

- A point  $P$  moves on  $xy$ -plane such that  $PS + PS' = 4$ , where  $S(K, 0)$  and  $S'(-K, 0)$ , then which of the following is not true about the locus of  $P$  ?  
 (1) Ellipse if  $K \in (-2, 2)$  (2) Line segment if  $K = \pm 2$   
 (3) Empty if  $K \in (-\infty, -2) \cup (2, \infty)$  (4) None of these
- The equation  $\left| \sqrt{x^2 + (y-1)^2} - \sqrt{x^2 + (y+1)^2} \right| = K$  will represent a hyperbola for -  
 (1)  $K \in (0, 2)$  (2)  $K \in (0, 1)$   
 (3)  $K \in (1, \infty)$  (4)  $K \in (0, \infty)$
- If a directrix of a hyperbola centered at the origin and passing through the point  $(4, -2\sqrt{3})$  is  $5x = 4\sqrt{5}$  and its eccentricity is  $e$ , then:  
 (1)  $4e^4 + 8e^2 - 35 = 0$  (2)  $4e^4 - 24e^2 + 35 = 0$   
 (3)  $4e^4 - 24e^2 + 27 = 0$  (4)  $4e^4 - 12e^2 - 27 = 0$
- The ellipse  $E_1 : \frac{x^2}{9} + \frac{y^2}{4} = 1$  is inscribed in a rectangle  $R$  whose sides are parallel to the coordinate axes. Another ellipse  $E_2$  passing through the point  $(0, 4)$  circumscribes the rectangle  $R$ . The length (in units) of the major axis of ellipse  $E_2$  is
- A hyperbola having the transverse axis of length 1 unit is confocal with the ellipse  $3x^2 + 4y^2 = 12$ . The square of length of conjugate axis of hyperbola is \_\_
- If the eccentricity and length of latus rectum of a hyperbola are  $\frac{\sqrt{13}}{3}$  and  $\frac{10}{3}$  units respectively, then find the length of the transverse axis.
- Let  $LL'$  be the latus rectum through the focus of the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  and  $A$  be the farther vertex. If  $\triangle ALL'$  is equilateral, then the eccentricity of the hyperbola is (axes are coordinate axes)  
 (1)  $\sqrt{3}$  (2)  $\sqrt{3} + 1$   
 (3)  $\frac{\sqrt{3}+1}{\sqrt{2}}$  (4)  $\frac{\sqrt{3}+1}{\sqrt{3}}$
- If  $S$  and  $S'$  are the foci of the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  and if  $PSP'$  is a focal chord with  $SP = 8$  then  $SS' =$   
 (1)  $4 + S'P$  (2)  $S'P - 1$   
 (3)  $4 + SP$  (4)  $SP - 1$
- A chord is drawn passing through  $P(2, 2)$  on the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  such that it intersects the ellipse at points  $A$  and  $B$ . Then the maximum value of  $PA \cdot PB$  is equal to  
 (1)  $\frac{61}{4}$  (2)  $\frac{59}{4}$   
 (3)  $\frac{71}{4}$  (4)  $\frac{63}{4}$
- If  $(a \sec \theta, b \tan \theta)$  &  $(a \sec \phi, b \tan \phi)$  be the coordinates of the ends of a focal chord passing through  $(ae, 0)$  of  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ , then  $\tan \frac{\theta}{2} \tan \frac{\phi}{2}$  equals to  
 (1)  $\frac{e-1}{e+1}$  (2)  $\frac{1-e}{1+e}$   
 (3)  $\frac{1+e}{1-e}$  (4)  $\frac{e+1}{e-1}$