5.8.3

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Question

5 pencils and 7 pens together cost ₹50, whereas 7 pencils and 5 pens together cost ₹46. Find the cost of one pencil and that of one pen.

Converting to Equations:

Let the cost of one pencil be x, pen be y.

$$5x + 7y = 50 \tag{1}$$

$$7x + 5y = 46 \tag{2}$$

Forming Augmented Matrix:

$$\begin{pmatrix} 5 & 7 & 50 \\ 7 & 5 & 46 \end{pmatrix} \tag{3}$$

Row Operation and Reduction:

$$\begin{pmatrix} 5 & 7 & 50 \\ 7 & 5 & 46 \end{pmatrix} \xrightarrow{R_2 \to R_2 - \frac{7}{5}R_1} \begin{pmatrix} 5 & 7 & 50 \\ 0 & -4.8 & -24 \end{pmatrix} \tag{4}$$

Back Substitution:

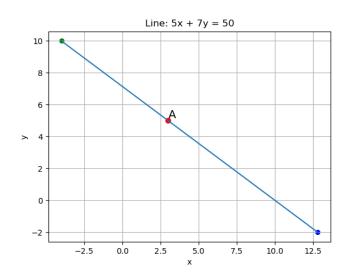
$$-4.8y = -24 \implies y = 5 \tag{5}$$

$$5x + 7y = 50 \implies 5x + 35 = 50 \implies x = 3$$
 (6)

Final Solution:

$$\mathbf{x} = \begin{pmatrix} 3 \\ 5 \end{pmatrix} \tag{7}$$

Cost of one pencil is ₹3 and one pen is ₹5.



Codes

For Codes, refer to the URL below:

https://github.com/Aditya-Mishra11005/ee1030-2025/tree/main/ee25btech11005/matgeo/5.8.3/Codes