

- If  $\theta$  lies in the second quadrant and  $3 \tan \theta + 4 = 0$ , then the value of  $2 \cot \theta - 5 \cos \theta + \sin \theta$  is  $\frac{6}{k}$  then find  $k$ .
- If  $\cos(\alpha + \beta) = \frac{3}{5}$ ,  $\sin(\alpha - \beta) = \frac{5}{13}$  and  $0 < \alpha, \beta < \frac{\pi}{4}$ , then  $\tan(2\alpha)$  is equal to:
  - $\frac{21}{16}$
  - $\frac{63}{52}$
  - $\frac{33}{52}$
  - $\frac{63}{16}$
- $\lambda = \sin^2(5^\circ) + \sin^2(10^\circ) + \dots + \sin^2(85^\circ)$ . Then number of positive divisors of  $2\lambda - 8$  is equal to
  - 2
  - 3
  - 4
  - 5
- For any  $\theta \in \left(\frac{\pi}{4}, \frac{\pi}{2}\right)$ , the expression  $3(\sin \theta - \cos \theta)^4 + 6(\sin \theta + \cos \theta)^2 + 4 \sin^6 \theta$  equals:
  - $13 - 4\cos^2 \theta + 6\cos^4 \theta$
  - $13 - 4\cos^6 \theta$
  - $13 - 4\cos^2 \theta + 6\sin^2 \theta \cos^2 \theta$
  - $13 - 4\cos^4 \theta + 2\sin^4 \theta \cos^2 \theta$
- The value of  $\frac{\sin 22^\circ \cos 8^\circ + \cos 158^\circ \cos 98^\circ}{\sin 23^\circ \cos 7^\circ + \cos 157^\circ \cos 97^\circ} =$ 
  - 1
  - 2
  - $\frac{1}{2}$
  - $\frac{1}{4}$
- If  $F(k) = \left(1 + \sin \frac{\pi}{2k}\right) \left(1 + \sin(k-1)\frac{\pi}{2k}\right) \left(1 + \sin(2k+1)\frac{\pi}{2k}\right) \left(1 + \sin(3k-1)\frac{\pi}{2k}\right)$ , then the value of  $F(1) + F(2) + F(3)$  is equal to
  - $\frac{3}{16}$
  - $\frac{1}{4}$
  - $\frac{5}{16}$
  - $\frac{7}{16}$
- Let the maximum and minimum value of the expression  $2 \cos^2 \theta + \cos \theta + 1$  is  $M$  and  $m$  respectively, then the value of  $\left[\frac{M}{m}\right]$  is, (where  $[.]$  is the greatest integer function)
- The maximum value of  $3 \cos \theta + 5 \sin\left(\theta - \frac{\pi}{6}\right)$  for any real value of  $\theta$  is :
  - $\sqrt{19}$
  - $\sqrt{31}$
  - $\frac{\sqrt{79}}{2}$
  - $\sqrt{34}$
- The number of integers in the range of  $3 \sin^2 x + 3 \sin x \cos x + 7 \cos^2 x$  are:
  - 3
  - 4
  - 5
  - 6
- Let  $\alpha = \max_{x \in \mathbb{R}} \{8^{2 \sin 3x} \cdot 4^{4 \cos 3x}\}$  and  $\beta = \min_{x \in \mathbb{R}} \{8^{2 \sin 3x} \cdot 4^{4 \cos 3x}\}$ . If  $8x^2 + bx + c = 0$  is a quadratic equation whose roots are  $\alpha^{1/5}$  and  $\beta^{1/5}$ , then the value of  $c - b$  is equal to :
  - 42
  - 47
  - 43
  - 50