

**BM-301**

**MATHEMATICS FOR COMPUTING**

Time Allotted: 3 Hours

Full Marks: 70

*The questions are of equal value.*

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable.*

**GROUP A**  
**(Multiple Choice Type Questions)**

1. Answer any *ten* questions.

10×1 = 10

(i) Maximum number of edges with  $n$  vertices in a completely connected graph is

- (A)  $(n - 1)$  (B)  $\frac{(n-1)}{2}$   
(C)  $\frac{n}{2}$  (D)  $\frac{n(n-1)}{2}$

(ii) Prim's algorithm is used to find the minimal spanning tree of a

- (A) dense graph (B) sparse graph  
(C) null graph (D) normal graph

(iii) A Simple graph has

- (A) no self loops (B) no parallel edges  
(C) both (A) and (B) (D) none of these

(iv) The generating function of  $\{1, 1, 1, \dots\}$  is

- (A)  $\frac{1}{(1-x)}$  (B)  $\frac{1}{(1+x)}$   
(C)  $\frac{1}{(1-x)(1+x)}$  (D) none of these

- (v) A Grammar is said to be regular if it is of  
(A) type 0 (B) type 1  
(C) type 2 (D) type 4
- (vi) The mathematical model of Mealy machine is a  
(A) 5 tuple (B) 4 tuple  
(C) 6 tuple (D) none of these
- (vii) If  $n! = x(n-2)!$  Then  $x =$   
(A)  $n$  (B)  $n-1$   
(C)  $n(n-2)$  (D)  $n(n-1)$
- (viii) Number of four digit numbers formed by digits 3, 1, 3, 1 is  
(A) 5 (B) 10  
(C) 20 (D) 6
- (ix) The proposition  $P \wedge (Q \wedge \neg Q)$  is a  
(A) contradiction (B) tautology  
(C) both (A) and (B) (D) none of these
- (x) Number of elements contained in an incidence matrix of a digraph is  
(A) 1 (B) 2  
(C) 3 (D) none of these
- (xi) A pseudo graph  
(A) Must have loops (B) Does not have loop  
(C) Must have parallel edges (D) None of these
- (xii) Choose the correct statement:  
(A) path is an open walk  
(B) every walk is a trail  
(C) every trail is a path  
(D) a vertex cannot appear twice in a walk

**GROUP B**  
**(Short Answer Type Questions)**

Answer any *three* questions.

3×5 = 15

2. In an examination a minimum is to be secured in each of the 5 subjects for a pass. In how many ways can a student fail?
3. Find the sequence from the generating function  $\frac{(3+7x)}{(1-x)(1+4x)}$
4. Prove that  $((P \wedge \neg Q) \rightarrow R) \rightarrow (P \rightarrow (Q \vee R))$  is a tautology.
5. Write a short note on Moore machine.
6. Show that a tree with  $n$  vertices has  $(n - 1)$  edges.

**GROUP C**  
**(Long Answer Type Questions)**

Answer any *three* questions.

3×15 = 45

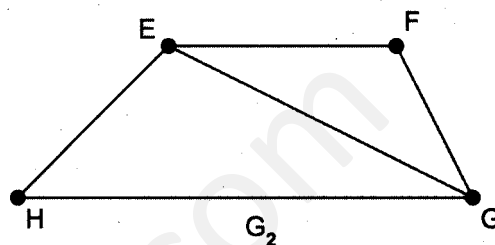
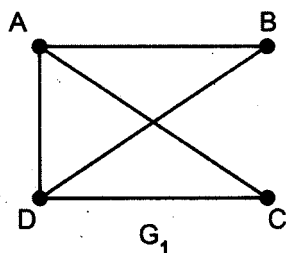
7. (a) Solve the following recurrence relation by generating function method: 5  
 $a^n - 2a_{n-1} + a_{n-2} = 2^{n-2}$  for  $n \geq 2$  and  $a_0 = 1, a_1 = 5$
- (b) What is a Deterministic Finite Automata (DFA)? Explain with suitable example. 5
- (c) Write CNF and DNF of the following statement:  $p \vee \{\neg p \rightarrow (q \vee (q \rightarrow \neg r))\}$  5
- 8.(a) Find the grammar of the set of the terminals  $\{a, b\}$  that generates the language 6  
 $L = \{a, ab, ab^2, ab^3, \dots\}$ .
- (b) Let  $Z$  be a set of all integers and a binary relation  $\rho$  is defined on  $Z$  by the rule, 6  
 $m \rho n$  means  $m - n$  is divisible by 5 such that  $\rho$  is an equivalence relation on  $Z$  and identify the equivalent classes.
- (c) Show that  $|2n = 2n\{1, 3, 5 \dots (2n-1)\}|_n$  3

9.(a) Find out the characteristic roots of the recurrence relation  $a_n + 4a_{n-1} + 3a_{n-2} = 0$  and hence solve it. 6

(b) Show that a simple graph with  $n$  vertices and  $k$  components has at most  $\frac{(n-k)(n-k+1)}{2}$  edges. 6

(c) Prove the following equivalence:  $\neg p \wedge q \Leftrightarrow \neg(p \vee (\neg p \wedge q))$  3

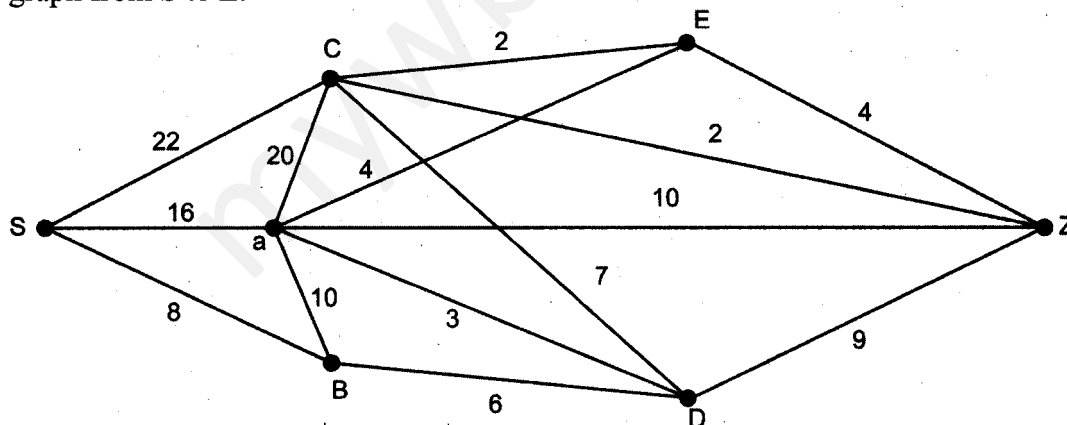
10.(a) Find whether the following two graphs are isomorphic or not: 5



(b) How many integral solutions are there of  $x_1 + x_2 + x_3 + x_4 + x_5 = 30$  where  $x_1 \geq 2$ ,  $x_2 \geq 3$ ,  $x_3 \geq 4$ ,  $x_4 \geq 2$ ,  $x_5 \geq 0$  6

(c) Determine the value of  $n$  if  $4 \times {}^nP_3 = {}^{n+1}P_3$ . 4

11.(a) Using Kruskal's algorithm find the minimal spanning tree from the following graph from S to Z. 6



(b) Write short note on Hamiltonian Graph. 3

(c) Using the principle of mathematical induction prove that 6

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$