### 4.10.3

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September 30, 2025

## Question

Find the vector equation of the plane passing through the intersection of the planes

$$\mathbf{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 6$$
 and  $\mathbf{r} \cdot (2\hat{i} + 3\hat{j} + 4\hat{k}) = -5$ ,

and the point (1,1,1).

#### Solution

Given planes:

$$\mathbf{n_1}^{\mathsf{T}}\mathbf{x} = c_1, \quad \mathbf{n_2}^{\mathsf{T}}\mathbf{x} = c_2,$$

with point

$$\mathbf{P} = \begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix}.$$

General form:

$$\mathbf{n_1}^{\mathsf{T}}\mathbf{x} - c_1 + \lambda(\mathbf{n_2}^{\mathsf{T}}\mathbf{x} - c_2) = 0, \quad \lambda = \frac{c_1 - \mathbf{n_1}^{\mathsf{T}}\mathbf{P}}{\mathbf{n_2}^{\mathsf{T}}\mathbf{P} - c_2}.$$

## Solution

Given:

$$\mathbf{n_1}=egin{pmatrix}1\\1\\1\end{pmatrix},\quad c_1=6,\quad \mathbf{n_2}=egin{pmatrix}2\\3\\4\end{pmatrix},\quad c_2=-5,$$
 
$$\mathbf{P}=egin{pmatrix}1\\1\\1\end{pmatrix}.$$

Evaluate:

$$\mathbf{n_1}^{\mathsf{T}} \mathbf{P} = 3, \quad \mathbf{n_2}^{\mathsf{T}} \mathbf{P} = 9, \quad \lambda = \frac{3}{14}.$$

#### Solution

Plane equation:

$$\mathbf{n_1}^{\top}\mathbf{x} - 6 + \frac{3}{14}\left(\mathbf{n_2}^{\top}\mathbf{x} + 5\right) = 0.$$

Or

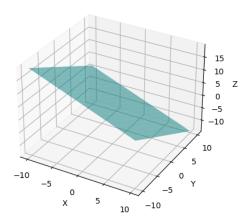
$$\begin{pmatrix} \frac{20}{14} \\ \frac{23}{14} \\ \frac{26}{14} \end{pmatrix}^{\top} \mathbf{x} = \frac{69}{14},$$

which gives integer form

$$(20 \quad 23 \quad 26)\mathbf{x} = 69$$
.

# Plot

Plane: 20x + 23y + 26z = 69



#### Codes

For Codes, refer to the URL below:

https://github.com/Aditya-Mishra11005/ee1030-2025/tree/temp/ee25btech11005/matgeo/4.10.3/Codes