

CHE312- Assignment

Group-18

Group Members

Aditya Singh Kaurav : 200055

Harjap Singh : 200405

Pradhyumna Lavania : 200692

Harshit Sinha : 200436

Pratibha Anand : 200713

Raghav Prakash Agarwal : 190659

Question

A copper cube of 1 m side is to be cooled from 120 °C to 50 °C using stagnant air at 25°C. Estimate the time required for this process, with and without approximating the cube as a sphere.

Solution

ASSUMPTIONS:

- Heat transfer due to radiations is negligible (as Copper has low emissivity).
- Density of Copper is taken to be constant as 8.96g/cm^3 during whole process.
- Temperature gradient inside the body are consider negligible (later, has been proved in IPYNB file)
- Heat capacity of Copper is considered at average temperature as 385J/kgC .
- While approximating as a sphere, we consider the same mass i.e. cube of copper and sphere of copper have same mass. So using **Mass-Volume-Density** relation, we get radius $=0.62\text{m}$. (same mass imply same volume, so $a^3 = (4/3)*\pi*r^3 \Rightarrow r =0.62\text{m}$)
- Integration is simplified by taking the areas of discrete intervals of 2.5 degrees.

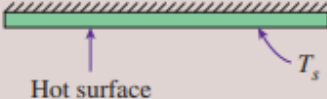
APPROACH:

Cube

- Cube is taken as made up of 4 vertical and 2 horizontal plates.
- Average Nusselt number's formula are used to calculate heat transfer coefficient at particular surface temperature.

$$\text{Nu} = \left\{ 0.825 + \frac{0.387 \text{Ra}_L^{1/6}}{[1 + (0.492/\text{Pr})^{9/16}]^{8/27}} \right\}^2$$

(complex but more accurate)

	10^4-10^7	(a) $Nu = 0.54 Ra_L^{1/4}$
(b) Lower surface of a hot plate (or upper surface of a cold plate)		
	10^5-10^{11}	(b) $Nu = 0.27 Ra_L^{1/4}$

- We calculate Rayleigh number using characteristic length scale, which comes out to be less than $1e+7$, so suitable formulas are used.
- Then, we use the discrete approach: at very temperature change of 2.5 degree C, we evaluate 'h'. In this way, we obtain nearly 30 values .
- During the estimation of each 'h', we find the values of ν, Pr, α and K at average of surface and surrounding temperature (EXCEL FILE is attached)
- We get a list of 'h' values.
- then we use numerical method approach to solve the following equation
: $-mC_p dT = hA_s(T-T_{\infty})dt$

$$\left(\begin{array}{c} \text{Heat transfer into the body} \\ \text{during } dt \end{array} \right) = \left(\begin{array}{c} \text{The increase in} \\ \text{the of the body} \\ \text{energy during } dt \end{array} \right)$$

or

$$hA_s(T_{\infty} - T)dt = mc_p dT$$

NUMERICAL METHOD APPROACH:

$$\begin{aligned}mC_p \frac{dT}{dt} &= -h_{conv} A_s (T - T_\infty) \\ \frac{dT}{dt} &= -\frac{h_{conv} A_s}{mC_p} (T - T_\infty) \\ dt &= -\frac{mC_p}{h_{conv} A_s (T - T_\infty)} dT \\ \Delta t &= -\frac{mC_p}{h_{conv} A_s (T - T_\infty)} \Delta T \\ \Sigma \Delta t &= \sum_{T=120^\circ C}^{T=50^\circ C} -\frac{mC_p}{h_{conv} A_s (T - T_\infty)} \Delta T\end{aligned}$$

h_{conv} is discretely calculated for different intervals of $2.5^\circ C$.

- After solving this we get $t = 1074224 \text{ sec} \sim 298 \text{ Hrs}$

INTEGRATION APPROACH:

More better results are obtained by applying polynomial fit to the h_{conv} data and then using Scipy library to evaluate integral.

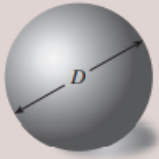
Fitted Curve Equation:-

$$h_{conv} = (1.437065 + 0.05147343T - 0.0001968346T^2)$$

Then integrating the equation we get the total time for cube as:
1115605 s ~ 308 Hrs

Sphere

- Again we follow the same approach, but now we calculate the 'h' at each of discrete temperature using the given formula:

Sphere		D	$Ra_D \leq 10^{11}$ $(Pr \geq 0.7)$	$Nu = 2 + \frac{0.589 Ra_D^{1/4}}{[1 + (0.469/Pr)^{9/16}]^{4/9}}$
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- Again we apply numerical method approach to calculate the time:
Which we get as $t = 1769687 \text{ sec} \sim 491 \text{ Hrs.}$

IPYNB file is attached containing all calculations, values and plots.

Values Obtained

Time to go from 120°C to 50°C in cube:

$t_{\text{cube}} = 298 \text{ Hrs}$

Time to go from 120°C to 50°C in sphere:

$t_{\text{sphere}} = 491 \text{ Hrs}$

Average convective Heat Transfer Coefficient (Cube):

$H_{\text{conv}} = 4.33 \text{ (W/m}^2\text{K)}$

Average convective Heat Transfer Coefficient (Sphere):

$H_{\text{conv}} = 0.54 \text{ (W/m}^2\text{K)}$

Biot Number comes out to be less than 0.1 in both cases (explicitly, shown in IPYNB file)

Conclusions:

-We found that for the same mass of copper, but the different shape we get different time for the transient process to take place. In the case of the sphere (radius = 0.62m), we get time = 1074224 sec (~298 hours) while in the case of cube we get time = 1769687 sec. (~ 491 hours). One of the possible reason for it can be that there is less surface area ($4\pi r^2 \sim 4.82\text{m}^2$) in case of sphere while there is ($6a^2 \sim 6\text{m}^2$) in case of cube. So large surface area will help in fastening the heat transfer process.