EE24BTECH11001 - Aditya Tripathy

Question:

If a line has direction ratios -18, 12, -4, what are its direction cosines? **Solution:** Let

$$\mathbf{A} = \begin{pmatrix} -18\\12\\-4 \end{pmatrix} \tag{1}$$

$$||A|| = \sqrt{\mathbf{A}^{\mathsf{T}} \mathbf{A}} \tag{2}$$

$$||A|| = \sqrt{\mathbf{A}^{\top} \mathbf{A}}$$

$$= \sqrt{(-18 \quad 12 \quad -4) \begin{pmatrix} -18 \\ 12 \\ -4 \end{pmatrix}}$$
(2)

$$\implies ||A|| = 22 \tag{4}$$

The unit direction vector of the line is

$$\frac{\mathbf{A}}{\|\mathbf{A}\|} = \frac{\begin{pmatrix} -18\\12\\-4 \end{pmatrix}}{22} = \begin{pmatrix} \frac{-9}{11}\\\frac{16}{11}\\\frac{-2}{11} \end{pmatrix}$$
 (5)

Hence, the direction cosines of the line are $\frac{-9}{11}$, $\frac{6}{11}$ and $\frac{-2}{11}$.

1

1000 Points on the Line

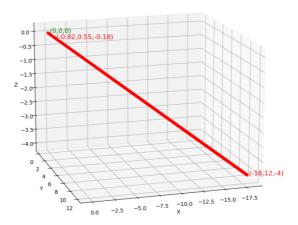


Fig. 0: Line with given direction ratios