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Time : 2 hrs Class X **Mathematics** 1. Write a rational expression whose numerator is a quadratic polynomial with zeros (4) 2 and -1 and whose denominator is a quadratic polynomial with zeros $\frac{1}{2}$ and 3. 2. Which term of the AP: 3,15,27,39..... will be 132 more than its 54th term. (4) **3.** For what value of k is the H.C.F of $x^2 + x - (2k + 2)$ and $2x^2 + kx - 12$ is x + 4? (4) **4.** Solve the following system of equations: (4) $\frac{x+1}{2} + \frac{y-1}{3} = 8$ and $\frac{x-1}{3} + \frac{y+1}{2} = 9$ 5. Solve: $\frac{2x}{x-3} + \frac{1}{2x+3} + \frac{3x+9}{(x-3)(2x+3)} = 0$ (4) **6.** Find the sum of the first n natural numbers. (5) 7. D is a point on the side BC of a tangle ABC such that \angle ADC = \angle BAC. Prove (5) that $\frac{CA}{CD} = \frac{CB}{CA}$ 8. The circle passing through the vertices A, B and C of a parallelogram ABCD (5) intersects side CD at the point P. Prove that AP = AD. [3] 9. Show, graphically that the following system of equations had no solutions: (5) 2x + 3y - 1 = 0 and $x + \frac{3}{2}y - 2 = 0$. **10.** If $S = \frac{n(n+1)}{2}$, Find n, if S = 276. (5) 11. A petrol tank is a cylinder of base diameter 21 cm and length 18 cm fitted (5)with conical ends each of axis-length 9 cm. Determine the capacity of the tank. 12. Prove: $\frac{\sin\theta + \cos\theta}{\sin\theta - \cos\theta} + \frac{\sin\theta - \cos\theta}{\sin\theta + \cos\theta} = \frac{2}{1 - 2\cos^2\theta} = \frac{2}{2\sin^2\theta - 1}$ (5)13. Construct a quadrilateral similar to a given quadrilateral ABCD in which AB = (5) 6.3 cm, BC = 5.2 cm, CD = 5.6 cm, DA = 7.1 cm and angle B = 600, whose side are $\frac{4}{5}$ th of the corresponding sides of ABCD. **14.** If the vertices A, B and C of the triangle ABC be (x_1, y_1) , (x_2, y_2) and (x_3, y_3) (5) respectively. Prove that the coordinates of centroid be($\frac{x_1 + x_2 + x_3}{3}$, $\frac{y_1 + y_2 + y_3}{3}$) **15.** The length of a line-segment is 10. If one end at (2, -3) and the abscissa of (5) the second end is 10, show that its ordinate is either 3 or -9. **16.** The mean of the following frequency table is 50, but the frequencies f_1 and f_2 (5)in classes 20-40 and 60-80 respectively are not know. Find these frequencies. Class: 0-20 20-40 40-60 60-80 80-100 Total

32

f2

f1

Fre(f): 17



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(5)

- **17.** A bag contains 5 red balls and some blue balls. If the probability of drawing a blue ball is double that of a red ball, find the number of blue alls in the bag.
- **18.** Prove, there is one and only one circle passing through three non-collinear point. Two chords AB and CD of lengths 5 cm and 11 cm respectively of a circle are parallel to each other and are on the same side of its centre. If the distance between AB and CD is 3 cm, find the radius of the circle.
- **19.** As observed from the light house, 100 m high above sea level, the angle of depression of a ship, sailing directly towards it, changes from 30° to 45°. Determine the distance traveled by the ship during the period of observation.
- **20.** Water in a canal, 30 dm wide and 12 dm deep is flowing with velocity of 10 km per hour. How much area will it irrigate in 30 min., if 8 cm of standing water is required. (5)
- 21. Prove, if two circles touch other internally, the point of contant lies on the lies on the line joining their centre. (5)

AB is a line-segment and M is its mid-point. Semicircles are drown with AM,MB and AB as diameters on the same side of the line AB. A circle is drawn to touch all the tree semicircles. Prove that its radius r is given by r=16 AB.