EE24BTECH11001 - Aditya Tripathy

Question:

Show that the points $P\begin{pmatrix} 5\\4 \end{pmatrix}$, $Q\begin{pmatrix} 7\\k \end{pmatrix}$ and $R\begin{pmatrix} 9\\-2 \end{pmatrix}$ are collinear.

Solution:

From (1.1.9.1), Points A, B, C are defined to be collinear if

$$rank \begin{pmatrix} (\mathbf{B} - \mathbf{A})^{\mathsf{T}} \\ (\mathbf{C} - \mathbf{A})^{\mathsf{T}} \end{pmatrix} = 1 \tag{0.1}$$

(0.2)

Therefore, there should be only 1 non-zero row in collinearity matrix after row-operations. So, forming the collinearity matrix and doing row operations,

$$\begin{pmatrix} 2 & k-4 \\ 4 & -6 \end{pmatrix} \xrightarrow{R_2 = R_2 - 2R_1} \begin{pmatrix} 2 & k-4 \\ 0 & 2-2k \end{pmatrix} \tag{0.3}$$

$$\implies 2 - 2k = 0 \implies k = 1 \tag{0.4}$$

Therefore k=1 will satisfy condition of collinearity.

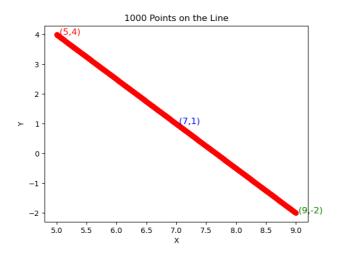


Fig. 0.1: Line joining the three given points