

Question Paper

Exam Date & Time: 04-Jul-2023 (02:30 PM - 05:30 PM)



MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. DEGREE EXAMINATIONS - JUNE/JULY 2023

SUBJECT: CSE 2254/CSE-2254 - FORMAL LANGUAGES AND AUTOMATA THEORY

(COMPUTER SCIENCE AND ENGINEERING - ARTIFICIAL INTELLIGENCE AND MACHINE LEARNING / COMPUTER SCIENCE / COMPUTER SCIENCE AND ENGINEERING - CYBER SECURITY)
(MAKEUP)

Marks: 50

Duration: 180 mins.

Answer all the questions.

- 1A) Design a deterministic and non-deterministic finite automaton (dfa and nfa) which accept a string containing "ion" at the end of a string in a string of {a-z}, e.g., "imagination" but not "image". Mention the quintuple representation of both dfa and nfa you designed. (4)
- 1B) Consider the language $L = \{(10)^n : n \geq 0\}$. Prove that Deterministic Finite Automata (DFA) is equivalent to non-Deterministic Finite Automata (NFA) on the language L. (4)
- 1C) The language, $L = \{a^n b^n c^n : n \geq 1\}$ is a context sensitive language. Design context sensitive grammar for the language. (2)
- 2A) The Grammar G, with productions. (2)
 $S \rightarrow S_1 B,$
 $S_1 \rightarrow a S_1 b,$
 $b B \rightarrow b b b B,$
 $a S_1 b \rightarrow a a,$
 $B \rightarrow \lambda$
Identify whether this is unrestricted grammar or not. Supplement your answer with proper technical justifications.
- 2B) Generate the regular expressions for the sets given below. (3)
i) $\{a^n : n \text{ is divisible by 2 or 3 or } n=5\}$
ii) $\{a^2, a^5, a^8, \dots\}$
iii) The set of all strings on {a,b} terminated by either 'a' or 'abb'
- 2C) Identify the languages given below is regular or not and support your answer with proper justifications. (5)
i) $L = \{a^n b^m c^k : n, m, k \geq 0\}$
ii) $L = \{a^i b^j : i, j \geq 0\}$
iii) $L = \{a^n : n \text{ is prime}\}$
iv) $L = \{w^R : w \in \{a,b\}^*\}$
v) $L = \{a^n : n \geq 100\}$
- 3A) Check whether the grammar $S \rightarrow a S b S \mid b S a S \mid \lambda$ is ambiguous or not for the sentence "abab", by deriving two distinct parse trees. (3)
- 3B) Simplify the Grammar given below and convert to Chomsky Normal Form (3)
 $S \rightarrow a B B a \mid a B \mid a D \mid C C$
 $B \rightarrow a B D \mid D \mid \lambda$

$C \rightarrow aCC|bCC$

$D \rightarrow ab|cd|B.$

- 3C) Show that language $L=\{a^n b^n c^n \mid n \geq 1\}$ is not CFG using pumping lemma. (4)
- 4A) Construct a PDA for the CFG $G= (\{S, A, B\}, \{0,1\}, S, \{S \rightarrow 0A, A \rightarrow 0AB \mid 1, B \rightarrow 1\})$ and show the sequence of moves for the string "000111". (3)
- 4B) Construct NPDA for the language $L=\{w \in \{a,b\}^* : n_a(w) = n_b(w)\}$. (3)
- 4C) Construct DPDA for the language $L= \{a^n b^{2n} c^{nd^{2n}} \mid n \geq 1\}$. (4)
- 5A) Design a Turing Machine using the state transition diagram to reverse a given string $w \in \{0,1\}^+$ such that the input tape will contain final state followed by reversed string. (4)
- 5B) Design a Transducer using state transition diagram to compute the sum or difference of two positive integers, X and Y. The integers are represented in the Turing machine with equal number of 1's separated by 0. (4)
- 5C) Construct a Grammar to generate a language $L= \{a^n b^n c^m \mid n, m \geq 1\}$. (2)

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