American Computer Science League

Contest #4

Elementary Division Solutions

1. Graph Theory B C 2. Graph Theory After drawing the graph, there is an edge from every vertex to every other vertex, 10 in all which makes it a complete graph.

3. Graph Theory

There are only 2 cycles in this graph, both of which must include all 5 vertices. Therefore, they are any cyclical sequence of ABDECA (e.g. DECABD) and CEDBAC (e.g. DBACED). In undirected graph, there is always an even number of cycles because you can go both ways.

4. Graph Theory

A simple path has no vertex repeated. There are no simple paths of length 1. Paths of length 2 include QPS and QTS. Paths of length 3 include QPTS, QTRS, and QTPS. Paths of length 4 include only QPTRS. With 5 vertices, there are no paths of length more than 4.

5. Graph Theory

The roads are the edges of the graph and the family names are the nodes. It is traversable if you can cross each road once and only once. There are 4 odd vertices (Atkins, Field, Clark, and Brown). Therefore, it is not traversable.

3. 2

4. QPS, QTS, QPTS, QTRS, QTPS, QPTRS

5. NOT POSSIBLE