

- The point having position vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$ ,  $3\hat{i} + 4\hat{j} + 2\hat{k}$  and  $4\hat{i} + 2\hat{j} + 3\hat{k}$  are the vertices of
  - right-angled triangle
  - isosceles triangle
  - equilateral triangle
  - collinear
- Given three vectors  $\vec{a} = 6\hat{i} - 3\hat{j}$ ,  $\vec{b} = 2\hat{i} - 6\hat{j}$  and  $\vec{c} = -2\hat{i} + 21\hat{j}$  such that  $\vec{\alpha} = \vec{a} + \vec{b} + \vec{c}$ . Then, the resolution of the vector  $\vec{\alpha}$  into components with respect to  $\vec{a}$  and  $\vec{b}$  is given by
  - $3\vec{a} - 2\vec{b}$
  - $3\vec{b} - 2\vec{a}$
  - $2\vec{a} - 3\vec{b}$
  - $\vec{a} - 2\vec{b}$
- If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are three non-zero vectors which are pairwise non-collinear. Also,  $\vec{a} + 3\vec{b}$  is collinear with  $\vec{c}$  and  $\vec{b} + 2\vec{c}$  is collinear with  $\vec{a}$ , then  $\vec{a} + 3\vec{b} + 6\vec{c}$  is
  - $\vec{a} + \vec{c}$
  - $\vec{a}$
  - $\vec{c}$
  - 0
- Let  $A(2\hat{i} + 3\hat{j} + 5\hat{k})$ ,  $B(-\hat{i} + 3\hat{j} + 2\hat{k})$  and  $C(\lambda\hat{i} + 5\hat{j} + \mu\hat{k})$  are vertices of a triangle and its median through  $A$  is equally inclined to the positive directions of the axes. The value of  $2\lambda - \mu$  is equal to
- Let  $\vec{a} = (1, 1, -1)$ ,  $\vec{b} = (5, -3, -3)$  and  $\vec{c} = (3, -1, 2)$ . If  $\vec{r}$  is collinear with  $\vec{c}$  and has length of  $\frac{|\vec{a} + \vec{b}|}{2}$ , then  $\vec{r}$  equals
  - $\pm 3\vec{c}$
  - $\pm \frac{3}{2}\vec{c}$
  - $\pm \vec{c}$
  - $\pm \frac{2}{3}\vec{c}$
- If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are unit vectors satisfying the relation  $\vec{a} + \vec{b} + \sqrt{3}\vec{c} = 0$ , then the angle between  $\vec{a}$  and  $\vec{b}$  is
  - $\frac{\pi}{6}$
  - $\frac{\pi}{4}$
  - $\frac{\pi}{3}$
  - $\frac{\pi}{2}$
- If  $|\vec{A} + \vec{B}| = n|\vec{A} - \vec{B}|$  and  $|A| = |B|$  then what is angle between  $\vec{A}$  and  $\vec{B}$ ?
  - $\theta = \cos^{-1}\left(\frac{n^2-1}{n^2+1}\right)$
  - $\theta = \sin^{-1}\left(\frac{n^2-1}{n^2+1}\right)$
  - $\theta = \sin^{-1}\left(\frac{n-1}{n+1}\right)$
  - $\theta = \cos^{-1}\left(\frac{n-1}{n+1}\right)$
- Let the vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are perpendicular to  $\vec{b} + \vec{c}$ ,  $\vec{c} + \vec{a}$  and  $\vec{a} + \vec{b}$  respectively. If  $|\vec{a} + \vec{b}| = 6$ ,  $|\vec{b} + \vec{c}| = 8$  and  $|\vec{c} + \vec{a}| = 10$ , then the value of  $|\vec{a} + \vec{b} + \vec{c}|$  is equal to
  - $5\sqrt{5}$
  - 50
  - $10\sqrt{2}$
  - 10
- The length of longer diagonal of the parallelogram constructed on  $5\vec{a} + 2\vec{b}$  and  $\vec{a} - 3\vec{b}$ . If it is given that  $|\vec{a}| = 2\sqrt{2}$ ,  $|\vec{b}| = 3$  and angle between  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{4}$  is
  - 15
  - $\sqrt{113}$
  - $\sqrt{593}$
  - $\sqrt{369}$
- If vector  $\vec{a} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and vector  $\vec{b} = -2\hat{i} + 2\hat{j} - \hat{k}$ , then  $\frac{\text{Projection of vector } \vec{a} \text{ on vector } \vec{b}}{\text{Projection of vector } \vec{b} \text{ on vector } \vec{a}} =$ 
  - $\frac{3}{7}$
  - $\frac{7}{3}$
  - 3
  - 7