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```
% Aditya Gopalan
% APPM 2360 Matlab Homework 5
% Due: Thursday, October 17, 2019
% Problem 1 - Main Script
```

```
clc
clear all
close all
```

```
A = [1 0 0 0; 1 -1 0 0; 0 1 -2 0; 1 -1 3 3]
B = [1 -1 -1 0 0 0; 0 1 0 1 -1 0; 0 0 1 -1 0 -1; 1 0 0 0 1 1]
```

$A =$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 1 & -2 & 0 \\ 1 & -1 & 3 & 3 \end{bmatrix}$$

$B =$

$$\begin{bmatrix} 1 & -1 & -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & -1 & 0 \\ 0 & 0 & 1 & -1 & 0 & -1 \\ 1 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

**(a)**

This matrix is a lower triangular matrix. The maximum rank of matrix testA would be 4 because this matrix has 4 pivot columns

---

**(b)**

```
J = rref(A)
% Matrix A has 4 pivot columns
% This means the rank(A) is still 4 since it matches the number of
  pivot
% columns
```

$J =$

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

**(c)**

```
R = det(A)
% Matrix A has a determinant of 6. This makes sense because if the
  rank
% of the matrix equals the number of rows, then the determinant is
  greater
% than zero. If the rank was less than the number of rows, then the
% determinant would be 0.
```

$R =$

6

**(d)**

A is invertible because the determinant is greater than 0 and the inverse is equal to 1/determinant

```
H = A^-1
K = rref(H)
```

$H =$

1.0000	0	0	0
1.0000	-1.0000	0	0
0.5000	-0.5000	-0.5000	0
-0.5000	0.1667	0.5000	0.3333

$K =$

1	0	0	0
---	---	---	---

---

0	1	0	0
0	0	1	0
0	0	0	1

**(e)**

```
b = [1 1 1 1]';  
x = A\b  
y = rref(x)  
% there are 4 solutions: 1, 0, -0.5, 0.5  
% The solution to the augmented matrix is 1.00
```

```
x =  
  
    1.0000  
         0  
   -0.5000  
    0.5000
```

```
y =  
  
    1  
    0  
    0  
    0
```

**(f)**

```
bab = [0 0 0 0]';  
h = A\bab  
% zero solutions
```

```
h =  
  
    0  
    0  
    0  
    0
```

**(g)**

```
A2 = [1 0 0 0; 1 0 1 3; 0 1 -2 0; 1 -1 3 3]  
TT = rref(A2)  
% Matrix A2 has 3 pivot columns. The last row does not have a pivot.
```

---

$A2 =$

1	0	0	0
1	0	1	3
0	1	-2	0
1	-1	3	3

$TT =$

1	0	0	0
0	1	0	6
0	0	1	3
0	0	0	0

**(h)**

```
bb = [1 1 1 1]'  
xx = A2\bb  
%two infinite solutions
```

$bb =$

1
1
1
1

*Warning: Matrix is singular to working precision.*

$xx =$

NaN
NaN
-Inf
Inf

**(i)**

```
bbb = [1 0 0 0]'  
xx = A2\bbb  
% no solutions
```

$bbb =$

1
0
0
0

---

*Warning: Matrix is singular to working precision.*

*xx =*

*NaN*  
*NaN*  
*NaN*  
*NaN*

**(j)**

```
BB = rref(B)
% four pivot columns
% B cannot have unique solutions because the determinant does not
% exist due
% to the fact that the rank of the matrix is less than the amount of
% rows
```

*BB =*

<i>1</i>	<i>0</i>	<i>0</i>	<i>0</i>	<i>0</i>	<i>0</i>
<i>0</i>	<i>1</i>	<i>0</i>	<i>1</i>	<i>0</i>	<i>1</i>
<i>0</i>	<i>0</i>	<i>1</i>	<i>-1</i>	<i>0</i>	<i>-1</i>
<i>0</i>	<i>0</i>	<i>0</i>	<i>0</i>	<i>1</i>	<i>1</i>

**(k)**

```
Hi = B'
HH = rref(Hi)
% matrix B transpose (Hi) has one pivot column
% B transpose cannot have any unique solution because it is not a
% square
% matrix.
```

*Hi =*

<i>1</i>	<i>0</i>	<i>0</i>	<i>1</i>
<i>-1</i>	<i>1</i>	<i>0</i>	<i>0</i>
<i>-1</i>	<i>0</i>	<i>1</i>	<i>0</i>
<i>0</i>	<i>1</i>	<i>-1</i>	<i>0</i>
<i>0</i>	<i>-1</i>	<i>0</i>	<i>1</i>
<i>0</i>	<i>0</i>	<i>-1</i>	<i>1</i>

*HH =*

<i>1</i>	<i>0</i>	<i>0</i>	<i>0</i>
<i>0</i>	<i>1</i>	<i>0</i>	<i>0</i>

---

$0$	$0$	$1$	$0$
$0$	$0$	$0$	$1$
$0$	$0$	$0$	$0$
$0$	$0$	$0$	$0$

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