

## Gibbs energy and equilibrium constant:-

$$\Delta G = \Delta G^\circ + RT \ln \Phi$$

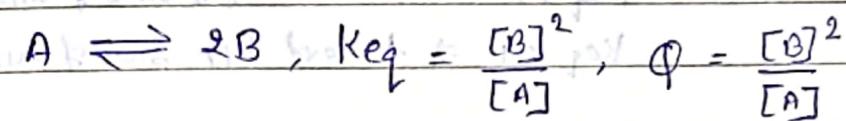
$\Delta G$  = Gibbs' energy change at any condit.

$\Delta G^\circ$  = G.E.C. under standard conditions

$$R = V.G.C. \rightarrow \frac{1}{3} (\Delta G = J) \rightarrow 2 (\Delta G = \text{cal})$$

$T$  = Temp. (K)

$\Phi$  = reaction quotient



$K_{eq}$	$\Phi$	Direction
① Constant	Variable	① $\Phi < K_{eq} \Rightarrow$ forward
② given	calculate	② $\Phi = K_{eq} \Rightarrow$ eq.
③ Defined only at equilibrium	It is defined at any time.	③ $\Phi > K_{eq} \Rightarrow$ backward

at equilibrium  $\Delta G = 0, \Phi = K_{eq}$ .

$$0 = \Delta G^\circ + RT \ln K_{eq}$$

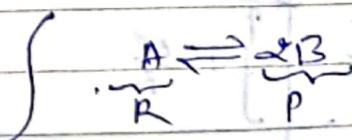
$$\left\{ \begin{array}{l} \Delta G^\circ = 0, K_{eq} = 1 \\ \Delta G^\circ < 0, K_{eq} > 1 \\ \Delta G^\circ > 0, K_{eq} < 1 \end{array} \right.$$

$$\Delta G^\circ = -RT \ln K_{eq}$$

$$\Delta G^\circ = -2.303 RT \log K_{eq}$$

$$\Delta G = -RT \ln K_{eq} + RT \ln \Phi$$

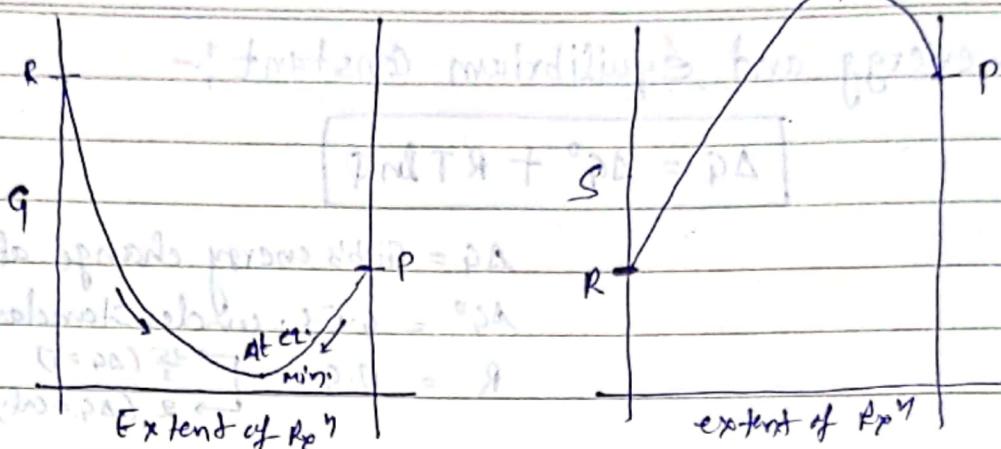
$$\Delta G = RT \ln \left( \frac{\Phi}{K_{eq}} \right)$$



(i)  $\Phi = K_{eq} \Rightarrow \Delta G = 0$  (eq.)

(ii)  $\Phi < K_{eq} \Rightarrow \Delta G < 0$  (spontaneous)

(iii)  $\Phi > K_{eq} \Rightarrow \Delta G > 0$  (Non-spont.)



$K_{eq} = 1 \Rightarrow$  mid point (min/max)

$K_{eq} > 1 \Rightarrow$  toward right side of mid (max/min)

$\frac{[A]}{[B]} = P \Rightarrow K_{eq} < 1 \Rightarrow$  toward left side of mid (min/max)

Q.M.P.

### Variation of $K_{eq}$ with Temp:-

$$\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ$$

$$\Delta G^\circ = -RT \ln K_{eq}$$

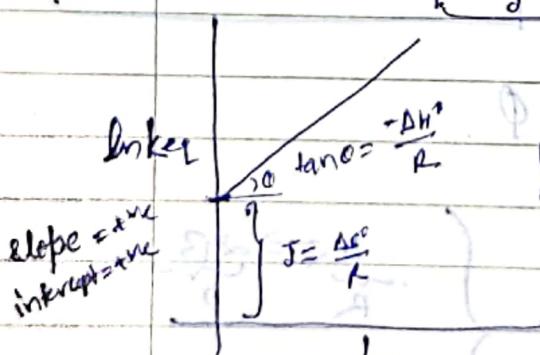
Compare.

$$-RT \ln K_{eq} = \Delta H^\circ - T \Delta S^\circ$$

$$\ln K_{eq} = \frac{\Delta H^\circ}{-RT} - \frac{\Delta S^\circ}{R}$$

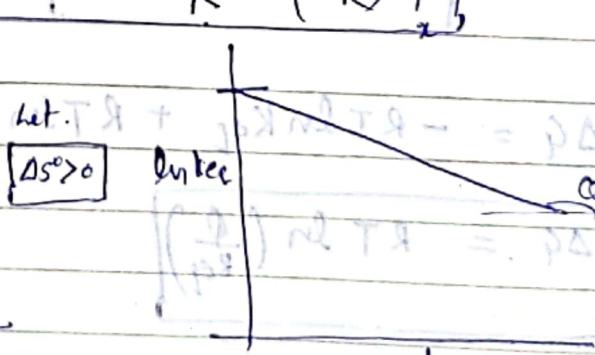
$$\ln K_{eq} = \frac{\Delta S^\circ}{R} + \left( \frac{-\Delta H^\circ}{R} \right) \frac{1}{T}$$

$$y = c + mx$$



slope = -ve  
intercept = c

$\frac{1}{T}$   
(exothermic  $P_n$ )  
( $\Delta H < 0$ )



slope = +ve  
Int = c = 0

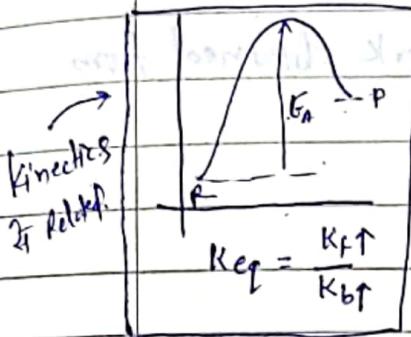
$\frac{1}{T}$   
(endothermic  $R_n$ )  
( $\Delta H > 0$ )

Chemical equilibrium

Endo - high Temp.  $[T \uparrow, K_{eq} \uparrow]$

Exo - low temp.  $[T \uparrow, K_{eq} \downarrow]$

$\Rightarrow \Delta S^\circ$  and  $\Delta H^\circ$  are assumed to be independent from temp.



①  $T = T_1, K_{eq} = K_1$

$$\ln K_1 = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_1} \quad \text{(i)}$$

②  $T = T_2, K_{eq} = K_2$

$$\ln K_2 = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_2} \quad \text{(ii)}$$

(ii) - (i)

$$\ln K_2 - \ln K_1 = \left[ \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_2} \right] - \left[ \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_1} \right]$$

$$\ln \left( \frac{K_2}{K_1} \right) = \frac{\Delta H^\circ}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

(Kinetics  
of 2<sup>nd</sup> Relatn)

$$\log \frac{K_2}{K_1} = \frac{\Delta H^\circ}{2.303R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

$$\begin{cases} \text{Cal } (R=2) \\ \Delta H^\circ \rightarrow J (R=\frac{25}{3}) \end{cases}$$

Physical significance of Gibbs Energy :-

$$G = H - TS$$

useful energy      Total energy      useless energy

$$\text{FLOT} \quad dU = dq + (dW_{p-v} + dW_{non-pv})$$

$$dU - dq - dW_{p-v} = dW_{non-pv}$$

$$dU - dq + Pdv = dW_{non-pv}$$

$$dW_{p-v} = -Pdv$$

at const temp. and pressure for R.P.

$$d(U+PV) - Tds = dW_{non-pv}$$

$$\begin{cases} ds = \frac{dQ_{rev}}{T} \end{cases}$$

$$dH - TdS = dW_{\text{non-}pv} \quad [H = U + Pv]$$

$$d(H - TS) = dW_{\text{nm-}pv}$$

$$\boxed{dG = dW_{\text{nm-}pv}} \quad (\text{since } dG = H - TS)$$

Decrease in gibb's energy denotes useful work obtained from system.

Formulae:-

$$\Delta G = \Delta G^\circ + RT \ln \varphi$$

$$\Delta G^\circ = -RT \ln K_{\text{eq}}$$

$$\Delta G^\circ = RT \ln \left( \frac{\varphi}{K_{\text{eq}}} \right)$$

Q. If eq. constant of a reversible rxn is 1 at 27°C then cal.  $\Delta G^\circ$  of the rxn.

$$\Delta G^\circ = -RT \ln K_{\text{eq}} = -2 \times 300 \times \ln 1$$

$$\Delta G^\circ = 0$$

at eq.  $\Delta G = 0$ ,  $\Delta G^\circ = 0$  when  $K_{\text{eq}} = 1$ .

Q. If  $\Delta G^\circ$  of a Rev. Rxn at 727°C is -4.606 K.cal/mole then cal. value of  $K_{\text{eq}}$ .

But?

$$\begin{cases} \Delta G^\circ = 0 \quad K_{\text{eq}} = 1 \\ \Delta G^\circ < 0 \quad K_{\text{eq}} > 1 \\ \Delta G^\circ > 0 \quad K_{\text{eq}} < 1 \end{cases}$$

$$\Delta G^\circ = -2.303 RT \log K_{\text{eq}}$$

$$\ln \varphi = 2.303 \log \varphi$$

$$-4.606 \times 10^3 = -2.303 \times 2 \times 10^3 \log K_{\text{eq}}$$

$$\log K_{\text{eq}} = 1$$

$$K_{\text{eq}} = 10^1 = 10$$

Q. For a Rev. Rxn  $A(g) \rightleftharpoons 2B(g)$ ,  $K_p = 100 \text{ bar}$  at 22°C if w/w contents P.P. of A and P.P. of B is 1 bar & 5 bar respectively then cal. value of  $\Delta G$  and Predict the direction of Rxn.

Soln:  $\varphi_p = \frac{(P_B)^2}{P_A} = \frac{(5)^2}{1} = 25 \quad \varphi_p < k_p \Rightarrow \text{forward dirn } (\Delta G, -ve \text{ at } 25^\circ\text{C})$

$$\Delta G = RT \ln \left( \frac{\varphi}{K_{eq}} \right)$$

$$= 2 \times 300 \ln \left( \frac{25}{100} \right)$$

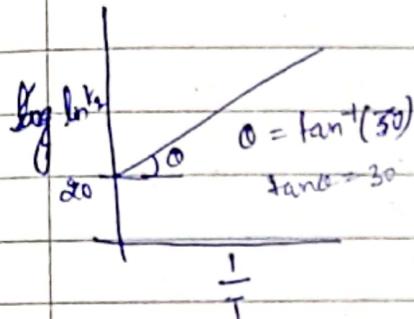
$$\left\{ \ln 2 = 0.693 \right\}$$

$$\Delta G = -600 \ln 4$$

$$\Delta G = -600 \times 2 \times 0.7 = -840 \text{ cal}$$

Soln:

Q. Cal Value of  $\Delta S^\circ$  and  $\Delta H^\circ$  from the following graph (in cal.)

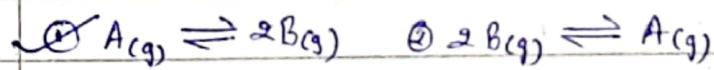


Soln:  $\ln K_{eq} = \frac{\Delta S^\circ}{R} + \left( -\frac{\Delta H^\circ}{R} \right) \times \frac{1}{T}$

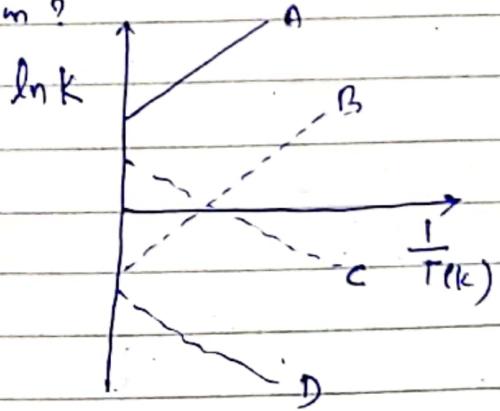
$$\frac{\Delta S^\circ}{R} = 20 \Rightarrow \Delta S^\circ = 20 \times 2 = 40 \text{ cal}$$

$$-\frac{\Delta H^\circ}{R} = 30 \Rightarrow -\Delta H^\circ = 30 \times 2$$

$$\Delta H^\circ = -30 \times 2 \text{ cal.}$$



Q. which of the following lines correctly show the temp. dependence of equilibrium constant K for an exothermic reaction?



Ⓐ A and B

Ⓑ B and C

Ⓒ C and D

Ⓓ A and D