

ANSWER KEYS

1. (4) 2. (3) 3. (4) 4. (2) 5. (1) 6. (3) 7. (2) 8. (3)
9. (8.00) 10. (3)

1. (4)

$$\begin{vmatrix} 2 & 1 & 1 \\ 3 & 2\lambda & 4 \\ 1 & 1 & -3\lambda \end{vmatrix} = 0; \quad \begin{vmatrix} 1 & 0 & 1 \\ 3-3\lambda & 2\lambda-4 & 4 \\ 0 & 1+3\lambda & -3\lambda \end{vmatrix} = 0$$

$$\begin{vmatrix} 0 & 0 & 1 \\ -2\lambda-1 & 2\lambda-4 & 4 \\ 3\lambda & 1+3\lambda & -3\lambda \end{vmatrix} = 0$$

$$\Rightarrow (3\lambda + 1)(2\lambda + 1) + 3\lambda(2\lambda - 4) = 0$$

$$\Rightarrow 6\lambda^2 + 5\lambda + 1 + 6\lambda^2 - 12\lambda = 0$$

$$\Rightarrow 12\lambda^2 - 7\lambda + 1 = 0$$

$$\Rightarrow (3\lambda - 1)(4\lambda - 1) = 0$$

$$\Rightarrow \lambda = \frac{1}{3}, \frac{1}{4} \Rightarrow \text{Sum} = \frac{7}{12}$$

2. (3)

The angle bisector for the given two lines $24x + 7y - 20 = 0$ and $4x - 3y - 2 = 0$,

$$\frac{24x+7y-20}{25} = \pm \frac{4x-3y-2}{5}$$

Taking positive sign, we get $2x + 11y - 5 = 0$.

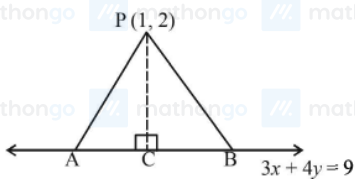
This equation of line is already given.

Therefore, the given three lines are concurrent with one line bisecting the angle between the other two.

3. (4) Point of intersection of $x + 3y - 9 = 0$ and $2x - y - 4 = 0$ is $(3, 2)$ lies on $4x + by - 2 = 0 \Rightarrow b = -5$.

\therefore req lines is $x - 4y + 5 = 0$

4.



(2)

Shortest distance of a point (x_1, y_1) from line

$$ax + by = c \text{ is } d = \frac{|ax_1 + by_1 - c|}{\sqrt{a^2 + b^2}}$$

Now shortest distance of $P(1, 2)$ from $3x + 4y = 9$ is

$$PC = d = \frac{|3(1) + 4(2) - 9|}{\sqrt{3^2 + 4^2}} = \frac{2}{5}$$

Given that $\triangle APB$ is an equilateral triangle Let 'a' be its side

then $PB = a$, $CB = \frac{a}{2}$

Now, In $\triangle PCB$, $(PB)^2 = (PC)^2 + (CB)^2$

(By Pythagoras theorem) $a^2 = \left(\frac{2}{5}\right)^2 + \frac{a^2}{4}$

$$a^2 - \frac{a^2}{4} = \frac{4}{25} \Rightarrow \frac{3a^2}{4} = \frac{4}{25}$$

$$a^2 = \frac{16}{75} \Rightarrow a = \sqrt{\frac{16}{75}} = \frac{4}{5\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{4\sqrt{3}}{15}$$

\therefore Length of Equilateral triangle $(a) = \frac{4\sqrt{3}}{15}$

5. (1) Here, $(x_1, y_1) = (3, 4)$ and $ax + by + c = 2x + y - 7 = 0$

$$\therefore a = 2, \quad b = 1, \quad c = -7$$

Let, (h, k) be the coordinates of the foot.

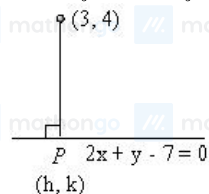
Then,

$$\frac{h-3}{2} = \frac{k-4}{1} = \frac{-(2 \times 3 + 1 \times 4 - 7)}{2^2 + 1^2} = \frac{-3}{5}$$

$$\Rightarrow \frac{h-3}{2} = \frac{-3}{5} \text{ and } \frac{k-4}{1} = \frac{-3}{5}$$

$$\Rightarrow h = \frac{-6}{5} + 3 \text{ and } k = \frac{-3}{5} + 4$$

$$\Rightarrow h = \frac{9}{5} \text{ and } k = \frac{17}{5}$$



6. (3)

Basically, we need to find the intersection of the ray and mirror.

Let us assume $A'(x_1, y_1)$ is the image of $A(2, 3)$ with respect to $x + y = 0$.

$$\Rightarrow A'(-3, -2)$$

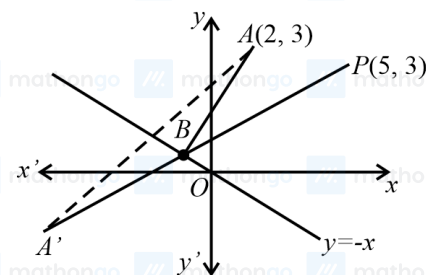
Now, we can say that B is the point of intersection of PA' with $x + y = 0$.

The slope of PA' is $\frac{5}{8}$.

Hence, the equation of the line PA' is given as,

$$y - 3 = \frac{5}{8}(x - 5)$$

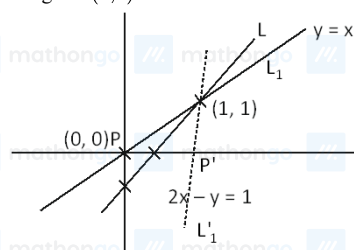
$$\Rightarrow 5x - 8y - 1 = 0$$



Now, on solving the equations $y + x = 0$ and $5x - 8y - 1 = 0$, we will get the point B as $\left(\frac{1}{13}, -\frac{1}{13}\right)$

7. (2) Image of $(0,0)$ w.r.t L lies on L_1

Image of $(0,0)$ w.r.t L is



$$\frac{x-0}{2} = \frac{y-0}{-1} = -2 \left(\frac{-1}{5} \right)$$

$$P' \equiv (x, y) = \left(\frac{4}{5}, \frac{-2}{5} \right)$$

Equation of L_1 which passes through $(1,1)$ and $\left(\frac{4}{5}, \frac{-2}{5}\right)$ is

$$y - 1 = \frac{\frac{-2}{5} - 1}{\frac{4}{5} - 1}(x - 1) = \frac{-7}{-1}(x - 1)$$

$$y = 7x - 6$$

8. (3) mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo

Let $P(h, k)$ be the point dividing the line segment in the ratio $2 : 3$, then

$$\begin{array}{c} 2 \qquad \qquad 3 \\ \hline A(5, 0) \qquad P(h, k) \qquad B(10 \cos \theta, 10 \sin \theta) \\ h = \frac{2(10 \cos \theta) + 3(5)}{2+3} = 4 \cos \theta + 3 \text{ and } k = \frac{2(10 \sin \theta) + 3(0)}{2+3} = 4 \sin \theta \end{array}$$

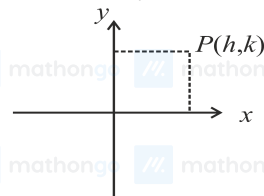
$$\therefore (h-3)^2 + k^2 = 16$$

\Rightarrow Locus of $P(h, k)$ is $(x-3)^2 + y^2 = 16$, which is a circle.

Hence, the perimeter of the circle is $2\pi(4) = 8\pi$ units

9. (8.00) mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo

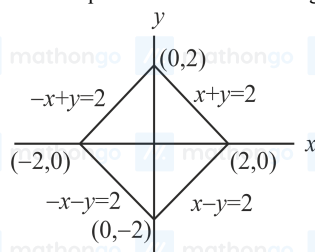
Let x axis and y axis be the two perpendicular lines. Let P be (h, k)



then $|h| + |k| = 2$

So locus of P is $\Rightarrow |x| + |y| = 2$

Which represents four lines forming a square



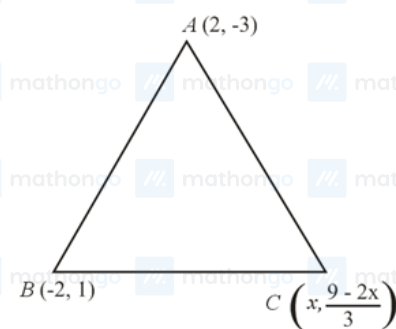
$$\text{Area} = 4 \left(\frac{1}{2} \cdot 2 \cdot 2 \right) = 8$$

10. (3) mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo mathongo

Given $A(2, -3)$ $B(-2, 1)$

The third vertex lies on $2x + 3y = 9$

i.e. $C\left(x, \frac{9-2x}{3}\right)$



\therefore Let $P(h, k)$ be any point on the required locus i.e. P is the centroid of the triangle ABC

$$\Rightarrow \left(\frac{2-2+x}{3}, \frac{-3+1+\frac{9-2x}{3}}{3} \right) = (h, k)$$

$$\therefore h = \frac{x}{3}, k = \frac{3-2x}{9}$$

Eliminating x from the above equations

$$\Rightarrow 9k = 3 - 2(3h)$$

$$\Rightarrow 9k = 3 - 6h$$

$$\Rightarrow 2h + 3k = 1$$

Hence, the locus of $P(h, k)$ is $2x + 3y = 1$