American Computer Science League

Contest #1

Elementary Division Solutions

 Computer Number Systems 2018₁₆ = 10 0000 0001 1000 because you need 4 bits for each digit. Grouping by 3 digits gives 10 000 000 011 000 = 20030₈. 	1. 20030 ₈ or 20030
2. Computer Number Systems	2. 44 or 44 ₁₀
Convert each of them to binary which gives $254_8 = 10101100_2$ which is 4 1's $139_{16} = 100111001_2$ which is 5 1's $44_{10} = 32 + 8 + 4 = 101100_2$ which is 3 1's	
3. Computer Number Systems	3. 227C or 227C ₁₆
$2AF4_{16} + 246_{16} = 2D3A_{16}$ because $4 + 6 = 10$ (A); $F + 4 = 19$ (3, carry 1); $A + 2 + 1 = 13$ (D); $2 + 0 = 2$ $D3A_{16} - ABE_{16} = 27C_{16}$ because E is greater than A so borrow 1 from the 3 (which is 16). Then $16 + A$ (10) $-E$ (14) $= 12$ (C). B if greater than 2 so borrow 1 from the D which becomes C. Then $16 + 2 - B$ (11) $= 7$. Finally, C (12) $-A$ (10) $= 2$ to get 227C.	
4. Computer Number Systems	4. 4
Counting in binary starting with 1 yields 1, 10, 11, 100, 101, 110, 111, 1000, 1001, 1010, 1011, 1100, 1101, 1110, 1111. Only 10, 1001, 1010, and 1100 satisfy the condition.	
5. Computer Number Systems	5. 61 ₁₀ or 61
Each color for an RGB code uses 2 hexadecimal digits. The BLUE component in RGB is the last 2 digits. Converting $3D_{16}$ to base $10 = 3 * 16 + 13 = 48 + 13 = 61$.	