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## **Assignment 3**

**AI1110**: Probability and Random Variables Indian Institute of Technology Hyderabad

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Question[12.13.5.9]:On a multiple choice examination with three possible answers for each of the five questions, what is the probability that a candidate would get four or more correct answers just by guessing

**Solution:** Let X be the number of correct answers that the candidate gets just by guessing.

$$X = bin(n, p) \tag{1}$$

Where,

$$n = 5$$
(total no of questions) (2)

$$p = \frac{1}{3} \text{(probability of guessing a question correct)} \tag{3}$$

$$\therefore q = 1 - p = 1 - \frac{1}{3} = \frac{2}{3} \tag{4}$$

The probability mass function for candidate getting k correct answers just by guessing:

$$p_X(k) = \Pr\left(X = k\right) \tag{5}$$

$$= {}^{n}C_{k} \times p^{k} \times q^{(n-k)} \tag{6}$$

$$= {}^{5}C_{k} \times \left(\frac{1}{3}\right)^{k} \times \left(\frac{2}{3}\right)^{(5-k)} \tag{7}$$

Then, the probability that the candidate gets four or more correct answers just by guessing is:

$$\Pr(X \ge 4) = p_X(4) + p_X(5) \tag{8}$$

$$= {}^{5}C_{4} \times \left(\frac{1}{3}\right)^{4} \times \left(\frac{2}{3}\right)^{(5-4)} + {}^{5}C_{5} \times \left(\frac{1}{3}\right)^{5} \times \left(\frac{2}{3}\right)^{(5-5)} \tag{9}$$

$$= 5 \times \left(\frac{1}{3}\right)^4 \times \left(\frac{2}{3}\right)^1 + \left(\frac{1}{3}\right)^5 \times \left(\frac{2}{3}\right)^0 \tag{10}$$

$$=\frac{11}{243}$$
 (11)

 $\therefore$  The probability that a candidate would get four or more correct answers just by guessing is  $\frac{11}{243}$ .