Aditya Thapliyal
E-40

Tutorial-3

Q1
```
for (i=0 to n)
{ if (arr[i]==key)
    break;
}
```

Q2)
```
void insertion sort (int arr[], int n)
{ for (int i=1; i<n; ++i)
  {
    j = i-1
    x = arr[i]
    while (j>-1 && arr[j]>x)
    { arr[j+1] = arr[j];
      j--;
    }
    arr[j+1] = x;
  }
}

void insertion (int arr[], int n)
{
  if (n<=1) return
  insertion sort (arr, n-1);
  int last = arr[n-1];
  int j = n-2
  while (j>=0 && arr[j]>last)
  { arr[j+1] = arr[j];
    j--;
  }
  arr[j+1] = last;
}
```

(3-2) Algs

Insertion sort doesn't need to know anything about what value it will sort during running & hence called online sort.

Other sorting Algos

1) Bubble Sort
2) Quick Sort
3) Merge Sort
4) Selection Sort
5) Heap Sort

(Imp) Complexity.

Name	Best	Worst	Avg.
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble	$O(n)$	$O(n^2)$	$O(n^2)$
Insertion	$O(n)$	$O(n^2)$	$O(n^2)$
Heap	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quick	$O(n \log n)$	$O(n^2)$	$O(n \log n)$
Merge	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$

(Imp)

Inplace	Stable	Online	← Sorting Type
Bubble	Merge	Insertion	
Selection	Bubble		
Insertion	Insertion		
Quick	~~Heap~~		
Heap	Count Sort		

(3-3) 4 July

Binary Search

Iterative

```
int bsearch (int a[], int l, int r, int key)
{
    while (l<=r)
    int m = (l+r)/2;
    if (a[m] == key)
      return m;
      else if (key < a[m])
        r = m-1;
      else l = m+1;
    }
  return -1;
}
```

Recursive

```
int bs (int ar, int l, int r, int k)
{ while (l<=r)
  { m = (l+r)/2
    if (k == a[m]
    return m;
    else if (key < a[m])
      return bs (ar, l, mid-1, k)
    else
    return bs (a, mid+1, r, k);
  }
return -1
```

Linear search - O(n)

Binary = O(log n)

Que

$T(n) = T(n/2) + 1$ - ①

$T(n/2) = T(n/4) + 1$ - ②

$T(n/4) = T(n/8) + 1$ - ③

$T(n) = T(n/2) + 1$

$T(n/4) + 1 + 1$

$T(n/8) + 1 + 1 + 1$

;

$T(n/2^k) + 1$ (k times)

Let $2^k = n$

$k = \log n$

$T(n) = T(n/n) + \log n$

$T(n) = T(1) + \log(n)$

$T(n) = O(\log n)$ →

Ans Best sorting for practical use

Quick sort is the fastest general sort.
It is stable & has the avg and best running time of O(nlogn)

Ans 31

(10) Quick sort gives the worst time complexity in

1) The array is sorted and either the first or the last element is selected as a pivot.

2) ~~Worst~~ Best case when the pivot is a mean element.

(11)

Merge sort →

Best case → $T(n) = 2T(n/2) + O(n)$

Worst case → $T(n) = 2T(n/2) + O(n)$

Quick sort

Best case → $T(n) = 2T(n/2) + O(n) \rightarrow O(n \log n)$

Worst case → $T(n) = T(n-1) + O(n) \rightarrow O(n^2)$

Ans To prevent bubble sort from scanning the whole array if it is sorted already then we can use a counter to check if any exchanges were made. If not then we break the loop and conclude that the array is sorted

```
void bubb ( int ar , int n )
{   int cnt=0;
    for (int i=0 ; i<n ; ++j )
    {
        for (int j=0; j<n ; ++j )
        {
            If (ar[j] > ar[j+1])
            { Swap (ar[j], ar[j+1]) cnt++; }
        }
        if( !cnt) break;
}
```