Trignometric Functions and Equations

EE24BTECH11001- ADITYA TRIPATHY

A: FILL IN THE BLANKS

- 1) Suppose $\sin^3 x \sin 3x = \sum_{m=0}^n C_m \cos x$ is an identity in x, where C_0, C_1, \dots, C_n are constants and $C_n \neq 0$ then the value of (1981 - 2Marks)
- 2) The solution set of the system of equations $x + y = \frac{2\pi}{3}$, $\cos x + \cos y = \frac{5}{2}$, where x and y are real, is (1987 - 2Mark)
- 3) The set of all x in the interval $[0, \pi]$ for which $2\sin^2 x - 3\sin x + 1 \ge 0$, is (1987 - 2mark)
- 4) The sides of a triangle in a given circle subtend angles α , β , γ . The minimum value of arithmetic mean of $\cos\left(\alpha + \frac{\pi}{2}\right)$, $\cos\left(\beta + \frac{\pi}{2}\right)$, $\cos\left(\gamma + \frac{\pi}{2}\right)$ is (1987 - 2Marks)equal to
- 5) The value of $\sin \frac{\pi}{14} \sin \frac{3\pi}{14} \sin \frac{5\pi}{14} \sin \frac{7\pi}{14}$ $\sin \frac{9\pi}{14} \sin \frac{11\pi}{14} \sin \frac{13\pi}{14}$ is equal to

(1991 - 2Marks)

- 6) If $K = \sin(\frac{\pi}{18}) \sin(\frac{5\pi}{18}) \sin(\frac{7\pi}{18})$ then the numerical value of K is (1993 - 2Marks)
- 7) If A > 0, B > 0 and $A + B = \frac{\pi}{3}$, then the maximum value $\tan A \tan B$ is (1993 - 2Marks)
- 8) General value of θ satisfying the equation $\tan^2 \theta + \sec 2\theta$ (1996 - 1Mark)
- 9) The real roots of the equation $\cos^{7} x$ + $\sin^4 x = 1$ in the interval $(-\pi, \pi)$ are (1997 - 2Marks)

B: True / False

- 1) If $\tan A = \frac{1-\cos B}{\sin B}$, then $\tan 2A = \tan B$ (1981 - 1Marks)
- 2) There exists a value of θ between 0 and 2π that satisfies the equation $\sin^4 \theta$ – $2\sin^2\theta - 1 = 0.$ (1984 - 1Marks)

C:MCQs with One Correct Answer

1) If $\tan \theta = -\frac{4}{3}$ then $\sin \theta$ is

(1979)

(a) $\frac{-4}{5}$ but not $\frac{4}{5}$

- (b) $\frac{4}{5}$ or $\frac{-4}{5}$ (c) $\frac{4}{5}$ but not $\frac{-4}{5}$
- (d) None of These
- 2) If $\alpha + \beta + \gamma = 2\pi$
 - (a) $\tan \frac{\alpha}{2} + \tan \frac{\beta}{2} + \tan \frac{\gamma}{2} = \tan \frac{\alpha}{2} \tan \frac{\beta}{2} \tan \frac{\gamma}{2}$
 - (b) $\tan \frac{\alpha}{2} \tan \frac{\beta}{2} + \tan \frac{\beta}{2} \tan \frac{\gamma}{2} + \tan \frac{\gamma}{2} \tan \frac{\alpha}{2} = 1$
 - (c) $\tan \frac{\alpha}{2} + \tan \frac{\beta}{2} + \tan \frac{\gamma}{2} = -\tan \frac{\alpha}{2} \tan \frac{\beta}{2} \tan \frac{\gamma}{2}$
 - (d) None of These
- 3) Given $A = \sin^2 \theta + \cos^4 \theta$ then for all real values of θ (1980)
 - (a) $1 \le A \le 2$

 - (b) $\frac{3}{4} \le A \le 1$ (c) $\frac{13}{16} \le A \le 1$ (d) $\frac{3}{4} \le A \le \frac{13}{16}$
- 4) The equation $2\cos^2 \frac{x}{2}\sin^2 x = x^2 + x^{-2}$ (1980)
 - (a) no real solution
 - (b) one real solution
 - (c) more than one real solution
 - (d) None of these
- 5) The general solution to the trignometric equation $\sin x + \cos x = 1$ is given by (1981 - 2Marks)
 - (a) $x = 2n\pi$; $n = 0, \pm 1, \pm 2 \cdots$
 - (b) $x = 2n\pi + \frac{\pi}{2}, n = 0, \pm 1, \pm 2 \cdots$
 - (c) $x = n\pi + (-1)^n \frac{\pi}{4}, n = 0, \pm 1, \pm 2 \cdots$
 - (d) none of these
- 6) The value of expression the $\sqrt{3}$ cosec 20° - sec 20° is equal to (1988 - 2Marks)

 - (b) $2 \sin 20^{\circ} / \sin 40^{\circ}$

 - (d) $2 \sin 20^{\circ} / \sin 40^{\circ}$