

Elementary Division Solutions

1. Boolean Algebra

NOT $(15 + 3 > 23 - 7)$ OR $(14 / 7 \geq 1^2 \text{ AND } 7 * 4 < 3 * 10)$
 NOT $(18 > 16)$ OR $(2 \geq 1 \text{ AND } 28 < 30)$
 NOT TRUE OR $(\text{TRUE AND TRUE}) = \text{FALSE OR TRUE}$
 TRUE

1. TRUE

2. Boolean Algebra

NOT $(A \text{ OR NOT } B)$ OR $(\text{NOT } B \text{ AND } A)$
 $= (\text{NOT } A \text{ AND NOT } (\text{NOT } B)) \text{ OR } (\text{NOT } B \text{ AND } A)$
 $= (\text{NOT } A \text{ AND } B) \text{ OR } (\text{NOT } B \text{ AND } A)$
 This is TRUE if A and B are different which is (0,1) and (1,0).

2. (0,1) and (1,0)

3. Boolean Algebra

1	2	3	4	5	6	7	8
A	B	$\sim A$	$\sim B$	$\sim A * \sim B$	$\sim(\sim A * \sim B)$	$A * B$	$6+7$
0	0	1	1	1	0	0	0
0	1	1	0	0	1	0	1
1	0	0	1	0	1	0	1
1	1	0	0	0	1	1	1

3. 1

4. Boolean Algebra

$\sim(A * \sim B) + \sim(\sim A * B) = \sim A + \sim(\sim B) + \sim(\sim A) + \sim B$
 $= \sim A + B + A + \sim B = 1$
 By regrouping, $(\sim A + A)$ and $(\sim B + B)$ are both 1 and $1 + 1 = 1$ in Boolean Algebra (not 2 as in regular arithmetic). This is always TRUE so it is a tautology.

4. 1

5. Boolean Algebra

A. $\sim(\sim B) + \sim(\sim A) = B \text{ OR } A$ which is TRUE for (1,1), (1,0), (0,1).
 B. $A + \sim B$ is TRUE if $A = 1$ or $B = 0$ which is (1,1), (1,0), and (0,0).
 C. $A * \sim B$ is only TRUE if $A = 1$ and $B = 0$ which is (1,0).
 D. $\sim(A * B) = \sim A + \sim B$ is TRUE $A = 0$ or $B = 0$ which is (0,1), (0,0), (1,0).
 Therefore, A, B, and D are all TRUE 3 times and FALSE once.

5. A, B, D