -10.610101 1.000000

Filtered Graph



File: out/112_dg_0_11100_f_0_9_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	3
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.832737	-0.026205	-55788.91989	4
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.342632	-82.342632
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.74678	-56.74678
36	$p_{0,1},$	$p_{0,15},$	1	-39.572909	-39.572909
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
250	$p_{0,13}$,	$p_{0,17},$	1	-24.735708	-24.735708
Sum					-215.9701636697528

 $\Delta G = \text{-}36.80832872167111$

 $\Delta E = -0.08225869104005183$

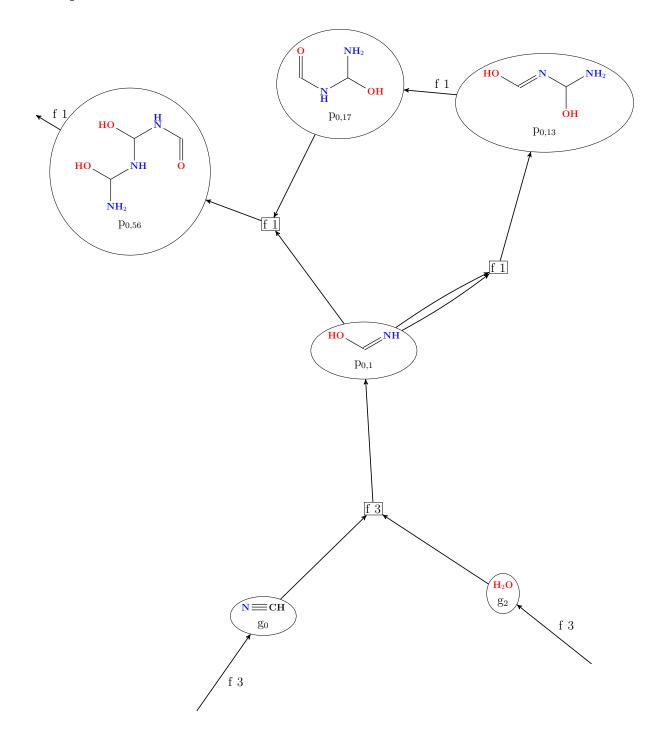
|E| = 7

|U| = 5

0.3.11 Solution 10

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 1.000000 0 g_{2} 3 0 -5.068043 -3.000000 0 p_{0,13} 0 0 -21.240635 1.000000 44 p_{0,17} -21.248844 -3.000000 45 0 0 p_{0,1} -10.610080 1.000000 21 0 0 -31.869324 -3.000000 67 $p_{0,56}$ 1



 $File: \ {\tt out/121_dg_0_11100_f_0_10_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	44
$p_{0,17}$	0	0	-55788.832737	-3.0	-55798.810092	45
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.286918	-82.286918
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-56.858207	-56.858207
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-30.406009	-30.406009
250	$p_{0,13},$	$p_{0,17},$	1	-33.958321	-33.958321
Sum					-215.9701636697515

 $\Delta E = -0.08225869104005135$

|E| = 6

|U| = 4

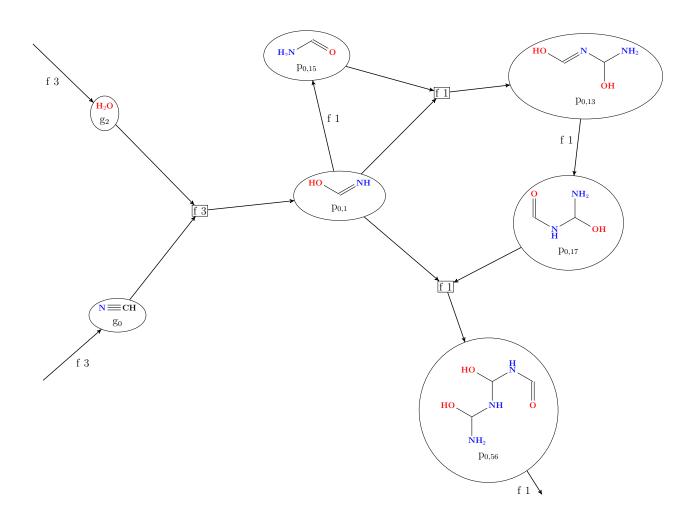
0.3.12 Solution 11

Overall Data

Objective value (non-integral): -0.0822587

Vertex/Graph In Out G logK t_order

Vertex/Graph	Ιn	Uut	G	LogK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	-3.000000	20
p_{0,13}	0	0	-21.240635	1.000000	44
p_{0,15}	0	0	-10.625174	-3.000000	22
p_{0,17}	0	0	-21.248844	-3.000000	45
r _ c - , - ,	0	0	-10.610080	1.000000	21
p_{0,56}	0	1	-31.869324	-3.000000	67



 $File: \ {\tt out/130_dg_0_11100_f_0_11_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
$\overline{g_0}$	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	20
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	21
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	44
$p_{0,15}$	0	0	-27896.389963	-3.0	-27906.367318	22
$p_{0,17}$	0	0	-55788.832737	-3.0	-55798.810092	45
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.286918	-82.286918
36	$p_{0,1},$	$p_{0,15},$	1	-52.0338	-52.0338
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-4.824407	-4.824407
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-30.406009	-30.406009
250	$p_{0,13},$	$p_{0,17},$	1	-33.958321	-33.958321
Sum					-215.97016366975024

 $\Delta G = \text{-}36.80832793402122$

 $\Delta E = \text{-}0.08225869104005086$

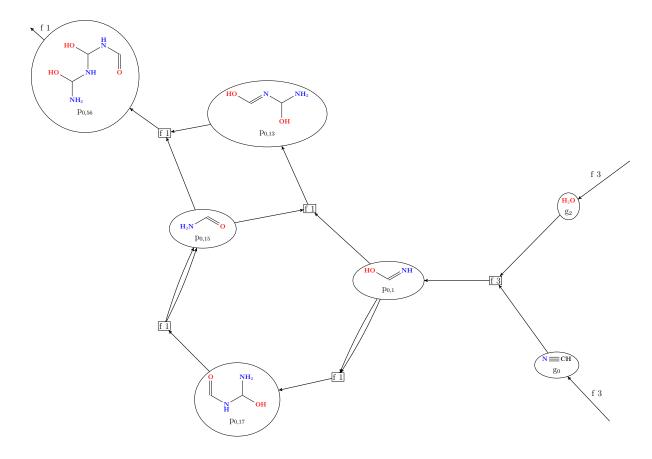
```
\begin{aligned} |E| &= 7 \\ |U| &= 5 \end{aligned}
```

0.3.13 Solution 12

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G t_order logK g_{0} 3 0 -5.507152 1.000000 0 3 0 g_{2} -5.068043 1.000000 10 p_{0,13} 0 0 -21.240678 1.000000 39 $p_{0,15}$ 0 0 -10.625174 -3.000000 27 $p_{0,17}$ 0 0 -21.248887 1.000000 26 $p_{0,1}$ 0 0 -10.610101 1.000000 11 $p_{0,56}$ 0 1 -31.869324 -3.000000 67

Filtered Graph



 $File: \ \mathtt{out/139_dg_0_11100_f_0_12_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	1.0	-13302.819176	10
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	11
$p_{0,13}$	0	0	-55767.391129	1.0	-55764.065344	39
$p_{0,15}$	0	0	-27896.389963	-3.0	-27906.367318	27
$p_{0,17}$	0	0	-55788.944315	1.0	-55785.61853	26
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	3	-94.74781	-94.74781
40	$p_{0,1}, p_{0,1},$	$p_{0,17},$	1	-78.411501	-78.411501
169	$p_{0,13}, p_{0,15},$	$p_{0,56}$,	1	-12.218995	-12.218995
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-4.880228	-4.880228
237	$p_{0,17},$	$p_{0,15}, p_{0,15},$	1	-25.544673	-25.544673
Sum					-215.9701636697477

 $\Delta G = -40.52988151794678$

 $\Delta E = -0.08225869104004989$

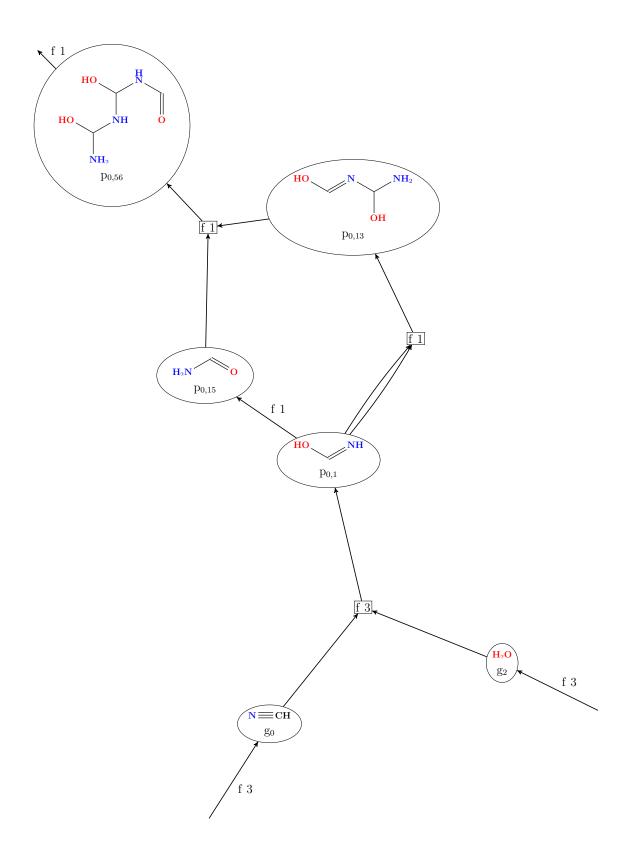
|E| = 7

|U| = 5

0.3.14 Solution 13

Overall Data

Objective value (non-integral): -0.0822587 Vertex/Graph In Out G logK t_order g_{0} 3 0 -5.507152 -3.000000 0 g_{2} 3 0 -5.068043 -3.000000 0 p_{0,13} 0 0 -21.240678 -2.923947 3 p_{0,15} -10.625195 -3.000000 63 0 0 p_{0,1} -10.610101 1.000000 1 0 0 -31.869324 -3.000000 67 $p_{0,56}$



 $File: \ {\tt out/148_dg_0_11100_f_0_13_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	-3.0	-14469.002933	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,13}$	0	0	-55767.391129	-2.923947	-55777.115547	3
$p_{0,15}$	0	0	-27896.445756	-3.0	-27906.423111	63
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-69.937454	-69.937454
30	$p_{0,1}, p_{0,1},$	$p_{0,13},$	1	-69.02763	-69.02763
36	$p_{0,1},$	$p_{0,15},$	1	-52.03388	-52.03388
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-215.97016366974685

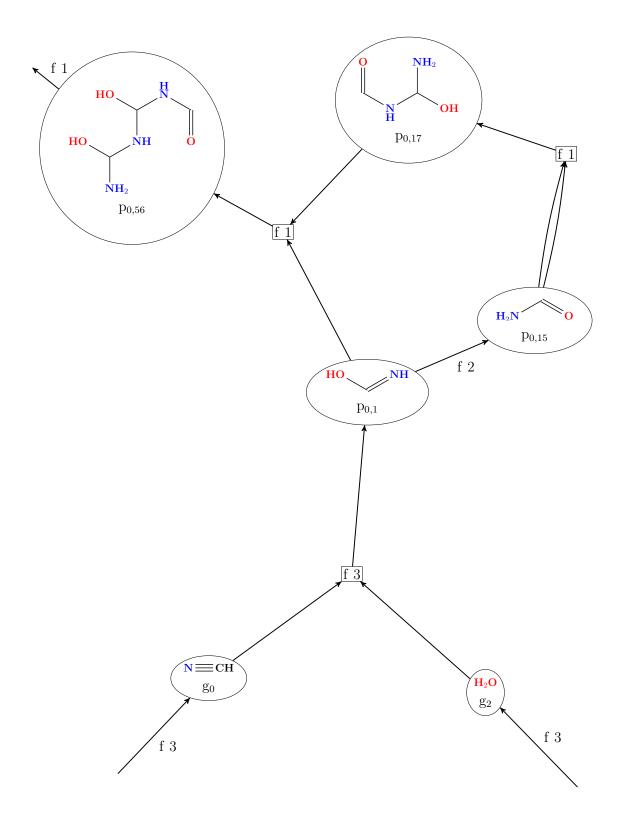
 $\Delta E = \text{-}0.08225869104004957$

|E| = 6

|U| = 4

0.3.15 Solution 14

Objective val	(nor	(non-integral): -0.0671649				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-3.000000	0	
p_{0,15}	0	0	-10.625174	1.000000	32	
p_{0,17}	0	0	-21.248844	0.727245	65	
p_{0,1}	0	0	-10.610080	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ {\tt out/157_dg_0_11100_f_0_14_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	32
$p_{0,17}$	0	0	-55788.832737	0.727245	-55786.414077	65
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.286918	-82.286918
36	$p_{0,1},$	$p_{0,15},$	2	-39.628622	-39.628622
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	0.0	0.0
196	$p_{0,1}, p_{0,17},$	$p_{0,56},$	1	-41.965293	-41.965293
Sum					-176.34154156596446

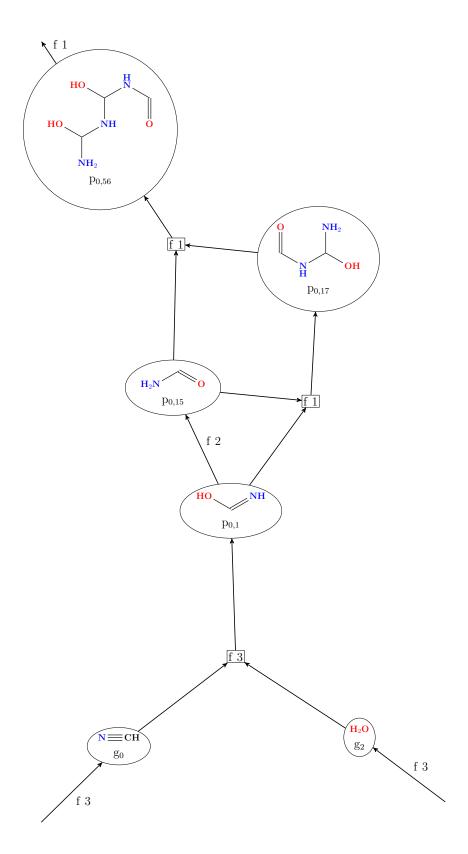
 $\Delta E = \text{-}0.06716494602181329$

|E| = 7

|U| = 4

0.3.16 Solution 15

Objective val	(non-integral): -0.0671649				
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	-3.000000	0
p_{0,15}	0	0	-10.625195	1.000000	2
p_{0,17}	0	0	-21.248887	0.025792	4
p_{0,1}	0	0	-10.610101	1.000000	1
p_{0,56}	0	1	-31.869324	-3.00000	67



 $File: \ \mathtt{out/166_dg_0_11100_f_0_15_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.445756	1.0	-27893.119971	2
$p_{0,17}$	0	0	-55788.944315	0.025792	-55788.858537	4
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-82.342632	-82.342632
36	$p_{0,1},$	$p_{0,15},$	2	-39.628701	-39.628701
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
183	$p_{0,1}, p_{0,15},$	$p_{0,17},$	1	-41.804106	-41.804106
Sum					-176.34154156596108

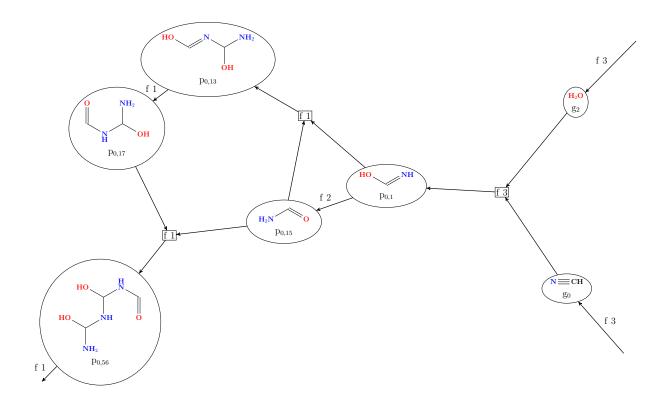
 $\Delta E = \text{-}0.067164946021812$

|E| = 7

|U| = 4

0.3.17 Solution 16

Objective val	Lue	(non-integral): -0.0671649				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	1.000000	0	
g_{2}	3	0	-5.068043	-3.000000	0	
p_{0,13}	0	0	-21.240635	1.000000	33	
p_{0,15}	0	0	-10.625174	1.000000	31	
p_{0,17}	0	0	-21.248887	0.009773	35	
p_{0,1}	0	0	-10.610101	-3.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



 $File: \ out/175_dg_0_11100_f_0_16_filt$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	-3.0	-27866.79441	1
$p_{0,13}$	0	0	-55767.279594	1.0	-55763.953809	33
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	31
$p_{0,17}$	0	0	-55788.944315	0.009773	-55788.911813	35
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1}$,	3	-94.74781	-94.74781
36	$p_{0,1},$	$p_{0,15},$	2	-27.16773	-27.16773
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.0	0.0
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-4.768693	-4.768693
250	$p_{0,13},$	$p_{0,17},$	1	-24.735708	-24.735708
Sum					-176.34154156595514

 $\Delta G = -36.808327671471254$

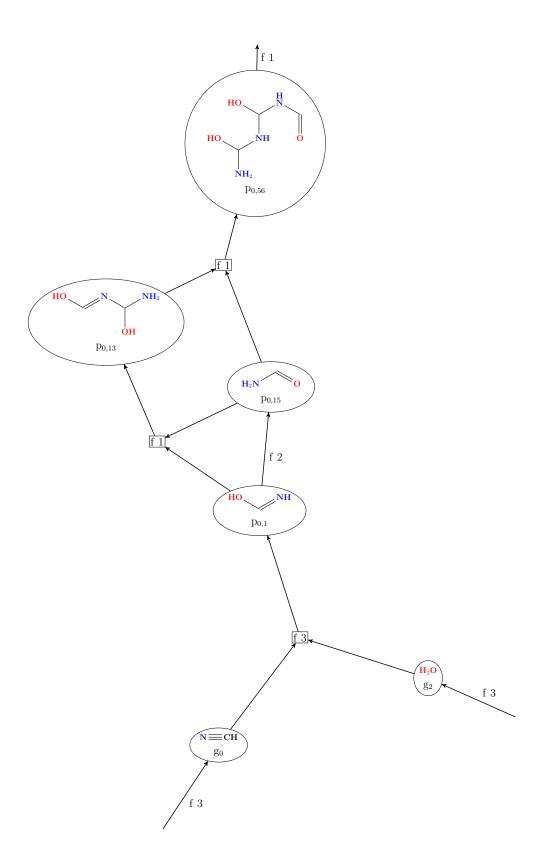
 $\Delta E = -0.06716494602180974$

|E| = 8

|U| = 5

0.3.18 Solution 17

Objective value (non-integral): -0.0671649					
Vertex/Graph	In	Out	G	logK	t_order
g_{0}	3	0	-5.507152	1.000000	0
g_{2}	3	0	-5.068043	1.000000	0
p_{0,13}	0	0	-21.240678	-3.000000	64
p_{0,15}	0	0	-10.625174	1.000000	2
p_{0,1}	0	0	-10.610080	1.000000	1
p_{0,56}	0	1	-31.869324	-3.000000	67



 $File: \ \mathtt{out/184_dg_0_11100_f_0_17_filt}$

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	1.0	-14455.699793	0
g_2	3	0	-13306.144961	1.0	-13302.819176	0
$p_{0,1}$	0	0	-27856.761341	1.0	-27853.435556	1
$p_{0,13}$	0	0	-55767.391129	-3.0	-55777.368484	64
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-94.692097	-94.692097
36	$p_{0,1},$	$p_{0,15},$	2	-39.628622	-39.628622
169	$p_{0,13}, p_{0,15},$	$p_{0,56},$	1	-12.218995	-12.218995
192	$p_{0,1}, p_{0,15},$	$p_{0,13},$	1	-29.746298	-29.746298
Sum					-176.3415415659492

 $\Delta G = -40.529881780496744$

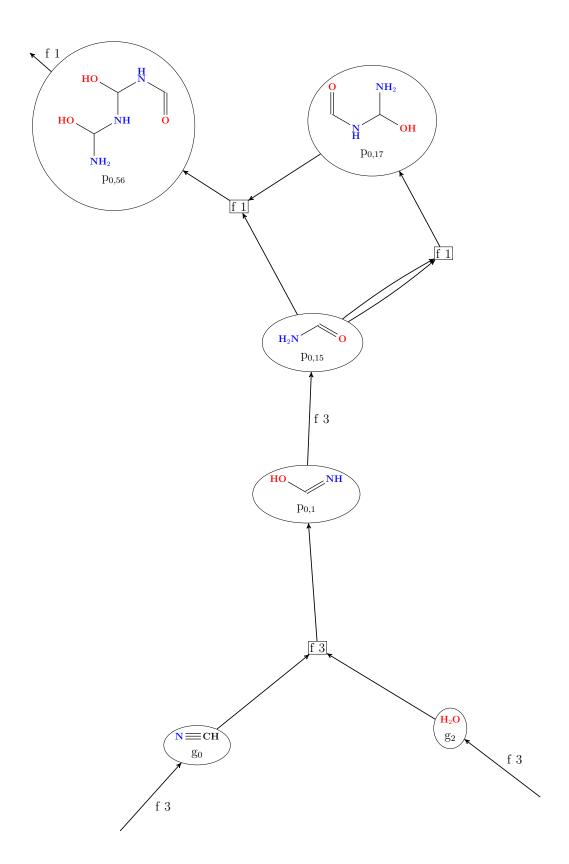
 $\Delta E = \text{-}0.06716494602180748}$

|E| = 7

|U| = 4

0.3.19 Solution 18

Objective value		(non-integral): -0.0520712				
Vertex/Graph	In	Out	G	logK	t_order	
g_{0}	3	0	-5.507152	-3.000000	0	
g_{2}	3	0	-5.068043	-3.000000	0	
p_{0,15}	0	0	-10.625174	1.000000	2	
p_{0,17}	0	0	-21.248887	0.007801	64	
p_{0,1}	0	0	-10.610101	1.000000	1	
p_{0,56}	0	1	-31.869324	-3.000000	67	



File: out/193_dg_0_11100_f_0_18_filt

Vertex	InFlow	OutFlow	$x_v^{\Delta G^0}$	x_v^K	$x_v^{\Delta G}$	t_v
g_0	3	0	-14459.025578	-3.0	-14469.002933	0
g_2	3	0	-13306.144961	-3.0	-13316.122316	0
$p_{0,1}$	0	0	-27856.817054	1.0	-27853.491269	1
$p_{0,15}$	0	0	-27896.389963	1.0	-27893.064178	2
$p_{0,17}$	0	0	-55788.944315	0.007801	-55788.918369	64
$p_{0,56}$	0	1	-83672.898792	-3.0	-83682.876147	67

Hyperedge	Source	Target	Flow	$x_e^{\Delta G}$	$\overline{x}_e^{\Delta G}$
6	$g_0, g_2,$	$p_{0,1},$	3	-69.937454	-69.937454
36	$p_{0,1},$	$p_{0,15},$	3	-39.572909	-39.572909
180	$p_{0,15}, p_{0,15},$	$p_{0,17},$	1	-2.342784	-2.342784
181	$p_{0,15}, p_{0,17},$	$p_{0,56},$	1	0.006113	0.006113
Sum					-136.71291946216934

 $\Delta E = \text{-}0.05207120100357216$

 $\begin{aligned} |E| &= 8 \\ |U| &= 4 \end{aligned}$