

1) Consider the following snapshot at time t_0

Snapshot at time T_0 :

	Allocation	Maximum	Available	Need
	A B C	A B C	A B C	A B C
P0	0 1 0	7 5 3	3 3 2	7 4 3
P1	2 0 0	3 2 2	→	1 2 2
P2	3 0 2	9 0 2	→	6 0 0
P3	2 1 1	2 2 2	→	0 1 1
P4	0 0 2	4 3 3	→	4 3 1
	<u>7 2 5</u>			

(i) Is the s/m in a safe state?

(ii) If a request from P1 arrives for (1, 0, 2) can the request be granted immediately

Solⁿ: Total instances of $A = 7 + 3 = 10$; $B = 2 + 3 = 5$; $C = 7$

(i) Safety algorithm:

work = Available, Finish[P₀-P₄] = false
work = [3, 3, 2]

(1) $i = P_0$ need[P₀] ≤ work
[7, 4, 3] \nless [3, 3, 2] P₀ cannot execute, wait

(2) $i = P_1$ need[P₁] ≤ work
[1, 2, 2] ≤ [3, 3, 2] P₁ executes

work = work + allocation

= [3, 3, 2] + [2, 0, 0]

work = [5, 3, 2], Finish[P₁] = True

(3) $i = P_2$ need $[P_2] \leq \text{work}$
 $[6, 0, 0] \not\leq [5, 3, 2]$ P_2 cannot execute, wait

(4) $i = P_3$ need $[P_3] \leq \text{work}$
 $[0, 1, 1] \leq [5, 3, 2]$ P_3 executes

$$\text{work} = \text{work} + \text{allocation}[P_3]$$

$$= [5, 3, 2] + [2, 1, 1]$$

$$\text{work} = [7, 4, 3], \text{ finish}[P_3] = \text{True}$$

(5) $i = P_4$ need $[P_4] \leq \text{work}$
 $[4, 3, 1] \leq [7, 4, 3]$ P_4 executes

$$\text{work} = \text{work} + \text{allocation}[P_4]$$

$$= [7, 4, 3] + [0, 0, 2]$$

$$= [7, 4, 5], \text{ finish}[P_4] = \text{True}$$

(6) $i = P_0$ $[7, 4, 3] \leq [7, 4, 5]$, P_0 executes

$$\text{work} = [7, 4, 5] + [0, 1, 0]$$

$$\text{work} = [7, 5, 5], \text{ finish}[P_0] = \text{True}$$

(7) $i = P_2$ $[6, 0, 0] \leq [7, 5, 5]$ P_2 executes

$$\text{work} = [7, 5, 5] + [3, 0, 2]$$

$$\text{work} = [10, 5, 7] = \text{Total no. of instances of Resource types}$$

$$\text{finish}[P_2] = \text{True}$$

$\therefore \langle P_1, P_3, P_4, P_0, P_2 \rangle$ safe sequence

(ii) Snapshot at time T_0 :

	Allocation	Maximum	Available	Need
	A B C	A B C	A B C	A B C
P0	0 1 0	7 5 3	3 3 2	7 4 3
P1	2 0 0	3 2 2	→	1 2 2
P2	3 0 2	9 0 2	→	6 0 0
P3	2 1 1	2 2 2	→	0 1 1
P4	0 0 2	4 3 3	→	4 3 1
	<u>2 5</u>			

$P_1 \xrightarrow{\text{request}} [1, 0, 2]$

(1) $\text{Request}[P_1] \leq \text{Need}[P_1]$

$$[1, 0, 2] \leq [1, 2, 2]$$

\therefore requested resources are needed

(2) $\text{Request}[P_1] \leq \text{Available}$

$$[1, 0, 2] \leq [3, 3, 2]$$

\therefore requested resources are available

(3) Assume P_1 is allocated requested resources.

$$\begin{aligned} \text{allocate}[P_1] &= \text{allocate}[P_1] + \text{Request}[P_1] \\ &= [2, 0, 0] + [1, 0, 2] = [3, 0, 2] \end{aligned}$$

$$\begin{aligned} \text{Need}[P_1] &= \text{Need}[P_1] - \text{Request}[P_1] \\ &= [1, 2, 2] - [1, 0, 2] = [0, 2, 0] \end{aligned}$$

$$\begin{aligned} \text{available} &= \text{available} - \text{Request}[P_1] \\ &= [3, 3, 2] - [1, 0, 2] = [2, 3, 0] \end{aligned}$$

Snapshot at time T0:

	Allocation	Maximum	Available	Need
	A B C	A B C	A B C	A B C
P0	0 1 0	7 5 3	2 3 0	7 4 3
P1	3 0 2	3 2 2	→	<u>0 2 0</u> changed
P2	3 0 2	9 0 2	→	6 0 0
P3	2 1 1	2 2 2	→	0 1 1
P4	0 0 2	4 3 3	→	4 3 1

With these changes safety algorithm is checked to find if the s/m is in safe state.

$$\text{work} = \text{available} = [2, 3, 0]$$

$$\text{finish}[P_0 - P_4] = \text{False}$$

$$1) i = P_0, \quad \text{need}[P_0] \leq \text{work} \\ [7, 4, 3] \not\leq [2, 3, 0] \quad P_0 \text{ cannot execute; wait}$$

$$2) i = P_1, \quad [0, 2, 0] \leq [2, 3, 0] \quad P_1 \text{ executes} \\ \text{work} = \text{work} + \text{allocation}[P_1] \\ = [2, 3, 0] + [3, 0, 2] \\ = [5, 3, 2], \quad \text{finish}[P_1] = \text{True}$$

$$3) i = P_2, \quad [6, 0, 0] \not\leq [5, 3, 2], \quad P_2 \text{ cannot execute}$$

$$4) i = P_3, \quad [0, 1, 1] \leq [5, 3, 2], \quad P_3 \text{ executes} \\ \text{work} = [5, 3, 2] + [2, 1, 1] \\ = [7, 4, 3], \quad \text{finish}[P_3] = \text{True}$$

$$5) i = P_4 \quad [4, 3, 1] \leq [7, 4, 3], P_4 \text{ executes}$$

$$\text{work} = [7, 4, 3] + [0, 0, 2]$$

$$= [7, 4, 5]$$

$$6) i = P_0, [7, 4, 3] \leq [7, 4, 5] P_0 \text{ executes}$$

$$\text{work} = [7, 4, 5] + [0, 1, 0]$$

$$= [7, 5, 5], \text{Finish}[P_0] = \text{True}$$

$$7) i = P_2, \text{need}[P_2] \leq \text{work}$$

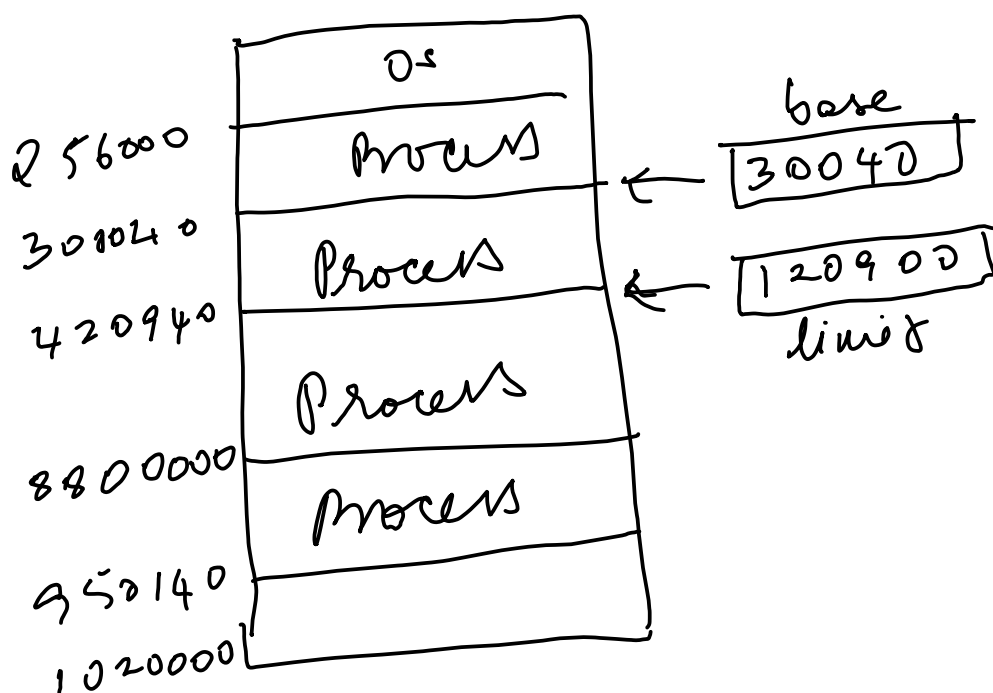
$$[6, 0, 0] \leq [7, 5, 5] P_2 \text{ executes}$$

$$\text{work} = [7, 5, 5] + [3, 0, 2]$$

$$= [10, 5, 7]$$

... safe sequence is $\langle P_1, P_3, P_4, P_0, P_2 \rangle$

∴ the request of P_1 can be granted



Deadlock detection

Five processes P0 through P4; three resource types

A (7 instances), B (2 instances), and C (6 instances)

Snapshot at time T0:

	Allocation	Request	Available
	A B C	A B C	A B C
P0	0 1 0	→ 0 0 0	0 0 0
P1	2 0 0	2 0 2	
P2	3 0 3	0 0 0	
P3	2 1 1	1 0 0	
P4	0 0 2	0 0 2	

If the requested resources are allocated,
check whether s/m will be in safe state.

Also, find the safe sequence.

Solⁿ: Initialization:

work = available

work = (0, 0, 0)

Finish(P₀ - P₄) = false
as all processes are
allocated some
resources

1) $i = P_0$; Request(P₀) ≤ work

(0, 0, 0) ≤ (0, 0, 0)

work = work + allocation[P₀]

= (0, 0, 0) + (0, 1, 0)

= (0, 1, 0), Finish[P₀] = true

$$2) \quad i = P_1 ; \quad (2, 0, 2) \not\leq (0, 1, 0)$$

$$3) \quad i = P_2 ; \quad (0, 0, 0) \leq (0, 1, 0)$$

$$\begin{aligned} \text{work} &= (0, 1, 0) + (3, 0, 3) \\ &= (3, 1, 3), \text{ finish}[P_1] = \text{True} \end{aligned}$$

$$4) \quad i = P_3 ; \quad (1, 0, 0) \leq (3, 1, 3)$$

$$\begin{aligned} \text{work} &= (3, 1, 3) + (2, 1, 1) \\ &= (5, 2, 4), \text{ finish}[P_3] = \text{True} \end{aligned}$$

$$5) \quad i = P_4 ; \quad (0, 0, 2) \leq (5, 2, 4)$$

$$\begin{aligned} \text{work} &= (5, 2, 4) + (0, 0, 2) \\ &= (5, 2, 6) \end{aligned}$$

$$6) \quad i = P_1 ; \quad (2, 0, 2) \leq (5, 2, 6)$$

$$\text{work} = (5, 2, 6) + (2, 0, 0)$$

$$\text{work} = (7, 2, 6) \quad \text{finish}[P_1] = \text{True}$$

Since $\text{finish}[P_0 - P_4] = \text{true}$, Alm is in safe state when the requested resources are allocated.

safe sequence $\langle P_0, P_2, P_3, P_4, P_1 \rangle$

Case II P_2 requests additional insts
- case of Type C.

Snapshot at time T_0 :

	Allocation	Request	Available
	A B C	A B C	A B C
P0	0 1 0	0 0 0	0 0 0
P1	2 0 0	2 0 2	
P2	3 0 3	0 0 1	
P3	2 1 1	1 0 0	
P4	0 0 2	0 0 2	

check if P_2 is safe if the requested resources are allocated.

Solⁿ: 1) $i = P_0$: $request[P_0] \leq work$
 $(0, 0, 0) \leq (0, 0, 0)$
 $work = (0, 1, 0)$, $Finish[P_0] = true$

2) $i = P_1$: $(2, 0, 2) \not\leq (0, 1, 0)$, false

3) $i = P_2$: $(0, 0, 1) \not\leq (0, 1, 0)$, false

4) $i = P_3$: $(1, 0, 0) \not\leq (0, 1, 0)$, false

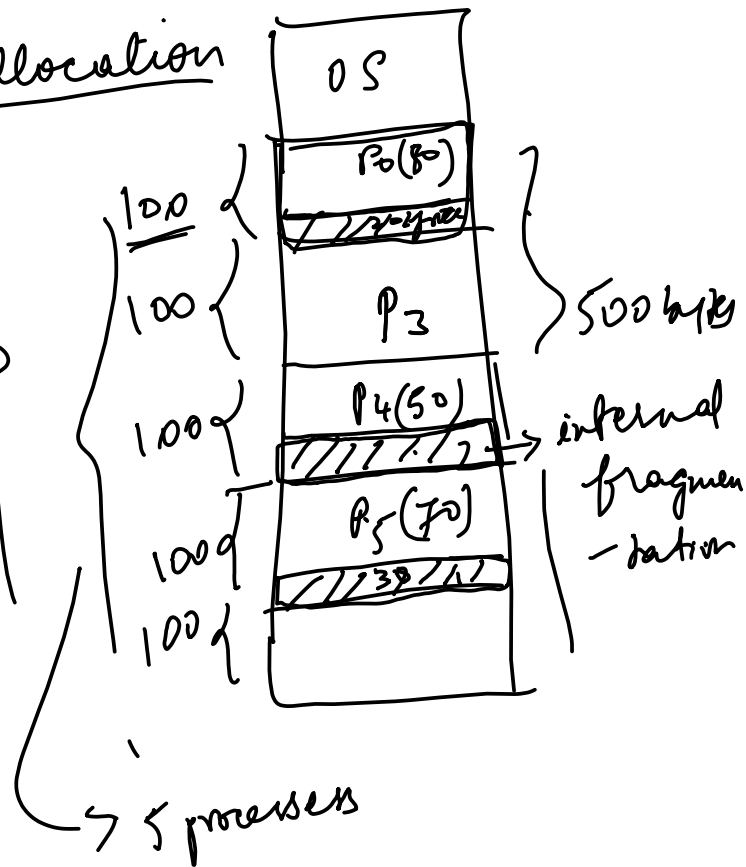
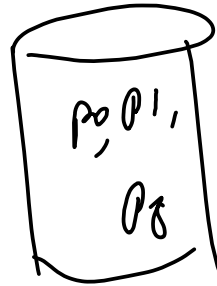
5) $i = P_4$: $(0, 0, 2) \not\leq (0, 1, 0)$, false

$\langle P_1, P_2, P_3, P_4 \rangle$ deadlocked processes

Contiguous memory allocation

→ fixed sized

$P_0 = 80$
 $P_1 = 150$
 $P_3 = 100$
 $P_4 = 50$

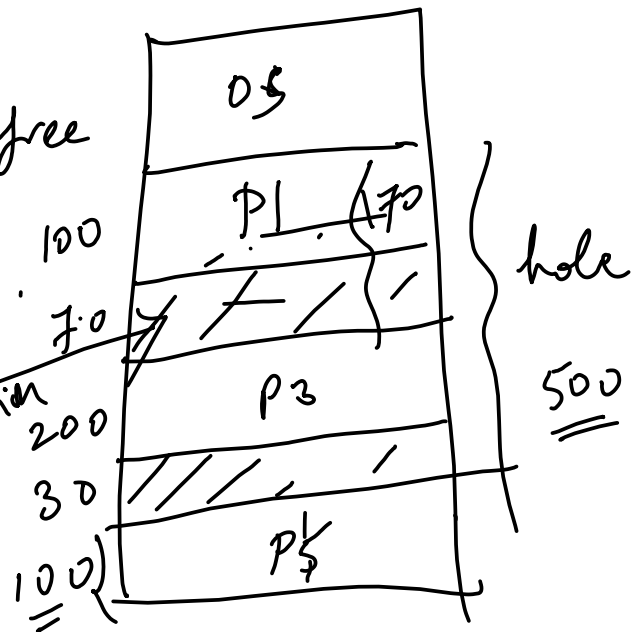


variable sized locations

* hole - available / unused / free memory space

$P_1 - 100$
 $P_2 - 70$
 $P_3 - 200$
 $P_4 - 30$
 $P_5 - 120$

external fragmentation



P_6 - 100 byte - wait

Limit Register (301)
Relocation Register (14500)

process - 0 to 300

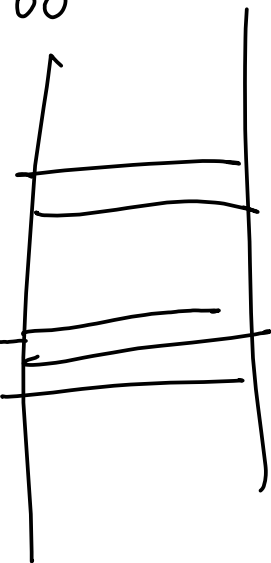
$$14500 + 0 \leq \text{PA process} \leq 14500 + 300$$

$$14800 \leq \leq 14800$$

$$LA = 400 > 301 \text{ -- trap } 14500$$

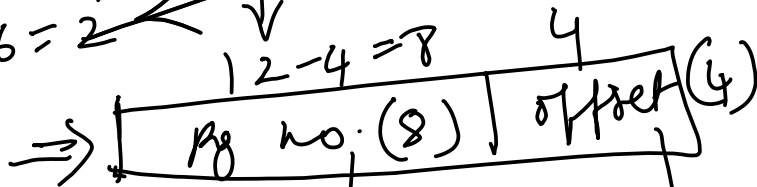
$$LA = 200 < 301$$

$$14500 + 200$$

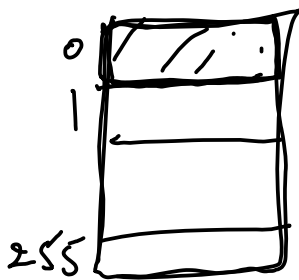


Paging — VA/2A → PA LA address space

$$4k = 4096 = 2^{12}$$



$$m \text{ bits} = 12 \text{ bits} \Rightarrow$$



$$2^8 \text{ pages} \Rightarrow 256$$

$$000 - \dots - 255$$

$$111 - \dots - 255$$

$$\frac{4}{2} = 16 \text{ bytes}$$

1) First fit
best
 worst fit

$$P_1 = \underline{\underline{150}}$$

$$P_2 = 200$$

$$P_3 = \underline{\underline{300}} \text{ (wast)}$$

$$\begin{array}{l} 2^0 = 1 \\ 2^1 = 2 \\ 2^2 = 4 \\ 2^3 = 8 \end{array}$$

$$\begin{array}{l} 2^4 = 16 \\ 2^5 = 32 \end{array}$$

$$2^6 = 64$$

$$2^7 = 128$$

$$2^8 = 256$$

$$2^9 = 512$$

$$2^{12} = 4 \text{ kB}$$

$$2^{15} = 32 \text{ k}$$

$$2^{22} = 4 \text{ MB} \quad 2^{32} = 4 \text{ B}$$

$$2^{25} = 32 \text{ M}$$

