

A \ B	C=0		C=1	
	00	01	11	10
0	m <sub>0</sub>	m <sub>1</sub>	m <sub>3</sub>	m <sub>2</sub>
1	m <sub>4</sub>	m <sub>5</sub>	m <sub>7</sub>	m <sub>6</sub>

4-variable

A \ B	C=0		C=1	
	00	01	11	10
0	m <sub>0</sub>	m <sub>1</sub>	m <sub>3</sub>	m <sub>2</sub>
1	m <sub>4</sub>	m <sub>5</sub>	m <sub>7</sub>	m <sub>6</sub>

3 variable

A \ B	0	1
	m <sub>0</sub>	m <sub>1</sub>
0	m <sub>0</sub>	m <sub>1</sub>
1	m <sub>2</sub>	m <sub>3</sub>

2 variable

working for plotting k-map

$$Let Y(A, B, C) = AB + A'BC$$

convert Y into canonical sop

$$Y = AB(C+C') + A'BC$$

$$= ABC + ABC' + A'BC$$

$$= 111 \quad 110 \quad 011$$

$$m_7 \quad m_6 \quad m_3$$

A \ BC	00	01	11	10
0	0	0	1	0
1	0	0	1	1

## Lecture 39

POS fn

$$Y = (A+B) \cdot \bar{A}$$

convert Y into canonical pos

$$= A+B \cdot A + B \cdot \bar{A}$$

$$= (A+B) \cdot (\bar{A}+B)(A+\bar{B})$$

$$00 \quad 10 \quad 11$$

A \ B	0	1
0	0	1
1	0	0

A \ BC	00	01	11	10
0	0	0	0	0
1	1	1	1	1



$$Y(A, B, C, D) = (A+B+C+D) \cdot (A+B+C) \cdot (A+B+E+D)$$

canonical pos form

$$= (A+B+C+D) \cdot (A+B+C) + (D\bar{D}) \cdot (A+B+E+D)$$

$$= (A+B+C+D) \cdot (A+B+C+D) \cdot (A+B+E+D)$$

0000

0100

0101

0111

A+B \ C+D				
	0+0	0+1	1+1	1+0
0+0	0	1	1	1
0+1	0	0	0	1
1+1	1	1	1	1
1+0	1	1	1	1

A \ BC				
	00	01	11	10
0	1	1	1	1
1	1	1	1	1

SOP

$Y = 1$   $Y = 0$  if 0 is seen  
all cells

A \ BC				
	00	01	11	10
0	1	1	0	0
1	1	1	0	0

$Y = \bar{B}$

A \ D				
	0	1	0	1
0	1	0	0	1
1	1	0	0	1
1	1	1	1	1

A \ BC				
	00	01	11	10
0	0	0	1	1
1	0	0	1	1

$Y = B$

A+B \ C+D				
	0+0	0+1	1+1	1+0
0+0	0	0	0	0
0+1	0	1	1	1
1+1	0	1	1	1
1+0	0	1	1	1

$Y = (C+D) \cdot (A+B)$

$Y = \bar{D} + A\bar{B}$

$$Y(A, B, C, D) = \sum m(0, 2, 4, 5, 6, 7, 12, 15) \quad \text{--- (1)}$$

$$Y(A, B, C, D) = \prod M[1, 3, 9, 10, 11, 13, 14] \quad \text{--- (2)}$$

①

AD \ CD	00	01	11	10
00	1	0	0	1
01	1	1	1	1
11	0	0	0	0
10	1	0	1	0

AD \ CD	00	01	11	10
00	1	0	0	1
01	1	0	0	1
11	1	0	0	1
10	1	1	1	0

$$Y(A, B, C) = \sum m(0, 1, 2, 5, 7) \quad Y(A, B, C, D) = \sum m(0, 1, 2, 5, 7, 14, 15)$$

A \ BC	00	01	11	10
0	1	1	1	0
1	0	1	1	0

$$Y = A\bar{B} + C$$

AB \ CD	00	01	11	10
00	1	1	1	0
01	0	1	1	0
11	1	0	1	0
10	1	0	0	0

$\rightarrow A\bar{B}$  (circles in row 00)  
 $\rightarrow B\bar{C}D$  (circles in column 01)  
 $\rightarrow A\bar{B}C$  (circle in cell 00, 11)  
 $\rightarrow A\bar{B}C\bar{D}$  (circle in cell 00, 10)

$$Y = A\bar{B}C + A\bar{B} + A\bar{B}C\bar{D} + B\bar{C}D$$



## Lecture 35

$$Y(A, B, C, D) = \sum m(0, 3, 5, 7, 9, 11, 12, 13)$$

SoP representation

AB \ CD	CD			
	00	01	11	10
00	1	0	1	0
01	0	1	1	0
11	1	0	1	1
10	0	1	1	0

Annotations:  $\bar{A}BD$  (circles at (0,1), (0,3), (1,3)),  $AB\bar{D}$  (circles at (1,1), (1,3), (3,1), (3,3)),  $CD$  (circles at (0,2), (1,2), (2,2), (3,2))

$$Y = \bar{A}BD + ABD + AB\bar{D} + CD$$

$$= \sum m(1, 2, 4, 6, 8, 10, 12)$$

POS

AB \ CD	CD			
	00	01	11	10
00	1	0	1	0
01	0	1	1	0
11	1	0	1	1
10	0	1	1	0

$$Y(A, B, C, D) = \sum m(0, 1, 2, 4, 5)$$

$d(5, 12)$

$d = \text{don't care}$

$x = 0 \text{ or } 1$

AB \ CD	CD			
	00	01	11	10
00	1			1
01			1	1
11	1			
10	1	1		1

Annotations:  $A'B'D'$  (circle at (0,4)),  $A'CD'$  (circle at (1,3)),  $A'BC$  (circle at (1,0)),  $A'B'D$  (circle at (3,4)),  $A'C'D$  (circle at (2,0))

$$Y = A'BC' + A'C'D' + A'DD' + A'CD' + A'BC + A'BD$$



$$Y(A, D, C, D) = T M \begin{pmatrix} 0, 1, 3, 5, 12, 9, 11, 12, 13 \end{pmatrix} \cdot d \begin{pmatrix} 2, 13, 15 \end{pmatrix}$$

$M_0, M_1, M_2, M_3, M_4, M_5, M_6, M_7, M_8, M_9, M_{10}, M_{11}, M_{12}, M_{13}, M_{14}, M_{15}$        $d_2, d_{13}, d_{15}$

A+B	0 1 0	0 1 1	1 1 1	1 1 0	
0 1 0	0	0	0	d	← A+B $Y = (A+B) \cdot (A'+B) \cdot \bar{D}$
0 1 1	1	0	0	1	
1 1 1	0	0	d	d	← A'+B
1 1 0	1	0	0	1	

$D'$

### Lecture 36

#### Electronic Instruments

1. Multimeter
2. Electronic voltmeter
3. Cathode ray oscilloscope (CRO)

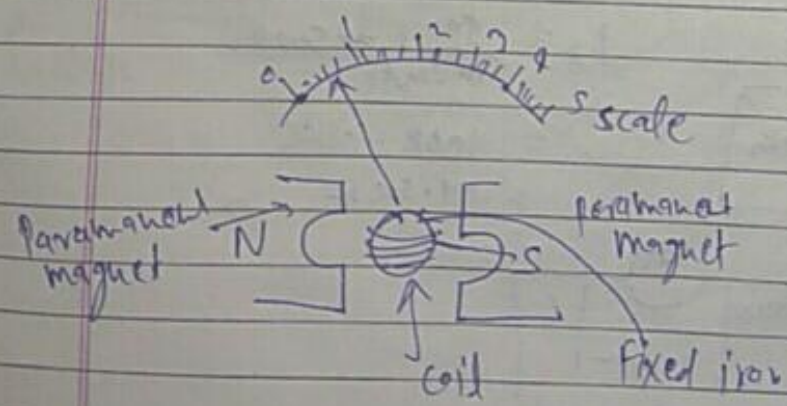
Resistance, I, V  
freq etc

#### Multimeter

Multi → many

Resistance, current, voltage measure by multimeter (CRO)

PMMC meter or d'Arsonval meter or eq. galvanometer





$I_d =$  Deflection torque

deflection torque

$$I_d \propto I$$

$$T_d = T_r$$

$$T_r$$

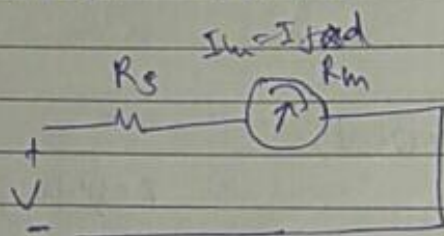
$$I_d \propto I$$

$$T_r \propto \theta$$

$$I \propto \theta$$

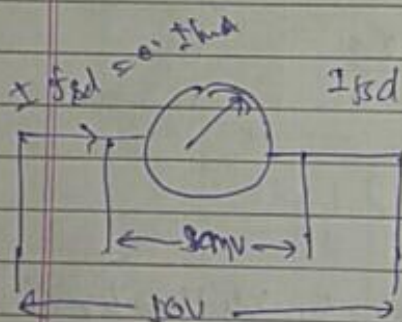
Voltage can be measure by using PMMC or Galvanometer

Multimeter  $\rightarrow$  PMMC



$R_m =$  internal resistance of PMMC

$$I_m = I_{fsd} = \text{full scale deflection current}$$



$$I_{fsd} = 0.1 \text{ mA}$$

$$R_m = 500 \Omega$$

$$V = I_{fsd} \times R_m = 0.1 \text{ mA} \times 500 \Omega = 50 \text{ mV}$$

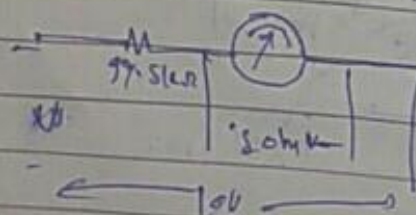
$R_s =$  series resistance

$$V = I_m R_s + I_m R_m$$

$$\frac{V}{I_m} = R_s + R_m$$

$$R_s = \frac{V}{I_m} - R_m$$

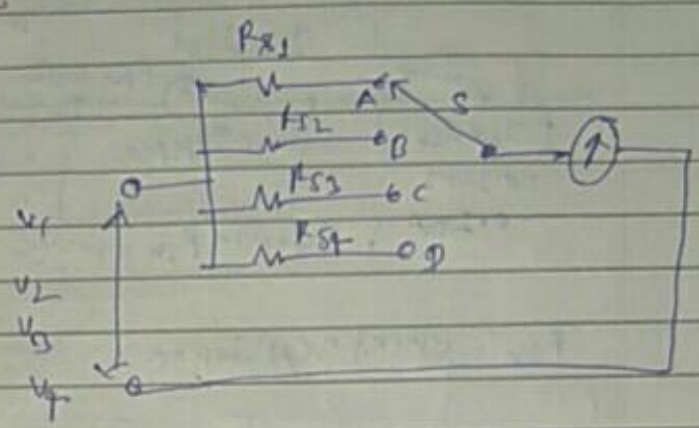
$$R_s = \frac{10}{0.1 \text{ mA}} - 500 \Omega = 100 \text{ k} - 500 \Omega = 99.5 \text{ k} \Omega$$





PMMC  $I_{fsd} = 0.1mA$   
 $R_m = 800\Omega$

- 0 - 90V  $R_{s1}$
- 0 - 50V  $R_{s2}$
- 0 - 100V  $R_{s3}$
- 0 - 500V  $R_{s4}$



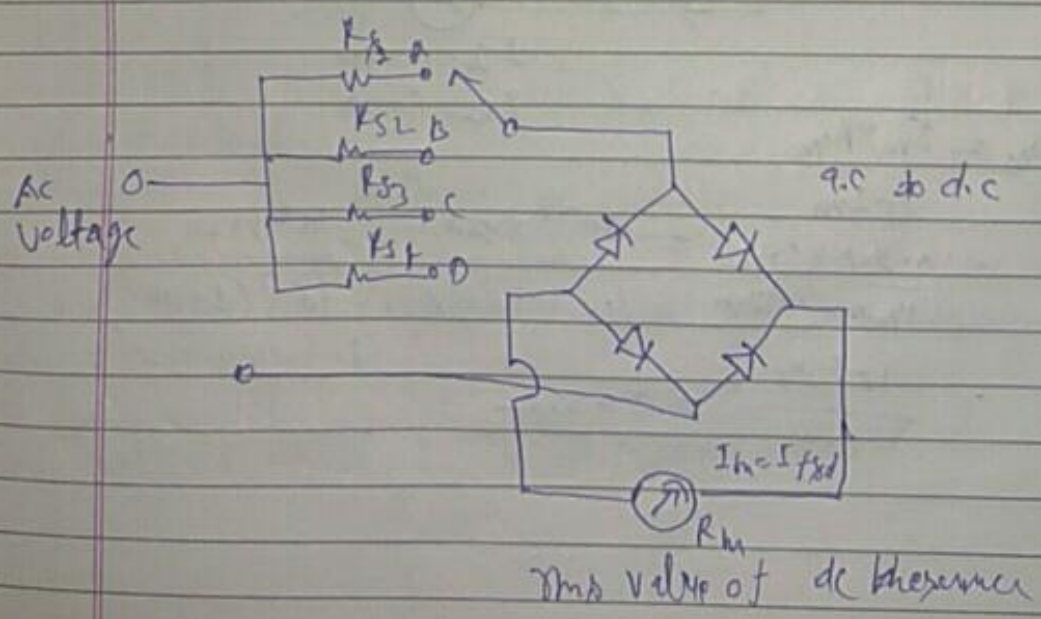
$$R_{s1} = \frac{V}{I_m} - R_m$$

$$= \frac{10}{0.1mA} - 800\Omega = 99.5k\Omega$$

$$R_{s2} = \frac{50}{0.1mA} - 800\Omega = 999.5k\Omega$$

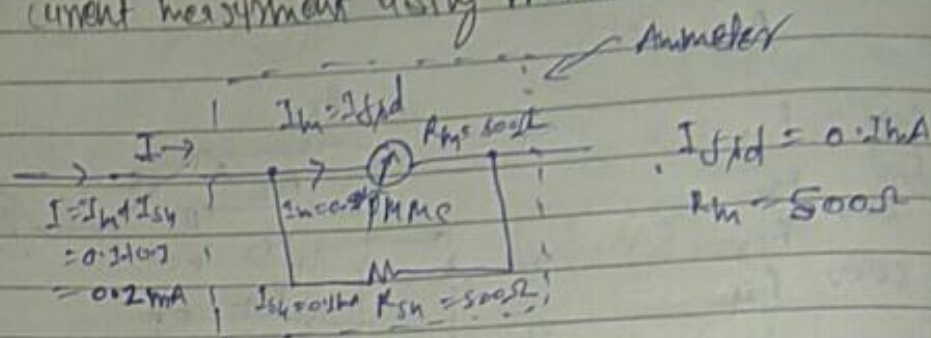
$$R_{s3} = \frac{100}{0.1mA} - 800 = 999.5k\Omega$$

$$R_{s4} = \frac{500}{0.1mA} - 800 = 9999.5k\Omega$$





## current measurement using PMMC



$R_{sh}$  = shunt resistance

$$I_m \times R_m = I_{sh} \times R_{sh}$$

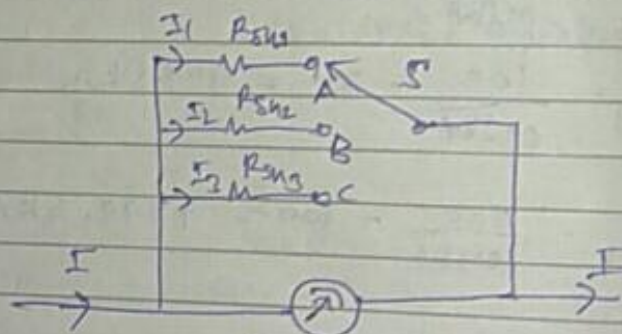
$$R_{sh} = \frac{I_m \times R_m}{I - I_m}$$

$$R_{sh} = \frac{0.1mA \times 500}{0.2mA - 0.1mA} = 500\Omega$$

$$I_1 = 1mA$$

$$I_2 = 10\mu A$$

$$I_3 = 100\mu A$$



$$I_m = 0.1mA$$

$$R_m = 500\Omega$$

$$R_{sh} = \frac{I_m \times R_m}{I - I_m}$$

$$I - I_m$$

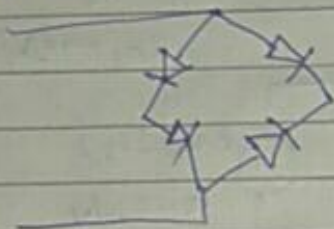
$$= \frac{0.1mA \times 500}{1mA - 0.1mA} = \frac{10^{-4} \times 500}{(10^{-3} - 10^{-4})} = \frac{10^{-4} \times 500}{10^{-4}(1 - 10^{-1})}$$

$$= \frac{10^{-4} \times 500}{0.9} = 55.55\Omega$$

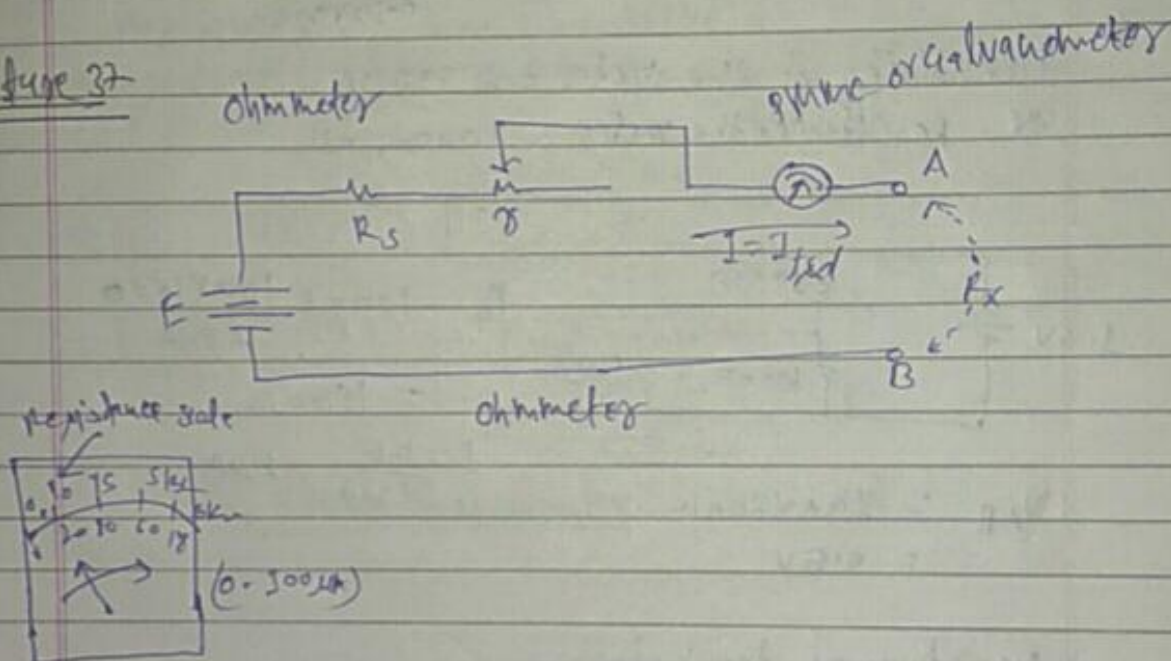


$$R_{sh2} = \frac{I_m \times R_m}{I_2 - I_m} = \frac{0.1 \text{ mA} \times 500 \Omega}{10 \text{ mA} - 0.1 \text{ mA}} = 5.0 \Omega$$

$$R_{shg} = \frac{I_m \times R_m}{I_g - I_m} = \frac{0.1 \text{ mA} \times 500}{100 \text{ mA} - 0.1 \text{ mA}} = 0.50 \Omega$$



### Lecture 37



Resistance scale of  
multimeter

Multimeter sensitivity

Greater the sensitivity  $\rightarrow$  Greater is the accuracy of measurement

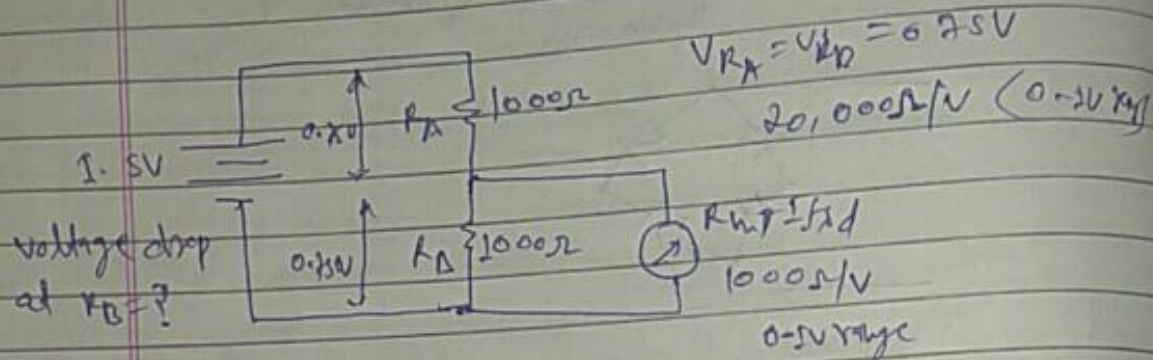
$$\text{Sensitivity} = \frac{1}{I_{fsd}} = \Omega / \text{volt}$$

$$= \frac{1}{0.5}$$

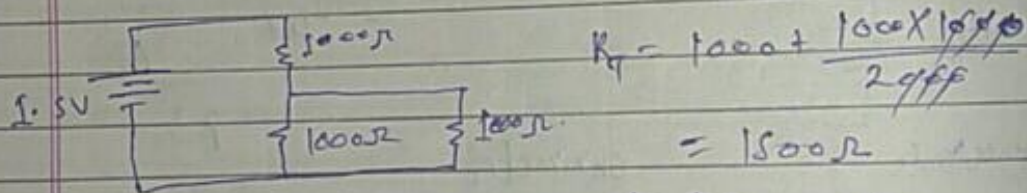


$\boxed{A} \quad 1000 \Omega/V$

$\boxed{R} \quad 5000 \Omega/V$



Sensitivity of the meter =  $1000 \Omega/V$   
 $\therefore$  Resistance of the meter =  $1000 \frac{\Omega}{V} \times 1V$   
 $= 1000 \Omega$



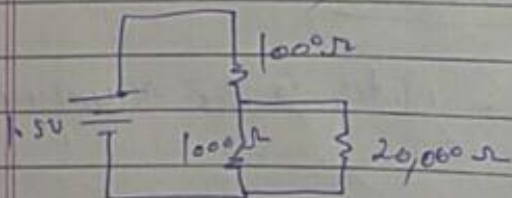
$R_T = 1000 + \frac{1000 \times 1000}{2000}$   
 $= 1500 \Omega$

$I = \frac{1.5}{1500} = 1mA$

$V_{AB} = I \times R_{AB}$   
 $= 0.5V$

Resistance of the meter

$= \frac{20,000 \times 1V}{1} = 20,000 \Omega$



$R_T = 1000 + \frac{1000 \times 20000}{21000}$   
 $= 1000 + 952.38$   
 $= 1952.38 \Omega$



$$I = \frac{1.5}{1952.33}$$

$$V_{AB} = I \times R_{AB} \\ = \frac{1.5}{1952.33} \times 10000 // 20000 \Omega$$

$$V_{AB} = 0.73V$$

## Loading effect in multimeter

1. Sensitivity  $\uparrow$ , Loading effect  $\downarrow$
2. Range (voltage range)  $\uparrow$ , then also  $\downarrow$

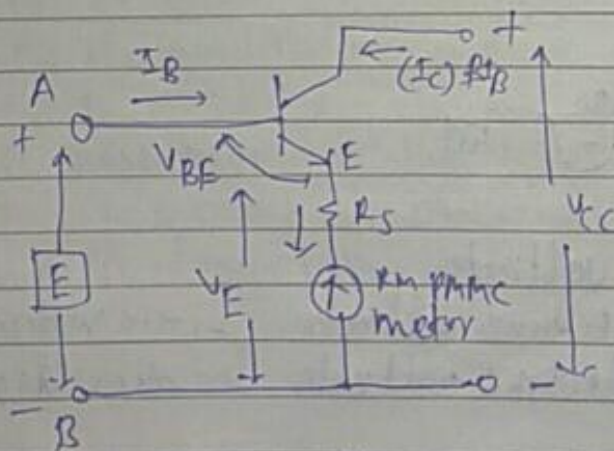
$$A \rightarrow 1000 \Omega/V \\ \rightarrow 0.5V$$

$$A \rightarrow 1000 \Omega/V \\ 5V \quad R_f = 1000 \Omega$$

$$B \rightarrow 20000 \Omega/V \\ \rightarrow 0.75V$$

$$B \rightarrow 1000 \Omega/V \\ 2V \quad R_f = 2000 \Omega \\ 0.75V$$

## Electronic voltmeter



Transistor voltmeter circuit



$$V_E = E - V_{BE}$$

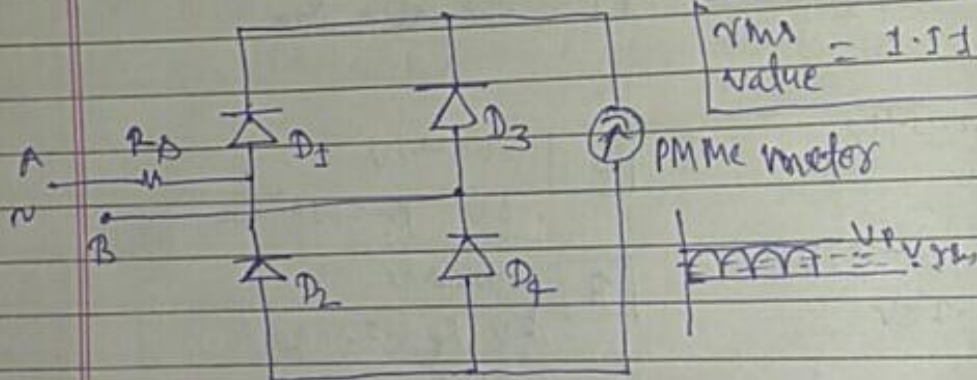
$$I_m = \frac{V_E}{R_s + R_m}$$

$R_s$  = series resistance  
 $R_m$  = meter resistance

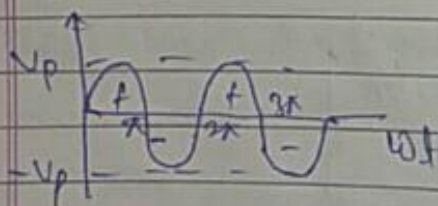
$R_i = \frac{V}{I_B} = \frac{E}{I_B}$  dc voltage  
 of the transistor voltmeter

$$I_C = \beta I_B$$

$$I_E = I_C + I_B = \beta I_B + I_B = I_m$$



Bridge rectifier voltmeter



Electronic voltmeter

1. Rectifier electronic voltmeter  $\rightarrow$  a.c voltage measurement
2. Transistor electronic voltmeter  $\rightarrow$  d.c voltage measurement

voltage is  
 applied  
 to the

1)

2)

1.

2.

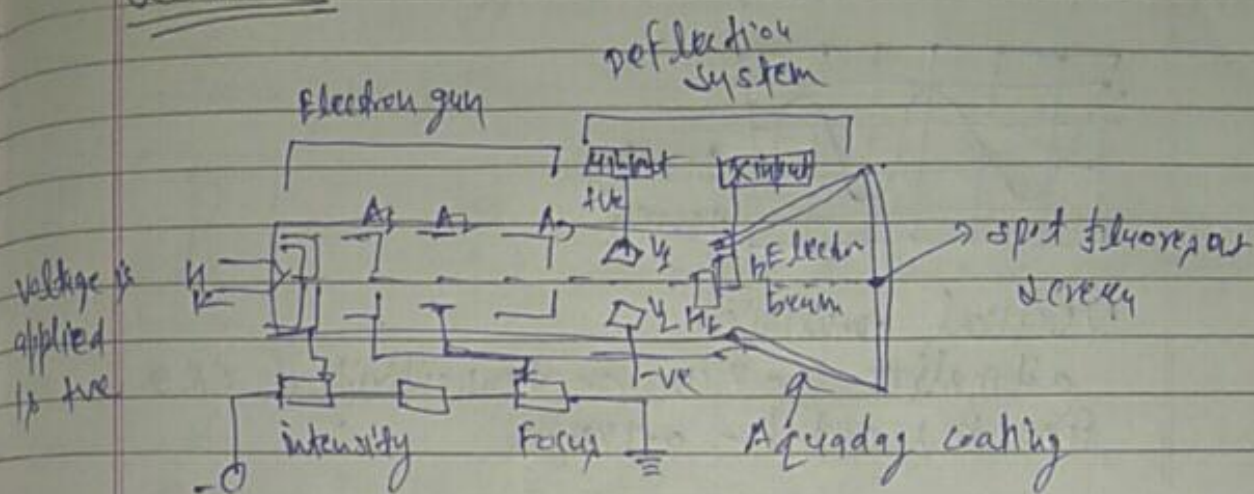
3.

4.

1)



## Lecture 28



high voltage supply

H - Heater

A<sub>2</sub> = Focusing

K = Cathode

A<sub>3</sub> = Accelerating

G = Control grid

V<sub>y</sub> = vertical

A<sub>1</sub> = Pre-accelerating anode

V<sub>x</sub> = horizontal

Fig: CRT

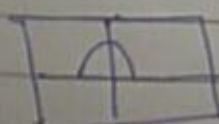
### Deflection plates

- 1) Horizontal deflection plate
- 2) vertical deflection plate

### Application of CRO

1. Analysis of waveform or study of waveforms
2. voltage measurement of the waveform
3. frequency measurement of the waveform
4. phase diff of waveform

- 1) 4 input terminal

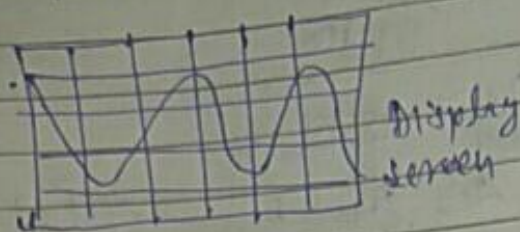


i) time base control

ii) vertical amplifier



## ii) Measurement of voltage



vertical amplifier  
 attenuator = 2 V/cm ← sensitivity of CRO  
 time base control = 0.1 ms/cm

$$V_{pp} = 4 \text{ cm} \times 2 \text{ V/cm} = 8 \text{ V}$$

$$V_p = \frac{V_{pp}}{2} = 4 \text{ V} \quad V_{rms} = \frac{V_p}{\sqrt{2}} = \frac{4}{\sqrt{2}}$$

Time period

$$T = 4 \text{ cm} \times 0.1 \text{ ms/cm} \\ = 0.4 \text{ ms}$$

$$\text{frequency} = \frac{1}{0.4 \text{ ms}}$$

Deflection sensitivity = 5 V/cm

4-input ← unknown ac voltage is applied  
 (vertical deflection plate) If 10 cm long straight line is observed on the screen.

ac voltage

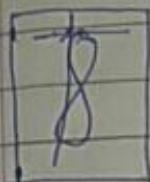
$$V_{pp} = 10 \text{ cm} \times 5 \text{ V/cm} \\ = 50 \text{ V}$$

$$V_p = 25 \text{ V} \quad V_{rms} = \frac{V_p}{\sqrt{2}}$$



unknown frequency

Lissajous pattern



X-input  $\leftarrow$  signal of known frequency

Y-input  $\leftarrow$  signal of unknown frequency

$f_v$  unknown

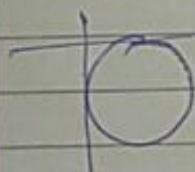
$f_H = 100 \text{ kHz}$

unknown frequency

$$\frac{f_v}{f_H} = \frac{\text{No. of horizontal tangents}}{\text{No. of vertical tangents}}$$

known  
freq

$$\frac{f_v}{f_H} = \frac{1}{2} \Rightarrow f_v = \frac{f_H}{2} = 50 \text{ kHz}$$



known freq  $f_H = 50 \text{ kHz}$   
 $f_v = ?$

$$\frac{f_v}{f_H} = \frac{1}{1} \Rightarrow f_v = f_H = 50 \text{ kHz}$$