## 1

## Assignment 2

## Roll Number - Name

6. If f(x) =

$$\begin{vmatrix} 1 & x & x+1 \\ 2x & x(x-1) & (x+1)x \\ 3x(x-1) & x(x-1)(x-2) & (x+1)x(x-1) \end{vmatrix}$$
then  $f(100)$  is equal to  $(1999 - 2Marks)$ 

- then f(100) is equal to
  - (b) 1
- (c) 100
- (d) -100
- 7. If the system of equations x ky z = 0, kx z = 0y-z=0, x+y-z=0 has a non-zero solution, then the possible values of k are (2000S)
  - (a) -1,2

(a) 0

- (b) 1,2
- (c) 0,1
- (d) -1,1
- 8. Let  $\omega = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$ . Then the value of the determinant

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 - \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^4 \end{vmatrix}$$

- (a)  $3\omega$
- (b)  $3\omega$  (c)  $3\omega^2$   $(\omega 1)$
- 9. The number of values of k for which the system of equations (k + 1) x + 8y = 4k; kx + (k + 3) y =3k-1 has infinitely many solutions is (2002S)
  - (a) 0
- (b) 1
- (c) 2
- (d) infinte
- 10. If  $A = \begin{pmatrix} \alpha & 0 \\ 1 & 1 \end{pmatrix}$  and  $B = \begin{pmatrix} 1 & 0 \\ 5 & 1 \end{pmatrix}$ , then value of  $\alpha$ for which  $A^2 = B$ , is
  - (a) 1

(b) 4

(c) 2

- (d) infinite
- 11. If the system of equations x+ay=0, az+y=0and ax + z = 0 has infinite solutions, then the value of a is (2003S)

(a) -1

(b) 1

(c) 0

- (d) no real values
- 12. Given 2x-y+2z = 2, x-2y+z = -4,  $x+y+\lambda z =$ 4 then the value of  $\lambda$  such that the given system of equation has NO solution, is

(2004S)

- (a) 3
- (b) 1
- (c) 0
- (d) -3
- 13. Is  $A = \begin{pmatrix} \alpha & 2 \\ 2 & \alpha \end{pmatrix}$  and  $|A^3| = 125$  then the value  $\alpha$ (2004S)
  - (a)  $\pm 1$ 
    - (b)  $\pm 2$
- $(c) \pm 3$
- 14.  $A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{pmatrix}$  and  $I = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ 2005S and  $A^{-1} = \left(\frac{1}{6}(A^2 + cA + dI)\right)$ , then the value of c and d are (2005S)
- (d)  $3\omega(1-\omega)$  (a) (b) (6,11) (c) (-6,11)(d) (6,-11) (-6,-11)
  - 15. If  $P = \begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$  and  $A = \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix}$  and  $Q = PAP^T$ and  $x = P^{T} Q^{2005} P$  then x is equal to

    - and x = 1 (a)  $\begin{vmatrix} 1 & 2005 \\ 0 & 1 \end{vmatrix}$ (b)  $\begin{vmatrix} 4 + 2005 \sqrt{3} & 6015 \\ 2005 & 4 2005 \sqrt{3} \end{vmatrix}$ (c)  $\frac{1}{4}\begin{vmatrix} 2 + \sqrt{3} & 1 \\ -1 & 2 \sqrt{3} \\ 2 + \sqrt{3} & 2005 \end{vmatrix}$ (d)  $\frac{1}{4}\begin{vmatrix} 2005 & 2 \sqrt{3} \\ 2 + \sqrt{3} & 2005 \end{vmatrix}$
  - P 16. Consider = $(-\sin(\beta-\alpha), -\cos\beta), Q$ =  $(\cos(\beta - \alpha), \sin\beta)$ R and = $(\cos(\beta - \alpha + \theta), \sin(\beta - \theta))$ where  $0 < \alpha, \beta, \theta < \frac{\pi}{4}$ . Then, (2008)
    - (a) P lies on the same segment RQ

(d) 205

- (b) Q lies on the line segment PR
- (c) R lies on the line segment QP
- (d) P,Q,R are non-collinear
- 17. the number of 3x3 matrices A whose entries are either 0 or 1 and for which the system  $A \begin{pmatrix} x \\ y \\ z \end{pmatrix} =$

 $\begin{pmatrix} 1\\0\\0 \end{pmatrix}$  has exactly two distinct solutions is (2008)

(a) 52

(b) 103

(c) 201

- (a) 0 (b)  $2^9 1$  (c) 168 (d) 2
- 18. Let  $\omega \neq 1$  be a cube root of unity and S be the set of all non-singular matrices of the form

$$\begin{vmatrix} 1 & a & b \\ \omega & 1 & c \\ \omega^2 & \omega & 1 \end{vmatrix}$$

where each of a, b and c is either  $\omega$  or  $\omega^2$ . Then the number of distinct matrices in the set S is (2008)

- (a) 2 (b) 6 (c) 4 (d) 8
- 19. Let  $P = (a_{ij})$  be 3x3 matrix and let  $Q = (b_{ij})$ , where  $b_{ij} = 2^{i+j}a_{ij}$  for  $1 \le i, j \le 3$ . If the determinant of P is 2, then the determinant of the matrix Q is (2012)
  - (a)  $2^{10}$  (b)  $2^{11}$  (c)  $2^{12}$  (d)  $2^{13}$
- 20. If P is a 3x3 matrix such that  $P^T = 2P + I$ , where  $P^T$  is the transpose of P and I is the 3x3 identity matrix, then there exists a column

matrix 
$$X = \begin{pmatrix} x \\ y \\ z \end{pmatrix} \neq \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$
 (2012)

(a) 
$$PX = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$
 (b)  $PX = X$ 

(c) 
$$PX = 2X$$
 (d)  $PX = -X$ 

21. Let  $P = \begin{pmatrix} 1 & 0 & 0 \\ 4 & 1 & 0 \\ 16 & 4 & 1 \end{pmatrix}$  and I be the identity matrix of order 3. If  $Q = \begin{pmatrix} q_{ij} \end{pmatrix}$  is a matrix such that  $P^{50} - Q = I$ , then  $\frac{q_{31} + q_{32}}{q_{21}}$  equals (JEEAdv.2016)