Assignment 2

Roll Number - Name

6. If f(x) =

$$\begin{vmatrix} 1 & x & x+1 \\ 2x & x(x-1) & (x+1)x \\ 3x(x-1) & x(x-1)(x-2) & (x+1)x(x-1) \end{vmatrix}$$

- then f(100) is equal to
- (1999 2Marks)

- (a) 0
- (b) 1
- (c) 100
- (d) -100
- 7. If the system of equations x ky z = 0, kx z = 0y-z=0, x+y-z=0 has a non-zero solution, then the possible values of k are (2000S)
 - (a) -1,2
- (b) 1,2
- (c) 0,1
- (d) -1,1
- 8. Let $\omega = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$. Then the value of the determinant

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 - \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^4 \end{vmatrix}$$

- (a) 3ω
- (b) 3ω (c) $3\omega^2$ $(\omega 1)$
- 9. The number of values of k for which the system of equations (k + 1) x + 8y = 4k; kx + (k + 3) y =3k-1 has infinitely many solutions is (2002S)
 - (a) 0
- (b) 1
- (c) 2
- (d) infinte

(d)

- 10. If $A = \begin{pmatrix} \alpha & 0 \\ 1 & 1 \end{pmatrix}$ and $B = \begin{pmatrix} 1 & 0 \\ 5 & 1 \end{pmatrix}$, then value of α for which $A^2 = B$, is
 - (a) 1

(b) 4

(c) 2

- (d) infinite
- 11. If the system of equations x+ay=0, az+y=0and ax + z = 0 has infinite solutions, then the value of a is (2003S)

(a) -1

(b) 1

(c) 0

- (d) no real values
- 12. Given 2x-y+2z = 2, x-2y+z = -4, $x+y+\lambda z =$ 4 then the value of λ such that the given system of equation has NO solution, is

(2004S)

- (a) 3
- (b) 1
- (c) 0
- (d) -3
- 13. Is $A = \begin{pmatrix} \alpha & 2 \\ 2 & \alpha \end{pmatrix}$ and $|A^3| = 125$ then the value α
 - (a) ± 1
- (b) ± 2
- $(c) \pm 3$
- 14. $A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{pmatrix}$ and $I = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ and $A^{-1} = \left(\frac{1}{6}(A^2 + cA + dI)\right)$, then the value of
 - (a) (b) (6,11) (c) (-6,11)(d) (6,-11)(-6, -11)
- 15. If $P = \begin{vmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{vmatrix}$ and $A = \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix}$ and $Q = PAP^T$ and $X = P^T Q^{2005} P$ then X is equal to

 - and x = PQ Tulen x is c_1 (a) $\begin{vmatrix} 1 & 2005 \\ 0 & 1 \end{vmatrix}$ (b) $\begin{vmatrix} 4 + 2005 \sqrt{3} & 6015 \\ 2005 & 4 2005 \sqrt{3} \end{vmatrix}$ (c) $\frac{1}{4} \begin{vmatrix} 2 + \sqrt{3} & 1 \\ -1 & 2 \sqrt{3} \\ 2005 & 2 \sqrt{3} \end{vmatrix}$ (d) $\frac{1}{4} \begin{vmatrix} 2005 & 2 \sqrt{3} \\ 2 + \sqrt{3} & 2005 \end{vmatrix}$
- 16. Consider P = $(-\sin(\beta-\alpha), -\cos\beta), Q$ = $(\cos(\beta - \alpha), \sin\beta)$ R $(\cos(\beta - \alpha + \theta), \sin(\beta - \theta))$ where $0 < \alpha, \beta, \theta < \frac{\pi}{4}$. Then, (2008)

(d) 205

- (a) P lies on the same segment RQ
- (b) Q lies on the line segment PR
- (c) R lies on the line segment QP
- (d) P,Q,R are non-collinear
- 17. the number of 3x3 matrices A whose entries are either 0 or 1 and for which the system $A \begin{pmatrix} x \\ y \end{pmatrix} =$
 - $\begin{bmatrix} 0 \\ 0 \end{bmatrix}$ has exactly two distinct solutions is (2008)
 - (a) 0
- (b) $2^9 1$ (c) 168

(a) 52

(b) 103

(c) 201

18. Let $\omega \neq 1$ be a cube root of unity and S be the set of all non-singular matrices of the form

$$\begin{vmatrix} 1 & a & b \\ \omega & 1 & c \\ \omega^2 & \omega & 1 \end{vmatrix}$$

where each of a, b and c is either ω or ω^2 . Then the number of distinct matrices in the set S is (2008)

- (a) 2
- (b) 6
- (c) 4
- (d) 8
- 19. Let $P = (a_{ij})$ be 3x3 matrix and let $Q = (b_{ij})$, where $b_{ij} = 2^{i+j}a_{ij}$ for $1 \le i, j \le 3$. If the determinant of P is 2, then the determinant of the matrix Q is
 - (a) 2^{10}

- (b) 2^{11} (c) 2^{12} (d) 2^{13}
- 20. If P is a 3x3 matrix such that $P^T = 2P + I$, where P^T is the transpose of P and I is the 3x3 identity matrix, then there exists a column

matrix
$$X = \begin{pmatrix} x \\ y \\ z \end{pmatrix} \neq \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$
 (2012)

(a)
$$PX = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$
 (b) $PX = X$

(c)
$$PX = 2X$$

(d)
$$PX = -X$$

21. Let
$$P = \begin{pmatrix} 1 & 0 & 0 \\ 4 & 1 & 0 \\ 16 & 4 & 1 \end{pmatrix}$$
 and I be the identity matrix

of order 3. If $Q = (q_i j)$ is a matrix such that $P^{50} - Q = I$, then $\frac{q_{31} + q_{32}}{q_{21}}$ equals (*JEEAdv*.2016)