

# Student Answer Script View



MIT MPL-BTech-M Sc - MCA - 1st-3rd-5th and 7th Semester - Mid Term Examination - Sep 2024 Answer Sheet

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**Year/Sem:** Semester 5  
**Subject Name:** PRINCIPLES OF CRYPTOGRAPHY  
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24.00  
30.00

Comments submitted by student.

**Q.No : 1)****Score : 0.50 / 0.50**

Akshay sends a message 'hi' to Akash at 6pm. However, when Akshay and Akash meet in real at 8pm, Akshay denies that he had sent the message to Akash. Make use of the described scenario, the attacker and the security goal being breached are respectively:

**Akshay, Authentication****Akash, Accountability,****Akshay, Accountability****Akash, Authentication**

**Q.No : 2)**

If  $x$  = remainder obtained by dividing  $7^{886}$  by 300, then evaluate the value of  $x$

 x = 7 x = 49 x = 1 x = 343

**Q.No : 3)****Score : 0.00 / 0.50**

For a 7-bit to 7-bit Substitution Block Cipher (Ideal Block Cipher), select how many sets of transformations are possible from Plaintext Blocks to Ciphertext Blocks?

- 128!
- 7!
- 128
- None of These

**Q.No : 4)****Score : 0.50 / 0.50**

If  $x = \text{Order of } 44 \pmod{19}$ , then evaluate the value of  $x$

**x = 9****x = 25****x = 4****x = 1**

**Q.No : 5**

If  $\text{GCD}(651, 168) = 651x + 168y$  ( $x, y \in \mathbb{Z}$ ), then  $(x, y) =$

- (4,-1)     (-1,4)     (-4,1)     None of These

**Q.No : 6****Score : 0.00 / 0.50**

Which among the following Statements is True?

11 is a primitive root of 18

49 doesn't have any primitive root

4 is primitive root of 16

7 is a primitive root of 9

Q.No : 7

Score : 0.00 / 0.50

Choose the plaintext corresponding to the ciphertext '**QJDFFOFWRHDQTSPY**' using Vigenere Cipher which uses only alphabets as the character set (by ignoring the case, and mapping with their default numerical equivalents) with the key '**MODULO**' is

 EVALUATIONSRIGHT EVALUATIONSDONE EVALUATIONMARKS None of These

**Q.No : 8****Score : 0.00 / 0.50**

Select the minimum length of the key required to define all possible 5-bit to 5-bit mappings in an ideal block cipher:

**32 Bits****20 Bytes****5! Bits****5! Bytes**

**Q.No : 9****Score : 0.50 / 0.50**

Which of the security mechanisms defined by X.800 is sufficient to counter any passive attack?

 Notarization Authentication Exchange Traffic Padding Digital Signature

**Q.No : 10)**

A Plaintext '**HI**' has been encrypted to a Ciphertext '**EE**' with a key '**SOFTWARE**' using Vigenere Cipher (Assume that only alphabets by ignoring the case has been used for encryption). If the attacker captures the Ciphertext and has a knowledge that Vigenere Cipher has been used for encryption, compute the maximum number of keys he/she would have to try for a successful Brute Force Attack.

**26<sup>8</sup>**    **8<sup>26</sup>**    **26**    **676**

**Q.No : 11)**

Explain the following security services defined by X.800 for data storages and data communications:- (a) Data Origin Authentication, (b) Access Control, (c) Non-Repudiation, (d) Peer Entity Authentication.

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Security services :- These are the services that are implemented to enhance the communication security and obtain security goals

### (a) Data Origin Authentication

This service is used to check the data packets coming from the legitimate entity, this helps us to understand if source is real entity

Ex:- Gmail uses this to validate the source of the email is legitimate or not.

### (b) Access Control

This method is implemented for, Confidentiality

This means - so that users can have restricted access Ex:- restricted access control , they can access the resources that they are allowed to

### (C) Non- Repudiation

This method takes the accountability of the sender for a communication  
Ex:- Digital Signature

### (d) Peer Entity Authentication

We authenticate between 2 peers to avoid replaying.

**Q.No : 12)****Score : 0.00 / 2.00**

List and explain any 4 design features to be considered in Feistel Cipher.



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Block is 64 bit

The



Q.No : 13)

Score : 2.00 / 2.00

Calculate Multiplicative Inverse of  $(x^3 + 1) \text{ mod } (x^4 + x + 1)$  in  $\text{GF}(2^4)$  by applying Extended Euclidean Algorithm (EEA) for Polynomials. (Show Long Division steps for all the iterations while calculating the quotients and remainders).

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MI  $(x^3 + 1) \text{ mod } (x^4 + x + 1)$  in  $\text{GF}(2^4)$

$$\begin{array}{ccccccccc}
 \text{Iter-1} & q(x) & a & b & r(x) & v|_1(x) & v2(x) & v(x) \\
 & x & x^4+x+1 & x^3+1 & | & 0 & | & x \\
 & & x & & & & & \\
 & x^3+1 & \overline{\quad\quad\quad\quad\quad} & & & & & \\
 & x^4 & +x & & & & & \\
 & +1 & +1 & & & & & \\
 \hline & & & 1 & & & & \\
 \end{array}$$

$r(x) =$   
 $v(x) = x$

$$\begin{aligned}
 v(x) &= v|_1(x) - q(x)(v2(x)) \\
 &= 0 - 1(x)
 \end{aligned}$$

$$= -x$$

following GF rules  $\Rightarrow v(x) = x$

So,

$\sum$ ( $\theta$ -2)

$$q_1(x)$$

$$a$$

$$b$$

$$\gamma$$

$$v_1(x)$$

$$v_2(x)$$

$$v(x)$$

$$x^3+1$$

$$x^3+1$$

$$1$$

$$0$$

$$1$$

$$x$$

$$x+1$$

$$1 \int \frac{x^3+1}{x^3+1}$$

$$\underline{\quad x^3 \quad} \downarrow$$

$$\underline{\quad -1 \quad}$$

$$\underline{\quad 0 \quad}$$

$$qv(x) = x^3+1$$

$$\gamma(x) = 0$$

So,

$$v(x) = v_1(x) - q \cdot v_2(x)$$

$$1 - x(x^3+1) = -x^4$$



by following GF rules  $v(x) = x^4$   
 Mod with  $x^4 + x + 1$   
 $v(x) = x^4 \text{ mod } (x^4 + x + 1)$

$$\begin{array}{r} | \\ x^4 + x + 1 \quad \int \\ \hline x^4 \\ - x^4 - x - 1 \\ \hline -x - 1 \text{ in GF} \\ \approx x + 1 \end{array}$$

So,  
It is 3

$q_1(x)$	a	b	$f(x)$	$v_1(x)$	$v_2(x)$	$v(x)$
-	1	0	-	$x$	$x+1$	-

Hence  $M I(x^3 + 1)$  in  $GF(2^4)$  is  $x$



Q.No : 14)

Assume that Feistel Cipher uses 16 rounds. The output of the 14<sup>th</sup> Round during Encryption is 0xAB; K<sub>15</sub> = 0xD, K<sub>16</sub> = 0xE. The round function F(x,y) = XOR(1-bit circular left shift of x, 1-bit circular right shift of y), where y is the Round Key (K<sub>j</sub>). Evaluate the value of Ciphertext (CT).

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Given that,

Output for 14<sup>th</sup> round = 0xAB

$$\text{So, } LD_{14} = 0xA = (1010)_2$$

$$RD_{14} = 0xB = (1011)_2$$

$$k_{15} = 0xD = (1101)_2$$

$$k_{16} = 0xE = (1110)_2$$

15<sup>th</sup> Round

$$LD_{15} = RD_{14} = (1011)_2$$

$$\begin{aligned} RD_{15} &= LD_{14} \oplus F(RD_{14}, k_{15}) \\ &= LD_{14} \oplus ((0111)_2 \oplus (1110)_2) \end{aligned}$$

$$= (1010)_2 \oplus (1001)_2$$

$$= \overline{(0011)_2}$$

Output for 15<sup>th</sup> sound = 10110011 = 0xB3

16<sup>th</sup> sound

$$LD_{16} = RD_{15} = (0011)_2$$

$$RD_{16} = LD_{15} \oplus F(RD_{15}, k_6)$$

$$= (1011)_2 \oplus ((0110)_2 \oplus (0111)_2)$$

$$= (1011)_2 \oplus (0001)_2$$

$$= (1010)_2$$



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So, output of 16<sup>th</sup> round is 0x3A

So, Final Ciphers text is 0xA3



Q.No : 15)

Score : 3.00 / 3.00

Calculate Multiplicative Inverse of  $(x^4 + 1) \bmod (x^5 + x^2 + 1)$  in  $\text{GF}(2^5)$  by applying Extended Euclidean Algorithm (EEA) for Polynomials. (Show Long Division steps for all the iterations while calculating the quotients and remainders).

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$$\text{MI} (x^4 + 1) \bmod (x^5 + x^2 + 1)$$

Iter-①

$q_1(x)$	$a$	$b$	$r(x)$	$u_1(x)$	$u_2(x)$	$u_3(x)$
$x$	$x^5 + x^2 + 1$	$x^4 + 1$	$x^2 + x + 1$	0	1	$x$

$$\begin{array}{r}
 & x \\
 x^4 + 1 & \overline{)x^5 + x^2 + 1} \\
 & x^5 + x \\
 \hline
 & x^2 + 1 \\
 & x^2 + x \\
 \hline
 & x
 \end{array}$$

$\in \text{GF}(2^5)$

$$\begin{aligned}
 r(x) &= x^2 + x + 1 \\
 q_1(x) &= x
 \end{aligned}$$

$$v(x) = u_1(x) - q_1 u_2(x)$$

$$= U - \lambda(1) = \neg \text{in } \mathcal{G}F(\mathbb{Q}_5)$$

$$= \mathcal{D}$$

It's ②

$q(x)$	$a$	$b$	$\gamma(x)$	$U(x)$	$U_2(x)$	$U(x)$
$x^3 + x^2 + x$	$x^4 + 1$	$x^3 + x + 1$	$x + 1$	$ $	$\mathcal{D}$	$x^3 + x^2 + 1$

$$\begin{array}{r}
 x^3 + x \\
 \hline
 x^4 + 1 \\
 \underline{-x^3 - x^2 + 1} \\
 \hline
 -x^3 - x^2 + 1 \quad \text{in } \mathcal{G}F(\mathbb{Q}_5)
 \end{array}$$

$\approx 1 \quad x^3 + x^2 + 1$   
 $\approx 1 \quad x^3 + x^2 + x$   
 $\approx 1 \quad x^3 + x^2 + 1$

$$\gamma(x) = x + 1$$

$$q(x) = x^3 + x$$

$1 - x \in GF(2^5)$

$$\approx x+1$$

$$\begin{aligned} V(x) &= V_1(x) - V_2(x) \\ &= 1 - x(x^2+x) \\ &= x^3 + x^2 + 1 \quad (\because \text{in } GF(2^5)) \end{aligned}$$

It's ③

$q(x)$	$a$	$b$	$\gamma(x)$	$V_1(x)$	$V_2(x)$	$V(x)$
$x$	$x^2+x+1$	$x+1$	1	$x$	$x^3+x^2+1$	$x^3+x^2$

$$\begin{array}{r} x \\ \hline x+1 \longdiv{x^3+x+1} \\ \underline{-x^3-x} \\ \hline x \end{array}$$

$$\begin{aligned} q(x) &= x \\ \gamma(x) &= 1 \end{aligned}$$

$$\begin{aligned}
 V(x) &= V_1(x) - q_V V_2(x) \\
 &= x - x(x^3 + x^2 + 1) \\
 &= x - x^4 - x^3 - x = x^4 + x^3 \quad (\because G(x))
 \end{aligned}$$

It's (4)

$q_V(x)$	$a$	$b$	$f(x)$	$V_1(x)$	$V_2(x)$	$V(x)$
$x+1$	$x+1$	1	0	$x^3 + x^2 + 1$	$x^4 + x^3$	0

$$\begin{array}{r}
 & x+1 \\
 \sqrt{-x} & \overline{x+1} \\
 -x & \hline
 1 & \overline{0}
 \end{array}$$

$$\begin{aligned}
 f(x) &= 0 \\
 q_V(x) &= x+1
 \end{aligned}$$



$$\begin{aligned}
 V(x) &= V_1(x) - qV_2(\lambda) \\
 &= \lambda^3 + \lambda^2 + 1 - (x+1)(\cancel{x^4+x^3}) \\
 &= \lambda^3 + \lambda^2 + 1 - \lambda^5 - \cancel{\lambda^4} + \cancel{\lambda^3} + \lambda^3 \\
 &= \lambda^5 + \lambda^2 + 1 \quad (\because \text{in } GF(2^5))
 \end{aligned}$$

Since it is same as the degree of irreducible polynomial

$$V(\lambda) = \lambda^5 + \lambda^2 + 1 \pmod{(\lambda^5 + \lambda^2 + 1)} = 0$$

It's  $\bar{5}$

$q(\lambda)$	$a$	$b$	$\gamma(x)$	$V_1(x)$	$V_2(x)$	$V(x)$
-	1	0	-	$x^4+x^3$	0	-

Hence MI is  $\cancel{x^4+x^3}$



**Q.No : 16**

When  $x$  ( $x \in \mathbb{N}$ ) is divided by **32** and **55**, the remainders obtained are **7** and **14** respectively. Apply Chinese Remainder Theorem (CRT) to write the corresponding Linear Congruence equations and evaluate the value of  $x$ .

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Given that  
Based on above information

$$x \equiv 7 \pmod{32}$$

$$x \equiv 14 \pmod{55}$$

$$\text{So, } a_1 = 7; a_2 = 14; m_1 = 32, m_2 = 55$$

$$M = \sum m_i$$

$$M = 32 \times 55 = 1760$$

$$m_1 = 55; M_2 = 32$$

$$\begin{aligned} N_1 &= M \lceil (m_1) \bmod (m_1) \rceil \\ &= M \lceil (55) \bmod (32) \rceil \end{aligned}$$

	a	b	$\gamma$	$v_1$	$v_2$	v
0	32	55	32	0	1	0
1	55	32	23	1	0	1
1	32	23	9	0	1	-1
2	23	9	5	1	-1	3
1	9	5	4	-1	3	-4
1	5	4	1	3	-4	7
4	4	1	0	-4	7	-32
-	1	0	-	(7)	-32	-



$$\text{So, } N_1 = 7$$

$$N_2 = M_1^{-1} (M_2) \bmod (n_2)$$

$$= M_1^{-1}(32) \bmod (55)$$

	a	b	x	v1	v2	v	-1
1	55	32	23	0	1		
1	32	23	9	1	-1	2	
2	23	9	5	-1	2	-5	
1	9	5	4	2	-5	7	
1	5	4	1	-5	7	-12	
4	4	1	0	7	-12	-55	
				17	-55	-	

$$\begin{array}{r} - \\ | \quad O \\ - \quad (-12) \end{array}$$

$$\text{So, MI} = -12 \bmod (55) = 43$$

$$\text{So, } N_2 = 43$$

$$\begin{aligned} x &= (a_1 M_1 + a_2 M_0 N_2) \bmod (n) \\ &= (7 \times 55 \times 7 + 43 \times 14 \times 32) \bmod (1760) \\ &= 21959 \bmod (1760) \end{aligned}$$

$$= 839$$

**Q.No : 17)**

A Plaintext (PT) was encrypted using Triple-Stage Columnar Transposition Cipher with the key 'ENDSEM' (Using only alphabets by ignoring the case and by using the padding 'X' if necessary). The Ciphertext (CT) corresponding to the PT is 'TTOTESYIHHUXDRERITXSSMXM'. Evaluate PT by discarding the padding 'X' (if any, after final stage decryption).

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Given that

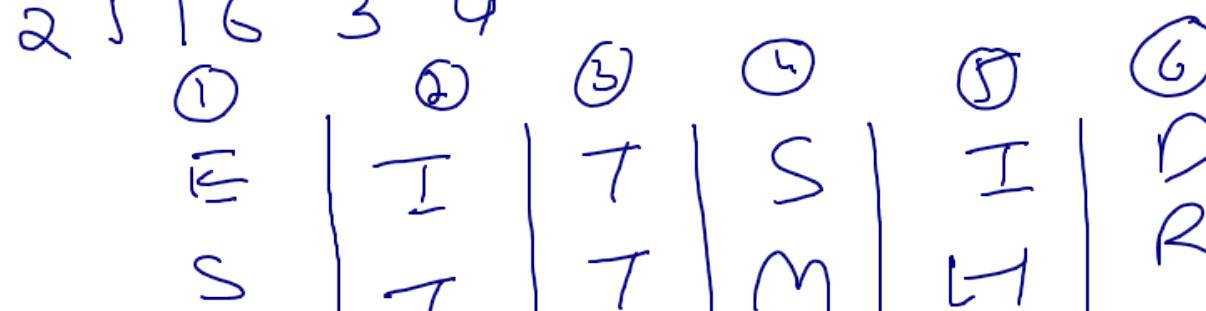
Triple stage columnar

CT: TTOTES Y I I H U X D R E R I T X S S M X M

Key: - ENDSEM

$$\text{No. of rows} = \frac{\text{len(CT)}}{\text{len(key)}} \\ = 24/6 = 4$$

ENDSEM  
so, orders  $\Rightarrow 25 | 634$



Stage -1

Y	X	O	X	U	E
I	S	T	M	X	R

so, first stage output :-

E I T S I D S 7 7 M H R Y X O X U E  
I S + M X R

Stage-2

E N D S E M so, order  $\Rightarrow$  2 5 1 6 3 4  
2 5 1 6 3 4



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(1)	(2)	(3)	(4)	(5)	(6)
I	U	E	T	T	Y
D	E	I	M	M	X
S	I	T	X	H	O
T	S	S	R	R	X

Output after Stage-2

I U E T T Y D E I M M X S I T X H O T  
 SS R R X

Stage-3

END SEM so, order  $\Rightarrow$  2 5 1 6 3 4  
 2 5 1 6 3 4      (1)      (2)      (3)      (4)      (5)      (6)

T	H	I	S	I	S
Y	O	G	R	M	I
O	T	E	R	N	T
E	S	T	X	X	X

So,

Encrypted Text is

THIS IS YOUR ~~MID TERM TEST XXX~~  
Ignore

So, final answer is

This is your mid term test

**Q.No : 18)****Score : 3.00 / 3.00**

State and Prove Fermat's Theorem for prime numbers. Apply Fermat's Theorem to calculate the remainder obtained when  $48^{783}$  is divided by 79 .



## Fermat's Theorem

This theorem states that, any positive integer power  $p-1$ , where  $p$  is a prime number, then its remainder when divided by  $p$  is 1

$$\cancel{a^{p-1} \pmod{p} \equiv 1}$$

P = prime  
since P is prime  
 $\text{GCD}(P, a) = 1$

### Proof:-

Assume a set of integers less than  $P$  like  $X = \{1, 2, 3, \dots, p-1\}$ , now multiply with  $a \pmod{p}$  to all elements of  $X$ , it becomes  $H = \{a \pmod{p}, 2a \pmod{p}, \dots, (p-1)a \pmod{p}\}$

In the new set of  $H$ , there are some

Now, we have  
Conditions to be checked

- (i) All numbers are below  $p$   
This is true because,  $\text{mod } p$  will always give less than  $p$
- (ii) There is no zero  
This is true because, since  $p$  is prime any multiplication can't generate  $p$ . So, none of the elements is zero
- (iii) All elements are unique  
Let us assume they are not unique, let there

$$\text{be } a^j \pmod{p} \equiv a^k$$

$$\Rightarrow j \pmod{p} \equiv k \quad (\because \text{since } a \notin p \text{ are co-primes})$$

This can't be possible as  $X$  has all unique values and  $j, k \in X$

So, we can say that  $X \neq Y$  have same elements but in a different order.

So, if we multiply all and take mod  $p$ , it should be same

$$\Rightarrow ((a \pmod{p})(2a \pmod{p}) \dots (p-1) \pmod{p}) \equiv (1 \times 2 \times 3 \times \dots \times (p-1)) \pmod{p}$$

$$\Rightarrow (a^{p-1} \times (p-1)!) \equiv (p-1)! \pmod{p}$$

as  $(P-1)!$  is coprime to  $P$ , we can cancel on both sides

$$\therefore a^{P-1} \equiv 1 \pmod{P}$$

hence Fermat's theorem is proved

To find :-  $48^{783} \pmod{79}$

79 is prime

so,  $48^{78} \pmod{79} = 1$



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$$\text{So, } 48^{780} \bmod 79 \Rightarrow (48^{78})^0 \bmod 79 = 1$$

$$\begin{aligned}\text{So, } 48^{783} &= (48^{780} \times 48^3) \bmod 79 \\ &= 1 \times 48^3 \bmod 79 \\ &\cancel{=} 1\end{aligned}$$



**Q.No : 19)**

A Plaintext (PT) was encrypted using Hill Cipher with a Key Matrix (K) as displayed in Figure 1. The character set consists of only alphabets by ignoring the case (the alphabets are mapped with their default numerical equivalents). The Ciphertext (CT) corresponding to the PT is '**CPSAPOQLNZIU**'. Calculate the Inverse Key Matrix ( $K^{-1} \bmod 26$ ). Also, Calculate the Plaintext (PT).

$$\begin{bmatrix} 6 & 24 & 1 \\ 13 & 16 & 10 \\ 20 & 17 & 15 \end{bmatrix}$$

**Figure 1:- Key Matrix (K) for Hill Cipher**



$$\text{Key} = \begin{bmatrix} 6 & 24 & 1 \\ 13 & 16 & 10 \\ 20 & 17 & 15 \end{bmatrix}$$

$$\text{CT} := \begin{bmatrix} C & P & S \\ A & P & G \\ Q & L & N \\ Z & I & O \end{bmatrix} = \begin{bmatrix} 2 & 15 & 18 \\ 0 & 15 & 14 \\ 16 & 11 & 13 \\ 25 & 8 & 20 \end{bmatrix}$$

Calculating  $E^{-1}$

$$\text{Det of } E = 44$$

$$E^{-1} = \begin{bmatrix} 70 & -343 & 224 \\ 5 & 70 & -17 \\ -99 & 378 & -21 \end{bmatrix} \quad 44^{-1} \pmod{26}$$

$$\text{m}(441) \bmod 26$$

a	a	b	x	v <sub>1</sub>	v <sub>2</sub>	v
16	441	26	25	0	1	-16
1	26	25	1	1	-16	13
25	25	1	0	-16	13	-441
-	1	0	-	<del>13</del>		0



$$\text{So } \begin{bmatrix} 70 & -343 & 224 \\ 5 & 70 & -47 \\ -99 & 378 & -26 \end{bmatrix} \times 17 \pmod{26}$$

$$\therefore \begin{bmatrix} 20 & 23 & 12 \\ 7 & 20 & \cancel{7} \\ 7 & 4 & 20 \end{bmatrix} = k^{-1}$$

So, now,  $C7xk^{-1}$

$$\text{So, } C7xk^{-1} = \begin{bmatrix} 11 & 2 & 21 \\ 21 & 18 & 21 \\ 20 & 16 & 9 \\ 20 & 9 & 2 \end{bmatrix}$$

~~-1 / √ (11) <~~

-1 u v y