

Gibb's energy and equilibrium constant:-

$$\Delta G = \Delta G^\circ + RT \ln Q$$

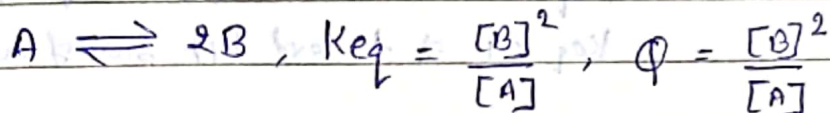
ΔG = Gibbs energy change at any condn.

ΔG° = G.E.C. under standard condition

R = U.G.C. $\rightarrow \frac{8.3}{2} (\Delta G = J)$
 $\rightarrow 2 (\Delta G = \text{cal})$

T = Temp. (K)

Q = Reaction Quotient



K_{eq}	Q	Direction
① Constant	Variable	① $Q < K_{eq} \Rightarrow$ Forward
② given	Calculate	② $Q = K_{eq} \Rightarrow$ eq.
③ Defined only at equilibrium	It is defined at any time.	③ $Q > K_{eq} \Rightarrow$ backward

at equilibrium $\Delta G = 0$, $Q = K_{eq}$.

$$0 = \Delta G^\circ + RT \ln K_{eq}$$

$$\left\{ \begin{array}{l} \Delta G^\circ = 0 \quad K_{eq} = 1 \\ \Delta G^\circ < 0 \quad K_{eq} > 1 \\ \Delta G^\circ > 0 \quad K_{eq} < 1 \end{array} \right.$$

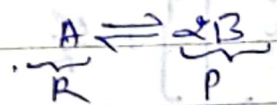
$$\Delta G^\circ = -RT \ln K_{eq}$$

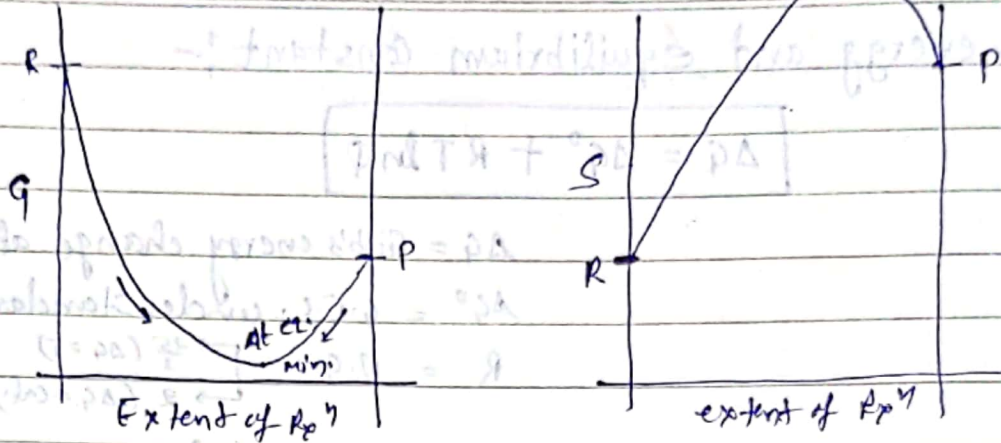
$$\Delta G^\circ = -2.303 RT \log K_{eq}$$

$$\Delta G = -RT \ln K_{eq} + RT \ln Q$$

$$\Delta G = RT \ln \left(\frac{Q}{K_{eq}} \right)$$

- (i) $Q = K_{eq} \Rightarrow \Delta G = 0$ (eq.)
(ii) $Q < K_{eq} \Rightarrow \Delta G < 0$ (spontaneous)
(iii) $Q > K_{eq} \Rightarrow \Delta G > 0$ (Non-spont.)





$K_{eq} = 1 \Rightarrow$ mid point (min/max)

$K_{eq} > 1 \Rightarrow$ toward right side of mid (max/min)

$K_{eq} < 1 \Rightarrow$ toward left side of mid (min/max)

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Variation of K_{eq} with Temp:-

$$\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ \quad (1)$$

$$\Delta G^\circ = -RT \ln K_{eq} \quad (2)$$

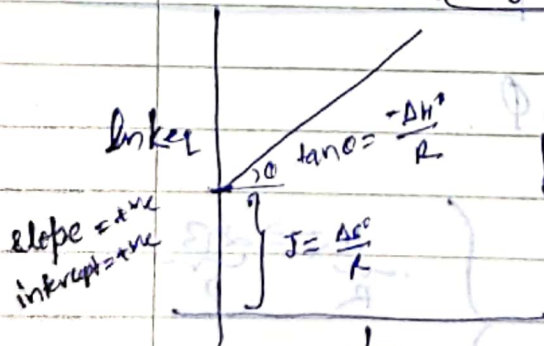
Compare.

$$-RT \ln K_{eq} = \Delta H^\circ - T \Delta S^\circ$$

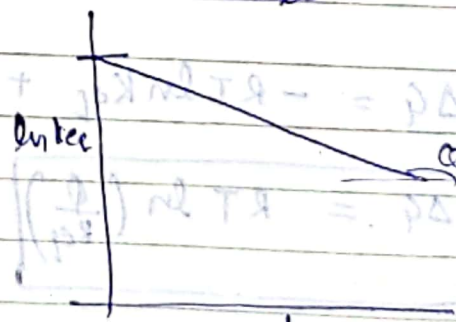
$$\ln K_{eq} = \frac{\Delta H^\circ}{-RT} - \frac{T \Delta S^\circ}{-RT}$$

$$\ln K_{eq} = \frac{\Delta S^\circ}{R} + \left(\frac{-\Delta H^\circ}{R} \right) \times \frac{1}{T}$$

$$y = c + mx$$



(exothermic R_p)
($\Delta H < 0$)

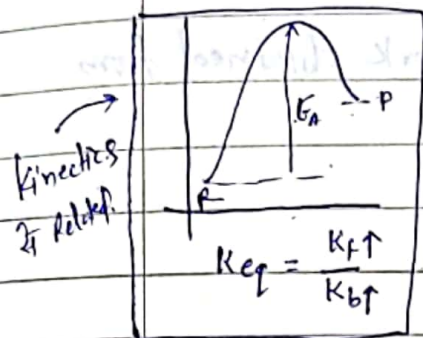


(endothermic R_p)
($\Delta H > 0$)

Slope = -ve
Int = (+)ve
 $\Delta > 90^\circ$

Chemical equilibrium \rightarrow Endo - high Temp $[T \uparrow, K_{eq} \uparrow]$
Exo - low temp. $[T \uparrow, K_{eq} \downarrow]$

$\Rightarrow \Delta S^\circ$ and ΔH° are assumed to be independent from temp.



① $T = T_1, K_{eq} = K_1$

$$\ln K_1 = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_1} \quad \text{--- (i)}$$

② $T = T_2, K_{eq} = K_2$

$$\ln K_2 = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_2} \quad \text{--- (ii)}$$

(ii) - (i)

$$\ln K_2 - \ln K_1 = \left[\frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_2} \right] - \left[\frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{R} \times \frac{1}{T_1} \right]$$

$$\ln \left(\frac{K_2}{K_1} \right) = \frac{\Delta H^\circ}{R} \left[\frac{1}{T_1} - \frac{1}{T_2} \right]$$

(Kinetics & Relatd.)

g.p.

$$\log \frac{K_2}{K_1} = \frac{\Delta H^\circ}{2.303 R} \left[\frac{1}{T_1} - \frac{1}{T_2} \right]$$

ΔH° Cal (R=2)
J (R=2.5/3)

Physical Significance of Gibbs Energy :-

$$G = H - TS$$

Useful energy \leftarrow Total energy \leftarrow useless energy

FLOT $dU = dq + (dw_{p-v} + dw_{non-pv})$

$$dU - dq - dw_{p-v} = dw_{non-pv}$$

$$dU - dq + pdv = dw_{non-pv} \quad [dw_{p-v} = -pdv]$$

at const temp. and pressure for R.P.

$$d(U + pv) - Tds = dw_{non-pv}$$

$$\left\{ ds = \frac{dq_{rev}}{T} \right\}$$

$$dH - Tds = dW_{nm-pv} \quad [H = U + pV]$$

$$d(H - TS) = dW_{nm-pv}$$

$$\boxed{dG = dW_{nm-pv}} \quad (G = H - TS)$$

Decrease in gibb's energy denotes useful work obtained from system.

Formulae:-

$$\Delta G = \Delta G^\circ + RT \ln Q$$

$$\Delta G^\circ = -RT \ln K_{eq}$$

$$\Delta G = RT \ln \left(\frac{Q}{K_{eq}} \right)$$

Q. If eq. constant of a reversible rxn is 1 at 27°C then cal. ΔG° of the rxn?

$$\Delta G^\circ = -RT \ln K_{eq} = -2 \times 300 \times \ln 1$$

$$\boxed{\Delta G^\circ = 0}$$

at eq $\Delta G = 0$, $\Delta G^\circ = 0$ when $K_{eq} = 1$.

Q. If ΔG° of a Rev. Rxn at 27°C is -4.606 K.cal/mole then cal value of K_{eq} .

Sol:

$$\boxed{\Delta G^\circ = -2.303 RT \log K_{eq}}$$

$$\left\{ \ln x = 2.303 \log x \right\}$$

$$-4.606 \times 10^3 = -2.303 \times 2 \times 10^3 \log K_{eq}$$

$$\log K_{eq} = 1$$

$$K_{eq} = 10^1 = 10$$

Q. For a Rev. Rxn $A(g) \rightleftharpoons 2B(g)$, $K_p = 10$ bar at 27°C if K_p is constant P.P. of A and P.P. of B is 1 bar & 5 bar respectively then cal. value of ΔG and Predict the direction of Rxn.

28) $Q_p = \frac{(P_B)^2}{P_A} = \frac{(5)^2}{1} = 25$ $Q_p < K_p \Rightarrow$ Forward dir. ($\Delta G, -ve$)

$$\Delta G = RT \ln \left(\frac{Q}{K_{eq}} \right)$$

$$= 2 \times 300 \ln \left(\frac{25}{100} \right)$$

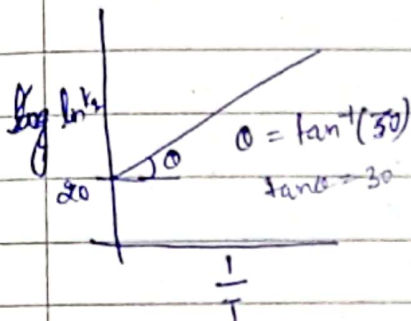
$$\left\{ \ln 2 = 0.693 \right\}$$

$$\Delta G = -600 \ln 4$$

$$\Delta G = -600 \times 2 \times 0.7 = -840 \text{ cal}$$

30-2-18

Q. Cal Value of ΔS° and ΔH° from the following graph (in cal.)



Sol: $\ln K_{eq} = \frac{\Delta S^\circ}{R} + \left(\frac{-\Delta H^\circ}{R} \right) \times \frac{1}{T}$

\downarrow \downarrow \downarrow
 y x z

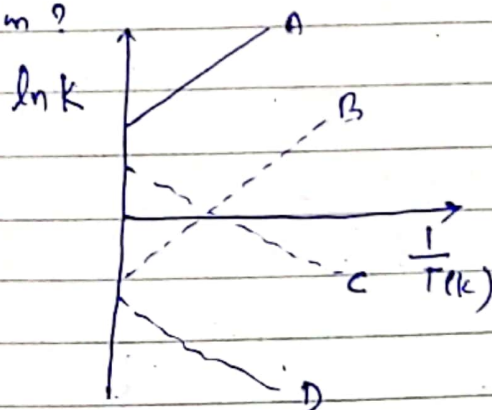
$$\frac{\Delta S^\circ}{R} = 20 \Rightarrow \Delta S^\circ = 20 \times 2 = 40 \text{ cal.}$$

$$-\frac{\Delta H^\circ}{R} = 30 \Rightarrow -\Delta H^\circ = 30 \times 2$$

$$\Delta H^\circ = -30 \times 2 \text{ cal.}$$



Q. which of the following lines correctly show the temp. dependence of equilibrium constant K for an exothermic reaction?



Ⓐ A and B

Ⓑ B and C

Ⓒ C and D

Ⓓ A and D