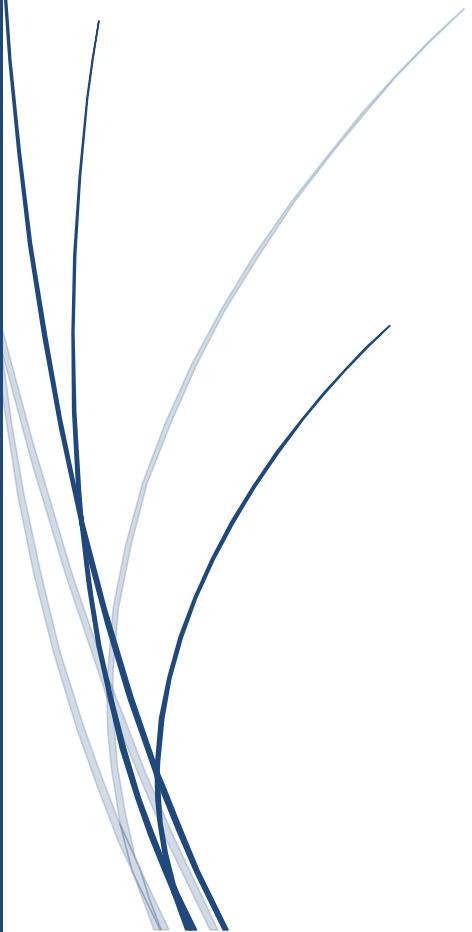




[Date]

# Complete placement course

Doubly linked list

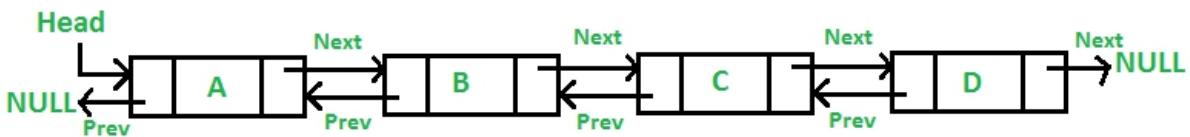


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# Doubly Linked List

## introduction and Insertion

A Doubly Linked List (DLL) contains an extra pointer, typically called *previous pointer*, together with next pointer and data which are there in singly linked list.



Following is representation of a DLL node in C language.

```
/* Node of a doubly linked list */
struct Node {
    int data;
    struct Node* next; // Pointer to next node in DLL
    struct Node* prev; // Pointer to previous node in DLL
};
```

### Advantages over singly linked list

- 1) A DLL can be traversed in both forward and backward direction.
- 2) The delete operation in DLL is more efficient if pointer to the node to be deleted is given.
- 3) We can quickly insert a new node before a given node.  
In singly linked list, to delete a node, pointer to the previous node is needed. To get this previous node, sometimes the list is traversed. In DLL, we can get the previous node using previous pointer.

### Disadvantages over singly linked list

- 1) Every node of DLL Require extra space for an previous pointer. It is possible to implement DLL with single pointer though (See [this](#) and [this](#)).

**2) All operations require an extra pointer previous to be maintained.** For example, in insertion, we need to modify previous pointers together with next pointers. For example in following functions for insertions at different positions, we need 1 or 2 extra steps to set previous pointer.

## Insertion

A node can be added in four ways

- 1) At the front of the DLL
- 2) After a given node.
- 3) At the end of the DLL
- 4) Before a given node.

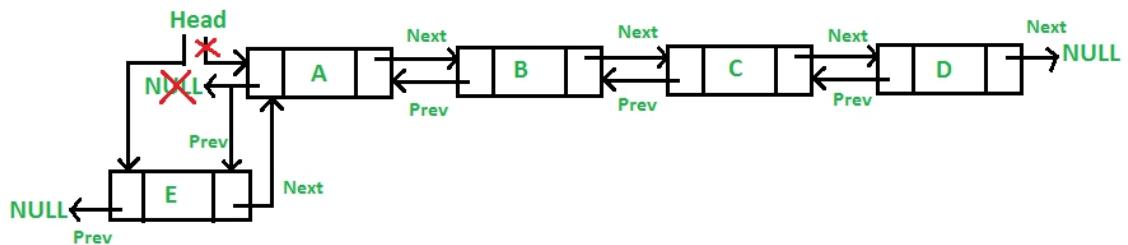
### 1) Add a node at the front: (A 5 steps process)

The new node is always added before the head of the given Linked List. And newly added node becomes the new head of DLL.

For example if the given Linked List is 10152025 and we add an item 5 at the front, then the Linked List becomes 510152025.

Let us call the function that adds at the front of the list is push().

The push() must receive a pointer to the head pointer, because push must change the head pointer to point to the new node



Following are the 5 steps to add node at the front.

```

/* Given a reference (pointer to pointer) to the head of a list
   and an int, inserts a new node on the front of the list. */
void push(struct Node** head_ref, int new_data)
{
    /* 1. allocate node */
    struct Node* new_node = (struct Node*)malloc(sizeof(struct Node));

    /* 2. put in the data */
    new_node->data = new_data;

    /* 3. Make next of new node as head and previous as NULL */
    new_node->next = (*head_ref);
    new_node->prev = NULL;

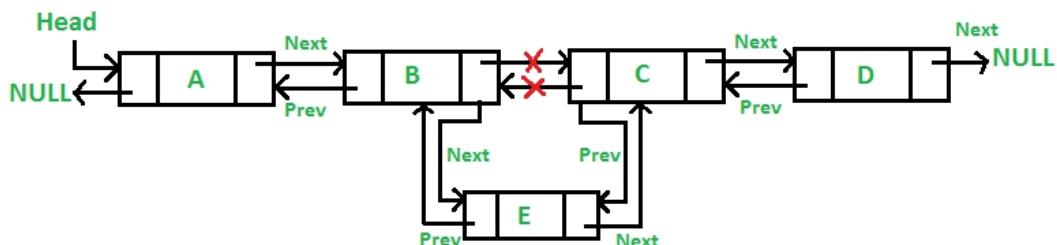
    /* 4. change prev of head node to new node */
    if ((*head_ref) != NULL)
        (*head_ref)->prev = new_node;

    /* 5. move the head to point to the new node */
    (*head_ref) = new_node;
}

```

## 2) Add a node after a given node.: (A 7 steps process)

We are given pointer to a node as `prev_node`, and the new node is inserted after the given node.



```

/* Given a node as prev_node, insert a new node after the given node */
void insertAfter(struct Node* prev_node, int new_data)
{
    /*1. check if the given prev_node is NULL */
    if (prev_node == NULL) {
        printf("the given previous node cannot be NULL");
        return;
    }

    /* 2. allocate new node */
    struct Node* new_node = (struct Node*)malloc(sizeof(struct Node));

    /* 3. put in the data */
    new_node->data = new_data;

    /* 4. Make next of new node as next of prev_node */
    new_node->next = prev_node->next;

    /* 5. Make the next of prev_node as new_node */
    prev_node->next = new_node;

    /* 6. Make prev_node as previous of new_node */
    new_node->prev = prev_node;

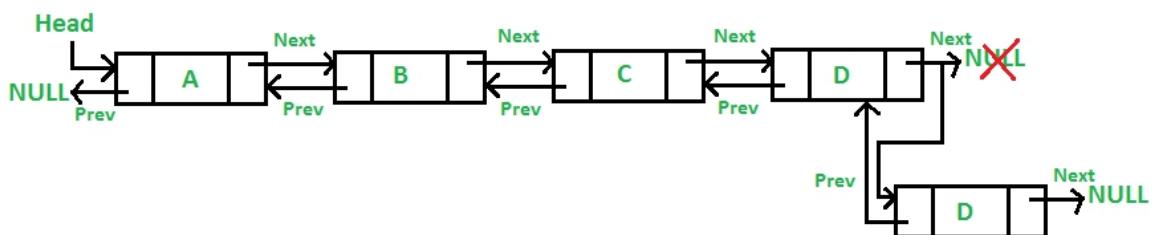
    /* 7. Change previous of new_node's next node */
    if (new_node->next != NULL)
        new_node->next->prev = new_node;
}

```

### 3) Add a node at the end: (7 steps process)

The new node is always added after the last node of the given Linked List. For example if the given DLL is 510152025 and we add an item 30 at the end, then the DLL becomes 51015202530.

Since a Linked List is typically represented by the head of it, we have to traverse the list till end and then change the next of last node to new node.



```

1  /* Given a reference (pointer to pointer) to the head
2   of a DLL and an int, appends a new node at the end */
3   void append(struct Node** head_ref, int new_data)
4  {
5      /* 1. allocate node */
6      struct Node* new_node = (struct Node*)malloc(sizeof(struct Node));
7      struct Node* last = *head_ref; /* used in step 5*/
8      /* 2. put in the data */
9      new_node->data = new_data;
10     /* 3. This new node is going to be the last node, so
11      make next of it as NULL*/
12     new_node->next = NULL;
13     /* 4. If the Linked List is empty, then make the new
14      node as head */
15     if (*head_ref == NULL) {
16         new_node->prev = NULL;
17         *head_ref = new_node;
18         return;
19     }
20     /* 5. Else traverse till the last node */
21     while (last->next != NULL)
22         last = last->next;
23     /* 6. Change the next of last node */
24     last->next = new_node;
25     /* 7. Make last node as previous of new node */
26     new_node->prev = last;
27     return;
28 }
29

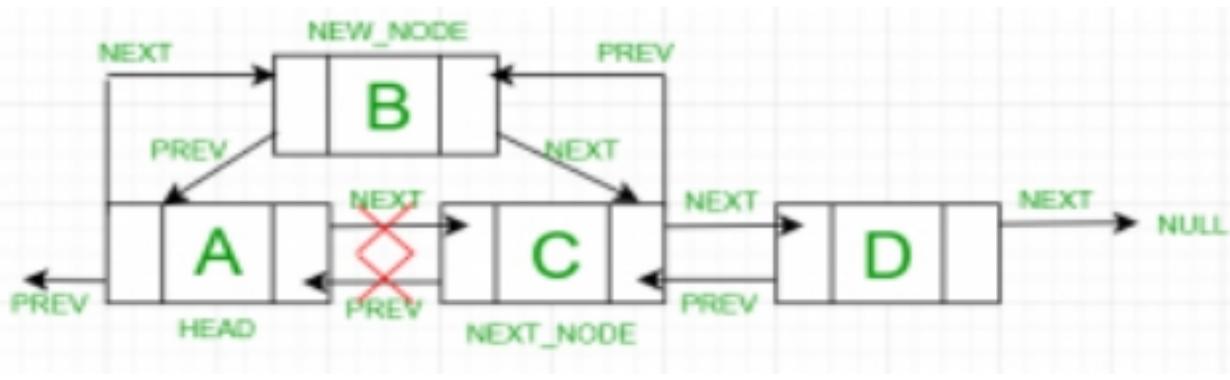
```

#### 4) Add a node before a given node:

##### Steps

Let the pointer to this given node be `next_node` and the data of the new node to be added as `new_data`.

1. Check if the `next_node` is `NULL` or not. If it's `NULL`, return from the function because any new node can not be added before a `NULL`
2. Allocate memory for the new node, let it be called `new_node`
3. Set `new_node->data = new_data`
4. Set the previous pointer of this `new_node` as the previous node of the `next_node`, `new_node->prev = next_node->prev`
5. Set the previous pointer of the `next_node` as the `new_node`, `next_node->prev = new_node`
6. Set the next pointer of this `new_node` as the `next_node`, `new_node->next = next_node;`
7. If the previous node of the `new_node` is not `NULL`, then set the next pointer of this previous node as `new_node`, `new_node->prev->next = new_node`
8. Else, if the `prev` of `new_node` is `NULL`, it will be the new head node. So, make `(*head_ref) = new_node`.



Below is the implementation of the above approach:

```

1 // A complete working C program to demonstrate all
2 // insertion before a given node
3 #include <stdio.h>
4 #include <stdlib.h>
5
6 // A linked list node
7 struct Node {
8     int data;
9     struct Node* next;
10    struct Node* prev;
11};
12
13 /* Given a reference (pointer to pointer) to the head of a
14 list and an int, inserts a new node on the front of the
15 list. */
16 void push(struct Node** head_ref, int new_data)
17 {
18     struct Node* new_node
19         = (struct Node*)malloc(sizeof(struct Node));
20
21     new_node->data = new_data;
22
23     new_node->next = (*head_ref);
24     new_node->prev = NULL;
25
26     if ((*head_ref) != NULL)
27         (*head_ref)->prev = new_node;
28
29     (*head_ref) = new_node;
30 }
31
32 /* Given a node as next_node, insert a new node before the
33 * given node */
34 void insertBefore(struct Node** head_ref,
35                  struct Node* next_node, int new_data)
36 {
37     /*1. check if the given next_node is NULL */
38     if (next_node == NULL) {
39         printf("the given next node cannot be NULL");
40         return;
41     }
42 }
```

```

43  /* 2. allocate new node */
44  struct Node* new_node
45      = (struct Node*)malloc(sizeof(struct Node));
46
47  /* 3. put in the data */
48  new_node->data = new_data;
49
50  /* 4. Make prev of new node as prev of next_node */
51  new_node->prev = next_node->prev;
52
53  /* 5. Make the prev of next_node as new_node */
54  next_node->prev = new_node;
55
56  /* 6. Make next_node as next of new_node */
57  new_node->next = next_node;
58
59  /* 7. Change next of new_node's previous node */
60  if (new_node->prev != NULL)
61      new_node->prev->next = new_node;
62  /* 8. If the prev of new_node is NULL, it will be
63  the new head node */
64  else
65      (*head_ref) = new_node;
66 }
67
68 // This function prints contents of linked list starting
69 // from the given node
70 void printList(struct Node* node)
71 {
72     struct Node* last;
73     printf("\nTraversal in forward direction \n");
74     while (node != NULL) {
75         printf(" %d ", node->data);
76         last = node;
77         node = node->next;
78     }
79
80     printf("\nTraversal in reverse direction \n");
81     while (last != NULL) {
82         printf(" %d ", last->data);
83         last = last->prev;
84     }
85 }
```

```
86
87 /* Driver program to test above functions*/
88 int main()
89 {
90     /* Start with the empty list */
91     struct Node* head = NULL;
92     push(&head, 7);
93
94     push(&head, 1);
95
96     push(&head, 4);
97
98     // Insert 8, before 1. So linked list becomes
99     // 4->8->1->7->NULL
100    insertBefore(&head, head->next, 8);
101
102    printf("Created DLL is: ");
103    printList(head);
104
105    getchar();
106    return 0;
107 }
```

#### Output:

```
Created DLL is:
Traversal in forward direction
4 8 1 7
Traversal in reverse direction
7 1 8 4
```

#### A complete working program to test above functions.

Following is complete program to test above functions.

```
1 // A complete working C++ program to
2 // demonstrate all insertion methods
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 // A linked list node
7 class Node
8 {
9     public:
10     int data;
11     Node* next;
12     Node* prev;
13 };
14
15 /* Given a reference (pointer to pointer)
16 to the head of a list
17 and an int, inserts a new node on the
18 front of the list. */
19 void push(Node** head_ref, int new_data)
20 {
21     /* 1. allocate node */
22     Node* new_node = new Node();
23
24     /* 2. put in the data */
25     new_node->data = new_data;
26
27     /* 3. Make next of new node as head
28     and previous as NULL */
29     new_node->next = (*head_ref);
30     new_node->prev = NULL;
31
32     /* 4. change prev of head node to new node */
33     if ((*head_ref) != NULL)
34         (*head_ref)->prev = new_node;
35
36     /* 5. move the head to point to the new node */
37     (*head_ref) = new_node;
38 }
39
40 /* Given a node as prev_node, insert
41 a new node after the given node */
42 void insertAfter(Node* prev_node, int new_data)
43 {
44     /*1. check if the given prev_node is NULL */
45     if (prev_node == NULL)
46     {
47         cout<<"the given previous node cannot be NULL":
```

```
48     return;
49 }
50
51 /* 2. allocate new node */
52 Node* new_node = new Node();
53
54 /* 3. put in the data */
55 new_node->data = new_data;
56
57 /* 4. Make next of new node as next of prev_node */
58 new_node->next = prev_node->next;
59
60 /* 5. Make the next of prev_node as new_node */
61 prev_node->next = new_node;
62
63 /* 6. Make prev_node as previous of new_node */
64 new_node->prev = prev_node;
65
66 /* 7. Change previous of new_node's next node */
67 if (new_node->next != NULL)
68     new_node->next->prev = new_node;
69 }
70
71 /* Given a reference (pointer to pointer) to the head
72 of a DLL and an int, appends a new node at the end */
73 void append(Node** head_ref, int new_data)
74 {
75     /* 1. allocate node */
76     Node* new_node = new Node();
77
78     Node* last = *head_ref; /* used in step 5*/
79
80     /* 2. put in the data */
81     new_node->data = new_data;
82
83     /* 3. This new node is going to be the last node, so
84         make next of it as NULL*/
85     new_node->next = NULL;
86
87     /* 4. If the Linked List is empty, then make the new
88         node as head */
89     if (*head_ref == NULL)
90     {
91         new_node->prev = NULL;
92         *head_ref = new_node;
93         return;
```

```
94     }
95
96     /* 5. Else traverse till the last node */
97     while (last->next != NULL)
98         last = last->next;
99
100    /* 6. Change the next of last node */
101    last->next = new_node;
102
103    /* 7. Make last node as previous of new node */
104    new_node->prev = last;
105
106    return;
107}
108
109 // This function prints contents of
110 // linked list starting from the given node
111 void printList(Node* node)
112{
113    Node* last;
114    cout<<"\nTraversal in forward direction \n";
115    while (node != NULL)
116    {
117        cout<<" " << node->data << " ";
118        last = node;
119        node = node->next;
120    }
121
122    cout<<"\nTraversal in reverse direction \n";
123    while (last != NULL)
124    {
125        cout<<" " << last->data << " ";
126        last = last->prev;
127    }
128}
129
130 /* Driver program to test above functions*/
131 int main()
132{
133    /* Start with the empty list */
134    Node* head = NULL;
135
136    // Insert 6. So linked list becomes 6->NULL
137    append(&head, 6);
138}
```

```

139     // Insert 7 at the beginning. So
140     // linked list becomes 7->6->NULL
141     push(&head, 7);
142
143     // Insert 1 at the beginning. So
144     // linked list becomes 1->7->6->NULL
145     push(&head, 1);
146
147     // Insert 4 at the end. So linked
148     // list becomes 1->7->6->4->NULL
149     append(&head, 4);
150
151     // Insert 8, after 7. So linked
152     // list becomes 1->7->8->6->4->NULL
153     insertAfter(head->next, 8);
154
155     cout << "Created DLL is: ";
156     printList(head);
157
158     return 0;
159 }
```

### Output:

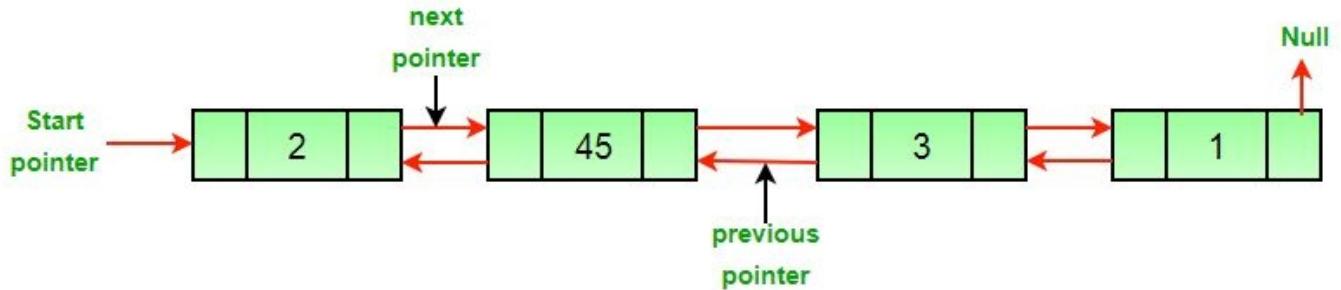
```

Created DLL is:
Traversal in forward direction
1 7 8 6 4
Traversal in reverse direction
4 6 8 7 1
```

## Delete a node in a Doubly Linked List

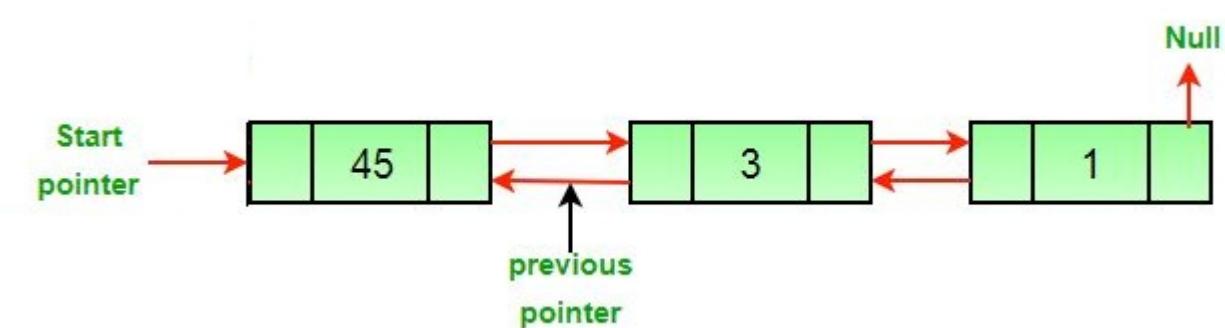
Write a function to delete a given node in a doubly-linked list.

Original Doubly Linked List

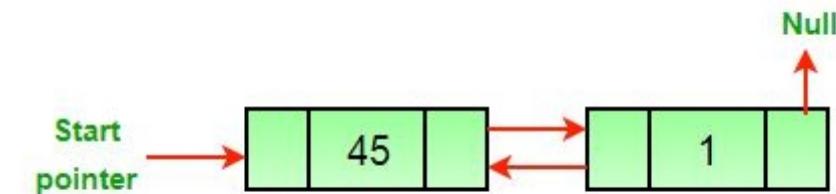


**Approach:** The deletion of a node in a doubly-linked list can be divided into three main categories:

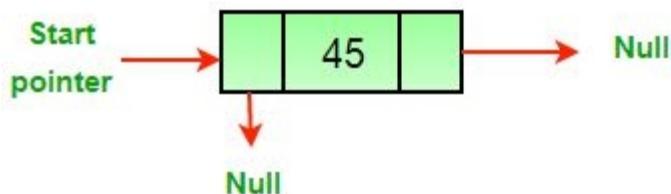
- After the deletion of the head node.



- After the deletion of the middle node.

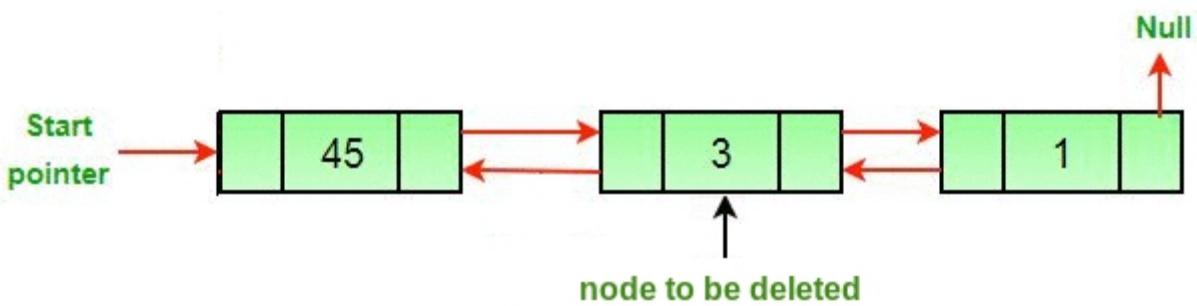


- After the deletion of the last node.



All three mentioned cases can be handled in two steps if the pointer of the node to be deleted and the head pointer is known.

1. If the node to be deleted is the head node then make the next node as head.
2. If a node is deleted, connect the next and previous node of the deleted node.



## Algorithm

- Let the node to be deleted be *del*.
- If node to be deleted is head node, then change the head pointer to next current head.

```
if headnode == del then
    headnode = del.nextNode
```

- Set *next* of previous to *del*, if previous to *del* exists.

```
if del.nextNode != none
    del.nextNode.previousNode = del.previousNode
```

- Set *prev* of next to *del*, if next to *del* exists.

```
if del.previousNode != none
    del.previousNode.nextNode = del.next
```

## Complexity Analysis:

- Time Complexity:** O(1).  
Since traversal of the linked list is not required so the time complexity is constant.
- Space Complexity:** O(1).  
As no extra space is required, so the space complexity is constant.

```
1 // C++ program to delete a node from
2 // Doubly Linked List
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 /* a node of the doubly linked list */
7 class Node
8 {
9     public:
10    int data;
11    Node* next;
12    Node* prev;
13 };
14
15 /* Function to delete a node in a Doubly Linked List.
16 head_ref --> pointer to head node pointer.
17 del --> pointer to node to be deleted. */
18 void deleteNode(Node** head_ref, Node* del)
19 {
20     /* base case */
21     if (*head_ref == NULL || del == NULL)
22         return;
23
24     /* If node to be deleted is head node */
25     if (*head_ref == del)
26         *head_ref = del->next;
27
28     /* Change next only if node to be
29      deleted is NOT the last node */
30     if (del->next != NULL)
31         del->next->prev = del->prev;
32
33     /* Change prev only if node to be
34      deleted is NOT the first node */
35     if (del->prev != NULL)
36         del->prev->next = del->next;
37
38     /* Finally, free the memory occupied by del*/
39     free(del);
40     return;
41 }
42
43 /* UTILITY FUNCTIONS */
44 /* Function to insert a node at the
45 beginning of the Doubly Linked List */
46 void push(Node** head_ref, int new_data)
47 {
```

```

48     /* allocate node */
49     Node* new_node = new Node();
50
51     /* put in the data */
52     new_node->data = new_data;
53
54     /* since we are adding at the beginning,
55      prev is always NULL */
56     new_node->prev = NULL;
57
58     /* link the old list off the new node */
59     new_node->next = (*head_ref);
60
61     /* change prev of head node to new node */
62     if ((*head_ref) != NULL)
63         (*head_ref)->prev = new_node;
64
65     /* move the head to point to the new node */
66     (*head_ref) = new_node;
67 }
68
69 /* Function to print nodes in a given doubly linked list
70 This function is same as printList() of singly linked list */
71 void printList(Node* node)
72 {
73     while (node != NULL)
74     {
75         cout << node->data << " ";
76         node = node->next;
77     }
78 }
79
80 /* Driver code*/
81 int main()
82 {
83     /* Start with the empty list */
84     Node* head = NULL;
85
86     /* Let us create the doubly linked list 10<->8<->4<->2 */
87     push(&head, 2);
88     push(&head, 4);
89     push(&head, 8);
90     push(&head, 10);
91
92     cout << "Original Linked list ";
93     printList(head);
94
95     /* delete nodes from the doubly linked list */
96     deleteNode(&head, head); /*delete first node*/
97     deleteNode(&head, head->next); /*delete middle node*/
98     deleteNode(&head, head->next); /*delete last node*/
99
100    /* Modified linked list will be NULL<->8<->NULL */
101    cout << "\nModified Linked list ";
102    printList(head);
103
104    return 0;
105 }
```

## Output:

```
Original Linked list 10 8 4 2
Modified Linked list 8
```

# Reverse a Doubly Linked List

Here is a simple method for reversing a Doubly Linked List. All we need to do is swap prev and next pointers for all nodes, change prev of the head (or start) and change the head pointer in the end.

```
1  /* C++ program to reverse a doubly linked list */
2  #include <bits/stdc++.h>
3  using namespace std;
4
5  /* a node of the doubly linked list */
6  class Node
7  {
8      public:
9      int data;
10     Node *next;
11     Node *prev;
12 };
13
14 /* Function to reverse a Doubly Linked List */
15 void reverse(Node **head_ref)
16 {
17     Node *temp = NULL;
18     Node *current = *head_ref;
19
20     /* swap next and prev for all nodes of
21      doubly linked list */
22     while (current != NULL)
23     {
24         temp = current->prev;
25         current->prev = current->next;
26         current->next = temp;
27         current = current->prev;
28     }
29
30     /* Before changing the head, check for the cases like empty
31      list and list with only one node */
32     if(temp != NULL )
33         *head_ref = temp->prev;
34 }
```

```
35
36
37
38 /* UTILITY FUNCTIONS */
39 /* Function to insert a node at the
40 begining of the Doubly Linked List */
41 void push(Node** head_ref, int new_data)
42 {
43     /* allocate node */
44     Node* new_node = new Node();
45
46     /* put in the data */
47     new_node->data = new_data;
48
49     /* since we are adding at the beginning,
50     prev is always NULL */
51     new_node->prev = NULL;
52
53     /* link the old list off the new node */
54     new_node->next = (*head_ref);
55
56     /* change prev of head node to new node */
57     if((*head_ref) != NULL)
58         (*head_ref)->prev = new_node ;
59
60     /* move the head to point to the new node */
61     (*head_ref) = new_node;
62 }
63
64 /* Function to print nodes in a given doubly linked list
65 This function is same as printList() of singly linked list */
66 void printList(Node *node)
67 {
68     while(node != NULL)
69     {
70         cout << node->data << " ";
71         node = node->next;
72     }
73 }
74
75 /* Driver code */
76 int main()
77 {
78     /* Start with the empty list */
79     Node* head = NULL;
```

```

80
81     /* Let us create a sorted linked list to test the functions
82     Created linked list will be 10->8->4->2 */
83     push(&head, 2);
84     push(&head, 4);
85     push(&head, 8);
86     push(&head, 10);
87
88     cout << "Original Linked list" << endl;
89     printList(head);
90
91     /* Reverse doubly linked list */
92     reverse(&head);
93
94     cout << "\nReversed Linked list" << endl;
95     printList(head);
96
97     return 0;
98 }
99

```

### Output:

```

Original linked list
10 8 4 2
The reversed Linked List is
2 4 8 10

```

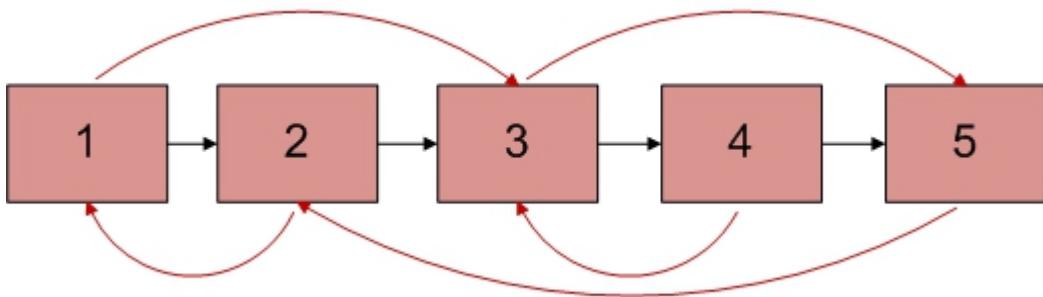
**Time Complexity:**  $O(N)$ , where  $N$  denotes the number of nodes in the doubly linked list.  
**Auxiliary Space:**  $O(1)$

## Clone a linked list with next and random pointer

You are given a Double Link List with one pointer of each node pointing to the next node just like in a single link list. The second pointer however CAN point to any node in the list and not just the previous node. Now write a program in  $O(n)$  time to duplicate this list.

That is, write a program which will create a copy of this list.

Let us call the second pointer as arbit pointer as it can point to any arbitrary node in the linked list.



### Uses Constant Extra Space

- 1) Create the copy of node 1 and insert it between node 1 & node 2 in original Linked List, create the copy of 2 and insert it between 2 & 3.. Continue in this fashion, add the copy of N afte the Nth node
- 2) Now copy the arbitrary link in this fashion

```
original->next->arbitrary = original->arbitrary->next; /*TRAVERSE  
TWO NODES*/
```

This works because `original->next` is nothing but copy of `original` and `Original->arbitrary->next` is nothing but copy of `arbitrary`.

- 3) Now restore the original and copy linked lists in this fashion in a single loop.

```
original->next = original->next->next;  
copy->next = copy->next->next;
```

- 4) Make sure that last element of `original->next` is `NULL`.

Time Complexity:  $O(n)$

Auxiliary Space:  $O(1)$

```
1 // C++ program to clone a linked list with next
2 // and arbit pointers in O(n) time
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 // Structure of linked list Node
7 struct Node
8 {
9     int data;
10    Node *next,*random;
11    Node(int x)
12    {
13        data = x;
14        next = random = NULL;
15    }
16};
17
18 // Utility function to print the list.
19 void print(Node *start)
20 {
21     Node *ptr = start;
22     while (ptr)
23     {
24         cout << "Data = " << ptr->data << ", Random = "
25             << ptr->random->data << endl;
26         ptr = ptr->next;
27     }
28 }
29
30 // This function clones a given linked list
31 // in O(1) space
32 Node* clone(Node *start)
33 {
34     Node* curr = start, *temp;
35
36     // insert additional node after
37     // every node of original list
38     while (curr)
39     {
40         temp = curr->next;
41
42         // Inserting node
43         curr->next = new Node(curr->data);
44         curr->next->next = temp;
45         curr = temp;
46     }
47 }
```

```
48     curr = start;
49
50     // adjust the random pointers of the
51     // newly added nodes
52     while (curr)
53     {
54         if(curr->next)
55             curr->next->random = curr->random ?
56                                         curr->random->next : curr->random;
57
58         // move to the next newly added node by
59         // skipping an original node
60         curr = curr->next?curr->next->next:curr->next;
61     }
62
63     Node* original = start, *copy = start->next;
64
65     // save the start of copied linked list
66     temp = copy;
67
68     // now separate the original list and copied list
69     while (original && copy)
70     {
71         original->next =
72             original->next? original->next->next : original->next;
73
74         copy->next = copy->next?copy->next->next:copy->next;
75         original = original->next;
76         copy = copy->next;
77     }
78
79     return temp;
80 }
81
82 // Driver code
83 int main()
84 {
85     Node* start = new Node(1);
86     start->next = new Node(2);
87     start->next->next = new Node(3);
88     start->next->next->next = new Node(4);
89     start->next->next->next->next = new Node(5);
90
91     // 1's random points to 3
92     start->random = start->next->next;
93 }
```

```
94     // 2's random points to 1
95     start->next->random = start;
96
97     // 3's and 4's random points to 5
98     start->next->next->random =
99         start->next->next->next->next;
100    start->next->next->next->random =
101        start->next->next->next->next;
102
103    // 5's random points to 2
104    start->next->next->next->next->random =
105        start->next;
106
107    cout << "Original list : \n";
108    print(start);
109
110    cout << "\nCloned list : \n";
111    Node *cloned_list = clone(start);
112    print(cloned_list);
113
114    return 0;
115 }
```

## Output

```
Original list :
Data = 1, Random = 3
Data = 2, Random = 1
Data = 3, Random = 5
Data = 4, Random = 5
Data = 5, Random = 2

Cloned list :
Data = 1, Random = 3
Data = 2, Random = 1
Data = 3, Random = 5
Data = 4, Random = 5
Data = 5, Random = 2
```

QuickSort on  
Doubly Linked  
List

Following is a typical recursive implementation of quick sort for arrays. The implementation uses last element as pivot.

```
/* A typical recursive implementation of Quicksort for array*/\n\n/* This function takes last element as pivot, places the pivot element at its\n   correct position in sorted array, and places all smaller (smaller than\n   pivot) to left of pivot and all greater elements to right of pivot */\nint partition (int arr[], int l, int h)\n{\n    int x = arr[h];\n    int i = (l - 1);\n\n    for (int j = l; j <= h- 1; j++)\n    {\n        if (arr[j] <= x)\n        {\n            i++;\n            swap (&arr[i], &arr[j]);\n        }\n    }\n    swap (&arr[i + 1], &arr[h]);\n    return (i + 1);\n}\n\n/* A[] --> Array to be sorted, l --> Starting index, h --> Ending index */\nvoid quickSort(int A[], int l, int h)\n{\n    if (l < h)\n    {\n        int p = partition(A, l, h); /* Partitioning index */\n        quickSort(A, l, p - 1);\n        quickSort(A, p + 1, h);\n    }\n}
```



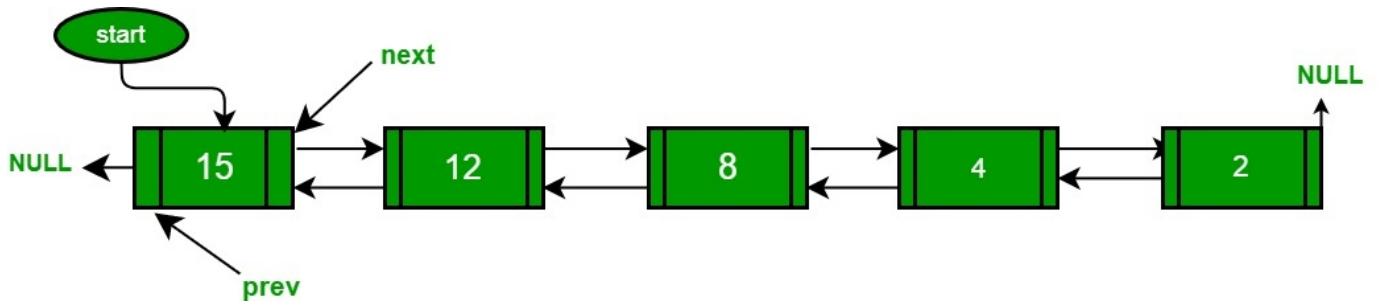
## Can we use the same algorithm for Linked List?

Following is C++ implementation for the doubly linked list. The idea is simple, we first find out pointer to the last node.

Once we have a pointer to the last node, we can recursively sort the linked list using pointers to first and last nodes of a linked list, similar to the above recursive function where we pass indexes of first and last array elements.

The partition function for a linked list is also similar to partition for arrays. Instead of returning index of the pivot element, it returns a pointer to the pivot element.

In the following implementation, quickSort() is just a wrapper function, the main recursive function is \_quickSort() which is similar to quickSort() for array implementation.



```

1 // A C++ program to sort a linked list using Quicksort
2 #include <bits/stdc++.h>
3 using namespace std;
4
5 /* a node of the doubly linked list */
6 class Node
7 {
8     public:
9         int data;
10        Node *next;
11        Node *prev;
12 };
13
14 /* A utility function to swap two elements */
15 void swap ( int* a, int* b )
16 { int t = *a; *a = *b; *b = t; }
17
18 // A utility function to find
19 // last node of linked list
20 Node *lastNode(Node *root)
21 {
22     while (root && root->next)
23         root = root->next;
24     return root;
25 }
26
27 /* Considers last element as pivot,
28 places the pivot element at its
29 correct position in sorted array,
30 and places all smaller (smaller than
31 pivot) to left of pivot and all greater
32 elements to right of pivot */
33 Node* partition(Node *l, Node *h)
34 {
35     // set pivot as h element
36     int x = h->data;
37
38     // similar to i = l-1 for array implementation
39     Node *i = l->prev;
40
41     // Similar to "for (int j = l; j <= h- 1; j++)"
42     for (Node *j = l; j != h; j = j->next)
43     {
44         if (j->data <= x)
45         {
46             // Similar to i++ for array
47             i = (i == NULL)? l : i->next;

```

```
48         swap(&(i->data), &(j->data));
49     }
50 }
51 i = (i == NULL)? l : i->next; // Similar to i++
52 swap(&(i->data), &(h->data));
53 return i;
54 }
55 }
56
57 /* A recursive implementation
58 of quicksort for linked list */
59 void _quickSort(Node* l, Node *h)
60 {
61     if (h != NULL && l != h && l != h->next)
62     {
63         Node *p = partition(l, h);
64         _quickSort(l, p->prev);
65         _quickSort(p->next, h);
66     }
67 }
68
69 // The main function to sort a linked list.
70 // It mainly calls _quickSort()
71 void quickSort(Node *head)
72 {
73     // Find last node
74     Node *h = lastNode(head);
75
76     // Call the recursive QuickSort
77     _quickSort(head, h);
78 }
79
80 // A utility function to print contents of arr
81 void printList(Node *head)
82 {
83     while (head)
84     {
85         cout << head->data << " ";
86         head = head->next;
87     }
88     cout << endl;
89 }
90
91 /* Function to insert a node at the
92 begining of the Doubly Linked List */
93 void push(Node** head_ref, int new_data)
```

```

94  {
95      Node* new_node = new Node; /* allocate node */
96      new_node->data = new_data;
97
98      /* since we are adding at the
99      beginning, prev is always NULL */
100     new_node->prev = NULL;
101
102     /* link the old list off the new node */
103     new_node->next = (*head_ref);
104
105     /* change prev of head node to new node */
106     if ((*head_ref) != NULL) (*head_ref)->prev = new_node ;
107
108     /* move the head to point to the new node */
109     (*head_ref) = new_node;
110 }
111
112 /* Driver code */
113 int main()
114 {
115     Node *a = NULL;
116     push(&a, 5);
117     push(&a, 20);
118     push(&a, 4);
119     push(&a, 3);
120     push(&a, 30);
121
122     cout << "Linked List before sorting \n";
123     printList(a);
124
125     quickSort(a);
126
127     cout << "Linked List after sorting \n";
128     printList(a);
129
130     return 0;
131 }
```

## Output

```

Linked List before sorting
30 3 4 20 5
Linked List after sorting
3 4 5 20 30
```

# Swap Kth node from beginning with Kth node from end in a Linked List

Given a singly linked list, swap kth node from beginning with kth node from end. **Swapping of data is not allowed, only pointers should be changed.** This requirement may be logical in many situations where the linked list data part is huge (For example student details like Name, RollNo, Address, ..etc). The pointers are always fixed (4 bytes for most of the compilers).

**Example:**

**Input:** 1 → 2 → 3 → 4 → 5, K = 2

**Output:** 1 → 4 → 3 → 2 → 5

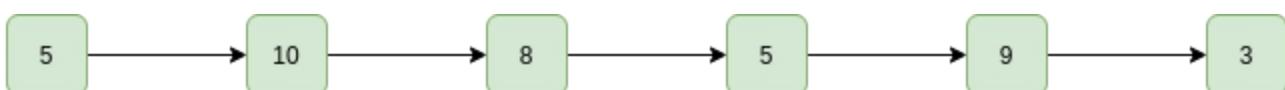
**Explanation:** The 2nd node from 1st is 2 and 2nd node from last is 4, so swap them.

**Input:** 1 → 2 → 3 → 4 → 5, K = 5

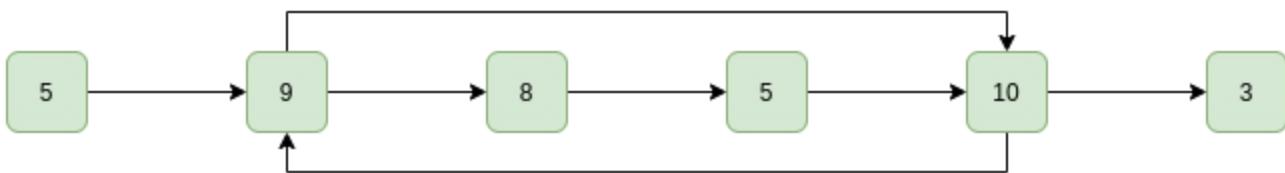
**Output:** 5 → 2 → 3 → 4 → 1

**Explanation:** The 5th node from 1st is 5 and 5th node from last is 1, so swap them.

**Illustration:**



ORIGINAL LIST      K = 2



NEW LIST

## Approach

: The idea is very simple find the k th node from the start and the kth node from last is n-k+1 th node from start. Swap both the nodes.

*However there are some corner cases, which must be handled*

1. Y is next to X
2. X is next to Y
3. X and Y are same
4. X and Y don't exist (k is more than number of nodes in linked list)

Below is the implementation of the above approach.

```
1 // A C++ program to swap Kth node
2 // from beginning with kth node from end
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 // A Linked List node
7 struct Node {
8     int data;
9     struct Node* next;
10};
11
12 /* Utility function to insert
13 a node at the beginning */
14 void push(struct Node** head_ref, int new_data)
15{
16    struct Node* new_node
17        = (struct Node*)malloc(
18            sizeof(struct Node));
19    new_node->data = new_data;
20    new_node->next = (*head_ref);
21    (*head_ref) = new_node;
22}
23
24 /* Utility function for displaying linked list */
25 void printList(struct Node* node)
26{
27    while (node != NULL) {
28        cout << node->data << " ";
29        node = node->next;
30    }
31    cout << endl;
32}
33
34 /* Utility function for calculating
35 length of linked list */
36 int countNodes(struct Node* s)
37{
38    int count = 0;
39    while (s != NULL) {
40        count++;
41        s = s->next;
42    }
43    return count;
44}
45
```

```

46 /* Function for swapping kth nodes
47 from both ends of linked list */
48 void swapKth(struct Node** head_ref, int k)
49 {
50     // Count nodes in linked list
51     int n = countNodes(*head_ref);
52
53     // Check if k is valid
54     if (n < k)
55         return;
56
57     // If x (kth node from start) and
58     // y(kth node from end) are same
59     if (2 * k - 1 == n)
60         return;
61
62     // Find the kth node from the beginning of
63     // the linked list. We also find
64     // previous of kth node because we
65     // need to update next pointer of
66     // the previous.
67     Node* x = *head_ref;
68     Node* x_prev = NULL;
69     for (int i = 1; i < k; i++) {
70         x_prev = x;
71         x = x->next;
72     }
73
74     // Similarly, find the kth node from
75     // end and its previous. kth node
76     // from end is (n-k+1)th node from beginning
77     Node* y = *head_ref;
78     Node* y_prev = NULL;
79     for (int i = 1; i < n - k + 1; i++) {
80         y_prev = y;
81         y = y->next;
82     }
83
84     // If x_prev exists, then new next of
85     // it will be y. Consider the case
86     // when y->next is x, in this case,
87     // x_prev and y are same. So the statement
88     // "x_prev->next = y" creates a self loop.
89     // This self loop will be broken
90     // when we change y->next.
91     if (x_prev)

```

```

92     x->next = y;
93
94     // Same thing applies to y_prev
95     if (y_prev)
96         y->next = x;
97
98     // Swap next pointers of x and y.
99     // These statements also break self
100    // loop if x->next is y or y->next is x
101    Node* temp = x->next;
102    x->next = y->next;
103    y->next = temp;
104
105    // Change head pointers when k is 1 or n
106    if (k == 1)
107        *head_ref = y;
108    if (k == n)
109        *head_ref = x;
110 }
111
112 // Driver program to test above functions
113 int main()
114 {
115     // Let us create the following
116     // linked list for testing
117     // 1->2->3->4->5->6->7->8
118     struct Node* head = NULL;
119     for (int i = 8; i >= 1; i--)
120         push(&head, i);
121
122     cout << "Original Linked List: ";
123     printList(head);
124
125     for (int k = 1; k < 9; k++) {
126         swapKth(&head, k);
127         cout << "\nModified List for k = " << k << endl;
128         printList(head);
129     }
130
131     return 0;
132 }
```

## Output:

```
Original Linked List: 1 2 3 4 5 6 7 8
```

```
Modified List for k = 1
```

```
8 2 3 4 5 6 7 1
```

```
Modified List for k = 2
```

```
8 7 3 4 5 6 2 1
```

```
Modified List for k = 3
```

```
8 7 6 4 5 3 2 1
```

```
Modified List for k = 4
```

```
8 7 6 5 4 3 2 1
```

```
Modified List for k = 5
```

```
8 7 6 4 5 3 2 1
```

```
Modified List for k = 6
```

```
8 7 3 4 5 6 2 1
```

```
Modified List for k = 7
```

```
8 2 3 4 5 6 7 1
```

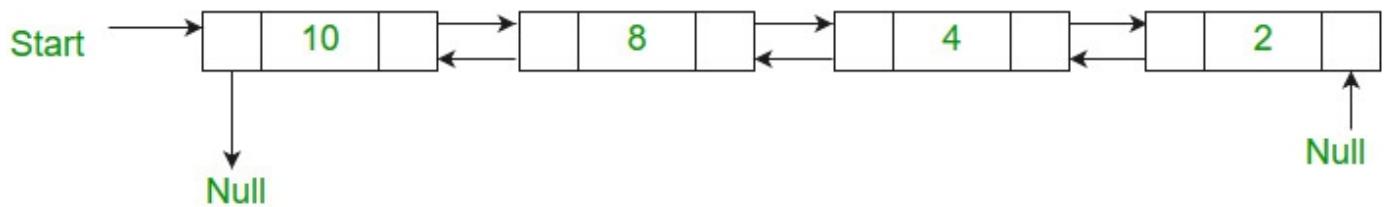
```
Modified List for k = 8
```

```
1 2 3 4 5 6 7 8
```

## Complexity Analysis:

- **Time Complexity:**  $O(n)$ , where  $n$  is the length of the list.  
One traversal of the list is needed.
- **Auxiliary Space:**  $O(1)$ .  
No extra space is required.

# Merge Sort for Doubly Linked List



Below is the implementation of merge sort for doubly linked list.

```
1 // C++ program for merge sort on doubly linked list
2 #include <bits/stdc++.h>
3 using namespace std;
4 class Node
5 {
6     public:
7         int data;
8         Node *next, *prev;
9     };
10
11 Node *split(Node *head);
12
13 // Function to merge two linked lists
14 Node *merge(Node *first, Node *second)
15 {
16     // If first linked list is empty
17     if (!first)
18         return second;
19
20     // If second linked list is empty
21     if (!second)
22         return first;
23
24     // Pick the smaller value
25     if (first->data < second->data)
26     {
27         first->next = merge(first->next, second);
28         first->next->prev = first;
29         first->prev = NULL;
30         return first;
31     }
32     else
33     {
34         second->next = merge(first, second->next);
35         second->next->prev = second;
36         second->prev = NULL;
37         return second;
38     }
39 }
```

```

40
41 // Function to do merge sort
42 Node *mergeSort(Node *head)
43 {
44     if (!head || !head->next)
45         return head;
46     Node *second = split(head);
47
48     // Recur for left and right halves
49     head = mergeSort(head);
50     second = mergeSort(second);
51
52     // Merge the two sorted halves
53     return merge(head,second);
54 }
55
56 // A utility function to insert a new node at the
57 // beginning of doubly linked list
58 void insert(Node **head, int data)
59 {
60     Node *temp = new Node();
61     temp->data = data;
62     temp->next = temp->prev = NULL;
63     if (!(*head))
64         (*head) = temp;
65     else
66     {
67         temp->next = *head;
68         (*head)->prev = temp;
69         (*head) = temp;
70     }
71 }
72
73 // A utility function to print a doubly linked list in
74 // both forward and backward directions
75 void print(Node *head)
76 {
77     Node *temp = head;
78     cout<<"Forward Traversal using next pointer\n";
79     while (head)
80     {
81         cout << head->data << " ";
82         temp = head;
83         head = head->next;
84     }
85     cout << "\nBackward Traversal using prev pointer\n";
86     while (temp)
87     {
88         cout << temp->data << " ";
89         temp = temp->prev;
90     }
91 }
92

```

```

93 // Utility function to swap two integers
94 void swap(int *A, int *B)
95 {
96     int temp = *A;
97     *A = *B;
98     *B = temp;
99 }
100
101 // Split a doubly linked list (DLL) into 2 DLLs of
102 // half sizes
103 Node *split(Node *head)
104 {
105     Node *fast = head, *slow = head;
106     while (fast->next && fast->next->next)
107     {
108         fast = fast->next->next;
109         slow = slow->next;
110     }
111     Node *temp = slow->next;
112     slow->next = NULL;
113     return temp;
114 }
115
116 // Driver program
117 int main(void)
118 {
119     Node *head = NULL;
120     insert(&head, 5);
121     insert(&head, 20);
122     insert(&head, 4);
123     insert(&head, 3);
124     insert(&head, 30);
125     insert(&head, 10);
126     head = mergeSort(head);
127     cout << "Linked List after sorting\n";
128     print(head);
129     return 0;
130 }
131

```

## Output

```

Linked List after sorting
Forward Traversal using next pointer
3 4 5 10 20 30
Backward Traversal using prev pointer
30 20 10 5 4 3

```

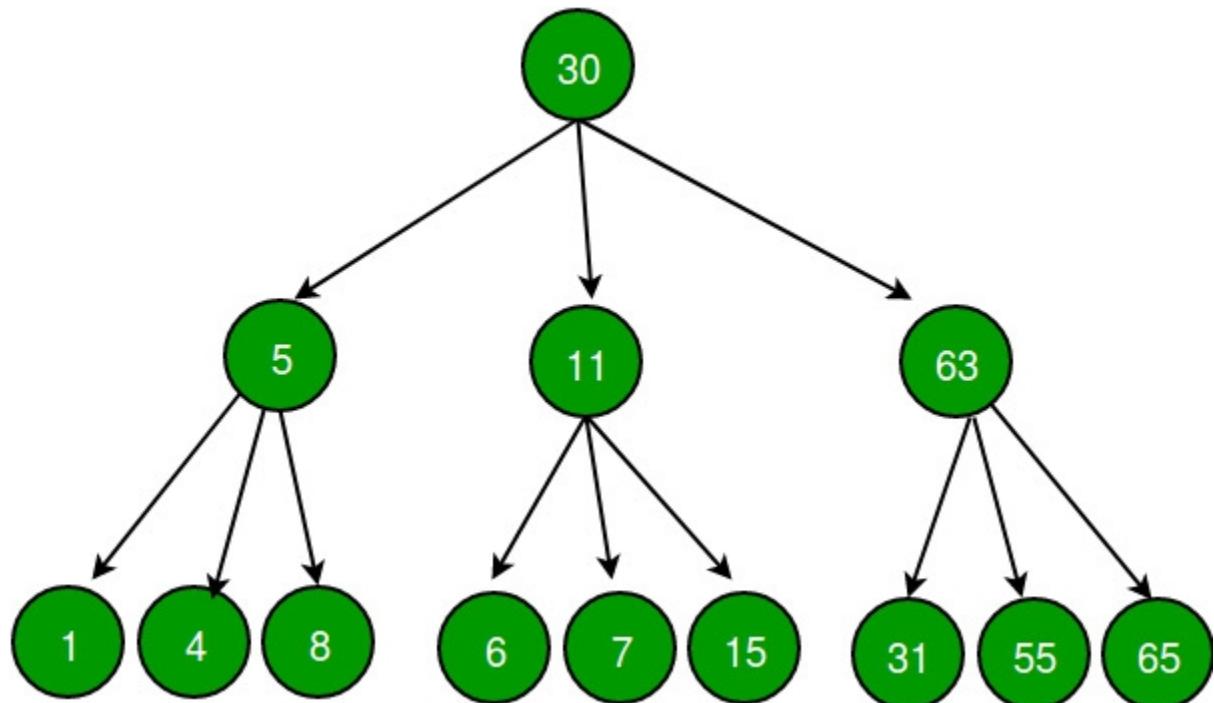
## Create a Doubly Linked List from a Ternary Tree

Given a ternary tree, create a doubly linked list out of it. A ternary tree is just like binary tree but instead of having two nodes, it has three nodes i.e. left, middle, right.

The doubly linked list should holds following properties –

1. Left pointer of ternary tree should act as prev pointer of doubly linked list.
2. Middle pointer of ternary tree should not point to anything.
3. Right pointer of ternary tree should act as next pointer of doubly linked list.
4. Each node of ternary tree is inserted into doubly linked list before its subtrees and for any node, its left child will be inserted first, followed by mid and right child (if any).

For the above example, the linked list formed for below tree should be  
NULL <- 30 <-> 5 <-> 1 <-> 4 <-> 8 <-> 11 <-> 6 <-> 7 <-> 15 <-> 63 <-> 31 <-> 55 <-> 65 -> NULL



The idea is to traverse the tree in preoder fashion similar to binary tree preorder traversal. Here, when we visit a node, we will insert it into [ ] doubly linked list in the end using a tail pointer. That we use to maintain the required insertion order. We then recursively call for left child, middle child and right child in that order.

```
1 // C++ program to create a doubly linked list out
2 // of given a ternary tree.
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 /* A ternary tree */
7 struct Node
8 {
9     int data;
10    struct Node *left, *middle, *right;
11 };
12
13 /* Helper function that allocates a new node with the
14 given data and assign NULL to left, middle and right
15 pointers.*/
16 Node* newNode(int data)
17 {
18     Node* node = new Node;
19     node->data = data;
20     node->left = node->middle = node->right = NULL;
21     return node;
22 }
23
24 /* Utility function that constructs doubly linked list
25 by inserting current node at the end of the doubly
26 linked list by using a tail pointer */
27 void push(Node** tail_ref, Node* node)
28 {
29     // initialize tail pointer
30     if (*tail_ref == NULL)
31     {
32         *tail_ref = node;
33
34         // set left, middle and right child to point
35         // to NULL
36         node->left = node->middle = node->right = NULL;
37
38         return;
39     }
40
41     // insert node in the end using tail pointer
42     (*tail_ref)->right = node;
43
44     // set prev of node
45     node->left = (*tail_ref);
46
47     // set middle and right child to point to NULL
48     node->right = node->middle = NULL;
49
50     // now tail pointer will point to inserted node
51     (*tail_ref) = node;
52 }
53
```

```

54  /* Create a doubly linked list out of given a ternary tree.
55  by traversing the tree in preoder fashion. */
56 Node* TernaryTreeToList(Node* root, Node** head_ref)
57 {
58     // Base case
59     if (root == NULL)
60         return NULL;
61
62     //create a static tail pointer
63     static Node* tail = NULL;
64
65     // store left, middle and right nodes
66     // for future calls.
67     Node* left = root->left;
68     Node* middle = root->middle;
69     Node* right = root->right;
70
71     // set head of the doubly linked list
72     // head will be root of the ternary tree
73     if (*head_ref == NULL)
74         *head_ref = root;
75
76     // push current node in the end of DLL
77     push(&tail, root);
78
79     //recurse for left, middle and right child
80     TernaryTreeToList(left, head_ref);
81     TernaryTreeToList(middle, head_ref);
82     TernaryTreeToList(right, head_ref);
83 }
84
85 // Utility function for printing double linked list.
86 void printList(Node* head)
87 {
88     printf("Created Double Linked list is:\n");
89     while (head)
90     {
91         printf("%d ", head->data);
92         head = head->right;
93     }
94 }
95
96 // Driver program to test above functions
97 int main()
98 {
99     // Construting ternary tree as shown in above figure
100    Node* root = newNode(30);
101
102    root->left = newNode(5);
103    root->middle = newNode(11);
104    root->right = newNode(63);
105

```

```

106     root->left->left = newNode(1);
107     root->left->middle = newNode(4);
108     root->left->right = newNode(8);
109
110     root->middle->left = newNode(6);
111     root->middle->middle = newNode(7);
112     root->middle->right = newNode(15);
113
114     root->right->left = newNode(31);
115     root->right->middle = newNode(55);
116     root->right->right = newNode(65);
117
118     Node* head = NULL;
119
120     TernaryTreeToList(root, &head);
121
122     printList(head);
123
124     return 0;
125 }
```

### Output:

```

Created Double Linked list is:
30 5 1 4 8 11 6 7 15 63 31 55 65
```

## Find pairs with given sum in doubly linked list

Given a sorted doubly linked list of positive distinct elements, the task is to find pairs in a doubly-linked list whose sum is equal to given value  $x$ , without using any extra space?

### Example:

```

Input : head : 1 <-> 2 <-> 4 <-> 5 <-> 6 <-> 8 <-> 9
        x = 7
Output: (6, 1), (5,2)
```

The expected time complexity is  $O(n)$  and auxiliary space is  $O(1)$ .

- A **simple approach** for this problem is to one by one pick each node and find a second element whose sum is equal to x in the remaining list by traversing in the forward direction. The time complexity for this problem will be  $O(n^2)$ , n is the total number of nodes in the doubly linked list. Initialize two pointer variables to find the candidate elements in the sorted doubly linked list. Initialize **first** with the start of the doubly linked list i.e; **first=head** and initialize **second** with the last node of the doubly linked list i.e; **second=last\_node**.
- We initialize **first** and **second** pointers as first and last nodes. Here we don't have random access, so to find the second pointer, we traverse the list to initialize the second.
- If current sum of **first** and **second** is less than x, then we move **first** in forward direction. If current sum of **first** and **second** element is greater than x, then we move **second** in backward direction.
- Loop termination conditions are also different from arrays. The loop terminates when two pointers cross each other (**second->next = first**), or they become the same (**first == second**).
- The case when no pairs are present will be handled by the condition "**first==second**"

```

1 // C++ program to find a pair with given sum x.
2 #include<bits/stdc++.h>
3 using namespace std;
4
5 // structure of node of doubly linked list
6 struct Node
7 {
8     int data;
9     struct Node *next, *prev;
10 };
11
12 // Function to find pair whose sum equal to given value x.
13 void pairSum(struct Node *head, int x)
14 {
15     // Set two pointers, first to the beginning of DLL
16     // and second to the end of DLL.
17     struct Node *first = head;
18     struct Node *second = head;
19     while (second->next != NULL)
20         second = second->next;
21
22     // To track if we find a pair or not
23     bool found = false;
24
25     // The loop terminates when two pointers
26     // cross each other (second->next
27     // == first), or they become same (first == second)
28     while (first != second && second->next != first)
29     {

```

```
31         if ((first->data + second->data) == x)
32     {
33         found = true;
34         cout << "(" << first->data << ", "
35             << second->data << ")" << endl;
36
37         // move first in forward direction
38         first = first->next;
39
40         // move second in backward direction
41         second = second->prev;
42     }
43     else
44     {
45         if ((first->data + second->data) < x)
46             first = first->next;
47         else
48             second = second->prev;
49     }
50 }
51
52 // if pair is not present
53 if (found == false)
54     cout << "No pair found";
55 }
56
57 // A utility function to insert a new node at the
58 // beginning of doubly linked list
59 void insert(struct Node **head, int data)
60 {
61     struct Node *temp = new Node;
62     temp->data = data;
63     temp->next = temp->prev = NULL;
64     if (!(*head))
65         (*head) = temp;
66     else
67     {
68         temp->next = *head;
69         (*head)->prev = temp;
70         (*head) = temp;
71     }
72 }
73
74 // Driver program
75 int main()
```

```

76  {
77      struct Node *head = NULL;
78      insert(&head, 9);
79      insert(&head, 8);
80      insert(&head, 6);
81      insert(&head, 5);
82      insert(&head, 4);
83      insert(&head, 2);
84      insert(&head, 1);
85      int x = 7;
86
87      pairSum(head, x);
88
89      return 0;
90  }

```

**Output:**

```

(1,6)
(2,5)

```

**Time complexity :**  $O(n)$

**Auxiliary space :**  $O(1)$

If linked list is not sorted, then we can sort the list as a first step. But in that case overall time complexity would become  $O(n \log n)$ .

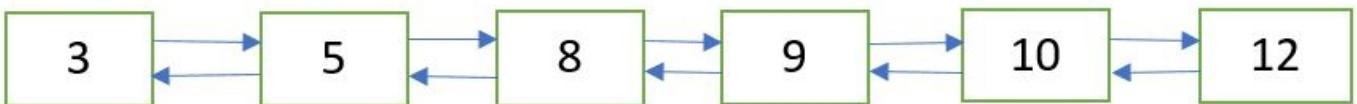
**Insert value in  
sorted way in a  
sorted doubly  
linked list**

Given a sorted doubly linked list and a value to insert, write a function to insert the value in sorted way.

Initial doubly linked list



## Doubly Linked List after insertion of 9



### Algorithm:

Let input doubly linked list is sorted in increasing order.

New node passed to the function contains data in the data part and previous and next link are set to NULL

```
sortedInsert(head_ref, newNode)
    if (head_ref == NULL)
        head_ref = newNode

    else if head_ref->data >= newNode->data
        newNode->next = head_ref
        newNode->next->prev = newNode
        head_ref = newNode

    else
        Initialize current = head_ref
        while (current->next != NULL and
               current->next->data < newNode->data)
            current = current->next

        newNode->next = current->next
        if current->next != NULL
            newNode->next->prev = newNode

            current->next = newNode
        newNode->prev = current
```

```
1 // C++ implementation to insert value in sorted way
2 // in a sorted doubly linked list
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 // Node of a doubly linked list
8 struct Node {
9     int data;
10    struct Node* prev, *next;
11 };
12
```

```
13 // function to create and return a new node
14 // of a doubly linked list
15 struct Node* getNode(int data)
16 {
17     // allocate node
18     struct Node* newNode =
19         (struct Node*)malloc(sizeof(struct Node));
20
21     // put in the data
22     newNode->data = data;
23     newNode->prev = newNode->next = NULL;
24     return newNode;
25 }
26
27 // function to insert a new node in sorted way in
28 // a sorted doubly linked list
29 void sortedInsert(struct Node** head_ref, struct Node* newNode)
30 {
31     struct Node* current;
32
33     // if list is empty
34     if (*head_ref == NULL)
35         *head_ref = newNode;
36
37     // if the node is to be inserted at the beginning
38     // of the doubly linked list
39     else if ((*head_ref)->data >= newNode->data) {
40         newNode->next = *head_ref;
41         newNode->next->prev = newNode;
42         *head_ref = newNode;
43     }
44
45     else {
46         current = *head_ref;
47
48         // locate the node after which the new node
49         // is to be inserted
50         while (current->next != NULL &&
51                current->next->data < newNode->data)
52             current = current->next;
53
54         /* Make the appropriate links */
55         newNode->next = current->next;
56
57         // if the new node is not inserted
58         // at the end of the list
59         if (current->next != NULL)
60             newNode->next->prev = newNode;
61
62         current->next = newNode;
63         newNode->prev = current;
64     }
65 }
66
```

```
67 // function to print the doubly linked list
68 void printList(struct Node* head)
69 {
70     while (head != NULL) {
71         cout << head->data << " ";
72         head = head->next;
73     }
74 }
75
76 // Driver program to test above
77 int main()
78 {
79     /* start with the empty doubly linked list */
80     struct Node* head = NULL;
81
82     // insert the following nodes in sorted way
83     struct Node* new_node = getNode(8);
84     sortedInsert(&head, new_node);
85     new_node = getNode(5);
86     sortedInsert(&head, new_node);
87     new_node = getNode(3);
88     sortedInsert(&head, new_node);
89     new_node = getNode(10);
90     sortedInsert(&head, new_node);
91     new_node = getNode(12);
92     sortedInsert(&head, new_node);
93     new_node = getNode(9);
94     sortedInsert(&head, new_node);
95
96     cout << "Created Doubly Linked Listn";
97     printList(head);
98     return 0;
99 }
100
```

### Output:

```
Created Doubly Linked List
3 5 8 9 10 12
```

Time Complexity: O(n)

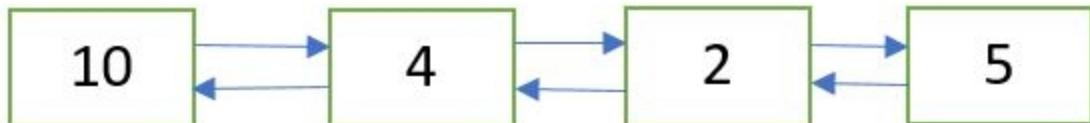
# Delete a Doubly Linked List node at a given position

Given a doubly linked list and a position  $n$ . The task is to delete the node at the given position  $n$  from the beginning.

Initial doubly linked list



Doubly Linked List after deletion of node at position  $n = 2$



**Approach:** Following are the steps:

1. Get the pointer to the node at position  $n$  by traversing the doubly linked list up to the  $n$ th node from the beginning.
2. Delete the node using the pointer obtained in Step 1.

```
1 /* C++ implementation to delete a doubly Linked List node
2 at the given position */
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 /* a node of the doubly linked list */
8 struct Node {
9     int data;
10    struct Node* next;
11    struct Node* prev;
12 };
13
14 /* Function to delete a node in a Doubly Linked List.
15 head_ref --> pointer to head node pointer.
16 del --> pointer to node to be deleted. */
17 void deleteNode(struct Node** head_ref, struct Node* del)
18 {
```

```

19     /* base case */
20     if (*head_ref == NULL || del == NULL)
21         return;
22
23     /* If node to be deleted is head node */
24     if (*head_ref == del)
25         *head_ref = del->next;
26
27     /* Change next only if node to be deleted is NOT
28      the last node */
29     if (del->next != NULL)
30         del->next->prev = del->prev;
31
32     /* Change prev only if node to be deleted is NOT
33      the first node */
34     if (del->prev != NULL)
35         del->prev->next = del->next;
36
37     /* Finally, free the memory occupied by del*/
38     free(del);
39 }
40
41 /* Function to delete the node at the given position
42 in the doubly linked list */
43 void deleteNodeAtGivenPos(struct Node** head_ref, int n)
44 {
45     /* if list in NULL or invalid position is given */
46     if (*head_ref == NULL || n <= 0)
47         return;
48
49     struct Node* current = *head_ref;
50     int i;
51
52     /* traverse up to the node at position 'n' from
53      the beginning */
54     for (int i = 1; current != NULL && i < n; i++)
55         current = current->next;
56
57     /* if 'n' is greater than the number of nodes
58      in the doubly linked list */
59     if (current == NULL)
60         return;
61
62     /* delete the node pointed to by 'current' */
63     deleteNode(head_ref, current);
64 }
65
66 /* Function to insert a node at the beginning
67 of the Doubly Linked List */
68 void push(struct Node** head_ref, int new_data)
69 {
70     /* allocate node */
71     struct Node* new_node =
72         (struct Node*)malloc(sizeof(struct Node));
73

```

```

74     /* put in the data */
75     new_node->data = new_data;
76
77     /* since we are adding at the beginning,
78     prev is always NULL */
79     new_node->prev = NULL;
80
81     /* link the old list off the new node */
82     new_node->next = (*head_ref);
83
84     /* change prev of head node to new node */
85     if ((*head_ref) != NULL)
86         (*head_ref)->prev = new_node;
87
88     /* move the head to point to the new node */
89     (*head_ref) = new_node;
90 }
91
92 /* Function to print nodes in a given doubly
93 linked list */
94 void printList(struct Node* head)
95 {
96     while (head != NULL) {
97         cout << head->data << " ";
98         head = head->next;
99     }
100}
101
102 /* Driver program to test above functions*/
103 int main()
104 {
105     /* Start with the empty list */
106     struct Node* head = NULL;
107
108     /* Create the doubly linked list 10<->8<->4<->2<->5 */
109     push(&head, 5);
110     push(&head, 2);
111     push(&head, 4);
112     push(&head, 8);
113     push(&head, 10);
114
115     cout << "Doubly linked list before deletion:n";
116     printList(head);
117
118     int n = 2;
119
120     /* delete node at the given position 'n' */
121     deleteNodeAtGivenPos(&head, n);
122
123     cout << "\nDoubly linked list after deletion:n";
124     printList(head);
125
126     return 0;
127 }
128

```

**Output:**

```
Doubly linked list before deletion:  
10 8 4 2 5  
Doubly linked list after deletion:  
10 4 2 5
```

## Count triplets in a sorted doubly linked list whose sum is equal to a given value x

Given a sorted doubly linked list of distinct nodes(no two nodes have the same data) and a value **x**. Count triplets in the list that sum up to a given value **x**.

Examples:

**Input :** DLL: 1 <-> 2 <-> 4 <-> 5 <-> 6 <-> 8 <-> 9  
**x = 17**

**Output :** 2

The triplets are:

(2, 6, 9) and (4, 5, 8)

**Input :** DLL: 1 <-> 2 <-> 4 <-> 5 <-> 6 <-> 8 <-> 9  
**x = 15**

**Output :** 5

### **Efficient Approach(Use of two pointers):**

Traverse the doubly linked list from left to right. For each **current** node during the traversal, initialize two pointers **first** = pointer to the node next to the **current** node and **last** = pointer to the last node of the list. Now, count pairs in the list from **first** to **last** pointer that sum up to value (**x - current node's data**) (algorithm described in post). Add this count to the **total\_count** of triplets. Pointer to the **last** node can be found only once in the beginning.

```

1 // C++ implementation to count triplets in a sorted doubly linked list
2 // whose sum is equal to a given value 'x'
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 // structure of node of doubly linked list
8 struct Node {
9     int data;
10    struct Node* next, *prev;
11 };
12
13 // function to count pairs whose sum equal to given 'value'
14 int countPairs(struct Node* first, struct Node* second, int value)
15 {
16     int count = 0;
17
18     // The loop terminates when either of two pointers
19     // become NULL, or they cross each other (second->next
20     // == first), or they become same (first == second)
21     while (first != NULL && second != NULL &&
22            first != second && second->next != first) {
23
24         // pair found
25         if ((first->data + second->data) == value) {
26
27             // increment count
28             count++;
29
30             // move first in forward direction
31             first = first->next;
32
33             // move second in backward direction
34             second = second->prev;
35         }
36
37         // if sum is greater than 'value'
38         // move second in backward direction
39         else if ((first->data + second->data) > value)
40             second = second->prev;
41
42         // else move first in forward direction
43         else
44             first = first->next;
45     }
46
47     // required count of pairs
48     return count;
49 }
50
51 // function to count triplets in a sorted doubly linked list
52 // whose sum is equal to a given value 'x'
53 int countTriplets(struct Node* head, int x)
54 {

```

```

55     // if list is empty
56     if (head == NULL)
57         return 0;
58
59     struct Node* current, *first, *last;
60     int count = 0;
61
62     // get pointer to the last node of
63     // the doubly linked list
64     last = head;
65     while (last->next != NULL)
66         last = last->next;
67
68     // traversing the doubly linked list
69     for (current = head; current != NULL; current = current->next) {
70
71         // for each current node
72         first = current->next;
73
74         // count pairs with sum(x - current->data) in the range
75         // first to last and add it to the 'count' of triplets
76         count += countPairs(first, last, x - current->data);
77     }
78
79     // required count of triplets
80     return count;
81 }
82
83 // A utility function to insert a new node at the
84 // beginning of doubly linked list
85 void insert(struct Node** head, int data)
86 {
87     // allocate node
88     struct Node* temp = new Node();
89
90     // put in the data
91     temp->data = data;
92     temp->next = temp->prev = NULL;
93
94     if ((*head) == NULL)
95         (*head) = temp;
96     else {
97         temp->next = *head;
98         (*head)->prev = temp;
99         (*head) = temp;
100    }
101 }
102
103 // Driver program to test above
104 int main()
105 {
106     // start with an empty doubly linked list
107     struct Node* head = NULL;
108
109     // insert values in sorted order

```

```
110     insert(&head, 9);
111     insert(&head, 8);
112     insert(&head, 6);
113     insert(&head, 5);
114     insert(&head, 4);
115     insert(&head, 2);
116     insert(&head, 1);
117
118     int x = 17;
119
120     cout << "Count = "
121     << countTriplets(head, x);
122     return 0;
123 }
124
```

#### Output:

```
Count = 2
```

**Time Complexity:**  $O(n^2)$

**Auxiliary Space:**  $O(1)$

## Remove duplicates from a sorted doubly linked list

Given a sorted doubly linked list containing  $n$  nodes. The problem is removing duplicate nodes from the given list.

#### Examples:

**Input :** DLL: 4<->4<->4<->4<->6<->8<->8<->10<->12<->12

**Output :** 4<->6<->8<->10<->12

## Algorithm:

```
removeDuplicates(head_ref, x)
    if head_ref == NULL
        return
    Initialize current = head_ref
    while current->next != NULL
        if current->data == current->next->data
            deleteNode(head_ref, current->next)
        else
            current = current->next
```

```
1  /* C++ implementation to remove duplicates from a
2   sorted doubly linked list */
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 /* a node of the doubly linked list */
8 struct Node {
9     int data;
10    struct Node* next;
11    struct Node* prev;
12 };
13
14 /* Function to delete a node in a Doubly Linked List.
15 head_ref --> pointer to head node pointer.
16 del --> pointer to node to be deleted. */
17 void deleteNode(struct Node** head_ref, struct Node* del)
18 {
19     /* base case */
20     if (*head_ref == NULL || del == NULL)
21         return;
22
23     /* If node to be deleted is head node */
24     if (*head_ref == del)
25         *head_ref = del->next;
26
27     /* Change next only if node to be deleted
28      is NOT the last node */
29     if (del->next != NULL)
30         del->next->prev = del->prev;
31
32     /* Change prev only if node to be deleted
33      is NOT the first node */
34     if (del->prev != NULL)
35         del->prev->next = del->next;
36
37     /* Finally, free the memory occupied by del*/
38     free(del);
39 }
40
```

```
41  /* function to remove duplicates from a
42  sorted doubly linked list */
43 void removeDuplicates(struct Node** head_ref)
44 {
45     /* if list is empty */
46     if ((*head_ref) == NULL)
47         return;
48
49     struct Node* current = *head_ref;
50     struct Node* next;
51
52     /* traverse the list till the last node */
53     while (current->next != NULL) {
54
55         /* Compare current node with next node */
56         if (current->data == current->next->data)
57
58             /* delete the node pointed to by
59              'current->next' */
60             deleteNode(head_ref, current->next);
61
62         /* else simply move to the next node */
63         else
64             current = current->next;
65     }
66 }
67
68 /* Function to insert a node at the beginning
69 of the Doubly Linked List */
70 void push(struct Node** head_ref, int new_data)
71 {
72     /* allocate node */
73     struct Node* new_node =
74         (struct Node*)malloc(sizeof(struct Node));
75
76     /* put in the data */
77     new_node->data = new_data;
78
79     /* since we are adding at the beginning,
80     prev is always NULL */
81     new_node->prev = NULL;
82
83     /* link the old list off the new node */
84     new_node->next = (*head_ref);
85
86     /* change prev of head node to new node */
87     if ((*head_ref) != NULL)
88         (*head_ref)->prev = new_node;
89
90     /* move the head to point to the new node */
91     (*head_ref) = new_node;
92 }
93 }
```

```

94  /* Function to print nodes in a given doubly linked list */
95  void printList(struct Node* head)
96  {
97      /* if list is empty */
98      if (head == NULL)
99          cout << "Doubly Linked list empty";
100
101     while (head != NULL) {
102         cout << head->data << " ";
103         head = head->next;
104     }
105 }
106
107 /* Driver program to test above functions*/
108 int main()
109 {
110     /* Start with the empty list */
111     struct Node* head = NULL;
112
113     /* Create the doubly linked list:
114     4<->4<->4<->4<->6<->8<->8<->10<->12<->12 */
115     push(&head, 12);
116     push(&head, 12);
117     push(&head, 10);
118     push(&head, 8);
119     push(&head, 8);
120     push(&head, 6);
121     push(&head, 4);
122     push(&head, 4);
123     push(&head, 4);
124     push(&head, 4);
125
126     cout << "Original Doubly linked list:n";
127     printList(head);
128
129     /* remove duplicate nodes */
130     removeDuplicates(&head);
131
132     cout << "\nDoubly linked list after"
133             " removing duplicates:n";
134     printList(head);
135
136     return 0;
137 }
138

```

**Output:**

```

Original Doubly linked list:
4 4 4 4 6 8 8 10 12 12
Doubly linked list after removing duplicates:
4 6 8 10 12

```

**Time Complexity:** O(n)

## Delete all occurrences of a given key in a doubly linked list

Given a doubly linked list and a key  $x$ . The problem is to delete all occurrences of the given key  $x$  from the doubly linked list.

Examples:

**Input :** DLL: 2 <-> 2 <-> 10 <-> 8 <-> 4 <-> 2 <-> 5 <-> 2

$x = 2$

**Output :** 10 <-> 8 <-> 4 <-> 5

**Algorithm:**

```
delAllOccurOfGivenKey(head_ref, x)
    if head_ref == NULL
        return
    Initialize current = head_ref
    Declare next
    while current != NULL
        if current->data == x
            next = current->next
            deleteNode(head_ref, current)
            current = next
        else
            current = current->next
```

**Time Complexity:** O(n)

```

1  /* C++ implementation to delete all occurrences
2  of a given key in a doubly linked list */
3  #include <bits/stdc++.h>
4
5  using namespace std;
6
7  /* a node of the doubly linked list */
8  struct Node {
9      int data;
10     struct Node* next;
11     struct Node* prev;
12 };
13
14 /* Function to delete a node in a Doubly Linked List.
15 head_ref --> pointer to head node pointer.
16 del --> pointer to node to be deleted. */
17 void deleteNode(struct Node** head_ref, struct Node* del)
18 {
19     /* base case */
20     if (*head_ref == NULL || del == NULL)
21         return;
22
23     /* If node to be deleted is head node */
24     if (*head_ref == del)
25         *head_ref = del->next;
26
27     /* Change next only if node to be deleted
28     is NOT the last node */
29     if (del->next != NULL)
30         del->next->prev = del->prev;
31
32     /* Change prev only if node to be deleted
33     is NOT the first node */
34     if (del->prev != NULL)
35         del->prev->next = del->next;
36
37     /* Finally, free the memory occupied by del*/
38     free(del);
39 }
40
41 /* function to delete all occurrences of the given
42   key 'x' */
43 void deleteAllOccurOfX(struct Node** head_ref, int x)
44 {
45     /* if list is empty */
46     if ((*head_ref) == NULL)
47         return;
48
49     struct Node* current = *head_ref;
50     struct Node* next;
51
52     /* traverse the list up to the end */
53     while (current != NULL) {
54
55         /* if node found with the value 'x' */
56         if (current->data == x) {
57

```

```
58     /* save current's next node in the
59      pointer 'next' */
60     next = current->next;
61
62     /* delete the node pointed to by
63      'current' */
64     deleteNode(head_ref, current);
65
66     /* update current */
67     current = next;
68 }
69
70     /* else simply move to the next node */
71 else
72     current = current->next;
73 }
74 }
75
76 /* Function to insert a node at the beginning
77 of the Doubly Linked List */
78 void push(struct Node** head_ref, int new_data)
79 {
80     /* allocate node */
81     struct Node* new_node =
82         (struct Node*)malloc(sizeof(struct Node));
83
84     /* put in the data */
85     new_node->data = new_data;
86
87     /* since we are adding at the beginning,
88     prev is always NULL */
89     new_node->prev = NULL;
90
91     /* link the old list off the new node */
92     new_node->next = (*head_ref);
93
94     /* change prev of head node to new node */
95     if ((*head_ref) != NULL)
96         (*head_ref)->prev = new_node;
97
98     /* move the head to point to the new node */
99     (*head_ref) = new_node;
100 }
101
102 /* Function to print nodes in a given doubly
103 linked list */
104 void printList(struct Node* head)
105 {
106     /* if list is empty */
107     if (head == NULL)
108         cout << "Doubly Linked list empty";
109
110     while (head != NULL) {
111         cout << head->data << " ";
112         head = head->next;
113     }
114 }
```

```
115  /* Driver program to test above functions*/
116  int main()
117  {
118      /* Start with the empty list */
119      struct Node* head = NULL;
120
121      /* Create the doubly linked list:
122         2<->2<->10<->8<->4<->2<->5<->2 */
123      push(&head, 2);
124      push(&head, 5);
125      push(&head, 2);
126      push(&head, 4);
127      push(&head, 8);
128      push(&head, 10);
129      push(&head, 2);
130      push(&head, 2);
131
132      cout << "Original Doubly linked list:n";
133      printList(head);
134
135      int x = 2;
136
137      /* delete all occurrences of 'x' */
138      deleteAllOccurOfX(&head, x);
139
140      cout << "\nDoubly linked list after deletion of "
141          << x << ":n";
142      printList(head);
143
144      return 0;
145  }
146
147
```

#### Output:

```
Original Doubly linked list:
2 2 10 8 4 2 5 2
Doubly linked list after deletion of 2:
10 8 4 5
```

# Remove duplicates from an unsorted doubly linked list

Given an unsorted doubly linked list containing **n** nodes. The problem is to remove duplicate nodes from the given list.

Input : DLL: 8<->4<->4<->6<->4<->8<->4<->10<->12<->12

Output : 8<->4<->6<->10<->12

```
1 // C++ implementation to remove duplicates from an
2 // unsorted doubly linked list
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 // a node of the doubly linked list
8 struct Node {
9     int data;
10    struct Node* next;
11    struct Node* prev;
12 };
13
14 // Function to delete a node in a Doubly Linked List.
15 // head_ref --> pointer to head node pointer.
16 // del --> pointer to node to be deleted.
17 void deleteNode(struct Node** head_ref, struct Node* del)
18 {
19     // base case
20     if (*head_ref == NULL || del == NULL)
21         return;
22
23     // If node to be deleted is head node
24     if (*head_ref == del)
25         *head_ref = del->next;
26
27     // Change next only if node to be deleted
28     // is NOT the last node
29     if (del->next != NULL)
30         del->next->prev = del->prev;
31
32     // Change prev only if node to be deleted
33     // is NOT the first node
34     if (del->prev != NULL)
35         del->prev->next = del->next;
36
37     // Finally, free the memory occupied by del
38     free(del);
39 }
```

```
40
41 // function to remove duplicates from
42 // an unsorted doubly linked list
43 void removeDuplicates(struct Node** head_ref)
44 {
45     // if DLL is empty or if it contains only
46     // a single node
47     if ((*head_ref) == NULL || 
48         (*head_ref)->next == NULL)
49         return;
50
51     struct Node* ptr1, *ptr2;
52
53     // pick elements one by one
54     for (ptr1 = *head_ref; ptr1 != NULL; ptr1 = ptr1->next) {
55         ptr2 = ptr1->next;
56
57         // Compare the picked element with the
58         // rest of the elements
59         while (ptr2 != NULL) {
60
61             // if duplicate, then delete it
62             if (ptr1->data == ptr2->data) {
63
64                 // store pointer to the node next to 'ptr2'
65                 struct Node* next = ptr2->next;
66
67                 // delete node pointed to by 'ptr2'
68                 deleteNode(head_ref, ptr2);
69
70                 // update 'ptr2'
71                 ptr2 = next;
72             }
73
74             // else simply move to the next node
75             else
76                 ptr2 = ptr2->next;
77         }
78     }
79 }
80
81 // Function to insert a node at the beginning
82 // of the Doubly Linked List
83 void push(struct Node** head_ref, int new_data)
84 {
85     // allocate node
86     struct Node* new_node =
87         (struct Node*)malloc(sizeof(struct Node));
88
89     // put in the data
90     new_node->data = new_data;
91
92     // since we are adding at the beginning,
93     // prev is always NULL
94     new_node->prev = NULL;
95 }
```

```
96     // link the old list off the new node
97     new_node->next = (*head_ref);
98
99     // change prev of head node to new node
100    if ((*head_ref) != NULL)
101        (*head_ref)->prev = new_node;
102
103    // move the head to point to the new node
104    (*head_ref) = new_node;
105 }
106
107 // Function to print nodes in a given doubly
108 // linked list
109 void printList(struct Node* head)
110 {
111     // if list is empty
112     if (head == NULL)
113         cout << "Doubly Linked list empty";
114
115     while (head != NULL) {
116         cout << head->data << " ";
117         head = head->next;
118     }
119 }
120
121 // Driver program to test above
122 int main()
123 {
124     struct Node* head = NULL;
125
126     // Create the doubly linked list:
127     // 8<->4<->4<->6<->4<->8<->4<->10<->12<->12
128     push(&head, 12);
129     push(&head, 12);
130     push(&head, 10);
131     push(&head, 4);
132     push(&head, 8);
133     push(&head, 4);
134     push(&head, 6);
135     push(&head, 4);
136     push(&head, 4);
137     push(&head, 8);
138
139     cout << "Original Doubly linked list:n";
140     printList(head);
141
142     /* remove duplicate nodes */
143     removeDuplicates(&head);
144
145     cout << "\nDoubly linked list after "
146         "removing duplicates:n";
147     printList(head);
148
149     return 0;
150 }
```

## Output

```
Original Doubly linked list:  
8 4 4 6 4 8 4 10 12 12  
Doubly linked list after removing duplicates:  
8 4 6 10 12
```

Time Complexity:  $O(n^2)$

Auxiliary Space:  $O(1)$

## Sort the biotonic doubly linked list

Sort the given biotonic doubly linked list. A biotonic doubly linked list is a doubly linked list which is first increasing and then decreasing. A strictly increasing or a strictly decreasing list is also a biotonic doubly linked list.

Input : DLL: 2<->5<->7<->12<->10<->6<->4<->1

Output : 1<->2<->4<->5<->6<->7<->10<->12

Input : DLL: 20<->17<->14<->8<->3

Output : 3<->8<->14<->17<->20

**Approach:** Find the first node in the list which is smaller than its previous node. Let it be **current**. If no such node is present then list is already sorted. Else split the list into two lists, **first** starting from **head** node till the **current's** previous node and **second** starting from **current** node till the end of the list. Reverse the **second** doubly linked list. Now merge the **first** and **second** sorted doubly linked list.. The final merged list is the required sorted doubly linked list.

```
1 // C++ implementation to sort the biotonic doubly linked list  
2 #include <bits/stdc++.h>  
3  
4 using namespace std;  
5  
6 // a node of the doubly linked list  
7 struct Node {  
8     int data;  
9     struct Node* next;  
10    struct Node* prev;  
11};  
12  
13 // Function to reverse a Doubly Linked List  
14 void reverse(struct Node** head_ref)  
15 {
```

```

16     struct Node* temp = NULL;
17     struct Node* current = *head_ref;
18
19     // swap next and prev for all nodes
20     // of doubly linked list
21     while (current != NULL) {
22         temp = current->prev;
23         current->prev = current->next;
24         current->next = temp;
25         current = current->prev;
26     }
27
28     // Before changing head, check for the cases
29     // like empty list and list with only one node
30     if (temp != NULL)
31         *head_ref = temp->prev;
32 }
33
34 // Function to merge two sorted doubly linked lists
35 struct Node* merge(struct Node* first, struct Node* second)
36 {
37     // If first linked list is empty
38     if (!first)
39         return second;
40
41     // If second linked list is empty
42     if (!second)
43         return first;
44
45     // Pick the smaller value
46     if (first->data < second->data) {
47         first->next = merge(first->next, second);
48         first->next->prev = first;
49         first->prev = NULL;
50         return first;
51     } else {
52         second->next = merge(first, second->next);
53         second->next->prev = second;
54         second->prev = NULL;
55         return second;
56     }
57 }
58
59 // function to sort a bitonic doubly linked list
60 struct Node* sort(struct Node* head)
61 {
62     // if list is empty or if it contains a single
63     // node only
64     if (head == NULL || head->next == NULL)
65         return head;
66
67     struct Node* current = head->next;
68
69     while (current != NULL) {
70

```

```

71         // if true, then 'current' is the first node
72         // which is smaller than its previous node
73         if (current->data < current->prev->data)
74             break;
75
76         // move to the next node
77         current = current->next;
78     }
79
80     // if true, then list is already sorted
81     if (current == NULL)
82         return head;
83
84     // spilt into two lists, one starting with 'head'
85     // and other starting with 'current'
86     current->prev->next = NULL;
87     current->prev = NULL;
88
89     // reverse the list starting with 'current'
90     reverse(&t);
91
92     // merge the two lists and return the
93     // final merged doubly linked list
94     return merge(head, current);
95 }
96
97 // Function to insert a node at the beginning
98 // of the Doubly Linked List
99 void push(struct Node** head_ref, int new_data)
100 {
101     // allocate node
102     struct Node* new_node =
103         (struct Node*)malloc(sizeof(struct Node));
104
105     // put in the data
106     new_node->data = new_data;
107
108     // since we are adding at the beginning,
109     // prev is always NULL
110     new_node->prev = NULL;
111
112     // link the old list off the new node
113     new_node->next = (*head_ref);
114
115     // change prev of head node to new node
116     if ((*head_ref) != NULL)
117         (*head_ref)->prev = new_node;
118
119     // move the head to point to the new node
120     (*head_ref) = new_node;
121 }
122
123 // Function to print nodes in a given doubly
124 // linked list
125 void printList(struct Node* head)

```

```

126  {
127      // if list is empty
128      if (head == NULL)
129          cout << "Doubly Linked list empty";
130
131      while (head != NULL) {
132          cout << head->data << " ";
133          head = head->next;
134      }
135  }
136
137 // Driver program to test above
138 int main()
139 {
140     struct Node* head = NULL;
141
142     // Create the doubly linked list:
143     // 2<->5<->7<->12<->10<->6<->4<->1
144     push(&head, 1);
145     push(&head, 4);
146     push(&head, 6);
147     push(&head, 10);
148     push(&head, 12);
149     push(&head, 7);
150     push(&head, 5);
151     push(&head, 2);
152
153     cout << "Original Doubly linked list:n";
154     printList(head);
155
156     // sort the biotonic DLL
157     head = sort(head);
158
159     cout << "\nDoubly linked list after sorting:n";
160     printList(head);
161
162     return 0;
163 }
164

```

## Output

```

Original Doubly linked list:
2 5 7 12 10 6 4 1
Doubly linked list after sorting:
1 2 4 5 6 7 10 12

```

Time Complexity: O(n)

# Sort a k sorted doubly linked list

Given a doubly linked list containing  $n$  nodes, where each node is at most  $k$  away from its target position in the list. The problem is to sort the given doubly linked list.

For example, let us consider  $k$  is 2, a node at position 7 in the sorted doubly linked list, can be at positions 5, 6, 7, 8, 9 in the given doubly linked list.

Examples:

Input : DLL: 3 <-> 6 <-> 2 <-> 12 <-> 56 <-> 8

$k = 2$

Output : 2 <-> 3 <-> 6 <-> 8 <-> 12 <-> 56

**Naive Approach:** Sort the given doubly linked list using the insertion sort technique. While inserting each element in the sorted part of the list, there will be at most  $k$  swaps to place the element to its correct position since it is at most  $k$  steps away from its correct position.

```
1 // C++ implementation to sort a k sorted doubly
2 // linked list
3 #include<bits/stdc++.h>
4 using namespace std;
5
6 // a node of the doubly linked list
7 struct Node {
8     int data;
9     struct Node* next;
10    struct Node* prev;
11};
12
13
14 // function to sort a k sorted doubly linked list
15 struct Node* sortAKSortedDLL(struct Node* head, int k)
16 {
17     if(head == NULL || head->next == NULL)
18         return head;
19
20     // perform on all the nodes in list
21     for(Node *i = head->next; i != NULL; i = i->next) {
22         Node *j = i;
23         // There will be atmost k swaps for each element in the list
24         // since each node is k steps away from its correct position
25         while(j->prev != NULL && j->data < j->prev->data) {
26             // swap j and j.prev node
27             Node* temp = j->prev->prev;
28             Node* temp2 = j->prev;
29             Node *temp3 = j->next;
30             j->prev->next = temp3;
31             j->prev->prev = j;
32             j->prev = temp;
```

```

33         j->next = temp2;
34         if(temp != NULL)
35             temp->next = j;
36         if(temp3 != NULL)
37             temp3->prev = temp2;
38     }
39     // if j is now the new head
40 // then reset head
41     if(j->prev == NULL)
42         head = j;
43 }
44 return head;
45 }
46
47 // Function to insert a node at the beginning
48 // of the Doubly Linked List
49 void push(struct Node** head_ref, int new_data)
50 {
51     // allocate node
52     struct Node* new_node =
53         (struct Node*)malloc(sizeof(struct Node));
54
55     // put in the data
56     new_node->data = new_data;
57
58     // since we are adding at the beginning,
59     // prev is always NULL
60     new_node->prev = NULL;
61
62     // link the old list off the new node
63     new_node->next = (*head_ref);
64
65     // change prev of head node to new node
66     if ((*head_ref) != NULL)
67         (*head_ref)->prev = new_node;
68
69     // move the head to point to the new node
70     (*head_ref) = new_node;
71 }
72
73 // Function to print nodes in a given doubly linked list
74 void printList(struct Node* head)
75 {
76     // if list is empty
77     if (head == NULL)
78         cout << "Doubly Linked list empty";
79
80     while (head != NULL) {
81         cout << head->data << " ";
82         head = head->next;
83     }
84 }
85

```

```

86 // Driver program to test above
87 int main()
88 {
89     struct Node* head = NULL;
90
91     // Create the doubly linked list:
92     // 3<->6<->2<->12<->56<->8
93     push(&head, 8);
94     push(&head, 56);
95     push(&head, 12);
96     push(&head, 2);
97     push(&head, 6);
98     push(&head, 3);
99
100    int k = 2;
101
102    cout << "Original Doubly linked list:\n";
103    printList(head);
104
105    // sort the bitonic DLL
106    head = sortAKSortedDLL(head, k);
107
108    cout << "\nDoubly linked list after sorting:\n";
109    printList(head);
110
111    return 0;
112 }
113
114 // This code is contributed by sachinjain74754.
115

```

## Output

```

Original Doubly linked list:
3 6 2 12 56 8
Doubly Linked List after sorting:
2 3 6 8 12 56

```

**Time Complexity:**  $O(n*k)$

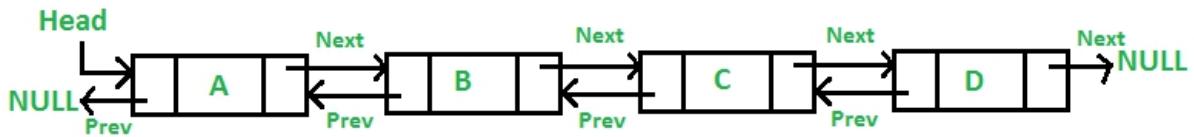
**Auxiliary Space:**  $O(1)$

Go through below problem..

<https://www.geeksforgeeks.org/convert-a-given-binary-tree-to-doubly-linked-list-set-4/>

# Program to find size of Doubly Linked List

Given a doubly linked list , the task is to find the size of that doubly linked list. For example, size of below linked list is 4.



A doubly linked list is a linked data structure that consists of a set of sequentially linked records called nodes. Each node contains two fields, called links, that are references to the previous and to the next node in the sequence of nodes.

Traversal of a doubly linked list can be in either direction. In fact, the direction of traversal can change many times, if desired.

## Algorithm :

- 1) Initialize size to 0.
- 2) Initialize a node pointer, temp = head.
- 3) Do following while temp is not NULL  
.....a) temp = temp -> next  
.....b) size++;
- 4) Return size.

```
1 // A complete working C++ program to
2 // find size of doubly linked list.
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 // A linked list node
7 struct Node
8 {
9     int data;
10    struct Node *next;
11    struct Node *prev;
12 };
13
14 /* Function to add a node to front of doubly
15 linked list */
```

```

16 void push(struct Node** head_ref, int new_data)
17 {
18     struct Node* new_node = new Node;
19     new_node->data = new_data;
20     new_node->next = (*head_ref);
21     new_node->prev = NULL;
22     if ((*head_ref) != NULL)
23         (*head_ref)->prev = new_node ;
24     (*head_ref) = new_node;
25 }
26
27 // This function returns size of linked list
28 int findSize(struct Node *node)
29 {
30     int res = 0;
31     while (node != NULL)
32     {
33         res++;
34         node = node->next;
35     }
36     return res;
37 }
38
39 /* Driver program to test above functions*/
40 int main()
41 {
42     struct Node* head = NULL;
43     push(&head, 4);
44     push(&head, 3);
45     push(&head, 2);
46     push(&head, 1);
47     cout << findSize(head);
48     return 0;
49 }
```

**Output:**

4

Sorted insert in a  
doubly linked list  
with head and  
tail pointers

A doubly linked list is a linked list that consists of a set of sequentially linked records called

nodes. Each node contains two fields that are references to the previous and to the next node in the sequence of nodes.

The task is to create a doubly linked list by inserting nodes such that list remains in ascending order on printing from left to right. Also, we need to maintain two pointers, head (points to first node) and tail (points to last node).

**Examples:**

```
Input : 40 50 10 45 90 100 95
```

```
Output :10 40 45 50 90 95 100
```

```
Input : 30 10 50 43 56 12
```

```
Output :10 12 30 43 50 56
```

### Algorithm:

The task can be accomplished as:

1. If Linked list is empty then make both the left and right pointers point to the node to be inserted and make its previous and next field point to NULL.
2. If node to be inserted has value less than the value of first node of linked list then connect that node from previous field of first node.
3. If node to be inserted has value more than the value of last node of linked list then connect that node from next field of last node.
4. If node to be inserted has value in between the value of first and last node, then check for appropriate position and make connections.

```
1  /* C++ program to insert tail nodes in doubly
2  linked list such that list remains in
3  ascending order on printing from left
4  to right */
5  #include <bits/stdc++.h>
6  using namespace std;
7
8 // A linked list node
9 class Node
10 {
11     public:
12     Node *prev;
13     int info;
14     Node *next;
15 };
16
17 // Function to insert tail new node
18 void nodeInsetail(Node **head,
19                     Node **tail,
20                     int key)
21 {
```

```
22     Node *p = new Node();
23     p->info = key;
24     p->next = NULL;
25
26     // If first node to be inserted in doubly
27     // linked list
28     if ((*head) == NULL)
29     {
30         (*head) = p;
31         (*tail) = p;
32         (*head)->prev = NULL;
33         return;
34     }
35
36
37     // If node to be inserted has value less
38     // than first node
39     if ((p->info) < ((*head)->info))
40     {
41         p->prev = NULL;
42         (*head)->prev = p;
43         p->next = (*head);
44         (*head) = p;
45         return;
46     }
47
48     // If node to be inserted has value more
49     // than last node
50     if ((p->info) > ((*tail)->info))
51     {
52         p->prev = (*tail);
53         (*tail)->next = p;
54         (*tail) = p;
55         return;
56     }
57
58     // Find the node before which we need to
59     // insert p.
60     Node *temp = (*head)->next;
61     while ((temp->info) < (p->info))
62         temp = temp->next;
63
64     // Insert new node before temp
65     (temp->prev)->next = p;
66     p->prev = temp->prev;
67     temp->prev = p;
68     p->next = temp;
69 }
70
71 // Function to print nodes in from left to right
72 void printList(Node *temp)
73 {
74     while (temp != NULL)
75     {
76         cout << temp->info << " ";
77         temp = temp->next;
78 }
```

```

78     }
79 }
80
81 // Driver program to test above functions
82 int main()
83 {
84     Node *left = NULL, *right = NULL;
85     nodeInsetail(&left, &right, 30);
86     nodeInsetail(&left, &right, 50);
87     nodeInsetail(&left, &right, 90);
88     nodeInsetail(&left, &right, 10);
89     nodeInsetail(&left, &right, 40);
90     nodeInsetail(&left, &right, 110);
91     nodeInsetail(&left, &right, 60);
92     nodeInsetail(&left, &right, 95);
93     nodeInsetail(&left, &right, 23);
94
95     cout<<"Doubly linked list on printing"
96     | " from left to right\n";
97     printList(left);
98
99     return 0;
100 }
101
102 // This code is contributed by rathbhupendra
103

```

Output

**Output:**

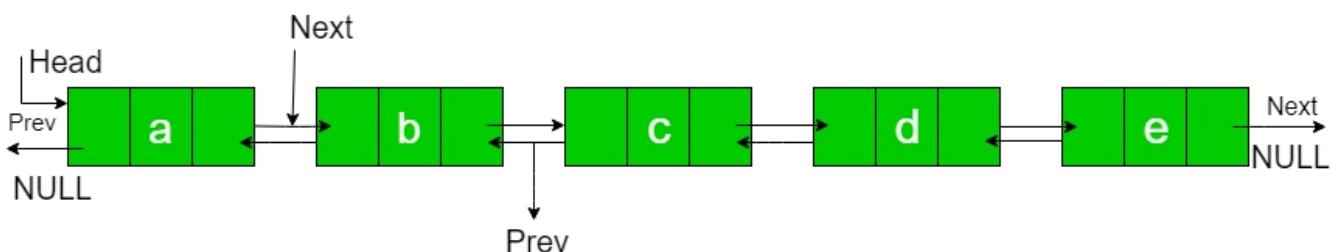
```

Doubly linked list on printing from left to right
10 23 30 40 50 60 90 95 110

```

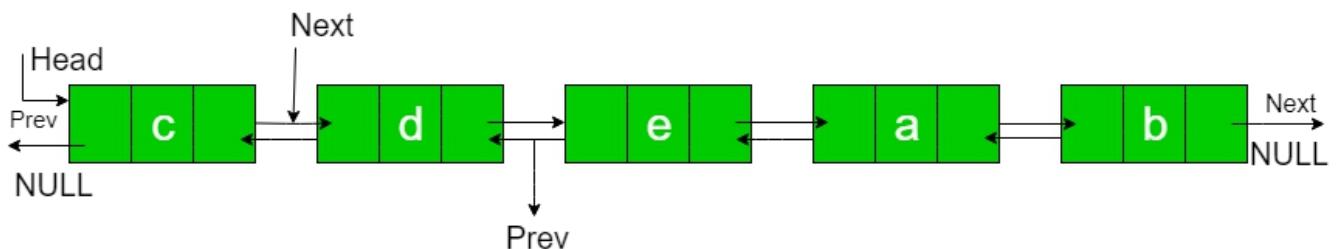
## Rotate Doubly linked list by N

Given a doubly linked list, rotate the linked list counter-clockwise by N nodes. Here N is a given positive integer and is smaller than the count of nodes in linked list.



N = 2

Rotated List:



Examples:

Input : a b c d e N = 2

Output : c d e a b

Input : a b c d e f g h N = 4

Output : e f g h a b c d

- Asked in amazon

To rotate the Doubly linked list, we need to change next of Nth node to NULL, next of last node to previous head node, and prev of head node to last node and finally change head to (N+1)th node and prev of new head node to NULL (Prev of Head node in doubly linked list is NULL)

So we need to get hold of three nodes: Nth node, (N+1)th node and last node. Traverse the list from beginning and stop at Nth node. Store pointer to Nth node. We can get (N+1)th node using NthNode->next. Keep traversing till end and store pointer to last node also. Finally, change pointers as stated above and at Last Print Rotated List using PrintList Function.

```
1 // C++ program to rotate a Doubly linked
2 // list counter clock wise by N times
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 /* Link list node */
7 struct Node {
8     char data;
9     struct Node* prev;
10    struct Node* next;
11 };
12
13 // This function rotates a doubly linked
14 // list counter-clockwise and updates the
15 // head. The function assumes that N is
```

```
16 // smallerthan size of linked list. It
17 // doesn't modify the list if N is greater
18 // than or equal to size
19 void rotate(struct Node** head_ref, int N)
20 {
21     if (N == 0)
22         return;
23
24     // Let us understand the below code
25     // for example N = 2 and
26     // list = a <-> b <-> c <-> d <-> e.
27     struct Node* current = *head_ref;
28
29     // current will either point to Nth
30     // or NULL after this loop. Current
31     // will point to node 'b' in the
32     // above example
33     int count = 1;
34     while (count < N && current != NULL) {
35         current = current->next;
36         count++;
37     }
38
39     // If current is NULL, N is greater
40     // than or equal to count of nodes
41     // in linked list. Don't change the
42     // list in this case
43     if (current == NULL)
44         return;
45
46     // current points to Nth node. Store
47     // it in a variable. NthNode points to
48     // node 'b' in the above example
49     struct Node* NthNode = current;
50
51     // current will point to last node
52     // after this loop current will point
53     // to node 'e' in the above example
54     while (current->next != NULL)
55         current = current->next;
56
57     // Change next of last node to previous
58     // head. Next of 'e' is now changed to
59     // node 'a'
60     current->next = *head_ref;
61
62     // Change prev of Head node to current
63     // Prev of 'a' is now changed to node 'e'
64     (*head_ref)->prev = current;
65
66     // Change head to (N+1)th node
67     // head is now changed to node 'c'
68     *head_ref = NthNode->next;
69
70     // Change prev of New Head node to NULL
71     // Because Prev of Head Node in Doubly
```

```

72     // linked list is NULL
73     (*head_ref)->prev = NULL;
74
75     // change next of Nth node to NULL
76     // next of 'b' is now NULL
77     NthNode->next = NULL;
78 }
79
80 // Function to insert a node at the
81 // beginning of the Doubly Linked List
82 void push(struct Node** head_ref, int new_data)
83 {
84     struct Node* new_node = new Node;
85     new_node->data = new_data;
86     new_node->prev = NULL;
87     new_node->next = (*head_ref);
88     if ((*head_ref) != NULL)
89         (*head_ref)->prev = new_node;
90     *head_ref = new_node;
91 }
92
93 /* Function to print linked list */
94 void printList(struct Node* node)
95 {
96     while (node->next != NULL) {
97         cout << node->data << " "
98             << "<=>" 
99             << " ";
100        node = node->next;
101    }
102    cout << node->data;
103 }
104
105 // Driver's Code
106 int main(void)
107 {
108     /* Start with the empty list */
109     struct Node* head = NULL;
110
111     /* Let us create the doubly
112     linked list a<->b<->c<->d<->e */
113     push(&head, 'e');
114     push(&head, 'd');
115     push(&head, 'c');
116     push(&head, 'b');
117     push(&head, 'a');
118
119     int N = 2;
120
121     cout << "Given linked list \n";
122     printList(head);
123     rotate(&head, N);
124
125     cout << "\nRotated Linked list \n";
126     printList(head);
127
128     return 0;
129 }
```

**Output:**

```
Given linked list  
a b c d e  
Rotated Linked list  
c d e a b
```

## Priority Queue using Doubly Linked List

Given Nodes with their priority, implement a priority queue using doubly linked list.

- `push()`: This function is used to insert a new data into the queue.
- `pop()`: This function removes the element with the lowest priority value form the queue.
- `peek() / top()`: This function is used to get the lowest priority element in the queue without removing it from the queue.

**Approach :**

1. Create a doubly linked list having fields info(hold the information of the Node), priority(hold the priority of the Node), prev(point to previous Node), next(point to next Node).
2. Insert the element and priority in the Node.
3. Arrange the Nodes in the increasing order of priority.

```
1 // C++ code to implement priority  
2 // queue using doubly linked list  
3 #include <bits/stdc++.h>  
4 using namespace std;  
5  
6 // Linked List Node  
7 struct Node {  
8     int info;  
9     int priority;  
10    struct Node *prev, *next;  
11};  
12  
13 // Function to insert a new Node  
14 void push(Node** fr, Node** rr, int n, int p)  
15 {  
16     Node* news = (Node*)malloc(sizeof(Node));  
17     news->info = n;  
18     news->priority = p;
```

```

20     // If linked list is empty
21     if (*fr == NULL) {
22         *fr = news;
23         *rr = news;
24         news->next = NULL;
25     }
26     else {
27         // If p is less than or equal front
28         // node's priority, then insert at
29         // the front.
30         if (p <= (*fr)->priority) {
31             news->next = *fr;
32             (*fr)->prev = news->next;
33             *fr = news;
34         }
35
36         // If p is more rear node's priority,
37         // then insert after the rear.
38         else if (p > (*rr)->priority) {
39             news->next = NULL;
40             (*rr)->next = news;
41             news->prev = (*rr)->next;
42             *rr = news;
43         }
44
45         // Handle other cases
46         else {
47
48             // Find position where we need to
49             // insert.
50             Node* start = (*fr)->next;
51             while (start->priority > p)
52                 start = start->next;
53             (start->prev)->next = news;
54             news->next = start->prev;
55             news->prev = (start->prev)->next;
56             start->prev = news->next;
57         }
58     }
59 }
60
61 // Return the value at rear
62 int peek(Node* fr) { return fr->info; }
63
64 bool isEmpty(Node* fr) { return (fr == NULL); }
65
66 // Removes the element with the
67 // least priority value form the list
68 int pop(Node** fr, Node** rr)
69 {
70     Node* temp = *fr;
71     int res = temp->info;
72     (*fr) = (*fr)->next;
73     free(temp);
74     if (*fr == NULL)

```

```

75     *rr = NULL;
76     return res;
77 }
78
79 // Driver code
80 int main()
81 {
82     Node *front = NULL, *rear = NULL;
83     push(&front, &rear, 2, 3);
84     push(&front, &rear, 3, 4);
85     push(&front, &rear, 4, 5);
86     push(&front, &rear, 5, 6);
87     push(&front, &rear, 6, 7);
88     push(&front, &rear, 1, 2);
89
90     cout << pop(&front, &rear) << endl;
91     cout << peek(front);
92
93     return 0;
94 }
95

```

**Output:**

```

1
2

```

## Reverse a doubly linked list in groups of given size

Given a doubly linked list containing **n** nodes. The problem is to reverse every group of **k** nodes in the list.

**Input :** DLL: 10<->8<->4<->2

k = 2

**Output :** 8<->10<->2<->4

**Input :** 1<->2<->3<->4<->5<->6<->7<->8

k = 3

**Output :** 3<->2<->1<->6<->5<->4<->8<->7

**Approach:** Create a recursive function say **reverse(head, k)**. This function receives the head or the first node of each group of **k** nodes After reversing the group of **k** nodes the function checks whether next group of nodes exists in the list or not. If group exists then it makes a recursive call to itself with the first node of the next group and makes the necessary adjustments with the next and previous links of that group. Finally it returns the new head node of the reversed group.

```
1 // C++ implementation to reverse a doubly linked list
2 // in groups of given size
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 // a node of the doubly linked list
8 struct Node {
9     int data;
10    Node *next, *prev;
11 };
12
13 // function to get a new node
14 Node* getNode(int data)
15 {
16     // allocate space
17     Node* new_node = (Node*)malloc(sizeof(Node));
18
19     // put in the data
20     new_node->data = data;
21     new_node->next = new_node->prev = NULL;
22     return new_node;
23 }
24
25 // function to insert a node at the beginning
26 // of the Doubly Linked List
27 void push(Node** head_ref, Node* new_node)
28 {
29     // since we are adding at the beginning,
30     // prev is always NULL
31     new_node->prev = NULL;
32
33     // link the old list off the new node
34     new_node->next = (*head_ref);
35
36     // change prev of head node to new node
37     if ((*head_ref) != NULL)
38         (*head_ref)->prev = new_node;
39
40     // move the head to point to the new node
41     (*head_ref) = new_node;
42 }
43
44 // function to reverse a doubly linked list
45 // in groups of given size
46 Node* revListInGroupOfGivenSize(Node* head, int k)
47 {
```

```

48     Node *current = head;
49     Node* next = NULL;
50     Node* newHead = NULL;
51     int count = 0;
52
53     // reversing the current group of k
54     // or less than k nodes by adding
55     // them at the beginning of list
56     // 'newHead'
57     while (current != NULL && count < k)
58     {
59         next = current->next;
60         push(&newHead, current);
61         current = next;
62         count++;
63     }
64
65     // if next group exists then making the desired
66     // adjustments in the link
67     if (next != NULL)
68     {
69         head->next = revListInGroupOfGivenSize(next, k);
70         head->next->prev = head;
71     }
72
73     // pointer to the new head of the
74     // reversed group
75     return newHead;
76 }
77
78 // Function to print nodes in a
79 // given doubly linked list
80 void printList(Node* head)
81 {
82     while (head != NULL) {
83         cout << head->data << " ";
84         head = head->next;
85     }
86 }
87
88 // Driver program to test above
89 int main()
90 {
91     // Start with the empty list
92     Node* head = NULL;
93
94     // Create doubly linked: 10<->8<->4<->2
95     push(&head, getNode(2));
96     push(&head, getNode(4));
97     push(&head, getNode(8));
98     push(&head, getNode(10));
99
100    int k = 2;

```

```

101
102     cout << "Original list: ";
103     printList(head);
104
105     // Reverse doubly linked list in groups of
106     // size 'k'
107     head = revListInGroupOfGivenSize(head, k);
108
109     cout << "\nModified list: ";
110     printList(head);
111
112     return 0;
113 }
114

```

## Output

```

Original list: 10 8 4 2
Modified list: 8 10 2 4

```

## Time Complexity: O(n).

We can further simplify the implementation of this algorithm using the same idea with recursion in just one function.

```

// function to Reverse a doubly linked list
// in groups of given size
Node* reverseByN(Node* head, int k)
{
    if (!head)
        return NULL;
    head->prev = NULL;
    Node *temp, *curr = head, *newHead;
    int count = 0;
    while (curr != NULL && count < k) {
        newHead = curr;
        temp = curr->prev;
        curr->prev = curr->next;
        curr->next = temp;
        curr = curr->prev;
        count++;
    }
    // checking if the reversed LinkedList size is
    // equal to K or not
    // if it is not equal to k that means we have reversed
    // the last set of size K and we don't need to call the
    // recursive function
    if (count >= k) {
        head->next = reverseByN(curr, k);
    }
    return newHead;
}

```

# Thankyou

To be continued....