1

Assignment 1

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

CS22BTECH11061

Waghmare Aditya Abhaykumar

12.13.4.2 An urn contains 5 red and 2 black balls. Two balls are randomly drawn. Let X represent the number of black balls. What are the possible values of X? Is X a random variable?

Solution: Possible values of X are as follows -

$$X = \{0, 1, 2\} \tag{1}$$

A random variable is an assignment of real values to each outcome of the experiment. Therefore, X is an random variable.

Let N = R + B and n = r + b where,

Parameter	Value	Description
R	5	Red balls within N
В	2	Black balls within N
N	7	(R + G)
r	{0, 1, 2}	Red balls within n
b	{0, 1, 2}	Black balls within n
n	2	(r + g)

then

$$\Pr(r,b) = \frac{{}^{R}C_{r}{}^{B}C_{b}}{{}^{R+B}C_{r+b}}$$
 (2)

In our case,

$$R = 5$$

$$B=2$$

$$N = 5 + 2 = 7$$

and n = 2

Now,

$$n = r + b$$

$$\therefore 2 = r + b$$

$$\therefore r = 2 - b$$

Now as X = b and

$$\Pr(r,b) = \frac{{}^{R}C_{r}{}^{B}C_{b}}{{}^{R+B}C_{r+b}}$$
(3)

$$\therefore \Pr(X = b) = \frac{{}^{5}C_{2-b}{}^{2}C_{b}}{{}^{7}C_{2}}$$
 (4)

So, Probability Distribution of X can be given as

$$p_X(b) = \frac{{}^5C_{2-b}{}^2C_b}{21} \tag{5}$$

where $b = \{0, 1, 2\}$