e-Edge Education Centre

EEE- CONCEPT CAPSULE (CO-ORDINATE GEOMETRY)

GEOMETRY

CO-ORDINATE

The coordinates of a point on x-axis are of the form (x, 0) and a point on y-axis are of the form (0, y).

Section Formula

The co-ordinates of the point which divides the join of points $A(x_1, y_1)$ and $B(x_2, y_2)$ internally in the ratio m: n are

$$\left(\frac{mx_2+nx_1}{m+n}, \frac{my_2+ny_1}{m+n}\right)$$

Distance Formula

The distance between two points $A(x_1, y_1)$ and $B(x_2, y_2)$ is given by

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The distance of a point P(x, y) from the origin O(0, 0) is given by

$$OP = \sqrt{x^2 + y^2}$$

Mid Point Formula

The coordinates of the mid point of line segment joining the points $A(x_1, y_1)$ and $B(x_2, y_2)$ are

$$\left(\frac{x_1+x_2}{2},\frac{y_1+y_2}{2}\right)$$

Area of Triangle

The area of a triangle with vertices $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ is

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$\frac{1}{2}[(x_1y_2 + x_2y_3 + x_3y_1)$$

$$-(x_1y_3+x_2y_1+x_3y_2)]$$

Centroid Formula

The coordinates of centroid of the triangle formed by the points $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ are

$$\frac{x_1+x_2+x_3}{3}$$
, $\frac{y_1+y_2+y_3}{3}$

- In a parallelogram, diagonals bisect each other.
- In a square all four sides are equal and both diagonals are equal.
- In a rectangle opposite sides and both diagonals are equal.

Collinear Points

Three points $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ are collinear if area of triangle formed by these points is zero.

Three points A, B, C are collinear if AB + BC = AC i.e., sum of distances between two pairs of points is equal to distance between third pair.