Improving the discovery of Motifs in high-dimensional sequences of varying length

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Abstract

Acknowledgements

Many thanks to my mummy for the numerous packed lunches; and of course to Igor, my faithful lab assistant.

Declaration

I declare that this thesis was composed by myself, that the work contained herein is my own except where explicitly stated otherwise in the text, and that this work has not been submitted for any other degree or professional qualification except as specified.

(*M. Adnan Haider*)

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Chapter 1

Introduction

Over the course of the last decade, the mining of time-series data have received considerable attention within the data mining and machine learning community. The term 'time series' denotes a set of observations concurring any activity against different periods of time. The duration of time period may be in the order of microseconds or monthly or even annually depending on the domain. Mathematically, a time series is defined by the values $y_1, y_2 ... y_n$ at times $t_1, t_2 ... t_n$ where $y = f(t)$. The time t_i acts as an independent variable to estimate dependent variables y_i. The dimensionality of the series is denoted as **n** where '**n**' denotes the length of the sequence.

Time series analysis is used in many applications ranging from sales forecasting, budgetary analysis, stock market analysis and many more. One particular domain where the application of time series analysis is currently very popular is *motif* discovery- the problem of efficiently locating frequent/interesting sub-patterns in the data. The knowledge of motifs has been seen to have important applications in various aspects of data mining tasks. For instance:

- The discovery of association rules the reflect information of 'primitive shapes[1].

- The clustering of data into meaningful subgroups. Clustering is one of the most frequently used data mining tasks. It involves an unsupervised process for partitioning a dataset into meaningful groups. Such algorithms need to be specified on the initial seed of points and the number of cluster of groups. Motifs could potentially be used to address both

problems. In addition, seeding the algorithm with motifs rather than random points could speed up convergence [17].

- The identification of important sub-patterns in DNA and gene sequences[11]

In the analysis of speech data, motifs also play a very important role. Recent research have shown that detecting and isolating motifs in speech utterances is equivalent to extracting frequent spoken words or linguistic entities spoken by the speaker(s) [3,5]. These methodologies are based on understanding the underlying structure of the observed data and operate on the acoustic signal directly(i.e there is no intermediate recognition stage to map the audio signal to a symbolic representation). This allows the word acquisition process to be unsupervised which is completely a different approach to the current speech recognition systems that are built using a supervised training methodology employing manually transcribed speech to model the underlying speech process.

To identify and extract motifs from time series data, various clustering algorithms have been proposed. The most widely used and popular approaches include the use of:

1. Dynamic time warping algorithm(DTW) [2,3,4,5,6,11] that clusters similar sequences separated by time shifts or temporal dynamics

2. Single value decomposition(SVD)12]. The entire time series data set can be approximated by a low-rank approximation matrix achieved through transforming the data into an orthogonal feature space whose dimensionality is much lower than the original data sequences.

But unfortunately, directly applying these clustering algorithms to the features i.e the individual time series points may not lead to appealing results. Although the DTW algorithm is immune towards patterns shifted in time or distorted in size/shape, the time complexity of computing the DTW distance of two series is quadratic and is dependent on the dimensionality of the sequences or in other words the length of the sequences. To address this issue, linear-time constrained versions of DTW (Itakura parallelogram[19], Sakoe-Chiba band[18]) are used to constraint the size of the search space but the use of such constraints impact the accuracy of the algorithm[20].

The SVD too, also suffers from similar problems. For data sets where the dimensionality of the data is much higher than the sample size, the computational cost associated with the factorisation of the matrix is quite large. Apart from the computational cost, one of the main constraints of applying SVD is the requirement for all samples to share the same dimension which in the context of time series data means sequences must share the same length. This constraint greatly reduces the type of time series domains to which SVD can be applied to extract latent factors that denote motifs. The speech corpus is an example of one such domain. Data sets comprised of speech utterances are a good example where recorded utterances do not share the same dimensionality (i.e the same length) and signals that are acoustically similar may be a contracted/ expanded version of each other.

The discovery of motifs in high dimensional time series data(i.e long sequences) that vary in length is still a difficult problem to work with. To address the drawbacks of DTW and SVD, there has been some recent work conducted to improve these algorithms. In the paper " *Fast time series classification using numerosity reduction*", the authors address the drawbacks of DTW in handling high dimensional sequences. They propose an adaptive approach that initially uses a strict window constraint to reduce the search space of DTW but then gradually increase size of the window by discarding samples from the training set. Although this methodology improves the time complexity of the dynamic time warping algorithm by heuristically discarding regions in the input space, the methodology is more tailored to smart data selection rather than improving the algorithm itself. In the case of SVD, for high dimensional time series sequences which vary in length, the data matrix suffers in being incomplete. Carelessly addressing only the relatively few known entries is highly prone to over tting. Earlier works [21] relied on imputation to fill in missing ratings and make the rating matrix dense. However, imputation can be very expensive as it significantly increases the amount of data. In addition, the data may be considerably distorted due to inaccurate imputation.

The goal of this project is to improve the performance of these algorithms in handling time series sequences that have high dimensionality and vary in length . To be precise, in the first half of the project, I will be investigating

data mining and machine learning methods to improve the speed of the DTW algorithm **without** degrading the accuracy. And in the second half I will be ...

For this project, I will be using 3 time series data sets (details in chapter 2):

- TIGITS

- INLINESKATE

- CINC_ECG_TORSO

For a majority portion of the analysis, the TIDIGITS corpus will serve as the primary dataset used to investigate the performances of different models. The reason being the TIGITS corpus consists of long time series sequences that vary in length . Since each time sequence corresponds to a speech utterance spoken by a speaker, as result of environment, context and speaker differences the length of the time series sequences will not be the same. In comparison, the sequences with in each UCR data set share the same dimensionality i.e length. Furthermore, the length of the time series sequences on average is much higher in the TIDIGITS corpus than sequences of any data set in the UCR time series database.Thus the TIDIGITS data set is an ideal choice to investigate the performance of different models in my project.

The dissertation is organised as follows: Chapter 2 gives a description of the 3 time-series datasets used for this project. Chapter 4 provides a detailed back ground description of the DTW algorithm. Chapter 3 and 4 investigates methods to improve the performance of the DTW algorithm in terms of both accuracy and speed. Chapter4...

Chapter 2

Datasets

The primary dataset that I have used for this project is the 'TIGITS' corpus. (I need to give more description here)

For Training : The entire training data is used –To contain the computational complexitiy, I am usig samples from production 'a'

For the training set : To reduce the average mean time , I am using half of the training data set by choosing samples from one production: I have chosen:

225 samples from the boy category

234 samples from the girl category

495 samples from the men category

513 samples from the women category

Note : the size of the training set is half of the original training set but contains examples of all classes [1-9]

For the test set : Due to the high computational complexity, I am using only 1/3 of the test set I have chosen 162 random samples from boys

162 random samples from girls

326 random samples from men

326 random samples from women

Apart from the TIGITS, I have used two datasets from the UCR database:

The description of the data sets used for the next set of experiments are as follows:

1. CinC_ECG_torso

   - Length of the time series:1639

   - Size of test set:1380

   - Size of training set:40

   - Number of classes:4

2. InLineSkate

   - Length of the time series:1882

   - Size of test set:550

   - Size of training set:100

   - Number of classes:7

Chapter 3

DTW-Background

The Dynamic Time Warping algorithm measures the similarity between sequences varying in both time and speed. Formally, the problem formulation of the algorithm is stated as follows: Given two time series X, and Y, of lengths $|X|$ and $|Y|$,

$$X = x_1, x_2...x_{|X|} \tag{3.1}$$
$$Y = y_1, y_2...y_{|Y|} \tag{3.2}$$

construct a warping path W

$$W = w_1, w_2...w_k \text{ where max } (|X|, |Y| \leq k \leq |X| = |Y|$$

- Here k denotes the length of the warping path and the mth element of the warping path is $w_l = (n_l, m_l) \in [1:N] \times [1:M]$ for $l \in [1:k]$ where n_l is an index from the time series X and m_l is an index from the time series Y.

To properly understand the mechanism of the DTW algorithm, the definition of some key terminologies must first be stated:

1. Warping path: An (N,M)-warping path (or simply referred to as warping path if N and M are clear from the context) is a sequence $w = (w_1, ..., w_k)$ with $w_l = (n_l, m_l) \in [1:N] \times [1:M]$ for $l \in [1:k]$ satisfying the following three conditions.

(a) Boundary condition: $p_1 = (1,1)$ and $p_k = (N,M)$. The boundary condition enforces that the first elements of X and Y as well as the last elements of X and Y to be aligned with each other. In other words, the alignment refers to the entire sequences X and Y.

(b) Monotonicity condition requires that the path will not turn back on itself, both the i and j indexes either stay the same or increase, they never decrease.

(c) Step-size condition: $p_{l+1} - p_l \in \{(1,0),(0,1),(1,1)\}$ for $l \in$ [1:k-1]. The step size con- dition expresses a kind of continuity condition: no element in X and Y can be omitted and there are no replications in the alignment

Intuitively speaking, the (N,M)warping path$p = (p_1,...,p_k)$defines an alignment between two sequences $X = (x_1,x_2,...,x_N)$ and $Y = (y)1,y_2,...,y_M)$ by assigning the element x_i of X to the element y_j of Y.

2. Optimum Warping Path :

The optimal warp path corresponds to the minimum-distance warp path, where the distance of a warp path W is given as

$$Dist(W) = \sum_{i=1}^{K} dist(X,Y)_{|(w_i)}$$

$dist(X,Y)_{|(w_i)}$ represents the distance computed using an appropriate cost function between the time series points of x_{ni} of sequence X and y_{mi} of sequence Y.

$$dist(X,Y)_{|(w_i)} = dist(x_{ni},y_{mi})$$

The goal of the DTW algorithm is to compute the distance of the optimal warping path between two time series sequences. Instead of attempting to solve the entire problem all at once, the algorithm utilises the technique of dynamic programming to find an optimum alignment between two sequences through the computation of local distances between the points in the temporal sequences. The algorithm proceeds by iteratively filling in values for each cell (i,j) in the $|X|$ by $|Y|$ cost matrix D. The value of the cell (i,j) is given by

$D(x_{ni}, y_{mj})$ which corresponds to the minimum- distance warp path :

$$D(i, j) = Dist(i, j) + min(D(i-1, j), D(i-1, j-1), D(i, j-1))$$

An outline of the baseline DTW algorithm is given below:

Algorithm 1 Value-Based DTW

1: **procedure** VALUE-BASED(*seq*1, *seq*2) ▷ two raw sequences

2:      DTW= zeros(length(seq1)+1,length(seq2)+1)

3:      **for** i=1: to length(seq1) **do** ▷ Initialise the DTW cost matrix

4:          DTW(i,0) = ∞

5:      **end for**

6:      **for** i=1 to length(seq2) **do**

7:          DTW(0,i) = ∞

8:      **end for**

9:      **for** i=2 to length(seq1) **do**

10:          **for** j=2 to length(seq2) **do** ▷ cost(a,b)≡euclid(a,b)

11:          DTW(i,j) = cost(seq1(i),seq2(j)) + min{ DTW(i-1,j)+DTW(i,j-1)+DTW(i-1,j-1)}

12:          **end for**

13:      **end for**

14:      **return** result = $\dfrac{\text{DTW(n,m)}}{nm}$ ▷ n=length(seq1), m=length(seq2)

15: **end procedure**

The figure below gives an example of the optimal path found by the algorithm.
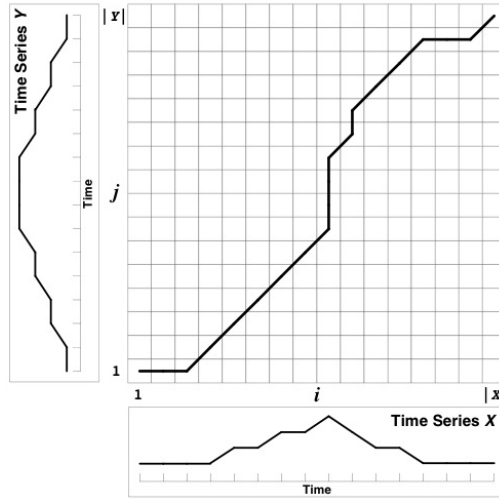
Figure 3.1: A cost matrix with the minimum-distance warp path traced through it.

The computational complexity of the DTW algorithm is $O(n^2)$ where n denotes the length of the sequences that are being compared. Thus for time series domains having high dimensions(long sequences), the time and computational costs incurred by the algorithm are quite high. To address this issue, two well-known global window constraints are employed: the Sakoe-Chiba band[18] and the Itakura parallelogram[19] . Figure 3.2 gives an illustration of the use of both constraints:
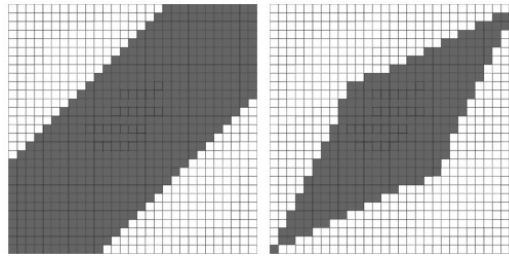
Figure 3.2: Two constraints: Sakoe-Chuba Band (left) and an Itakura Parallelogram (right), both have a width of 5.

The Sakoe-Chiba band runs along the main diagonal and has a fixed (horizontal and vertical) width .The Itakura parallelogram on the other hand describes a region that constrains the slope of a warping path. To constraint the time complexity to a minimum, the vast majority of the data mining researchers use a Sakoe-Chiba Band with a 10% width.

Chapter 4

Improving DTW

The Dynamic Time Warping(DTW) algorithm is the one of the oldest algorithms that is used to compare and cluster sequences varying in time, length and speed. Given two temporal sequences, the algorithm utilises the technique of dynamic programming to compute the cost of the optimum alignment path between them. The computed cost gives an indication of the degree of similarity. The smaller the cost, the more similar the sequences are.Intuitively speaking, DTW is a clustering algorithm that clusters similar patterns varying in time and speed. The time and computational complexity of this algorithm is $O(n^2)$ where n denotes the length of the sequences that are being compared. Thus for time series domains having high dimensions(long sequences), the time and computational costs incurred by the algorithm are quite high which makes DTW a very unattractive choice for clustering or discovering motifs in high dimensional data sets. Another drawback for working in high-dimensional spaces is the contrast between the distances of nearest and furthest points. The distances between such points become increasingly smaller as the dimensionality increases. This makes it difficult to construct meaningful cluster groups in such spaces.

To address the issue of the curse of dimensionality, DTW algorithms employ a window constraint to reduce the search space. The most commonly used are Sakoe-Chuba Band[18] and the Itakura window constraint[19]. Figure[3.2] gives an illustration on the nature of these window constraints. These constraints determine the allowable shapes that a warping path can take by

restricting the DTW to find an optimal warping path only through the constrained window. As the dimensionality(length) of the sequences increases, the size of the window is adjusted accordingly. Rigid window constraints impose a more rigid alignment that prevent an overly temporal skew between two sequences, by keeping frames of one sequence from getting too far from the other. The vast majority of the data mining researchers use a Sakoe-Chiba Band with a 10% width for the global constraint[23] to constraint the time complexity of DTW to a minimum. For clustering data sets such as speech utterances, the effect produced by such global constraints is highly undesirable. If we consider two utterances of a word spoken at different time frames, the patterns can have an overly temporal askew between them as result of the different contexts in which the words are spoken and/or as a result of different speakers speaking the same word. Thus it is necessary to explore alternative techniques to window constraints that can reduce the time complexity of the DTW algorithm to a minimum without decreasing accuracy.

Before investigating methods to improve the DTW algorithm itself, it is highly necessary to first understand the nature of the data sequences that the DTW is presented with. By achieving a thorough understanding of the data, we can achieve dimensionality reduction by isolating and identifying smaller set of new(current) features that are more relevant for the problem in hand. In this chapter, I investigate domain-dependent preprocessing techniques that can improve the DTW's performance by mapping the sequences to a lower dimensional space that captures the intrinsic structure of the data. There are presently two groups of preprocessing techniques commonly used to address this issue:

- Feature Selection

- Feature Extraction

Feature selection techniques involve selecting only a subset of attributes from the original data. With respect to the time series data, the process refers to sub-sampling the sequence. One of the most popular approaches to feature selection is the exploratory data analysis(EDA). EDA is an approach to data analysis that postpones the usual assumptions about what kind of model the data follows with the more direct approach of allowing the data itself to reveal

its underlying structure and models. The particular techniques employed in EDA are often quite simple, consisting of various techniques of:

1. Plotting the raw data such as data traces, histograms, histograms, probability plots, lag plots, block plots, and Youden plots.

2. Plotting simple statistics such as mean plots, standard deviation plots, box plots, and main effects plots of the raw data.

3. Positioning such plots so as to maximise our natural pattern-recognition abilities, such as using multiple plots per page.

Feature extraction processes on the other hand are concerned with the range of techniques that apply an appropriate functional mapping to the original attributes to extract new features. The intuition behind feature extraction is that the data vectors $\{x_n\}$ typically lie close to a non- linear manifold whose intrinsic dimensionality is smaller than that of the input space as a result of strong correlations between the input features. Hence by using appropriate functional mapping, we obtain a smaller set of features that capture the intrinsic correlation between the input features. By doing so, we move from working in high dimensional spaces to working in low dimensional spaces. The choice of appropriate functional mapping can also improve the clustering of data. For example, lets consider figure 4.1: The left- hand plot represents the locations of two dimensional data points in the original input space. The colours red and blue denote the classes to which the data points belong to. To cluster the data with respect to their classes, it will be ideal if we can partition the input space into disjoint regions where points belonging to the same class occupy the same region. This is achieved by mapping the points to a feature space spanned by two gaussian basis functions(shown on the right). Now, we can partition the feature space into two disjoint regions,, one of each cluster.
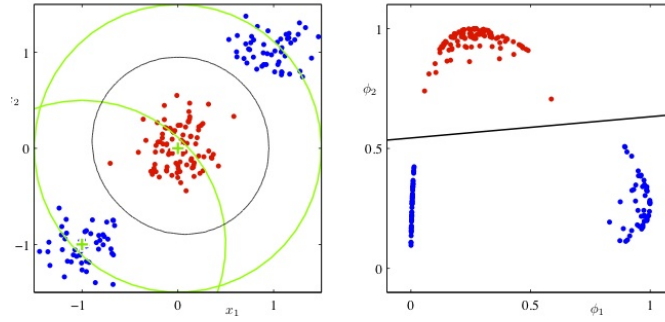
Figure 4.1: The figure on the right corresponds to location of the data points in the feature space spanned by gaussian basis functions $\phi_1(x)$ and $\phi_2(x)$

In the rest of this chapter, I explore a range of feature selection and extraction methods and investigate whether their application can improve the performance of the DTW algorithm in terms of both accuracy and time complexity.

4.1 Feature Selection

The computational and time complexity associated with the DTW algorithm is governed by the dimensionality of the time series. To get a feel of the data, I employed exploratory data analysis on the isolated word utterances belonging to the test and training data sets that I constructed from the TIDIGITS corpus. The aim here to identify and isolate redundant features from the time series data. To get an idea about the structure of the data, I have studied the plots of the time series sequences along with listening to the individual samples. Figure 4.2 gives the plot of raw signal corresponding to the word '8' by a speaker from the *boy* category. From the visual and auditory analysis, I have made the following observations:

- Long durations of silence occupy the beginning and end of each utterance. These durations of silence segments are considerably long compared to the interesting regions in the acoustic signal that actually contain information about the spoken digit . Removing these silence segments do not only reduce the dimensionality of the time series but also result in minimal loss of information.

- Through listening to numerous samples, I have discovered that the recordings are highly distorted when played in *matlab* even when the data is

scaled so that the sound is played as loud as possible without clipping. The distorted signal fails to provide any type of auditory clue about category of the speaker i.e whether the speaker belongs to { boy,girl, men,women} and the signal must be played multiple times for the word to be correctly identified.
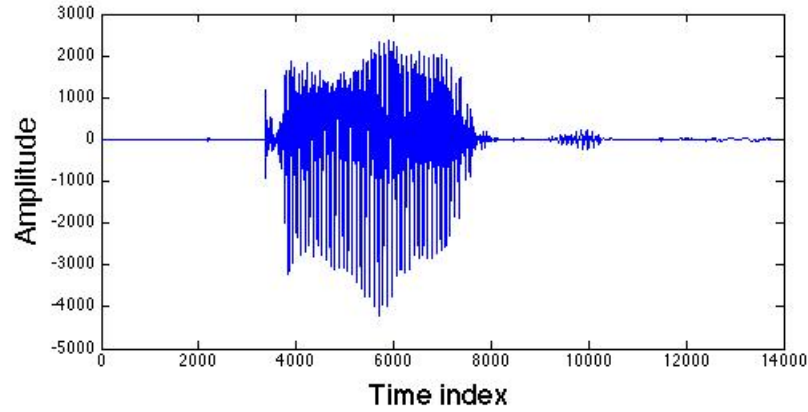
Figure 4.2: 'Raw 'signal

4.1.1 Signal Filter

Thus to remove these redundant attributes from the time series sequence, I have constructed the following algorithm: 'silencefilter' that performs feature selection by removing segments of silence. An outline of the algorithm is as follows:

Algorithm 2 SignalFilter

1: **procedure** SILENCEFILTER(*signal*)   ▷ raw signal
2:     $threshold = 0$
3:     maxAmplitude= max(rawSignal)
4:     Adapt the threshold based on the value taken by the maximum amplitude
5:     output← removeSilence(rawSignal,threshold)
6:     **return** output
7: **end procedure**

The algorithm removes all samples in the times series sequence whose magnitude is less than the threshold. The threshold used is an adaptive parameter. By using the information of the signal's maximum amplitude the algorithm

sets the threshold accordingly. It raises the threshold for signals correspond-
ing to speakers having a loud and deep voice and lowers the threshold for
signals corresponding to speakers having gentle and low voice.
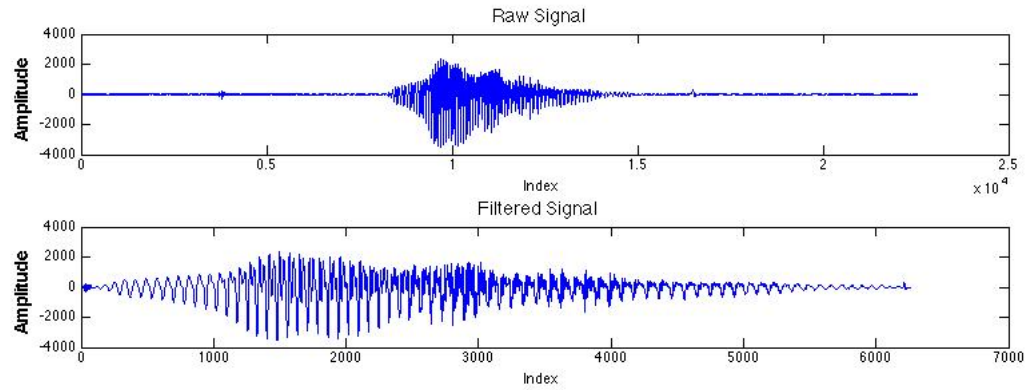
Figure 4.3: shows the raw acoustic signal corresponding to the utterances of the digit
'8' alongside with the version that has its dimensionality reduced by the filter discussed
above.

From figure 4.3, it can be observed that the filter preserves the interesting
patterns associated with the utterance while succeeding in reducing the di-
mensionality of the data. To investigate the effect of introducing this prior
feature selection step on the performance of the DTW algorithm , I conducted
the following experiment:

- Objective : Performance comparison between DTW equipped with a
  feature selection step against the based line DTW

- Dataset used: TIDIGITS Test-set size : 976 samples

category	sample size
boy	162
girl	162
men	326
women	326

Training data set size: 1467

category	sample size
boy	225
girl	234
men	495
women	513

- An outline of DTW used algorithm used for this experiment is given below.

Algorithm 3 Value-Based DTW

1: **procedure** VALUE-BASED(*seq*1, *seq*2) ▷ two raw sequences

2:     DTW= zeros(length(seq1)+1,length(seq2)+1)

3:     w = max($\lceil 0.1 * max(n.m) \rceil$, abs(n-m)) ▷ Window constraint

4:     **for** i=1: to length(seq1) **do** ▷ Initialise the DTW cost matrix

5:         DTW(i,0) = ∞

6:     **end for**

7:     **for** i=1 to length(seq2) **do**

8:         DTW(0,i) = ∞

9:     **end for**

10:     **for** i=2 to length(seq1) **do**

11:         **for** j=max(2, i-w) to min(length(seq2), i+w) **do** ▷ cost(a,b)≡euclid(a,b)

12:             DTW(i,j) = cost(seq1(i),seq2(j)) + min{ DTW(i-1,j)+DTW(i,j-1)+DTW(i-1,j-1)}

13:         **end for**

14:     **end for**

15:     **return** result = $\dfrac{\text{DTW(n,m)}}{nm}$ ▷ n=length(seq1), m=length(seq2)

16: **end procedure**

Note : The DTW algorithm is subjected to an adaptive window constraint. The focus of my research here is to improve the accuracy of the DTW algorithm while reducing the time and computational cost to a **minimum**. Even after applying the feature selection process, from initial experiments I have found the dimensionality of the time series sequences is still very high. Thus for these experiments, I have employed the Sakoe-Chuba band that is adaptive in size : w = max($\lceil 0.1 * max(n.m) \rceil$,

abs(n-m)). The lower bound of the window size is set to10% the size of the longest sequence because its is the standard size that the vast majority of the data mining researchers[23] use to keep the time complexity of DTW to a minimum.

- RESULTS:

Accuracy

	boy	girl	men	wo men
baseline+window constraint	8.90%	9.80%	9.60%	9.23%
Silence removed +window consraint	12.48%	12.96%	14.20%	14.95%

Figure 4.4

Log(time)

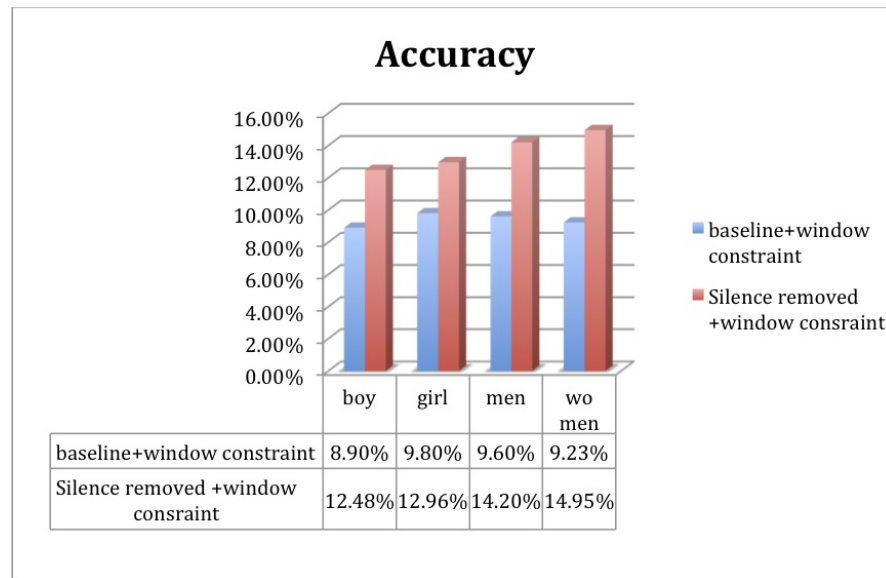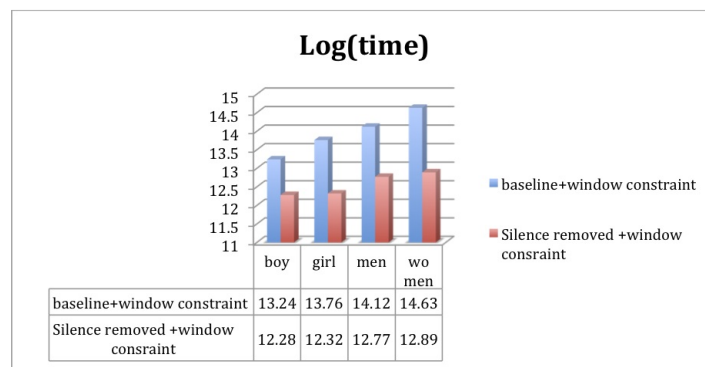|	boy	girl	men	wo men
baseline+window constraint	13.24	13.76	14.12	14.63
Silence removed +window consraint	12.28	12.32	12.77	12.89

Figure 4.5

Observations:

- From the results above, it can seen that the DTW algorithm achieves very poor accuracy. The reason for this lack of poor recall may be attributed to one or a combination of the following three factors:

- raw values- the value of a data point in a time series sequence is not a complete picture of the data point in relation to the rest of the sequence.

- window constraint- the optimum warping path exists outside the boundaries of the Sakoe-Chuba bands[3,6].

- not using MFCC values- The data set comprises of speech utterances. It is a widely known fact that for speech data, the MFCC feature vectors capture the information of phones that make up a word. Since different lexical identities are composed of different phones, these use of these vectors can provide effective clustering. (details of MFCC to follow)[3,4,5,6,7].

• Removing 'silence' segments improves **both** the accuracy and the time complexity of the algorithm. Reasons:

The DTW algorithm, aims to finds an optimum warping path in the search space bounded by the window constraints. Removing 'silence' segments proves to be highly advantageous because these 'silence' are present in all utterances. Thus there are not good discriminators for identifying different lexical identities. Taking these silences into account therefore degrades the performance of the DTW as they bring in an unwanted notion of similarity in dissimilar patterns.

The size of the DTW cost matrix is $O(mn)$. Achieving dimensionality reduction through feature selection reduces the size of the cost matrix and thus decreases the computational cost.

4.1.2 Downsampling

From further exploratory data analysis, I have observed that if I down-sample the utterances by $\frac{1}{2}$ which in other words means decreasing the sampling frequency by half, the resultant sampled signal is much clearer to understand. From the observation of figure 4.6, it can be seen that performing subsampling does keep the global trend of the signal intact but results in minute loss of local information. Furthermore through listening the sampled signals, I have discovered that losing some **local information** actually cleans the sig-

nal in a manner that allows the listener to identify the speaker's category and the lexical identity with ease.
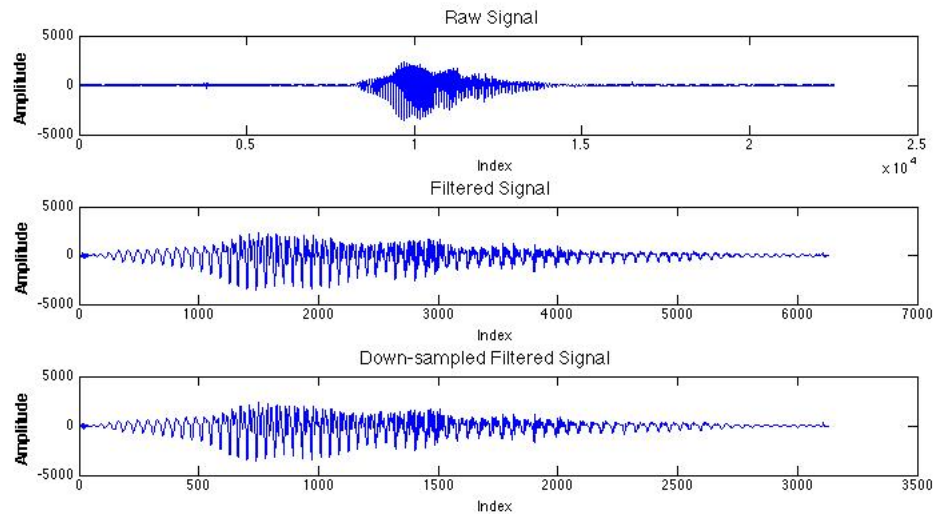
Figure 4.6: shows the raw acoustic signal of the digit '8' (top figure), the silence removed version of the signal(middle) and the silence removed and down sampled version of the acoustic signal (bottom)

To investigate whether performing further dimensionality reduction through downsampling improves the performance of the DTW, I conducted a third experiment using the same data set and the sample DTW algorithm discussed in 4.1.1. The results found are as follows:

	boy	girl	men	women
baseline+window constraint	8.90%	9.80%	9.60%	9.23%
Silence removed +window consraint	12.48%	12.96%	14.20%	14.95%
Silence removed+downsampling + window constraint	12.42%	11.18%	13.15%	13.42%

Figure 4.7: Performing silence removal followed by downsampling still achieves better accuracy than the base line DTW

Log(time)

	boy	girl	men	women
baseline+window constraint	13.24	13.76	14.12	14.63
Silence removed +window consraint	12.28	12.32	12.77	12.89
Silence removed +downsampling + window constraint	10.67	10.69	11.07	11.11

Figure 4.8: Integrating downsampling into the preprocessing step decreases the log(time)
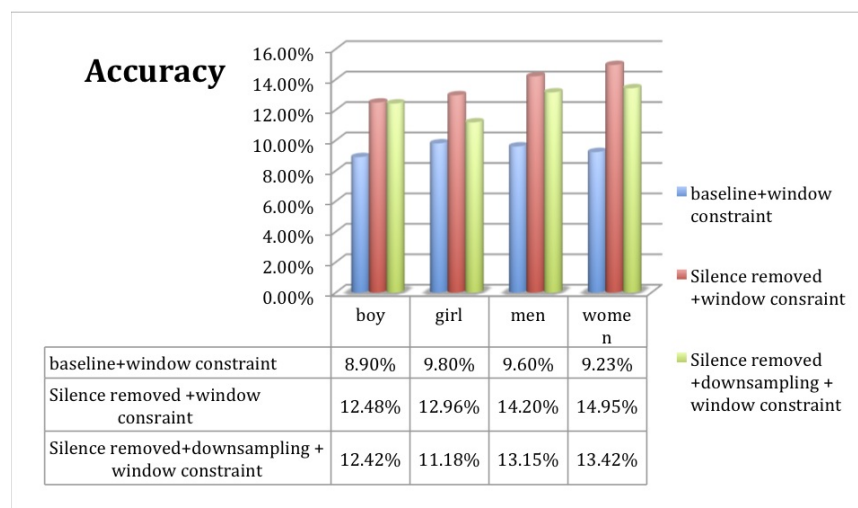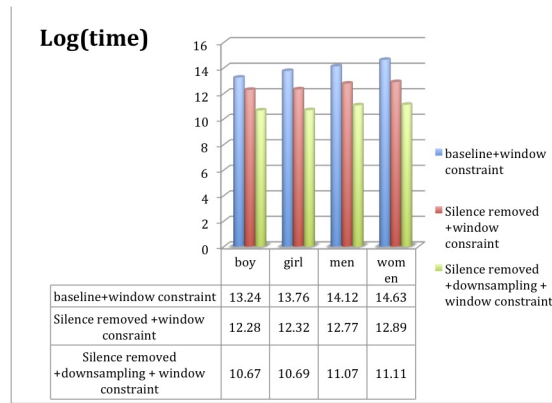
Observations:

- Performing down-sampling along with silence removal achieve a reduction in the log(time) by 1.5 on average. This is expected since in the first stage of the preprocessing phase, redundant features are dropped which reduces the dimensionality(i.e length) of the sequences. The length of the sequences is reduced even further through downsampling the the output sequences of stage 1. the computational cost of DTW is directly dependent on the length of the sequences, thus decrements in dimensionality leads to a decrease in the computational cost.

- Although the downsampling method seems to improve the quality of the signal from a listeners viewpoint, the accuracy of the DTW on the down-sampled sequences is seen to be actually less than the DTW algorithm that employs silence removal as the only pre-processing step. I found the cause of the anomaly to be 'soundsc' function of matlab. The function scales the acoustic signal as loud as possible without clipping causing the resultant signal hard to understand. The reason for the decrement in accuracy is quite obvious : removing attributes leads to a loss of information. The DTW's accuracy is reduced by 1% on average in comparison to the model that uses only silence removal as a pre-processing step. Even through loss achieves an accuracy that is 3% greater on average across the test data sets of all categories in comparison to the baseline DTW.

4.2 Feature extraction

From the analysis conducted so far, it can be concluded that heuristically selecting only significant attributes from the time series sequences does **improve** the accuracy and the speed of the DTW. However, from the observation of the experimental results,it is quite clear that the accuracy of the algorithm is very low. In this section, I investigate on the degree of influence that employing domain-dependent and domain dependent feature extraction methodologies have on the speed and accuracy of the DTW algorithm. There are two motivations behind conducting this analysis:

- The primary motivation is to investigate to what degree is this low error credited to not using features that incorporate information about the domain and the trends of the sequence and the degree of contribution that using a rigid window constraint has on the low accuracy . (The features that we have considered so far are the raw values indexed by time)

- The overall focus is to improve the speed of the DTW algorithm without degrading accuracy. By choosing an appropriate functional mapping, we can map the data to lower dimensional feature space that can captures the intrinsic qualities of the data. This not achieves dimensionality reduction of the time series sequences but also posses the potential to boost accuracy.

4.2.1 Domain-dependent feature extraction

The primary data set that I am working with for this project is the TIGITS corpus which is composed of speech utterances. For speech, the most commonly used features are the MFCC features-mel cepstrum ceptral coefficients. This feature representation is based on the idea of the cepstrum. For human speech, a speech waveform is created when a glottal source waveform of a particular frequency is passed through the vocal tract which because of its shape has a particular filtering characteristic. The exact position of the vocal tract is in fact the key attribute in providing useful information about phones(units of sounds). Cepstrum provides a useful way to separate the information of

the vocal tract from the glottal source.

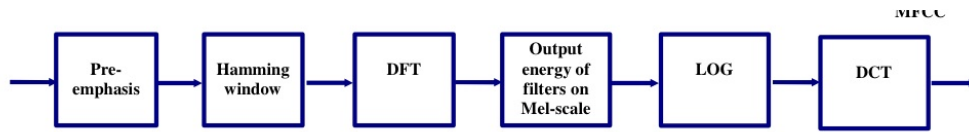A sketch of the MFCC feature extraction is given below:

Figure 4.9: MFCC feature extraction

i Pre-emphasis: boosts the energy of the signal at high frequencies to improve phone detection

ii Windowing: partitions the time series sequence into frames using a hamming window

iii DFT: extracts spectral information at different frequency bands

iv Mel scale : transforming to mel scale improves recognition performance by allowing the model to take into account the property of human hearing

v Log : makes the feature less sensitive to variations in input such as power variations on the speakers mouth.

vi Cepstrum : separate the information of the vocal tract from the glottal source. The first 12 cepstral values from spectrum of the log of the spectrum are used

Through the windowing process, the MFCC features extraction achieves dimensionality reduction. Each sequence is segmented into frames of length 20 to 30 ms which are then through appropriate functional mapping are converted into sequences of MFCC feature vectors. Since the result sequence of vectors is much smaller than the length of the original sequence resulting in the size of the DTW cost matrix is much smaller than before, This in turn lowers the time and computation cost incurred by the algorithm.

The experiments conducted in section 4.1.1 and 4.1.2, have shown that the DTW algorithm performs very poorly in terms of accuracy on the TIDIGITS test data when it employed a very constrained window to reduce the time complexity to a minimum. The reason for this low accuracy was narrowed

down to one or a combination of these factors : using a narrow window constraint, raw attribute values and not incorporating the use of domain and structural properties of the signal in the features(attributes). To investigate the influence of each these individual factors on the performance of DTW, I constructed the following 3 models:

i Model 1 employs MFCC feature extraction as a preprocessing step and then runs the DTW algorithm using the same window constraint mentioned in 4.1.1. The performance of this model can be used to investigate the contribution of using domain-dependent features in the performance of the DTW algorithm.

ii Model 2 employs a two stage preprocessing step. The feature selection procedure discussed in 4.1.1 is first applied to remove redundant features followed by MFCC feature extraction that achieves further dimensionality reduction(i.e reduction in length of the sequences) . In this model dimensionality reduction occurs at both stages of the preprocessing step. For these experiments, the downsampling method discussed in 4.1.2 was deemed not necessary because the feature extraction phase allows greater reduction in dimensionality without any loss of information. The sequence of vectors was then fed to the DTW algorithm augmented with the window constraint discussed in section 4.1.1.. The performance of this version of DTW can be compared with the version 1 DTW to decide on the pre-processing techniques that yields the best performance.

iii Model 3 is identical to the version 2 with the exception that this version does not employ the window constraint. The performance of this version of the DTW can be compared with the results found in section 4.1.1 and the performance of the other versions to investigate the influence of using window constraint on the accuracy of the DTW.

Experimental setup:

Data- set : The TIDIGITS training and test set (Chapter 2, 4.1.1)

RESULTS:
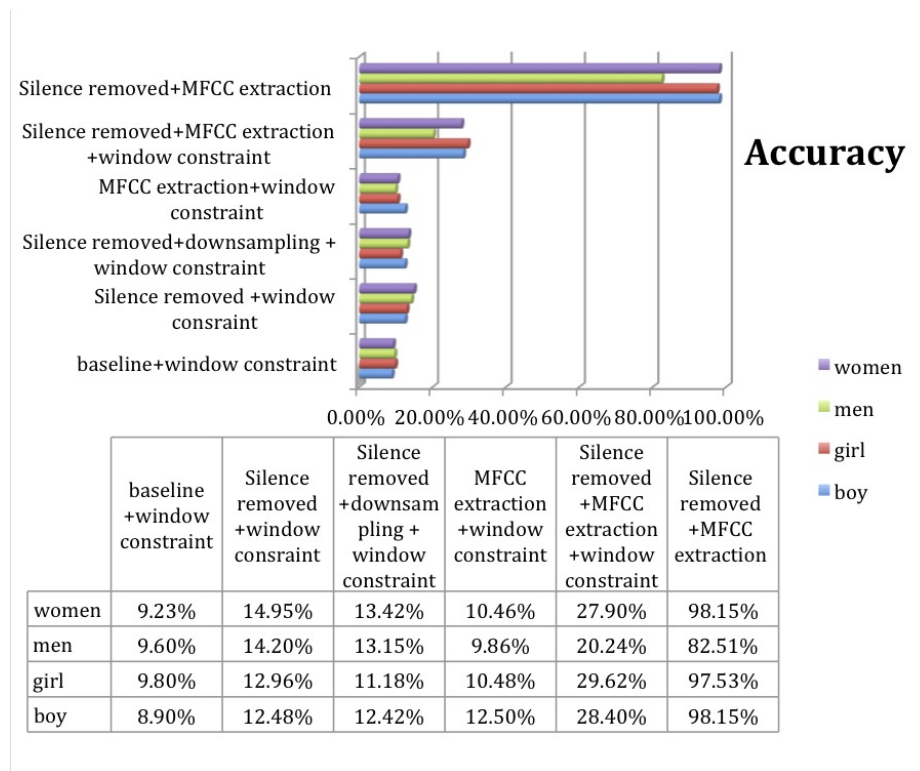
Figure 4.10: MFCC feature extraction

	baseline +window constraint	Silence removed +window consraint	Silence removed +downsam pling + window constraint	MFCC extraction +window constraint	Silence removed +MFCC extraction +window constraint	Silence removed +MFCC extraction
women	9.23%	14.95%	13.42%	10.46%	27.90%	98.15%
men	9.60%	14.20%	13.15%	9.86%	20.24%	82.51%
girl	9.80%	12.96%	11.18%	10.48%	29.62%	97.53%
boy	8.90%	12.48%	12.42%	12.50%	28.40%	98.15%
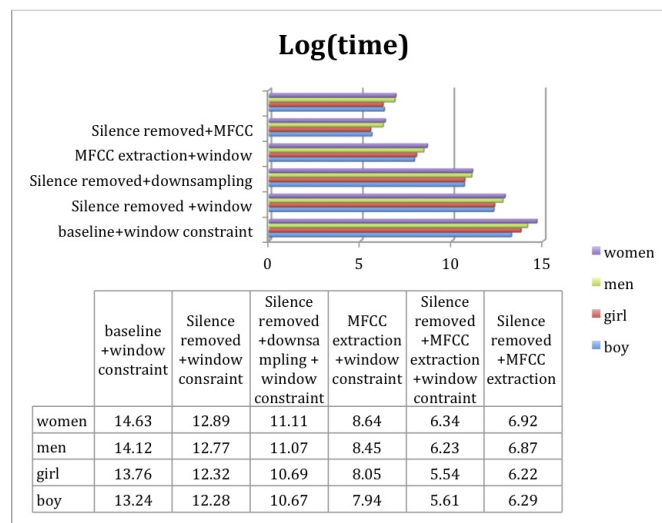
Figure 4.11: MFCC feature extraction

	baseline +window constraint	Silence removed +window consraint	Silence removed +downsa mpling + window constraint	MFCC extraction +window constraint	Silence removed +MFCC extraction +window contraint	Silence removed +MFCC extraction
women	14.63	12.89	11.11	8.64	6.34	6.92
men	14.12	12.77	11.07	8.45	6.23	6.87
girl	13.76	12.32	10.69	8.05	5.54	6.22
boy	13.24	12.28	10.67	7.94	5.61	6.29

Observations:

- Replacing raw values with MFCC features surprisingly only leads to a minimal increase in the accuracy of the DTW subjected to a window constraint. By comparing these results with the experiments done in 4.1.1,

it can observed that the presence of 'silence' forces the optimal warping path between utterances corresponding to identical lexical identities to occupy regions that are outside those that are bounded by the adaptive Sakoe-Chuba band constraints.

- Combining attribute/feature selection with MFCC feature extraction as a preprocessing step achieves greater improvement in accuracy and speed than using either of these approaches alone. In comparison to just using MFCC feature extraction as a preprocessing step, the algorithm's accuracy has been boosted up by 15.17% on average while the $log(time)$ have been reduced by 2.36. Similarly in comparison to just using feature selection as a preprocessing step, the algorithm's accuracy has increased by 12.9% on average while the $log(time)$ have been reduced by 6.5.

  From this observation alone, we deduce two facts, one of which is not that obvious: the accuracy of the DTW is governed by the removal 'silence' segments and the size of the Sakoe-Chuba band constraint. Since the main focus is to improve **both** the accuracy and speed of DTW in handling sequences of high-dimensionality i.e long lengths, removal of silence segments provides an ideal mechanism to improve the time complexity and the accuracy of the algorithm.

- Model 3 achieves almost near perfect accuracy. Dropping the window constraint improves the accuracy by 67.15% on average over model 2. Thus 67.15% times on avergage, the optimum warping path lay outside the regions bounded by the Sakoe-Chuba band constraints, This proves that patterns belonging to the same lexical identity can have an overly temporal askew between them as result of the different contexts in which the words are spoken and/or as a result of different speakers speaking the same word.

  Although removing the window constraint does degrade the time complexity in comparison to the log(time) cost of model 2, if we compare the log(time) of model 3 with the other models, we can observe that model 3 achieves lower $log(time)$ s than any of the model with the exception of model 2.

  Conclusion

Therefore from this analysis, it can be concluded that equipping DTW with preprocessing techniques constructed by performing exploratory data analysis and integrating metadata(i.e knowledge of the domain) can serve as an alternative to equipping the algorithm with rigid window constraints to handle high dimensional time series sequences in terms of both accuracy and speed.

Chapter 5

Extending DTW

So far, we have investigated methodologies that integrate meta data (i.e knowledge of the domain) in the pre-processing stage. The problem with such methodologies is that the same algorithm cannot be extended across multiple domains since the feature extraction process is highly domain-dependent. The MFCC feature vectors, for example, that we considered in the previous section can only be employed for data sets that comprise of speech utterances. In the first half of this chapter, I investigate feature extraction methodologies that are entirely data driven so that we can construct a methodology for improving DTW's speed and accuracy that can be extended across multiple domains. In the second half of this chapter, I investigate alternative measures to using window constraints that can improve the performance of the algorithm terms of **both** time and accuracy across all time series domains.

5.1   Domain-independent feature extraction

Ideally, we require features that reflect information about the structure of the data. This allows the DTW to built a complete picture of the data point in relation to the rest of the sequence and hence achieve better optimal alignments between similar sequences.The fundamental problem of baseline (value-based) DTW is that the numerical value of a data point in a time series sequence is not a complete picture of the data point in relation to the rest of the sequence. The context such as the position of the points in relation to their neighbours

is ignored. To fix this issue, an alternative form of DTW known as *derivative* DTW is proposed but it too fails to achieve better performance across all domains as it ignores to take into account the common sub-patterns between two sequences(mainly global trends).

For feature extraction, the methodology that I have used for this setup is based on Xie and Wiltgen's paper[2]. In their paper, the authors highlight a domain-independent feature extraction process where each point in the time series sequence is replaced by a 4 dimensional vector. In this vector, the first two features correspond to information regarding the local trends around a point and the last two features reflect the position of that point with respect to the global shape of the sequence. From experiments conducted on the UCR data sets, they have observed that embedding DTW with this feature extraction process yields greater accuracy across all datasets.

Definition of local feature given in [2] is as follows:

$$f_{\text{local}}(r_i) = (r_i - r_{i-1}, r_i - r_{i+1})$$

The first feature reflects the difference between the values of the current index and the previous index while the second feature reflects the difference between the values in the current index and the succeeding index.

The extraction of global features however, is constrained by two factors: the features must reflect information about global trends and must be in the same scaling order as the local features. Being in the same scale allows them to be combined with local features. In [2], the authors used the following method to extract global features from the time series sequence:

$$f_{\text{global}}(r_i) = (r_i - \sum_{k=1}^{i-1} \frac{r_k}{i-1}, r_i - \sum_{k=i+1}^{M} \frac{r_k}{M-i})$$

The first feature represents the deviation of the value of the current index from the mean of the values of the sequence that has been seen so far while the second feature represents the deviation of the current value from the mean of the values that is yet to be seen. This formulation allows the detection of significant 'drops' or 'rises' in the series.

Note : The local and global features have no definition for the first and last

points in a sequence.To keep the terminology clear, I to refer the length of the time series as the dimension of the time series. Each dimension i.e each point in the time series can be a value or in this case a 4-d vector.

When working with high dimensional time series(i.e sequences with long lengths) data, the main drawback of employing this feature extraction method is that it does not offer the advantage of dimensionality reduction. The dimensionality of a transformed time series sequence is just two dimensions less than the dimensionality of the original sequence. The DTW algorithm combined with this feature extraction process therefore suffers from the curse of dimensionality as before. To address this issue, the DTW algorithm is subjected to the adaptive Sakoe-Chuba band window constraint (4.1.1) that reduces the search space by restricting the algorithm to look for optimal paths only through limited cells in the DTW cost matrix.

Xie and Witgen[2] have already shown that augmenting this feature extraction methodology to the DTW algorithm does allow the algorithm to achieve better accuracy on datasets from different domains. However, due to the availability of sufficient computing power, they didn't use any window constraints when performing their experiments. For problem scenarios where the speed of the DTW is considered a priority, it will be interesting to investigate whether this methodology can allow DTW to achieve better performance in terms of accuracy over the base line method when subjected to the window constraint.

To investigate the effect of introducing this prior feature selection step on the performance of the DTW algorithm that employs a rigid window constraint, I conducted the following 2 experiment:

Objective Compare the affect of using global and local features to using raw values on the performance of the DTW subjected to a window constraint

- Experiment 1

  Datasets: TIDIGITS data set(4.1.1)

  To compare the effect on the accuracy between using only raw values, removing silence segments and using global and local features, as a prior step to the feature extraction process, I applied the feature selection process that I have discussed 4.1.1 to reduce the dimensionality of

the sequences compared the algorithm performance against the baseline model and the model that I had investigated in 4.1.1.

RESULTS

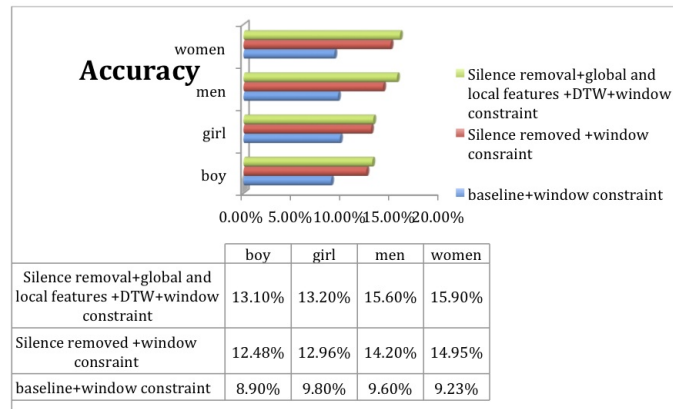A summary of the results are given below:

	boy	girl	men	women
Silence removal+global and local features +DTW+window constraint	13.10%	13.20%	15.60%	15.90%
Silence removed +window consraint	12.48%	12.96%	14.20%	14.95%
baseline+window constraint	8.90%	9.80%	9.60%	9.23%

Figure 5.1

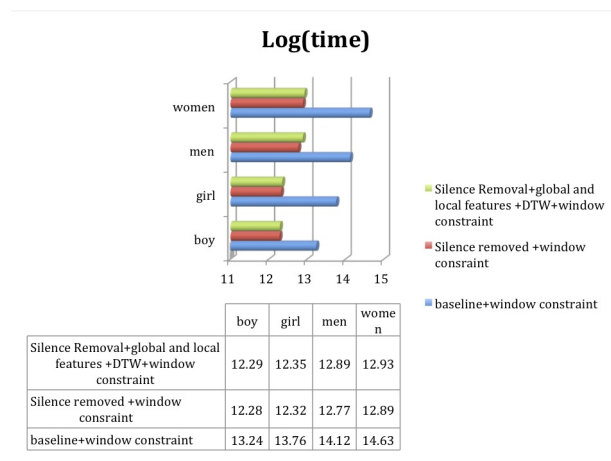|	boy	girl	men	women
Silence Removal+global and local features +DTW+window constraint	12.29	12.35	12.89	12.93
Silence removed +window consraint	12.28	12.32	12.77	12.89
baseline+window constraint	13.24	13.76	14.12	14.63

Figure 5.2

Observation:

Surprisingly, by comparing these results with the previous experiments, it can now concluded that for the TIDIGITS dataset(2.1), removing redundant features i.e removing regions of silence is a greater contributing factor in improving the performance of a window constrained DTW than applying a feature extraction process that integrates meta data(4.2.1) or that captures information about local and global trends. Using local

and global features only leads to an average improvement of 0.8% over the model that performs only silence removal as a preprocessing step.

One obvious observation is the poor performance shown by all 3 models in terms of accuracy. From the analysis conducted so far, the reason for this poor performance can be narrowed down to the use of the rigid window constraint imposed to minimise the time complexity.The computational cost incurred by the algorithm is higher than the version used for the model of 4.1.1 One possible explanation is that the cost of applying the euclidean metric on vectors >cost of applying the euclidean metric on points. Since the euclidean metric is applied *mn* times. The overall computational cost increases.

- Experiment 2 Datasets: UCR datasets: InlineSkate and Cinc_ECG_Torso
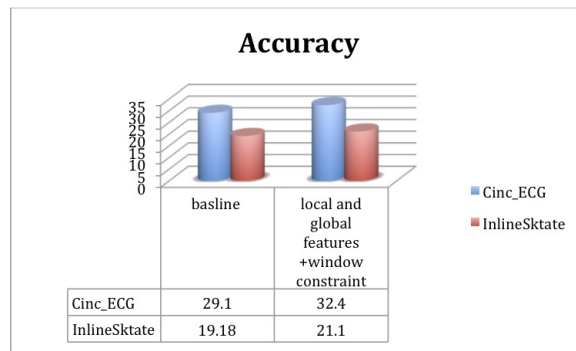
The results are as follows:

	basline	local and global features +window constraint
Cinc_ECG	29.1	32.4
InlineSktate	19.18	21.1

Figure 5.3: Using features that reflect information of trends improves the accuracy of the algorithm

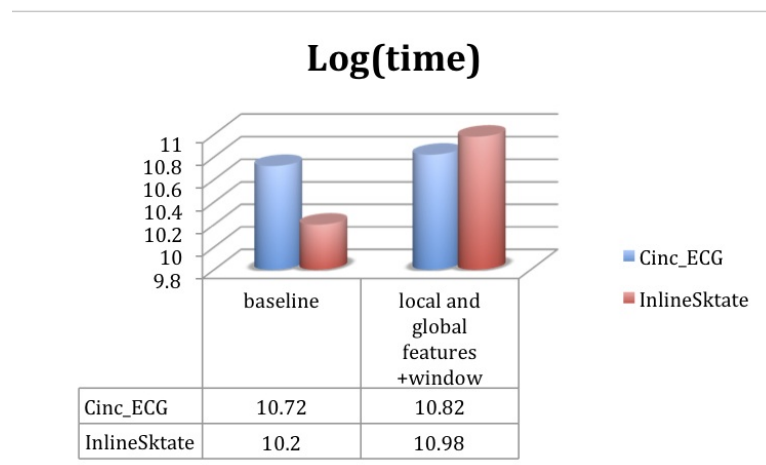|	baseline	local and global features +window
Cinc_ECG	10.72	10.82
InlineSktate	10.2	10.98

Figure 5.4: The computation time incurred

Observation

- The differences between performances of the two versions of DTW are consistent with the observations made in the previous experiment. For the Cinc_ECG_Torso time series data set, using global and local features improves the accuracy by 3.2% whereas for the InlineSkate data set, the accuracy improves by 1.92%. Thus it is safe to conclude that replacing each point in the time series sequence with a vector that reflect the relation of the point with the respect to the trends increase the number of the optimal warping paths that lie with in the regions bounded by the Sakoe-Chuba band constraint.The time complexity incurred by the algorithm under the new model is worse in comparison to the baseline model. Thus although we achieve an improvement in accuracy, we are loosing performance in speed. The accuracy of both the baseline and the current model is very low. This shows that a majority of the optimal warping between sequences belonging to the same class lie outside the Sakoe-Chuba band.

From the results of the experiments that has been conducted so far, it can be observed that the prominent factor responsible for the low accuracy of the DTW is the window constraint that keeps points(or vectors) of one sequence from getting too far from the other. Increasing the width of the Sakoe-Chuba band will although increase the accuracy of the DTW (as seen in 4.2) but will definitely cause an reduction in speed. One of the primary goals of this project is to improve the performance of the DTW in handling sequences of high dimensionality(i.e log lengths). Thus **minimising** time complexity is as important as improving the accuracy. This provides the motivation to investigate alternative methods that can a better balance between the two conflicting goals of accuracy and speed.

In the next section, I investigate a self-proposed method that is aimed to help DTW tackle the two conflicting objectives more effectively than using rigid window constraints. The new proposed methodology uses the data-driven feature extraction process that is discussed in the current section. The aim here to use the advantages presented by this domain independent feature extraction process [2] without being subject to the model's drawbacks.

5.2   Adapting DTW

The feature extraction methodology discussed above maps the time series sequence to a time series sequence of vectors whose length is $\|X_n\| - 2$. (where $\|X_n\|$ denotes the length of the original time series sequence). The DTW augmented with these features will still suffer from large time and computational complexity if the dimensionality of the data is high. In the MFCC feature extraction process, the time series sequence is first segmented into series of frames of length 20ms i.e 200 points. Through appropriate functional mapping, each frame is then mapped to a vector. Because the length of the resultant sequence of vectors is much smaller than the length of the original time series, the size of the DTW cost matrix. This reduces the search space and thus decrease the time complexity of the DTW algorithm.

Using the MFCC feature extraction method as motivation, in the proposed model the sequence of 4d vectors extracted using the feature extraction process discussed in 5.1 are segmented using windows of size 50 which in the case of the speech data corresponds to width of 5 ms . The original time series is reduced to series of matrices where the columns of the matrices consist of 4-d feature vectors corresponding to a particular time slice. The length of the series is now 50 times smaller than before. Now if we adapt the cost function of DTW to work on series of frames rather than series of vectors as before we can achieve a large improvement in both accuracy and computational cost associated than imposing a **window** constraint.

The problem now can be shifted to finding an appropriate kernel that can be used to compute the similarity between matrices composed of feature vectors. Ideally, we want a metric that takes into account the variation of speed and time when comparing two similar subsequences. We will want to compare the global and local properties associated with a point in one subsequence with the global and local properties of points at different regions in the second sub-sequence illustrated by figure 2. Using a euclidean metric in this scenario is inappropriate. The euclidean metric in this context is identical to linear time warping where the two subsequences will be matched based on a linear match of the two temporal dimensions. In our context, we need a kernel that computes the similarity between two sub-sequences by warping the time axis.

The motivation behind the kernel that I propose for aiding DTW to tackle high-dimensional sequences(i.e sequences with long lengths) comes from the polynomial kernel.

Let x and z be two dimensional vectors. Consider the simple polynomial kernel of degree 2 : $k(x,z) = (x^T z)^2$. This kernel can expressed as :

$$
\begin{aligned}
k(x,z) &= (x^T x')^2 \\
&= (x_1 z_1 + x_2 z_2)^2 \\
&= x_1^2 z_1^2 + 2 x_1 z_1 x_2 z_2 + x_2^2 z_2^2 \\
&= (x_1^2, 2 x_1 x_2, x_2^2)(z_1^2, 2 z_1 z_2, z_2^2)^T \\
&= \phi(x)^T \phi(z)
\end{aligned}
$$

The 2nd order polynomial kernel is equivalent to a corresponding feature mapping $\phi(x)$ that maps a two dimensional vector to $x_1^2, 2 x_1 x_2, x_2^2)$ where each attribute is monomial of order 2 . Generalising this notion to order M then $k(x,z) = (x^T z)^M$ contains all monomials of order M. Now, if we imagine x and z to be two images, then the polynomial kernel represents a particular weighted sum of all possible products of M pixels in the first image with M pixels in the second image.

Using this as motivation I propose the following kernel:.

$$
k(x,z) = < \sum_{i=1}^{n} x_i, \sum_{j=1}^{n} z_j >
$$

where n denotes the length of the window and x_i and z_j represents the 4-dimensional features indexed by the points in two sub-sequences.

To motivate the reasoning behind the construction of this particular kernel lets consider the following signals:
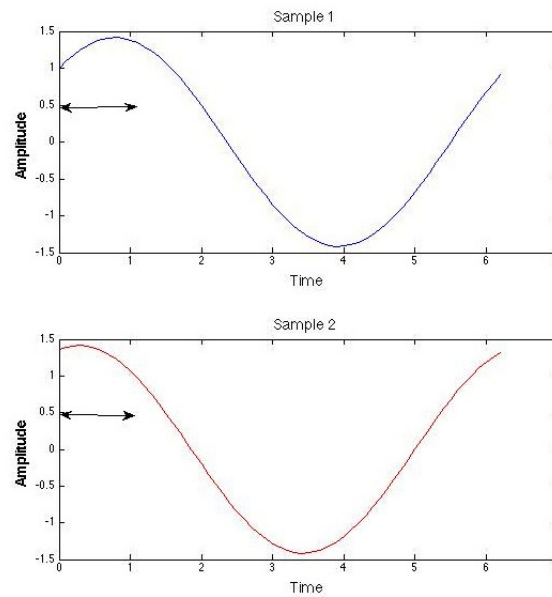
Figure 5.5: Two signals separated by translation

The signal denoted by the 'red' color is a 'slower' version of the signal denoted by the 'blue' color . In the above example, if we are comparing the similarity between the time slices spanned by the arrows, an ideal kernel must be invariant to the time offsets of the signals and thus should consider all possible pairings between the vectors in the subsequences. Intuitively speaking, the kernel must behave like a DTW algorithm.

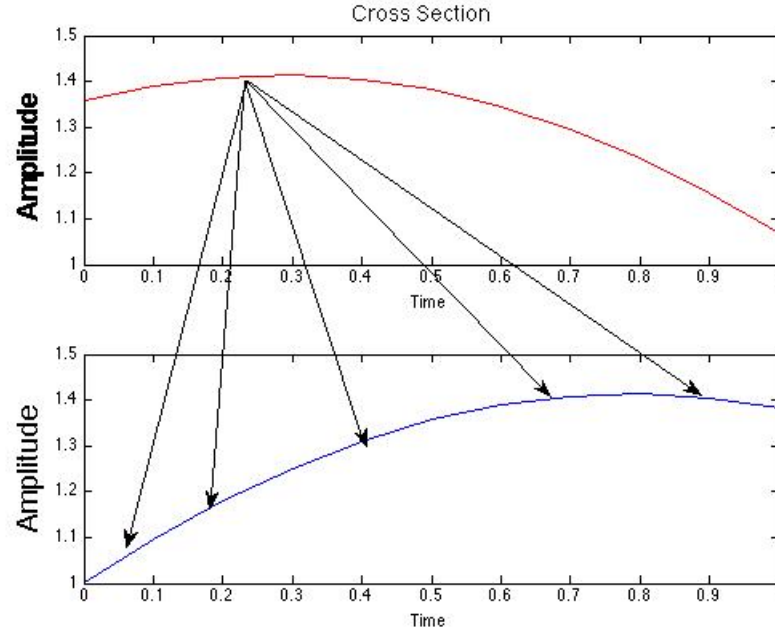Figure 5.6: Two identical subsequences varying in time

For time slices of width *n*, the kernel metric can be expanded and expressed as :

$$
\begin{aligned}
k(x,z) &= \ <\sum_{i=1}^{n} x_i, \sum_{j=1}^{n} z_i> \\
&= \ <(x_1+x_2+x_3+..),(z_1+z_2+z_3+..)> \\
&= \ <x_1,z_1>+<x_1,z_2>+<x_1,z_2>...+<x_2,z_1>+<x_2,z_2>+<x_2,z_3>+......
\end{aligned}
$$

From above expression, we can see that the proposed kernel corresponds to a sum of all possible dot products of pairs belonging to the set $\{(x_i z_i)|x_i \in \text{seq}1, z_i \in \text{seq}2\}$. Similar to the polynomial kernel, the proposed kernel allows us to match all possible pairs of vectors belonging to the two sub-sequences given by the matrices. It is easy to check that this proposed kernel is in fact a valid kernel:

- K(x,z)= K(z,x) ⇒the function is symmetric.

- The kernel satisfies Mercer's theorem : K(x,z) =$\phi(x)^T \phi(x)$ where the feature mapping corresponds to a finite summation of vectors $\phi(y) = \sum_{i=1}^{n} y_i$.

Augmenting the kernel to the DTW algorithm allows DTW to work on high-

dimensional time sequences without using a window constraint. However the accuracy and computational cost of the DTW is now dependent on the size of the time slices used to segment the original sequences in the first place. To use this kernel as an appropriate cost function in the DTW algorithm, we need a functional mapping that:

1. constraints the codomain to be in the range from 0 to ∞.

2. ensures larger values given by the function signify great degree of dissimilarity and smaller values signify a high degree of similitude.

An ideal cost function that make use of dot products is the *arc-cosine*. Hence I embedded the kernel function in the cosine distance:

$$\theta = \frac{<X,Z>}{|X||Z|}$$

where $X = \sum_{i=1}^{n} x_i$ and $Z = \sum_{j=1}^{n} z_i$

A formal outline of the algorithm is as follows:

Algorithm 4 Adapted DTW

1: **procedure** VALUE-BASED($seq1, seq2$)   ▷ two sequences of feature vectors
2:     seq_1←segment(seq1,n) ▷ Segment the sequences using a window of size n
3:     seq_2←segment(seq2,n)
4:     **for** i=1: to length(seq_1) **do**   ▷ Initialise the DTW cost matrix
5:         DTW(i,0) = ∞
6:     **end for**
7:     **for** i=1 to length(seq_2) **do**
8:         DTW(0,i) = ∞
9:     **end for**
10:    **for** i=2 to length(seq_1) **do**
11:        **for** j=max(2, i-w) to min(length(seq_2), i+w) **do**
12:            DTW(i,j) = $\theta = \frac{<X,Z>}{|X||Z|}$ + min{ DTW(i-1,j)+DTW(i,j-1)+DTW(i-1,j-1)}
13:        **end for**   ▷ $X = \sum_{i=1}^{n} x_i$ and $Z = \sum_{j=1}^{n} z_i$
14:    **end for**
15:    **return** result = $\frac{DTW(n,m)}{nm}$ ▷ n=length(seq1), m=length(seq2)
16: **end procedure**

5.2.1 Testing the methodology

The changes that I have introduced in the previous section to the 'Dynamic Time Warping' algorithm is aimed to improve the algorithm's performance in handling long time series sequences. In this section, I investigate the performance of this proposed methodology against the versions of the DTW algorithm that employ the Sakoe-Chuba band constraint (discussed in 4.1.1). The window constraint that I have used so far is the most rigid constraint that can be imposed on the DTW algorithm without forcing the algorithm to behave like the euclidean metric. In order to compare the performance of using my proposed method with that of using the window constraint, I have conducted the following 3 experiments: **Experiment 1**

In the first experiment I , I take the model discussed in 5.1 for the TIDIGITS data set which consists of applying two stage feature selection process which involves silence removal and downsampling followed by the feature extraction phase of [2] and investigate the differences in the performance between the DTW algorithm is equipped with the changes I propose and the DTW algorithm using a window constraint. The results found from the experiments are as follows:
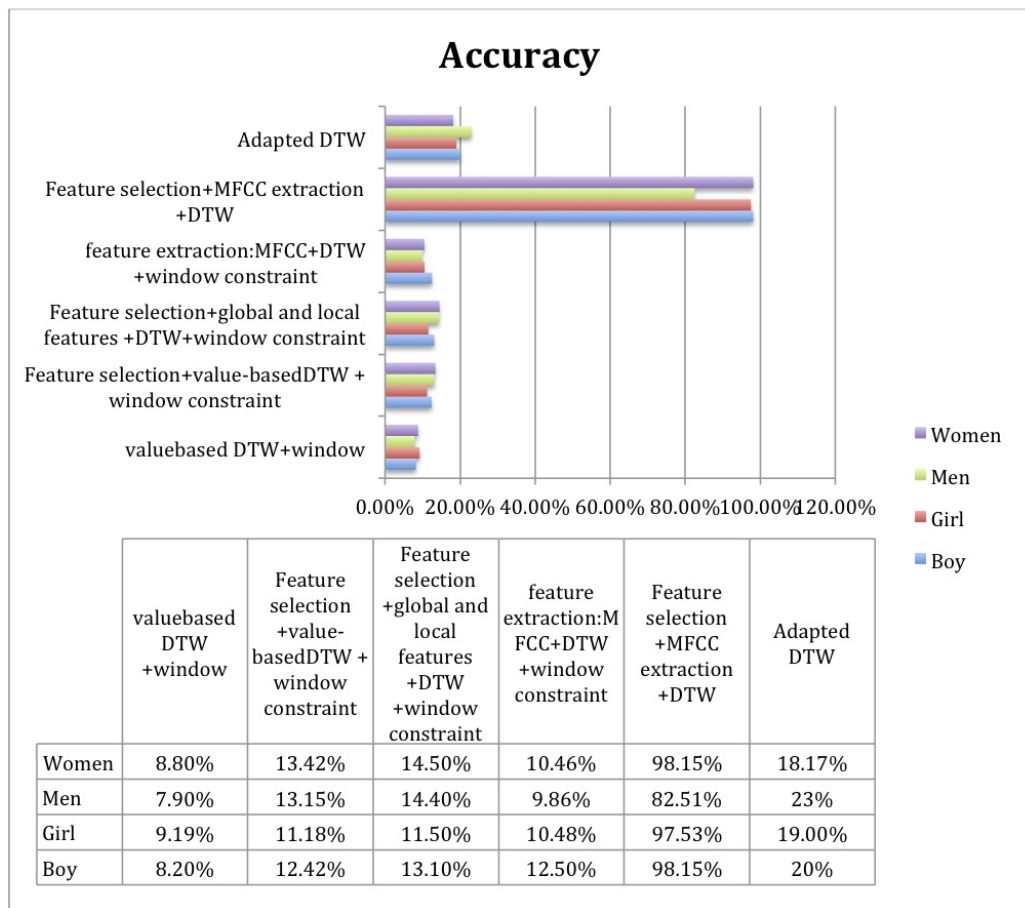
Accuracy

	valuebased DTW +window	Feature selection +value-basedDTW + window constraint	Feature selection +global and local features +DTW +window constraint	feature extraction:MFCC+DTW +window constraint	Feature selection +MFCC extraction +DTW	Adapted DTW
Women	8.80%	13.42%	14.50%	10.46%	98.15%	18.17%
Men	7.90%	13.15%	14.40%	9.86%	82.51%	23%
Girl	9.19%	11.18%	11.50%	10.48%	97.53%	19.00%
Boy	8.20%	12.42%	13.10%	12.50%	98.15%	20%

Figure 5.7: Accuracy

Log(Time)

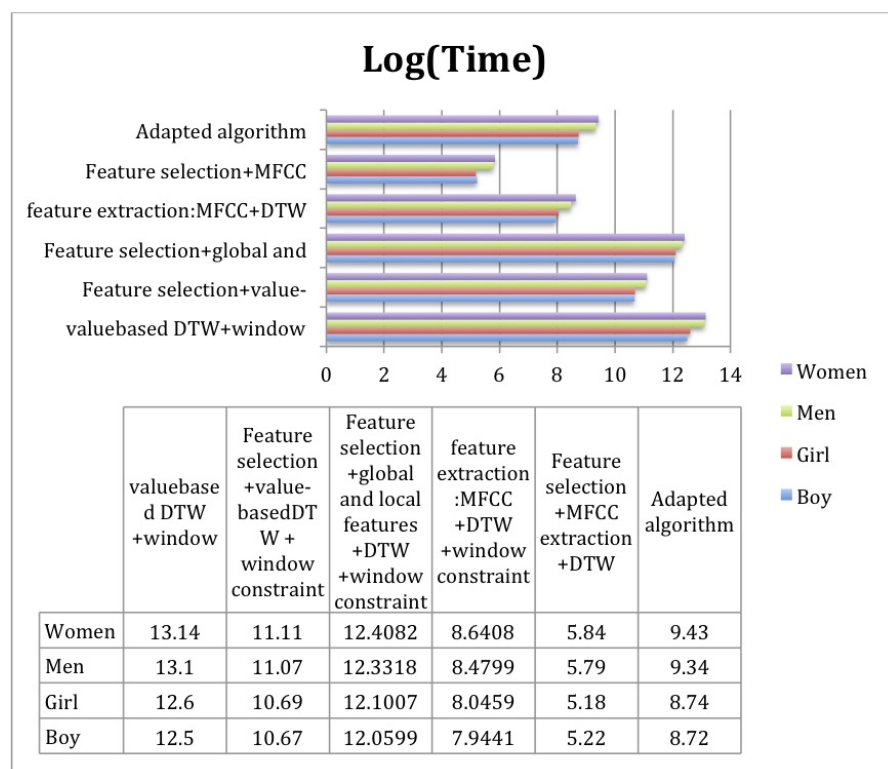|	valuebased DTW +window	Feature selection +value-basedDTW + window constraint	Feature selection +global and local features +DTW +window constraint	feature extraction:MFCC +DTW +window constraint	Feature selection +MFCC extraction +DTW	Adapted algorithm
Women	13.14	11.11	12.4082	8.6408	5.84	9.43
Men	13.1	11.07	12.3318	8.4799	5.79	9.34
Girl	12.6	10.69	12.1007	8.0459	5.18	8.74
Boy	12.5	10.67	12.0599	7.9441	5.22	8.72

Figure 5.8: Time complexity

There are quite number of interesting observations that can made from the graphs and the tables given by figures [4.3,4.4].

- The proposed algorithm achieves better accuracy for test samples belonging to all categories than any of algorithms that employ the rigid window constraint of $w = max(\lceil 0.1 * max(n.m) \rceil, abs(n-m))$. The most interesting result is that the new algorithm incurs a lower computational cost than any of these DTW algorithms.

- From examining the improvements in accuracy across all categories, it can be concluded that for the TIGITS dataset, the new algorithm is invariant to variations introduced in the acoustic signals by different speakers .

- The methodology behind my proposed approach and that of approach 4 includes the same pre-processing stage. Th input to the DTW algorithm is constructed by using the domain dependent feature selection process mentioned in section followed by a domain independent feature extraction mapping (i.e the local and global features defined in section). Both approaches differ however, in their use of a cost function and a window constraint. The proposed approach doesn't subject DTW to any window constraints and utilised the kernel function that I constructed in the cost metric. Approach 4 on the other hand, employs the euclidean metric an subjects DTW to the window constraint of of $w = max(\lceil 0.1 * max(n.m) \rceil,$ abs(n-m)) The proposed DTW segments sequences into frames and employ a cost function on the frames. This reduces the dimensionality of the time series sequences and allows the algorithm to achieve a time and computational cost than is lower than the cost incurred by any of the investigated adaptations of the DTW algorithm that employs window constraints.

To confirm that the performance of the new algorithm is not tailored for this particular time-series data set, I have applied the tested the algorithm on the two largest time series data sets in UCR database.

Unlike the speech utterances, the time series sequences within each data set share the same length.

5.2.2 Experimental setup

The focus now is to check how well/ bad is the performance of the new DTW algorithm against DTW algorithms using window constraints when applied to datasets that belong to other application domains . The domain -dependent pre-processing policies are dropped for this set of experiments as these procedures were specifically designed for speech data. Thus in this section, I compare my proposed approach against:

- Approach 1

- Approach 4

As a I mentioned, the domain-dependent feature selection process of silence removal and subsampling is dropped from all approaches. However, the feature extraction process that involves extracting local and global features is kept since this procedure is domain independent.

One of the factors that I have also investigated in these experiments is the size of the time slices used in the algorithm that I proposed. For the TIDIGITS data set, I have used window slices of 50 ms. Reducing the size of the windows should principally increase both accuracy and time-complexity . The core kernel used by the new algorithm is based on the function:

$$k(x,z) = < \sum_{i=1}^{n} x_i, \sum_{j=1}^{n} z_j >$$

k(x,z) represents the sum of all possible dot-products . Having a smaller window allows the sum to be dominated by dot products of vectors that are most similar. However smaller window frames results in longer time series sequence of frames. This in turn increases the time and computational complexity incurred by the DTW algorithm.

Figure [4.5] and figure[4.6] shows the accuracies and log(time) of the algorithms for the two datasets:

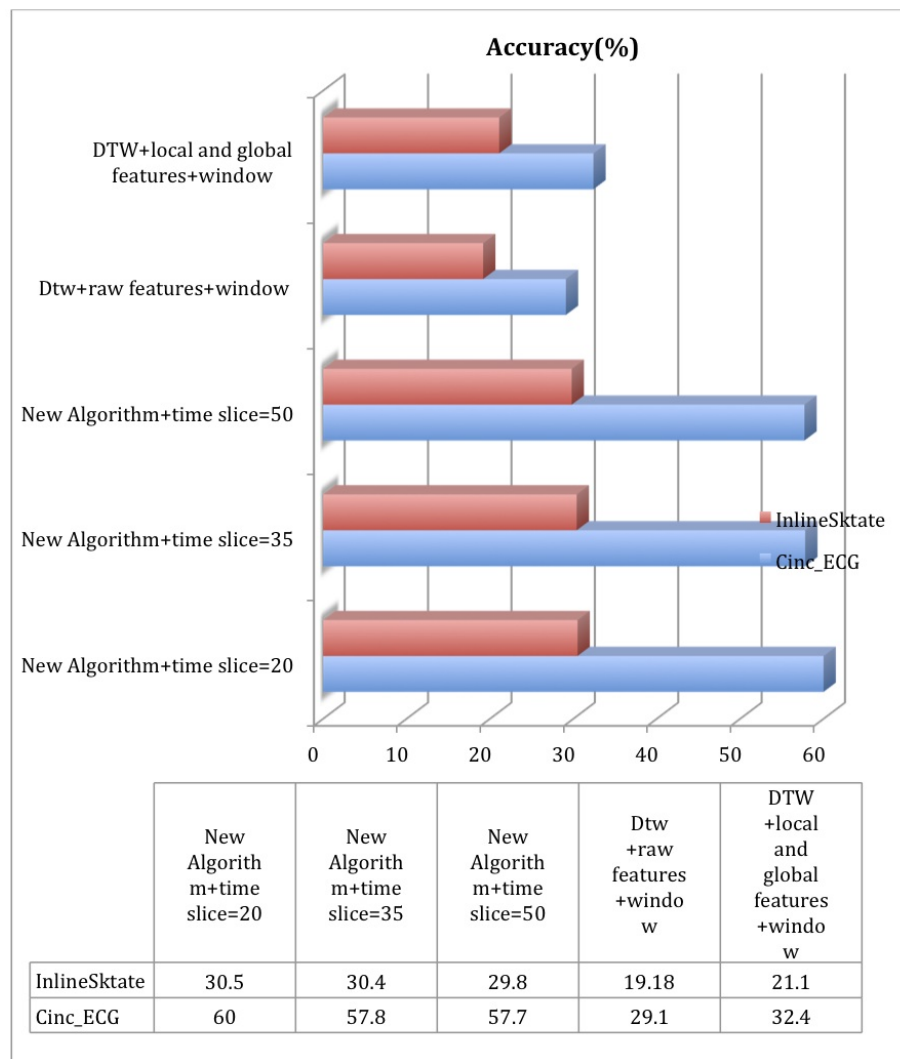|	New Algorithm+time slice=20	New Algorithm+time slice=35	New Algorithm+time slice=50	Dtw +raw features +window	DTW +local and global features +window
InlineSktate	30.5	30.4	29.8	19.18	21.1
Cinc_ECG	60	57.8	57.7	29.1	32.4

Figure 5.9: Accuracy

Observation:

- The new algorithm indeed achieves better accuracy than any versions of the window constrained DTW algorithm employing domain-independent feature extraction

- Comparatively, the performance of the new algorithm does improve if smaller window slices are employed to partition the time series sequence of vectors.
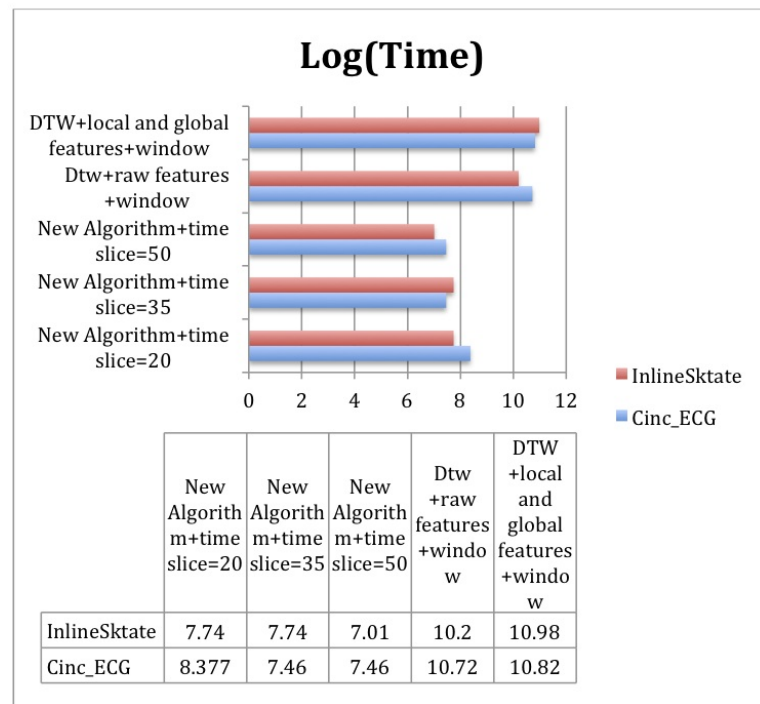
Figure 5.10: Time complexity

The table from the figure:

	New Algorithm+time slice=20	New Algorithm+time slice=35	New Algorithm+time slice=50	Dtw+raw features+window	DTW+local and global features+window
InlineSktate	7.74	7.74	7.01	10.2	10.98
Cinc_ECG	8.377	7.46	7.46	10.72	10.82

Observation:

- The new algorithm incurs less time and computational cost than any versions of the window constrained DTW algorithm employing domain-independent feature extraction

- Comparatively, the time complexity of the new algorithm increases when smaller window slices are used to partition the sequence

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