

Day - 06

- ① 3 student be seated in a row?

$$3! = 3 \times 2 \times 1 = 6 \text{ ways}$$

- ② A box contain 5 different colored balls
How many ways can you pick 1 ball?

→ 5 ways

- ③ exchanging letter in "CAT": $3! = 3 \times 2 \times 1 = 6$

- ④ choosing 2 suits from 4: $C(4, 2) = 6 \text{ ways}$

$$4! / (2! \times 2!) = 6 \text{ ways}$$

- ⑤ 2-digit number from 1, 2, 3: $P(3, 2) = 3! / (3-2)!$

$$= 6 \text{ ways}$$

- ⑥ 2-digit number from 1, 2, 3, 4, 5 (even)

$$2 \times P(4, 3) = 2 \times 24 = 48 \text{ ways}$$

- ⑦ 3-digit numbers from 1, 2, 3, 4, 5

$$P(5, 3) = 5! / (5-3)! = 24 \text{ ways}$$

- ⑧ passwords from A, B, C, D

$$P(4, 3) = 4! / (4-3)! = 24 \text{ ways}$$

- ⑨ Committee of 3 from 7 people

$$C(7, 3) = 7!$$

- ⑩ Probability of picking a green ball from
3 red, 2 green

$$\begin{aligned} \text{Total} &= 5 \quad \text{green} = 2 \\ &= \frac{2}{5} \end{aligned}$$

⑪ How many 3-digit no from 1, 2, 3, 4 without repetition

First digit 4 choices. Second 3. Third = 2.

$$4 \times 3 \times 2 = 24$$

⑫. — ways to choose 3 from 7 people (committee)

$$7C3 = \underline{35} \text{ ways}$$

⑬ = Probability of drawing a King from 52 card

$$\text{Kings} = 4$$

$$= 4/52 = 1/13$$

⑭ ways to arrange 5 books on a shelf?

$$5! = 120 \text{ ways}$$

⑮ Probability of black ball from 6 white & 4 black?

$$\text{Total} = 10, \text{ black} = 4$$

$$= 4/10 = 2/5$$

⑯ Password from A, B, C, D taken 3 at a time order matter = $4P3 = 4 \times 3 \times 2 = \underline{24}$

⑰ Probability of getting even number when die is rolled?

Even no = 2, 4, 6 \rightarrow 3 outcomes

$$= 3/6 = 1/2$$

⑱ ways to choose 2 letters from "MATH"? All 4 letters are different \rightarrow

$$= 4C2 = 6 \text{ ways}$$

12) Probability of heart from standard deck?
13 hearts out of 52
 $= 13/52 = 1/4$

13) ways to arrange 4 people around a circular table?
Circular permutation: $(n-1)!$
 $= 3! = 6$ ways

14) 4-digit even number using 1, 2, 3, 4, 5 without repetition. Even numbers end in 2 or 4.
Case 1 (ends in 2): Remaining: 1, 3, 4, 5 $\rightarrow 3! = 6$
Case 2 (ends in 4): Remaining: 1, 3, 2, 5 $\rightarrow 3! = 6$
Total $= 6 + 6 = 12$

15) Probability both balls are green (3R, 4B, 5G)?
Total balls = 12.
Way to choose 2 green = $5C2 = 10$
Total ways = $12C2 = 66$
 $= 10/66 = 5/33$

16) ways to arrange 5 students such that 2 don't sit together?
Total ways without restriction = $5! = 120$

Treat 2 as one unit: $4! \times 2! = 48$

Not together = $120 - 48 = 72$ ways

17) From 10 men & 8 women, Committee of 4 with at least 2 women?

Total with

$$2W, 2M = 8C2 \times 10C2 = 28 \times 45 = 1260$$

$$3W, 1M = 8C3 \times 10C1 = 56 \times 10 = 560$$

$$4 \text{ women} = 8C4 = 70$$

$$\frac{1}{10} \text{ total} = 1260 + 560 + 70 = 1890 \text{ ways}$$

25. Die rolled twice. probability $\text{Sum} = 7$

$$\text{Total outcomes} = 6 \times 6 = 36$$

pairs (1,6), (2,5), (3,4), (4,3), (5,2), (6,1) \rightarrow

6 Outcomes

$$= 6/36 = \underline{\underline{1/6}}$$