

## UNIVERSITY OF PETROLEUM & ENERGY STUDIES, DEHRADUN

Program	B. Tech SCS	Semester	II
Course	Mathematics II	<b>Course Code</b>	MATH 1005
Session	Jan-May 2018	Topic	<b>Probability &amp; Statistics</b>

1. A random variable *X* has the following probability mass function

x	10	11	12	13	14	15	16
P(x)	0	k	2 <i>k</i>	2 <i>k</i>	3 <i>k</i>	$3k^2$	$7k^2 + k$

- a. Find the value of *k*
- b. Find P(10 < X < 15)?
- 2. Probability density function of a continuous random variable X is given by

$$f(x) = ke^{-2|x|}, -\infty < x < \infty.$$

- a. Find k.
- b. Find the value of  $P(0 \le X < 1)$ ,  $P(X \ge 7)$ .
- c. Find distribution function of X.
- 3. A function is defined by  $f(x) = \begin{cases} e^{-x}, x \ge 0 \\ 0, x < 0. \end{cases}$ 
  - a. Find the cumulative distribution function F(2).
- **4.** Find moment generating function of a random variable which follows (i) B(n,p) (ii)  $P(\mu)$  and (iii) $N(m,\sigma)$ .
- 5. Find Mean, Variance, Skewness and Kurtosis for the following data.

x	10	11	12	13

- **6.** A random variable *X* assumes the values -1, 0, 1 with probabilities  $\frac{1}{3}$ ,  $\frac{1}{2}$ ,  $\frac{1}{6}$  respectively. Find the distribution function of *X*.
- 7. Find the first four moments of the following data.

Values	15 – 25	30 - 40	45 – 55	55 – 75				
Frequency	15	10	20	25				

Hence find Mean, Variance, Skewness and Kurtosis

- **8.** Show that the distribution is moderately positively skewed. and curve is Mesokurtic, if first four central moments of a distribution are 0,2.5,0.7 and 18.75.
- **9.** Show that the following distribution is positively skewed

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70
Obtained							
Frequency	6	12	22	24	16	12	8

- **10.** Show that the mean and the variance of the discrete Binormal distribution is given by *np* and *npq* respectively.
- **11.** Solve the following problems.
  - (i)In a sample of 1000 cases, the mean of a certain test is 14 and S.D. is 2.5. Assuming the distribution to be normal, find
    - a. how many students score between 12 and 15?
    - b. how many score above 18?
    - c. how many score 16?
  - (ii). Suppose a radio active source emits particle follows a Poisson distribution on average 2.5 particles per second. Calculate the probability that two or more particles will be emitted in an interval of 4 second.
  - (iii). Suppose that the probability of an item being defective in a mass production process is 0.01. If 20 items are selected at random, then what is the probability that exactly 2 will be defective?