## Solution 11.16.3.4

## Aditya Vikram Singh\*

**Question 4** A card is selected from a pack of 52 cards

- (a) How many points are there in the sample space?
- (b) Calculate the probability that the cards is an ace of spades.
- (c) Calculate the probability that the card is (i) an ace (ii)black card.

**Solution:** S is a sample space of given cards, Let the random variables(r.v), where X,Y and Z are uniformly distributed r.v's.

TABLE 3
RANDOM VARIABLE AND PROBABILITY TABLE

Random independent variable	value of R.V
X(denotes colour)	1,2
Y(denotes type of card)	1,2,3,4
Z(denotes value of card chosen)	$1 \le Z \le 13$

$$\Pr(X) = \frac{26}{52} = \frac{1}{2} \tag{1}$$

$$\Pr(Y) = \frac{13}{52} = \frac{1}{4} \tag{2}$$

$$\Pr(Z) = \frac{4}{52} = \frac{1}{13} \tag{3}$$

- (a) The number of sample space points is 52
- (b)

$$Pr(Y = 1, Z = 1) = Pr(Y = 1) Pr(Z = 1)$$
 (5)

$$= \left(\frac{1}{4}\right) \left(\frac{1}{13}\right) \tag{6}$$

(4)

$$=\frac{1}{52}\tag{7}$$

\*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All content in this manual is released under GNU GPL. Free and open source.

(c) The probability when the card choosen is,

(i) an ace

$$\Pr(Z=1) = \frac{1}{13}.$$
 (8)

(ii) black card

$$\Pr(X = 1) = \frac{1}{2}.\tag{9}$$