

1.6.5

EE24BTECH11001 - Aditya Tripathy

Question:

Show that the points $(2, 3, 4)$, $(-1, -2, 1)$, $(5, 8, 7)$ are collinear.

Solution:

From (1.1.9.1), Points A, B, C are defined to be collinear if

$$\text{rank} \begin{pmatrix} (\mathbf{B} - \mathbf{A})^\top \\ (\mathbf{C} - \mathbf{A})^\top \end{pmatrix} = 1 \quad (0.1)$$

(0.2)

So, forming the collinearity matrix and doing row operations,

$$\begin{pmatrix} -3 & -5 & -3 \\ 3 & 5 & 3 \end{pmatrix} \xrightarrow{R_2 = R_2 + R_1} \begin{pmatrix} -3 & -5 & -3 \\ 0 & 0 & 0 \end{pmatrix} \quad (0.3)$$

(0.4)

Since there is only one non-zero row, $\text{rank} = 1$. Hence the points are collinear.

1000 Points on the Line

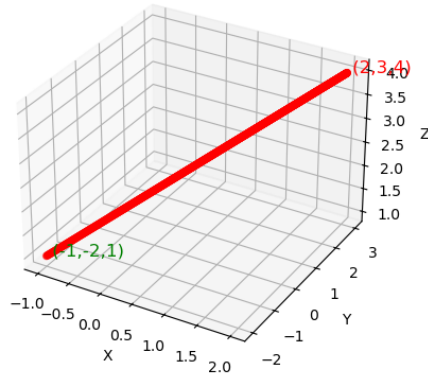


Fig. 0.1: Line joining the three given points