EE24BTECH11001 - Aditya Tripathy

Question:

A coin is tossed twice, what is the probability that atleast one tail occurs?

Solution:

The sample space is

$$\Omega = [HH, HT, TH, TT] \tag{0.1}$$

Assuming equally likely outcomes,

$$\Pr\left(\omega \in \Omega\right) = \frac{1}{4} \tag{0.2}$$

Define a discrete random variable X = number of tails in the sequence.

$$Pr(X \ge 1) = 1 - Pr(X < 1)$$
 (0.3)

$$=1-\frac{1}{4}=\frac{3}{4}\tag{0.4}$$

Simulation: The following shows how the relative frequency reaches true probability with increasing number of trials of the event.

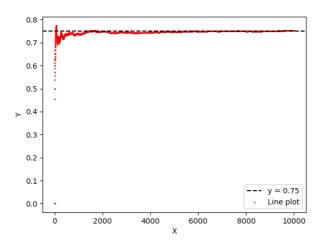


Fig. 0.1: Relative Frequency tends to True Probability

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