# MATHEMATICS (SEMESTER - 2)

# CS/BCA/SEM-2/BM-201/09



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2.	Signature of Invigilator  Reg.  Signature of the Officer-in-Charge	. No													
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	CS/BC ENGINEERING & MAN MATHEM	IAGI	ЕМІ	ENT	EX	AM	IINA	ATIC	ONS		 2-2	009	<b>-</b> -		
Tin	ne: 3 Hours]									·		[ Fı	ıll M	larks	s : 70

#### **INSTRUCTIONS TO THE CANDIDATES:**

- 1. This Booklet is a Question-cum-Answer Booklet The Booklet consists of **32 pages**. The questions of this concerned subject commence from Page No 3.
- 2. a) In **Group A**, Questions are of Mult ple Choice type. You have to write the correct choice in the box provided **against each question**.
  - b) For **Groups B** & **C** you have to answer the questions in the space provided marked 'Answer Sheet'. Questions of **Group B** are Short answer type. Questions of **Group C** are Long answer type. Write on both sides of the paper.
- 3. **Fill in your Roll No. in the box** provided as in your Admit Card before answering the questions.
- 4. Read the instructions given inside carefully before answering.
- 5. You should not forget to write the corresponding question numbers while answering.
- 6. Do not write your name or put any special mark in the booklet that may disclose your identity, which will render you liable to disqualification. Any candidate found copying will be subject to Disciplinary Action under the relevant rules.
- 7. Use of Mobile Phone and Programmable Calculator is totally prohibited in the examination hall.
- 8. You should return the booklet to the invigilator at the end of the examination and should not take any page of this booklet with you outside the examination hall, **which will lead to disqualification**.
- 9. Rough work, if necessary is to be done in this booklet only and cross it through.

No additional sheets are to be used and no loose paper will be provided

# FOR OFFICE USE / EVALUATION ONLY Marks Obtained Group - A Group - B Group - C Question Number Marks Obtained Marks Obtained

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Head-Examiner,	/Co-Ordinator	/Scrutineer

2324 (11/06)



## **ENGINEERING & MANAGEMENT EXAMINATIONS, JUNE - 2009**

# **MATHEMATICS**

# **SEMESTER - 2**

Time: 3 Hours]	[ Full Marks : 70
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#### **GROUP - A**

# ( Multiple Choice Type Questions )

1.	Choose the correct alte	ernatives for any ten of	the following:	10 × .	I = IO

- i) If  $\alpha$  = (1, 0, 3) and  $\beta$  = (-1, 2, 5), then  $\alpha$  + 3  $\beta$  is equal to
  - a) (-2, 6, 18)

b) (2, -6, -18)

c) (2, -6, 18)

- d) (-1, -3, 5).
- ii) The basis of a vector space on ains
  - a) linearly independent set of vectors
  - b) linearly dep ndent set of vectors
  - c) scalars only
  - d) none of these.
- iii) Integrating factor of x dx = -y dy is
  - a) 1/(xy)

b)  $1/(x^2 + y^2)$ 

c)  $1/y^2$ 

d) none of these.



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iv) The infinite series  $\int_{n=1}^{\infty} \frac{1}{n^p}$  converges if

a) p = 1 b)

p > 1

c) p < 1 d)

none of these.

v) The order and degree of the differential equation  $\left(\frac{d^2 y}{dx^2}\right)^{2/3} - 3\frac{dy}{dx} = 4$  are

a) 2, 2

b)  $2, \frac{2}{3}$ 

c) 2, 1

d) 2, 3

vi) If the three vectors (5, 2, 3), (7, 3, x) and (9, 4, 5) are linearly dependent, then x is

a) 1

b) 2

c) 3

d) 4

vii) If  $\lim_{n \to \infty} a_n = 0$ , then the series  $\Sigma (-1)^n a_n$  is

a) convergent

b) divergent

c) oscillatory

d) none of these.

viii) The family of curves  $y = e^x$  ( A cos  $x + B \sin x$  ) is represented by the differential equation

a) 
$$\frac{d^2 y}{dx^2} = 2 \frac{dy}{dx} - y$$

b) 
$$\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = 2\frac{\mathrm{d}y}{\mathrm{d}x} - 2y$$

c) 
$$\frac{d^2 y}{dx^2} = \frac{dy}{dx} - 2y$$

d) 
$$\frac{d^2 y}{dx^2} = 2\frac{dy}{dx} + y.$$



		5			$\simeq$
ix)	The	sequence $1, \frac{1}{2}, \frac{1}{3}, \dots \frac{1}{n}, \dots$	onverge	es to	
	a)	•	b)	0	
	c)	1	d)	$\frac{1}{2}$ .	
x)	The	four vectors ( 1, 1, 0, 0 ), ( 1,	0, 0, 1	), ( 1, 0, $\alpha$ , 0, ) and ( 0, 1, $\alpha$ ,	b) are
	linea	rly independent if			
	a)	а п 0, b п 2	b)	а π 2, b π 0	
	c)	$a \pi 0, b \pi - 2$	d)	$a \pi - 2, b \pi 0.$	
xi)	The	solution of $\log\left(\frac{\mathrm{d}y}{\mathrm{d}x}\right) = ax + by$	is		
	a)	$b e^{-ax} + a e^{-by} + k = 0$	b)	$b e^{ax} + a e^{-by} + k = 0$	
	c)	$b e^{-ax} + a e^{by} + k = 0$	d)	$b e^{ax} + a e^{by} + k = 0.$	
xii)	lim n Ø •	$\frac{x^n}{n}$ is equal to			
	a)	0	b)	1	
	c)	- 1	d)	none of these.	

xiii) The lower bound of the sequence  $\left\{\frac{(-1)^{n-1}}{n!}\right\}$  ) is

a)  $-\frac{1}{2}$ 

b) -

c) 1

d) 0.

xiv) The value of  $\lim_{n \neq \infty} \log (1/n)$  is equal to

a) 0

b) 1

c) - •

d) none of these.



#### 6 **GROUP – B**

#### (Short Answer Type Questions)

Answer any three of the following.

 $3 \times 5 = 15$ 

- 2. Find the equation of curve whose slope at any point (x, y) on it is 2y and which passes through the point (3, 1).
- 3. Test for the convergence of the series :

$$x + \frac{2^2 x^2}{2!} + \frac{3^3 x^3}{3!} + \frac{4^4 x^4}{4!} + \dots, x > 0.$$

- 4. Examine whether the vectors (1, 2, 3, 0), (2, 1, 0, 3), (1, 1, 1, 1) and (2, 3, 4, 1) are linearly dependent or not. If yes, find among them which are independent.
- 5. Solve any three:

a) 
$$x \frac{dy}{dx} + y = y^2 \log x$$

b) 
$$\cos^2 x \frac{dy}{dx} + y = \tan x$$

c) 
$$y = px - \frac{a}{p}$$
 where  $p = \frac{dy}{dx}$ 

d) 
$$\left(D^2 - 2D + 1\right) y = x e^x \text{ where } D = \frac{d}{dx}$$

6. Define the limit of a sequence. Find

$$\lim_{n \not o} \left[ \frac{1}{n^2} + \frac{2}{n^2} + \dots + \frac{n}{n} \right] .$$

#### **GROUP - C**

#### (Long Answer Type Questions)

Answer any three of the following.

 $3 \times 15 = 45$ 

- 7. a) Define basis of a vector space V. Show that  $\alpha_1 = (1, 0, 0)$ ,  $\alpha_2 = (0, 1, 0)$  and  $\alpha_3 = (0, 0, 1)$  form a basis of the vector space  $V_3$ .
  - b) If  $\{\alpha, \beta, \gamma\}$  be a basis of real vector space V and  $c \pi 0$  be a real number, examine whether  $\{\alpha + c \beta, \beta + c \gamma, \gamma + c \alpha\}$  is a basis of V or not.
  - c) Find the value of k for which the vectors (1, 2, 1), (k, 1, 1) and (1, 1, 2) in  $R^3$  are linearly dependent.



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8. Test the convergence of any *three* of the following series :

$$3 \times 5 = 15$$

a) 
$$1 + \frac{x}{2} + \frac{x^2}{5} + \frac{x^2}{10} + \dots$$

b) 
$$\left(\frac{1}{3}\right)^2 + \left(\frac{1.2}{3.5}\right)^2 + \left(\frac{1.2.3}{3.5.7}\right)^2 + \dots$$

c) 
$$\alpha \left( 1 + \frac{1}{\sqrt{n}} \right)^{-\sqrt{n}}$$

d) 
$$\frac{\alpha}{n=1} \left( \frac{\cos nx}{n^2} \right)$$
.

9. Solve any *three* of the following:

$$3 \times 5 = 15$$

a) 
$$\frac{dy}{dx} + \frac{y \log y}{x} = \frac{y (\log y)^2}{x^2}$$

b) 
$$y = 2 px - p^2$$
 where  $p = \frac{dy}{dx}$ 

c) 
$$e^x \sin y \, dx + (e^x + 1) \cos y \, dy = 0$$

d) 
$$(D^2 - 2D)y = e^x \sin x$$
.

- 10. a) Prove that  $s = \{(0, 1, 1), (1, 0, 1), (1, 1, 0) \text{ is a basis of } R^3 .$ 
  - b) Show that  $w = \{ (x, y \mid z) \land R^3 / x + y + z = 0 \}$  is a sub-space of  $R^3$  and find a basis of w.
  - c) Determine K so that the set S is linearly dependent in  $R^3$

$$S = \{ (1, 2, 1), (k, 3, 1), (2, k, 0) \}.$$

$$5 + 5 + 5$$

- 11. a) Define the linear sum of two sets of vectors S and T.
  - b) If S and T are two sub-spaces of a vector space V, obtain a relation between rank (S), rank (T) and rank (V).
  - c) Let  $T: R^2 \varnothing R^2$  be a linear transformation such that T(1, 1) = (2, -3) and T(1, -1) = (4, 7). Find the matrix of T.



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12. a) Using D' Alembert's ratio test, show that the following series is convergent :

$$x^{2} + (2^{2} / 3.4) x^{4} + (2^{2}.4^{2} / 3.4.5.6) x^{6} + \dots$$

- b) Prove that every absolutely convergent series is convergent.
- c) Show that the following series is convergent :

$$u_n = \sqrt{n^3 + 1} - \sqrt{n^3}$$
 in  $n \mid [1, \bullet]$ .

**END**