

2171011

End Semester Examination 2024

Name of the Course: BCA

Semester:4

Name of the Course: **Computer Based Numerical and Statistical Techniques**

Course Code: TBC 405

Time: 3 Hours**MM: 100****Note:**

- (i) All questions are compulsory.
(ii) Answer any two sub questions among a, b, c in each main question.
(iii) Total marks in each question are twenty.
(iv) Each sub question carries ten marks.

Q.1	(10 × 2 = 20 Marks)																		
a)	Find the root of the equation $x^3-5x+1=0$ using the secant method.						CO1												
b)	Find a real root of the equation $\cos x=3x-1$ and correct up to three decimal places using the iteration method.																		
c)	Find the root of the equation $x\log_{10}x = 1.2$ using the false position Method.																		
Q.2	(10 × 2 = 20 Marks)																		
a)	Solve the system of linear equations by Gauss elimination method. $\begin{aligned} x+2y+z &= 3 \\ 2x+3y+3z &= 10 \\ 3x-y+2z &= 13 \end{aligned}$						CO2												
b)	From the following table find the number of students who obtain less than 45 marks																		
<table><tr><td>Marks</td><td>30-40</td><td>40-50</td><td>50-60</td><td>60-70</td><td>70-80</td></tr><tr><td>No of Students</td><td>31</td><td>42</td><td>51</td><td>35</td><td>31</td></tr></table>								Marks	30-40	40-50	50-60	60-70	70-80	No of Students	31	42	51	35	31
Marks	30-40	40-50	50-60	60-70	70-80														
No of Students	31	42	51	35	31														
c)	Find the value of $f(41)$ by applying Gauss's forward from the following data																		
<table><tr><td>X</td><td>30</td><td>35</td><td>40</td><td>45</td><td>50</td></tr><tr><td>F(x)</td><td>3678.2</td><td>2995.1</td><td>2400.1</td><td>1876.2</td><td>1416.3</td></tr></table>							X	30	35	40	45	50	F(x)	3678.2	2995.1	2400.1	1876.2	1416.3	
X	30	35	40	45	50														
F(x)	3678.2	2995.1	2400.1	1876.2	1416.3														
Q.3	(10 × 2 = 20 Marks)																		
a)	Evaluate $\int_0^6 \frac{1}{1+x^2} dx$ by trapezoidal rule, where the interval of integration is subdivided into six equal parts.						CO3												

b)	Using Taylor's series find the solution of the differential equation $xy' = x - y, y(2) = 2$ at $x = 2.1$ correct to five decimal places.																				
c)	Find the solution of the differential equation. $\frac{dy}{dx} = y - x$ given $y(0) = 2$ using Runge Kutta method at $x = 0.2$.																				
Q.4	(10 × 2 = 20 Marks)																				
a)	Using the method of least square to fit the non-linear curve of the form $y = ae^{bx}$ to the following data- <table><tr><td>x</td><td>0</td><td>2</td><td>4</td></tr><tr><td>y</td><td>5.013</td><td>10</td><td>31.52</td></tr></table>	x	0	2	4	y	5.013	10	31.52	CO4											
x	0	2	4																		
y	5.013	10	31.52																		
b)	Fit a second-degree parabola for the following data- <table><tr><td>X</td><td>0.0</td><td>1.0</td><td>2.0</td><td>3.0</td><td>4.0</td></tr><tr><td>Y</td><td>1.0</td><td>4.0</td><td>10.0</td><td>17.0</td><td>30.0</td></tr></table>	X	0.0	1.0	2.0	3.0	4.0	Y	1.0	4.0	10.0	17.0	30.0								
X	0.0	1.0	2.0	3.0	4.0																
Y	1.0	4.0	10.0	17.0	30.0																
c)	The following table given age(x) in years of cars and annual maintenance cost (y) in hundred rupees. <table><tr><td>X</td><td>1</td><td>3</td><td>5</td><td>7</td><td>9</td></tr><tr><td>Y</td><td>15</td><td>18</td><td>21</td><td>23</td><td>22</td></tr></table> Estimate the maintenance cost for a 4 year old car after finding the regression equation	X	1	3	5	7	9	Y	15	18	21	23	22								
X	1	3	5	7	9																
Y	15	18	21	23	22																
Q.5																					
a)	Write a short note on- 1. Components of time series 2. Frequency Distribution	CO5																			
b)	Compute the 4 yearly moving averages and calculate the trend values from the following data: <table><tr><td>X</td><td>1991</td><td>1992</td><td>1993</td><td>1994</td><td>1995</td><td>1996</td><td>1997</td><td>1998</td></tr><tr><td>Y</td><td>36</td><td>43</td><td>43</td><td>34</td><td>44</td><td>54</td><td>34</td><td>24</td></tr></table>		X	1991	1992	1993	1994	1995	1996	1997	1998	Y	36	43	43	34	44	54	34	24	
X	1991		1992	1993	1994	1995	1996	1997	1998												
Y	36	43	43	34	44	54	34	24													
c)	Explain various Models and methods used for forecasting.																				