Boost.Ratio 2.1.0

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Overview

How to Use This Documentation

This documentation makes use of the following naming and formatting conventions.

- Code is in fixed width font and is syntax-highlighted.
- Replaceable text that you will need to supply is in italics.
- Free functions are rendered in the code font followed by (), as in free_function().
- If a name refers to a class template, it is specified like this: class_template<>; that is, it is in code font and its name is followed by <> to indicate that it is a class template.
- If a name refers to a function-like macro, it is specified like this: MACRO(); that is, it is uppercase in code font and its name is followed by () to indicate that it is a function-like macro. Object-like macros appear without the trailing ().
- Names that refer to *concepts* in the generic programming sense are specified in CamelCase.



Note

In addition, notes such as this one specify non-essential information that provides additional background or rationale.

Finally, you can mentally add the following to any code fragments in this document:

```
// Include all of Ratio files
#include <boost/ratio.hpp>
using namespace boost;
```

Motivation

Boost.Ratio aims to implement the compile time ratio facility in C++0x, as proposed in **N2661 - A Foundation to Sleep On**. That document provides background and motivation for key design decisions and is the source of a good deal of information in this documentation.

Description

The Boost.Ratio library provides:

- A class template, ratio, for specifying compile time rational constants such as 1/3 of a nanosecond or the number of inches per
 meter. ratio represents a compile time ratio of compile time constants with support for compile time arithmetic with overflow
 and division by zero protection.
- It provides a textual representation of boost::ratio<N, D> in the form of a std::basic_string which can be useful for I/O.
- Some extension related to the Rational Constant concept enabling the use of ratio<> in the context of Boost.MPL numeric metafunctions.



User's Guide

Getting Started

Installing Ratio

Getting Boost.Ratio

Boost.Ratio is in the latest Boost release in the folder /boost/ratio. Documentation, tests and examples folder are at boost/libs/ratio/.

You can also access the latest (unstable?) state from the Boost trunk directories boost/ratio and libs/ratio.

Just go to the wiki and follow the instructions there for anonymous SVN access.

Where to install Boost.Ratio?

The simple way is to decompress (or checkout from SVN) the files in your BOOST_ROOT directory.

Building Boost.Ratio

Boost.Ratio is a header only library, so no need to compile anything, you just need to include <boost/ratio.hpp>.

Requirements

Boost.Ratio depends on some Boost libraries. For these specific parts you must use either Boost version 1.39.0 or later (even older versions may work).

In particular, Boost.Ratio depends on:

Boost.Config for configuration purposes, ...

Boost.Integer for cstdint conformance, and integer traits ...

Boost.MPL for MPL Assert and bool, logical ...

Boost.StaticAssert for STATIC_ASSERT, ...

Boost.TypeTraits for is_base, is_convertible ...

Boost.Utility/EnableIf for enable_if, ...

Building an executable that uses Boost.Ratio

No link is needed.

Exception safety

All functions in the library are exception-neutral, providing the strong exception safety guarantee.

Thread safety

All functions in the library are thread-unsafe except when noted explicitly.

Tested compilers

Boost.Ratio should work with an C++03 conforming compiler. The current version has been tested on:

Windows with



• MSVC 10.0

MinGW with

- GCC 4.5.0
- GCC 4.5.0 -std=c++0x
- GCC 4.5.2
- GCC 4.5.2 std = c + +0x
- GCC 4.6.0
- GCC 4.6.0 -std=c++0x

Ubuntu with * GCC 4.4.6 * GCC 4.4.6 -std=c++0x * GCC 4.5.4 * GCC 4.5.4 -std=c++0x * GCC 4.6.1 * GCC 4.

OsX with

- GCC 4.1.2
- GCC 4.6.2
- GCC 4.6.2 -std=c++0x
- GCC 4.7.0
- GCC 4.7.0 std = c + +0x
- GCC 4.7.1
- GCC 4.7.1 -std=c++0x
- clang 1.6
- clang 2.9
- clang 2.9 std = c + +0x
- clang 3.0
- clang 3.0 -std=c++0x
- clang 3.1
- clang 3.1 std = c + +0x
- clang 3.1 std = c + +0x stdlib = libc + +
- clang 3.2
- clang 3.2 -std=c++11
- clang 3.2 -std=c++11 -stdlib=libc++



Note

Please let us know how this works on other platforms/compilers.





Note

Please send any questions, comments and bug reports to boost <at> lists <dot> boost <dot> org.

Tutorial

Ratio

ratio is a general purpose utility inspired by Walter Brown allowing one to easily and safely compute rational values at compile-time. The ratio class catches all errors (such as divide by zero and overflow) at compile time. It is used in the duration and time_point classes to efficiently create units of time. It can also be used in other "quantity" libraries or anywhere there is a rational constant which is known at compile-time. The use of this utility can greatly reduce the chances of run-time overflow because the ratio (and any ratios resulting from ratio arithmetic) are always reduced to the lowest terms.

ratio is a template taking two intmax_ts, with the second defaulted to 1. In addition to copy constructors and assignment, it only has two public members, both of which are static const intmax_t. One is the numerator of the ratio and the other is the denominator. The ratio is always normalized such that it is expressed in lowest terms, and the denominator is always positive. When the numerator is 0, the denominator is always 1.

Example:

```
typedef ratio<5, 3> five_thirds;
// five_thirds::num == 5, five_thirds::den == 3

typedef ratio<25, 15> also_five_thirds;
// also_five_thirds::num == 5, also_five_thirds::den == 3

typedef ratio_divide<five_thirds, also_five_thirds>::type one;
// one::num == 1, one::den == 1
```

This facility also includes convenience typedefs for the SI prefixes atto through exa corresponding to their internationally recognized definitions (in terms of ratio). This is a tremendous syntactic convenience. It will prevent errors in specifying constants as one no longer has to double count the number of zeros when trying to write millions or billions.

Example:

```
typedef ratio_multiply<ratio<5>, giga>::type _5giga;
// _5giga::num == 50000000000, _5giga::den == 1

typedef ratio_multiply<ratio<5>, nano>::type _5nano;
// _5nano::num == 1, _5nano::den == 200000000
```

Ratio I/O

For each ratio<N, D> there exists a ratio_string<ratio<N, D>, CharT> for which you can query two strings: symbol and prefix. For those ratio's that correspond to an SI prefix prefix corresponds to the internationally recognized prefix, stored as a basic_string<CharT>. For example ratio_string<mega, char>::prefix() returns string("mega"). For those ratios that correspond to an SI prefix symbol corresponds to the internationally recognized symbol, stored as a basic_string<CharT>. For example, ratio_string<mega, char>::symbol() returns string("M"). For all other ratios, both prefix() and symbol() return a basic_string containing "[ratio::num/ratio::den]".

ratio_string<ratio<N, D>, CharT> is only defined for four character types:

- char: UTF-8
- char16_t: UTF-16



- char32_t: UTF-32
- wchar_t: UTF-16 (if wchar_t is 16 bits) or UTF-32

When the character is char, UTF-8 will be used to encode the names. When the character is char16_t, UTF-16 will be used to encode the names. When the character is char32_t, UTF-32 will be used to encode the names. When the character is wchar_t, the encoding will be UTF-16 if wchar_t is 16 bits, and otherwise UTF-32.

The symbol (Greek mu or μ) for micro is defined by Unicode to be U+00B5.

Examples:

```
#include <boost/ratio/ratio_io.hpp>
#include <iostream>
int main()
    using namespace std;
    using namespace boost;
    cout << "ratio_string<deca, char>::prefix() = "
             ratio_string<deca, char>::prefix() << '\n';
    cout << "ratio_string<deca, char>::symbol() = "
         << ratio_string<deca, char>::symbol() << '\n';</pre>
    cout << "ratio_string<giga, char>::prefix() = "
         << ratio_string<giga, char>::prefix() << '\n';</pre>
    cout << "ratio_string<giga, char>::symbol() = "
         << ratio_string<giga, char>::symbol() << '\n';</pre>
    cout << "ratio_string<ratio<4, 6>, char>::prefix() = "
         << ratio_string<ratio<4, 6>, char>::prefix() << '\n';</pre>
    cout << "ratio_string<ratio<4, 6>, char>::symbol() = "
         << ratio_string<ratio<4, 6>, char>::symbol() << '\n';</pre>
```

The output will be

```
ratio_string<deca, char>::prefix() = deca
ratio_string<deca, char>::symbol() = da
ratio_string<giga, char>::prefix() = giga
ratio_string<giga, char>::symbol() = G
ratio_string<ratio<4, 6>, char>::prefix() = [2/3]
ratio_string<ratio<4, 6>, char>::symbol() = [2/3]
```

Ratio MPL Numeric Metafunctions

With the view of the _ratio class as a Rational Constant we can mix _ratio<> and Boost.MPL Integral Constants in the same expression, as in

```
typedef mpl::times<int_<5>, giga>::type _5giga;
// _5giga::num == 5000000000, _5giga::den == 1

typedef mpl::times<int_<5>, nano>::type _5nano;
// _5nano::num == 1, _5nano::den == 200000000
```



Example

SI units

This example illustrates the use of type-safe physics code interoperating with boost::chrono::duration types, taking advantage of the **Boost.Ratio** infrastructure and design philosophy.

Let's start by defining a length class template that mimics boost::chrono::duration, which represents a time duration in various units, but restricts the representation to double and uses **Boost.Ratio** for length unit conversions:

```
template <class Ratio>
class length {
private:
    double len_;
public:
    typedef Ratio ratio;
    \texttt{length()} \; : \; \texttt{len}_(\texttt{1}) \; \left\{\,\right\}
    length(const double& len) : len_(len) {}
    template <class R>
    length(const length<R>& d)
             : len_(d.count() * boost::ratio_divide<Ratio, R>::type::den /
                                  boost::ratio_divide<Ratio, R>::type::num) {}
    double count() const {return len_;}
    length& operator+=(const length& d) {len_ += d.count(); return *this;}
    length& operator-=(const length& d) {len_ -= d.count(); return *this;}
    length operator+() const {return *this;}
    length operator-() const {return length(-len_);}
    length& operator*=(double rhs) {len_ *= rhs; return *this;}
    length& operator/=(double rhs) {len_ /= rhs; return *this;}
};
```

Here's a small sampling of length units:

Note that since length's template parameter is actually a generic ratio type, so we can use boost::ratio allowing for more complex length units:

```
typedef length<boost::ratio_multiply<boost::ratio<12>, inch::ratio>::type> foot; // 12 inchs
typedef length<boost::ratio_multiply<boost::ratio<5280>, foot::ratio>::type> mile; // 5280 feet
```

Now we need a floating point-based definition of seconds:

We can even support sub-nanosecond durations:



```
typedef boost::chrono::duration<double, boost::pico> picosecond; // 10^-12 seconds
typedef boost::chrono::duration<double, boost::femto> femtosecond; // 10^-15 seconds
typedef boost::chrono::duration<double, boost::atto> attosecond; // 10^-18 seconds
```

Finally, we can write a proof-of-concept of an SI units library, hard-wired for meters and floating point seconds, though it will accept other units:

```
template <class R1, class R2>
class quantity
    double q_;
public:
    typedef R1 time_dim;
    typedef R2 distance_dim;
    quantity() : q_(1) {}
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<1>, boost::ratio<0> >
    double q_;
public:
    quantity() : q_(1) {}
    \texttt{quantity}(\texttt{seconds } \texttt{d}) \; : \; \texttt{q\_(d.count())} \; \; \big\{\big\} \quad // \; \texttt{note:} \quad \texttt{only User1::seconds needed here}
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<0>, boost::ratio<1> >
    double q_;
public:
    quantity() : q_(1) {}
    quantity(meter d) : q_(d.count())  {} // note: only User1::meter needed here
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
template <>
class quantity<boost::ratio<0>, boost::ratio<0> >
    double q_;
public:
    quantity() : q_(1) {}
    quantity(double d) : q_(d) \{ \}
    double get() const {return q_;}
    void set(double q) {q_ = q;}
};
```

That allows us to create some useful SI-based unit types:



To make quantity useful, we need to be able to do arithmetic:

```
template <class R1, class R2, class R3, class R4>
quantity<typename boost::ratio_subtract<R1, R3>::type,
         typename boost::ratio_subtract<R2, R4>::type>
operator/(const quantity<R1, R2>& x, const quantity<R3, R4>& y)
    typedef quantity<typename boost::ratio_subtract<R1, R3>::type,
                    typename boost::ratio_subtract<R2, R4>::type> R;
    Rr;
    r.set(x.get() / y.get());
    return r;
template <class R1, class R2, class R3, class R4>
quantity<typename boost::ratio_add<R1, R3>::type,
         typename boost::ratio_add<R2, R4>::type>
operator*(const quantity<R1, R2>& x, const quantity<R3, R4>& y)
    typedef quantity<typename boost::ratio_add<R1, R3>::type,
                     typename boost::ratio_add<R2, R4>::type> R;
   r.set(x.get() * y.get());
    return r;
template <class R1, class R2>
quantity<R1, R2>
operator + (const \ quantity < R1 \ , \ R2 > \& \ x \ , \ const \ quantity < R1 \ , \ R2 > \& \ y)
{
    typedef quantity<R1, R2> R;
    Rr;
    r.set(x.get() + y.get());
    return r;
template <class R1, class R2>
quantity<R1, R2>
operator-(const quantity<R1, R2>& x, const quantity<R1, R2>& y)
    typedef quantity<R1, R2> R;
    Rri
    r.set(x.get() - y.get());
    return r;
```

With all of the foregoing scaffolding, we can now write an exemplar of a type-safe physics function:

```
Distance
compute_distance(Speed v0, Time t, Acceleration a)
{
    return v0 * t + Scalar(.5) * a * t * t; // if a units mistake is made here it won't compile
}
```



Finally, we can exercise what we've created, even using custom time durations (User1::seconds) as well as Boost time durations (boost::chrono::hours). The input can be in arbitrary, though type-safe, units, the output is always in SI units. (A complete Units library would support other units, of course.)

```
int main()
    typedef boost::ratio<8, BOOST_INTMAX_C(0x7FFFFFFFD)> R1;
    typedef boost::ratio<3, BOOST INTMAX C(0x7FFFFFFFD) > R2;
    typedef User1::quantity<boost::ratio_subtract<boost::ratio<0>, boost::ratio<1> >::type,
                           boost::ratio_subtract<boost::ratio<1>, boost::ratio<0> >::type > RR;
    typedef boost::ratio_subtract<R1, R2>::type RS;
    std::cout << RS::num << '/' << RS::den << '\n';
    std::cout << "*********\n";
    std::cout << "* testUser1 *\n";
    std::cout << "*********\n";
    User1::Distance d( User1::mile(110) );
    User1::Time t( boost::chrono::hours(2) );
    RR r=d / t;
    //r.set(d.get() / t.get());
    User1::Speed rc= r;
    User1::Speed s = d / t;
    std::cout << "Speed = " << s.get() << " meters/sec\n";
   User1::Acceleration a = User1::Distance( User1::foot(32.2) ) / User1::Time() / User1::Time();
    std::cout << "Acceleration = " << a.get() << " meters/sec^2\n";</pre>
    User1::Distance df = compute_distance(s, User1::Time( User1::seconds(0.5) ), a);
    std::cout << "Distance = " << df.get() << " meters\n";</pre>
    std::cout << "There are "
        << User1::mile::ratio::den << '/' << User1::mile::ratio::num << " miles/meter";
    User1::meter mt = 1;
    User1::mile mi = mt;
    std::cout << " which is approximately " << mi.count() << '\n';
    std::cout << "There are "
        << User1::mile::ratio::num << '/' << User1::mile::ratio::den << " meters/mile";</pre>
    mi = 1;
    mt = mi;
    std::cout << " which is approximately " << mt.count() << '\n';</pre>
    User1::attosecond as(1);
    User1::seconds sec = as;
    std::cout << "1 attosecond is " << sec.count() << " seconds\n";
    std::cout << "sec = as; // compiles\n";</pre>
    sec = User1::seconds(1);
    as = seci
    std::cout << "1 second is " << as.count() << " attoseconds\n";</pre>
    std::cout << "as = sec; // compiles\n";</pre>
    std::cout << "\n";
    return 0;
```

See the source file example/si_physics.cpp

External Resources

C++ Standards Committee's current Working Paper

The most authoritative reference material for the library is the C++ Standards Committee's current Working Paper (WP). 20.6 Compile-time rational arithmetic "ratio"



N2661 - A Foundation to Sleep On

From Howard E. Hinnant, Walter E. Brown, Jeff Garland and Marc Paterno. Is very informative and provides motivation for key design decisions

LWG 1281. CopyConstruction and Assignment between ratios having the same normalized form

From Vicente Juan Botet Escriba.



Reference

Header config.hpp>

```
// Configuration macros
#define BOOST_RATIO_VERSION
#define BOOST_RATIO_EXTENSIONS
#define BOOST_RATIO_PROVIDES_DEPRECATED_FEATURES_SINCE_V2_0_0
#define BOOST_RATIO_DONT_PROVIDE_DEPRECATED_FEATURES_SINCE_V2_0_0
#define BOOST_RATIO_USES_STATIC_ASSERT
#define BOOST_RATIO_USES_MPL_ASSERT
#define BOOST_RATIO_USES_ARRAY_ASSERT
```

Extensions

When BOOST_RATIO_EXTENSIONS is defined, **Boost.Ratio** provides in addition some extension to the C++ standard, see below.

Deprecated

When BOOST_RATIO_PROVIDES_DEPRECATED_FEATURES_SINCE_V2_0_0 is defined the deprecated features stated as DEPREC-ATED V2 are provided.

When BOOST_RATIO_DONT_PROVIDE_DEPRECATED_FEATURES_SINCE_V2_0_0 is defined the deprecated features stated as DEPRECATED V2 are NOT provided.

Version

BOOST_RATIO_VERSION stands for the Boost.Ratio version which can be 1 or 2. The default up to 1.55 is version 1. Since 1.56 it will be 2.

When BOOST_RATIO_VERSION is 1 BOOST_RATIO_PROVIDES_DEPRECATED_FEATURES_SINCE_V2_0_0 is defined by default.

When BOOST_RATIO_VERSION is 2 BOOST_RATIO_DONT_PROVIDE_DEPRECATED_FEATURES_SINCE_V2_0_0 is defined by default.

Static Assert

When BOOST_NO_STATIC_ASSERT is defined, the user can select the way static assertions are reported. Define

- BOOST_RATIO_USES_STATIC_ASSERT to use Boost.StaticAssert.
- BOOST_RATIO_USES_MPL_ASSERT to use **Boost.MPL** static assertions.
- BOOST_RATIO_USES_ARRAY_ASSERT to use **Boost.Ratio** internal static assertions.

The default behavior is as if BOOST_RATIO_USES_ARRAY_ASSERT was defined.

When BOOST_RATIO_USES_MPL_ASSERT is not defined the following symbols are defined as shown:

```
#define BOOST_RATIO_OVERFLOW_IN_ADD "overflow in ratio add"
#define BOOST_RATIO_OVERFLOW_IN_SUB "overflow in ratio sub"
#define BOOST_RATIO_OVERFLOW_IN_MUL "overflow in ratio mul"
#define BOOST_RATIO_OVERFLOW_IN_DIV "overflow in ratio div"
#define BOOST_RATIO_NUMERATOR_IS_OUT_OF_RANGE "ratio numerator is out of range"
#define BOOST_RATIO_DIVIDE_BY_0 "ratio divide by 0"
#define BOOST_RATIO_DENOMINATOR_IS_OUT_OF_RANGE "ratio denominator is out of range"
```



Depending upon the static assertion system used, a hint as to the failing assertion will appear in some form in the compiler diagnostic output.

C++0x Recommendation

Header <boost/ratio.hpp>

This header includes all the ratio related header files

```
#include <boost/ratio/ratio.hpp>
#include <boost/ratio/ratio_io.hpp>
#include <boost/ratio/rational_constant.hpp>
```

Header <boost/ratio/ratio_fwd.hpp>

This header provides forward declarations for the <boost/ratio/ratio.hpp> file.

```
namespace boost
    template <boost::intmax_t N, boost::intmax_t D = 1> class ratio;
    // ratio arithmetic
    template <class R1, class R2> struct ratio_add;
    template <class R1, class R2> struct ratio_subtract;
    template <class R1, class R2> struct ratio_multiply;
    template <class R1, class R2> struct ratio_divide;
#ifdef BOOST_RATIO_EXTENSIONS
    template <class R,int P> struct ratio_power;
    template <class R> struct ratio_negate;
    template <class R> struct ratio_sign;
    template <class R> struct ratio_abs;
    template <class R1, class R2> struct ratio_gcd;
    template <class R1, class R2> struct ratio_lcm;
#endif
    // ratio comparison
    template <class R1, class R2> struct ratio_equal;
    template <class R1, class R2> struct ratio_not_equal;
    template <class R1, class R2> struct ratio_less;
    template <class R1, class R2> struct ratio_less_equal;
    template <class R1, class R2> struct ratio_greater;
    template <class R1, class R2> struct ratio_greater_equal;
    // convenience SI typedefs
    typedef ratio<1LL, 100000000000000000LL> atto;
   typedef ratio<1LL, 100000000000LL> pico;
                           1000000000LL> nano;
    typedef ratio<1LL,
    typedef ratio<1LL,
                                 1000000LL> micro;
    typedef ratio<1LL,
                                    1000LL> milli;
    typedef ratio<1LL,
                                     100LL> centi;
                                     10LL> deci;
    typedef ratio<1LL,
    typedef ratio<
                                10LL, 1LL> deca;
   typedef ratio<
                               100LL, 1LL> hecto;
                              1000LL, 1LL> kilo;
    typedef ratio<
    typedef ratio<
                           1000000LL, 1LL> mega;
    typedef ratio<
                         1000000000LL, 1LL> giga;
                      1000000000000LL, 1LL> tera;
    typedef ratio<
    typedef ratio< 100000000000000LL, 1LL> peta;
    typedef ratio<100000000000000000LL, 1LL> exa;
```



Header <boost/ratio/ratio.hpp>

ratio is a facility which is useful in specifying compile-time rational constants. Compile-time rational arithmetic is supported with protection against overflow and divide by zero. Such a facility is very handy to efficiently represent 1/3 of a nanosecond, or to specify an inch in terms of meters (for example 254/10000 meters - which ratio will reduce to 127/5000 meters).

Class Template ratio<>

```
template <boost::intmax_t N, boost::intmax_t D>
class ratio {
public:
    static const boost::intmax_t num;
    static const boost::intmax_t den;
    typedef ratio<num, den> type;
    #ifdef BOOST_RATIO_EXTENSIONS
    typedef mpl::rational_c_tag tag;
    typedef boost::rational<boost::intmax_t> value_type;
    typedef boost::intmax_t num_type;
    typedef boost::intmax_t den_type;
    ratio() = default;
    template <intmax_t _N2, intmax_t _D2>
    ratio(const ratio<_N2, _D2>&);
    template <intmax_t _N2, intmax_t _D2>
    ratio& operator=(const ratio<_N2, _D2>&);
    static value_type value();
    value_type operator()() const;
    #endif
};
```

A diagnostic will be emitted if ratio is instantiated with D = 0, or if the absolute value of N or D cannot be represented. **Note:** These rules ensure that infinite ratios are avoided and that for any negative input, there exists a representable value of its absolute value which is positive. In a two's complement representation, this excludes the most negative value.

The members num and den will be normalized values of the template arguments N and D computed as follows. Let gcd denote the greatest common divisor of N's absolute value and of D's absolute value. Then:

- num has the value sign(N)*sign(D)*abs(N)/gcd.
- den has the value abs(D)/gcd.

The nested typedef type denotes the normalized form of this ratio type. It should be used when the normalized form of the template arguments are required, since the arguments are not necessarily normalized.



Two ratio classes ratio<N1,D1> and ratio<N2,D2> have the same normalized form if ratio<N1,D1>::type is the same type as ratio<N2,D2>::type

Construction and Assignment

Included only if BOOST_RATIO_EXTENSIONS is defined.

Default Constructor

```
ratio()=default;
```

Effects: Constructs a ratio object.

Copy Constructor

```
template <intmax_t N2, intmax_t D2>
  ratio(const ratio<N2, D2>& r);
```

Effects: Constructs a ratio object.

Remarks: This constructor will not participate in overload resolution unless r has the same normalized form as *this.

Assignement

```
template <intmax_t N2, intmax_t D2>
  ratio& operator=(const ratio<N2, D2>& r);
```

Effects: Assigns a ratio object.

Returns: *this.

Remarks: This operator will not participate in overload resolution unless r has the same normalized form as *this.

MPL Numeric Metafunctions

Included only if BOOST_RATIO_EXTENSIONS is defined.

In order to work with **Boost.MPL** numeric metafunctions as a Rational Constant, the following has beed added:

```
typedef mpl::rational_c_tag tag;
typedef boost::rational<boost::intmax_t> value_type;
typedef boost::intmax_t num_type;
typedef boost::intmax_t den_type;
```

Observers

Included only if BOOST_RATIO_EXTENSIONS is defined.

```
static value_type value();
value_type operator()() const;
```

Returns: value_type(num,den);

ratio Arithmetic

For each of the class templates in this section, each template parameter refers to a ratio. If the implementation is unable to form the indicated ratio due to overflow, a diagnostic will be issued.



ratio_add<>

```
template <class R1, class R2> struct ratio_add {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den + R2::num * R1::den , R1::den * R2::den>::type.

ratio_subtract<>

```
template <class R1, class R2> struct ratio_subtract {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den - R2::num * R1::den, R1::den * R2::den>::type.

ratio_multiply<>

```
template <class R1, class R2> struct ratio_multiply {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::num, R1::den * R2::den>::type.

ratio_divide<>

```
template <class R1, class R2> struct ratio_divide {
   typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<R1::num * R2::den, R2::num * R1::den>::type.

ratio_power<>

Included only if BOOST_RATIO_EXTENSIONS is defined.

```
template <class R, int P> struct ratio_power {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for R* *R P times.

ratio_negate<>

Included only if BOOST_RATIO_EXTENSIONS is defined.

This extension of the C++ standard helps in the definition of some **Boost.MPL** numeric metafunctions.

```
template <class R> struct ratio_negate {
   typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio < -R::num, R::den > ::type.

ratio_abs<>

Included only if BOOST_RATIO_EXTENSIONS is defined.



This extension of the C++ standard helps in the definition of some **Boost.MPL** numeric metafunctions.

```
template <class R> struct ratio_abs {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<abs_c<intmax_t,R::num>::value, R::den>::type.

ratio_sign<>

Included only if BOOST_RATIO_EXTENSIONS is defined.

This extension of the C++ standard helps in the definition of some **Boost.MPL** numeric metafunctions.

```
template <class R> struct ratio_sign {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for sign_c<intmax_t,R::num>::type.

ratio_gcd<>

Included only if BOOST_RATIO_EXTENSIONS is defined.

This extension of the C++ standard helps in the definition of some **Boost.MPL** numeric metafunctions.

```
template <class R1, class R2> struct ratio_gcd {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<gcd_c<intmax_t, R1::num, R2::num>::value, mp1::lcm_c<intmax_t, R1::den, R2::den>::value>::type.

ratio_lcm<>

Included only if BOOST_RATIO_EXTENSIONS is defined.

This extension of the C++ standard helps in the definition of some **Boost.MPL** numeric metafunctions.

```
template <class R1, class R2> struct ratio_lcm {
  typedef [/see below] type;
};
```

The nested typedef type is a synonym for ratio<lcm_c<intmax_t, R1::num, R2::num>::value, gcd_c<intmax_t, R1::den, R2::den>::value>::type.

ratio Comparison

ratio_equal<>

If R1::num == R2::num && R1::den == R2::den, ratio_equal derives from true_type, else derives from false_type.



ratio_not_equal<>

ratio_less<>

```
template <class R1, class R2>
struct ratio_less
   : public boost::integral_constant<bool, [/see below] > {};
```

If R1::num * R2::den < R2::num * R1::den, ratio_less derives from true_type, else derives from false_type.

ratio_less_equal<>

ratio_greater<>

```
template <class R1, class R2> struct ratio_greater
     : public boost::integral_constant<bool, ratio_less<R2, R1>::value> {};
```

ratio_greater_equal<>

SI typedefs

The International System of Units specifies twenty SI prefixes. Boost.Ratio defines all except yocto, zepto, zetta, and yotta

```
// convenience SI typedefs
typedef ratio<1LL, 1000000000000000000LL> atto;
typedef ratio<1LL,
typedef ratio<1LL,
100000000000000LL> femto;
typedef ratio<1LL,
1000000000000LL> pico;
                      100000000000LL> pico;
typedef ratio<1LL,
                           1000000000LL> nano;
typedef ratio<1LL,
                                1000000LL> micro;
typedef ratio<1LL,
                                   1000LL> milli;
typedef ratio<1LL,
                                     100LL> centi;
                                      10LL> deci;
typedef ratio<1LL,
typedef ratio<
                                10LL, 1LL> deca;
typedef ratio<
                               100LL, 1LL> hecto;
                               1000LL, 1LL> kilo;
typedef ratio<
typedef ratio<
                          1000000LL, 1LL> mega;
                       1000000000LL, 1LL> giga;
typedef ratio<
                    1000000000000LL, 1LL> tera;
typedef ratio<
                1000000000000000LL, 1LL> peta;
typedef ratio<
typedef ratio<100000000000000000LL, 1LL> exa;
```

IEC typedefs

Included only if BOOST_RATIO_EXTENSIONS is defined.

The Specific units of IEC 60027-2 A.2 and ISO/IEC 80000 specifies height IEC prefixes. **Boost.Ratio** defines all except zebi and yobi



Limitations

The following are limitations of Boost.Ratio relative to the specification in the C++0x draft standard:

- Four of the SI units typedefs -- yocto, zepto, zetta, and yotta -- are to be conditionally supported, if the range of intmax_t allows, but are not supported by **Boost.Ratio**.
- Ratio values should be of type static constexpr intmax_t (see Ratio values should be constexpr), but for compiler not supporting constexpr today, **Boost.Ratio** uses static const intmax_t instead.
- Rational arithmetic should use template aliases (see Rational Arithmetic should use template aliases), but those are not available in C++03, so inheritance is used instead.

Extensions

When BOOST_RATIO_EXTENSIONS is defined Boost.Ratio provides the following extensions:

- Extends the requirements of the C++0x draft standard by making the copy constructor and copy assignment operator have the same normalized form (see copy constructor and assignment between ratios having the same normalized form).
- More C++ standard like metafunctions applied to ratio types, like __static_abs or __static_negate.
- An __Boost_Mpl rational constant concept and the associated __Boost_Mpl arithmetic and comparison specializations including __numeric_cast, __plus, __equal_to between others.

Ratio I/O

Header <boost/ratio/ratio_io.hpp>

This header provides ratio_string<> which can generate a textual representation of a ratio<> in the form of a std::ba-sic_string<>. These strings can be useful for I/O.



```
namespace boost {
    template <class Ratio, class charT> struct ratio_string;
    template <> struct ratio_string<atto, char>;
    template <> struct ratio_string<atto, char16_t>;
    template <> struct ratio_string<atto, char32_t>;
    template <> struct ratio_string<atto, wchar_t>;
    template <> struct ratio_string<femto, char>;
    template <> struct ratio_string<femto, char16_t>;
    template <> struct ratio_string<femto, char32_t>;
    template <> struct ratio_string<femto, wchar_t>;
    template <> struct ratio_string<pico, char>;
    template <> struct ratio_string<pico, char16_t>;
    template <> struct ratio_string<pico, char32_t>;
    template <> struct ratio_string<pico, wchar_t>;
    template <> struct ratio_string<nano, char>;
    template <> struct ratio_string<nano, char16_t>;
    template <> struct ratio_string<nano, char32_t>;
    template <> struct ratio_string<nano, wchar_t>;
    template <> struct ratio_string<micro, char>;
    template <> struct ratio_string<micro, char16_t>;
    template <> struct ratio_string<micro, char32_t>;
    template <> struct ratio_string<micro, wchar_t>;
    template <> struct ratio_string<milli, char>;
    template <> struct ratio_string<milli, char16_t>;
    template <> struct ratio_string<milli, char32_t>;
    template <> struct ratio_string<milli, wchar_t>;
    template <> struct ratio_string<centi, char>;
    template <> struct ratio_string<centi, char16_t>;
    template <> struct ratio_string<centi, char32_t>;
    template <> struct ratio_string<centi, wchar_t>;
    template <> struct ratio_string<deci, char>;
    template <> struct ratio_string<deci, char16_t>;
    template <> struct ratio_string<deci, char32_t>;
    template <> struct ratio_string<deci, wchar_t>;
    template <> struct ratio_string<deca, char>;
    template <> struct ratio_string<deca, char16_t>;
    template <> struct ratio_string<deca, char32_t>;
    template <> struct ratio_string<deca, wchar_t>;
    template <> struct ratio_string<hecto, char>;
    template <> struct ratio_string<hecto, char16_t>;
    template <> struct ratio_string<hecto, char32_t>;
    template <> struct ratio_string<hecto, wchar_t>;
    template <> struct ratio_string<kilo, char>;
    template <> struct ratio_string<kilo, char16_t>;
    template <> struct ratio_string<kilo, char32_t>;
    template <> struct ratio_string<kilo, wchar_t>;
    template <> struct ratio_string<mega, char>;
    template <> struct ratio_string<mega, char16_t>;
    template <> struct ratio_string<mega, char32_t>;
    template <> struct ratio_string<mega, wchar_t>;
```



```
template <> struct ratio_string<giga, char>;
template <> struct ratio_string<giga, char16_t>;
template <> struct ratio_string<giga, char32_t>;
template <> struct ratio_string<giga, wchar_t>;
template <> struct ratio_string<tera, char>;
template <> struct ratio_string<tera, char16_t>;
template <> struct ratio_string<tera, char32_t>;
template <> struct ratio_string<tera, wchar_t>;
template <> struct ratio_string<peta, char>;
template <> struct ratio_string<peta, char16_t>;
template <> struct ratio_string<peta, char32_t>;
template <> struct ratio_string<peta, wchar_t>;
template <> struct ratio_string<exa, char>;
template <> struct ratio_string<exa, char16_t>;
template <> struct ratio_string<exa, char32_t>;
template <> struct ratio_string<exa, wchar_t>;
template <> struct ratio_string<kibi, char>;
template <> struct ratio_string<kibi, char16_t>;
template <> struct ratio_string<kibi, char32_t>;
template <> struct ratio_string<kibi, wchar_t>;
template <> struct ratio_string<mebi, char>;
template <> struct ratio_string<mebi, char16_t>;
template <> struct ratio_string<mebi, char32_t>;
template <> struct ratio_string<mebi, wchar_t>;
template <> struct ratio_string<gibi, char>;
template <> struct ratio_string<gibi, char16_t>;
template <> struct ratio_string<gibi, char32_t>;
template <> struct ratio_string<gibi, wchar_t>;
template <> struct ratio_string<tebi, char>;
template <> struct ratio_string<tebi, char16_t>;
template <> struct ratio_string<tebi, char32_t>;
template <> struct ratio_string<tebi, wchar_t>;
template <> struct ratio_string<pebi, char>;
template <> struct ratio_string<pebi, char16_t>;
template <> struct ratio_string<pebi, char32_t>;
template <> struct ratio_string<pebi, wchar_t>;
template <> struct ratio_string<yobi, char>;
template <> struct ratio_string<yobi, char16_t>;
template <> struct ratio_string<yobi, char32_t>;
template <> struct ratio_string<yobi, wchar_t>;
```

Template Class ratio_string<>

```
template <class Ratio, class CharT>
struct ratio_string
{
    static std::basic_string<CharT> symbol();
    static std::basic_string<CharT> prefix();
    static std::basic_string<CharT> short_name(); // DEPRECATED V2
    static std::basic_string<CharT> long_name(); // DEPRECATED V2
};
```



The class template ratio_string provides textual representations of the associated ratio appropriate for the character type charT.

The primary template provides generic strings. Specializations provide the same static member functions but these functions return the English SI prefix and symbol names as specified by the General Conference on Weights and Measures.

Static Member function prefix()

```
template<class Ratio, class CharT>
basic_string<charT>
ratio_string<Ratio, CharT>::prefix();
```

Returns: A basic_string of the form: [Ratio::num/Ratio::den]

Example: ratio_string<ratio<2, 60>, wchar_t>::prefix() returns L"[1/30]".

Static Member function symbol()

```
template<class Ratio, class CharT>
basic_string<charT>
ratio_string<Ratio, CharT>::symbol();
```

Returns: prefix().

Static Member function long_name() DEPRECATED V2

```
template<class Ratio, class CharT>
basic_string<charT>
ratio_string<Ratio, CharT>::long_name();
```

Returns: prefix().

Static Member function short_name() DEPRECATED V2

```
template<class Ratio, class CharT>
basic_string<charT>
ratio_string<Ratio, CharT>::short_name();
```

Returns: symbol().

Specializations for ratio_string<>

With compilers supporting char16_t and char32_t and with a standard library don't providing std::u16string and std::u32string you will need to define the macros BOOST_NO_CXX11_U16STRING and BOOST_NO_CXX11_U32STRING until Boost.Config defines them.

For each specialization the table gives the return value for prefix() and symbol().



Table 1. The return values of specializations of ratio_string

Specialization	prefix()	symbol()
ratio_string <atto, char=""></atto,>	"atto"	"a"
ratio_string <atto, char16_t=""></atto,>	u"atto"	u"a"
ratio_string <atto, char32_t=""></atto,>	U"atto"	U"a"
ratio_string <atto, wchar_t=""></atto,>	L"atto"	L"a"
ratio_string <femto, char=""></femto,>	"femto"	"f"
ratio_string <femto, char16_t=""></femto,>	u"femto"	u"f"
ratio_string <femto, char32_t=""></femto,>	U"femto"	U"f"
ratio_string <femto, wchar_t=""></femto,>	L"femto"	L"f"
ratio_string <pico, char=""></pico,>	"pico"	"p"
ratio_string <pico, char16_t=""></pico,>	u"pico"	u"p"
ratio_string <pico, char32_t=""></pico,>	U"pico"	"q"U
ratio_string <pico, wchar_t=""></pico,>	L"pico"	L"p"
ratio_string <nano, char=""></nano,>	"nano"	"a"
ratio_string <nano, char16_t=""></nano,>	u"nano"	u"a"
ratio_string <nano, char32_t=""></nano,>	U"nano"	U"a"
ratio_string <nano, wchar_t=""></nano,>	L"nano"	L"a"
ratio_string <micro, char=""></micro,>	"micro"	u8"\u00B5"
ratio_string <micro, char16_t=""></micro,>	u"micro"	u"\u00B5"
ratio_string <micro, char32_t=""></micro,>	U"micro"	U"\u00B5"
ratio_string <micro, wchar_t=""></micro,>	L"micro"	Lu8"\u00B5"
ratio_string <milli, char=""></milli,>	"milli"	"m"
ratio_string <milli, char16_t=""></milli,>	u"milli"	u"m"
ratio_string <milli, char32_t=""></milli,>	U"milli"	U"m"
ratio_string <milli, wchar_t=""></milli,>	L"milli"	L"m"
ratio_string <centi, char=""></centi,>	"centi"	" C "
ratio_string <centi, char16_t=""></centi,>	u"centi"	u"c"
ratio_string <centi, char32_t=""></centi,>	U"centi"	U"c"



Specialization	prefix()	symbol()
ratio_string <centi, wchar_t=""></centi,>	L"centi"	L"c"
ratio_string <deci, char=""></deci,>	"deci"	"d"
ratio_string <deci, char16_t=""></deci,>	u"deci"	u"d"
ratio_string <deci, char32_t=""></deci,>	U"deci"	U"d"
ratio_string <deci, wchar_t=""></deci,>	L"deci"	L"d"
ratio_string <deca, char=""></deca,>	"deca"	"da"
ratio_string <deca, char16_t=""></deca,>	u"deca"	u"da"
ratio_string <deca, char32_t=""></deca,>	U"deca"	U"da"
ratio_string <deca, wchar_t=""></deca,>	L"deca"	L"da"
ratio_string <hecto, char=""></hecto,>	"hecto"	"h"
ratio_string <hecto, char16_t=""></hecto,>	u"hecto"	u"h"
ratio_string <hecto, char32_t=""></hecto,>	U"hecto"	U"h"
ratio_string <hecto, wchar_t=""></hecto,>	L"hecto"	L"h"
ratio_string <kilo, char=""></kilo,>	"kilo"	"k"
ratio_string <kilo, char16_t=""></kilo,>	u"kilo"	u"k"
ratio_string <kilo, char32_t=""></kilo,>	U"kilo"	U"k"
ratio_string <kilo, wchar_t=""></kilo,>	L"kilo"	L"k"
ratio_string <mega, char=""></mega,>	"mega"	"M"
ratio_string <mega, char16_t=""></mega,>	u"mega"	u"M"
ratio_string <mega, char32_t=""></mega,>	U"mega"	U"M"
ratio_string <mega, wchar_t=""></mega,>	L"mega"	L"M"
ratio_string <giga, char=""></giga,>	"giga"	" G "
ratio_string <giga, char16_t=""></giga,>	u"giga"	u"G"
ratio_string <giga, char32_t=""></giga,>	U"giga"	U"G"
ratio_string <giga, wchar_t=""></giga,>	L"giga"	L"G"
ratio_string <tera, char=""></tera,>	"tera"	"T"
ratio_string <tera, char16_t=""></tera,>	u"tera"	u"T"
ratio_string <tera, char32_t=""></tera,>	U"tera"	U"T"



Specialization	<pre>prefix()</pre>	symbol()
ratio_string <tera, wchar_t=""></tera,>	L"tera"	L"T"
ratio_string <peta, char=""></peta,>	"peta"	"P"
ratio_string <peta, char16_t=""></peta,>	u"peta"	u"P"
ratio_string <peta, char32_t=""></peta,>	U"peta"	U"P"
ratio_string <peta, wchar_t=""></peta,>	L"peta"	L"P"
ratio_string <exa, char=""></exa,>	"exa"	"E"
ratio_string <exa, char16_t=""></exa,>	u"exa"	u"E"
ratio_string <exa, char32_t=""></exa,>	U"exa"	U"E"
ratio_string <exa, wchar_t=""></exa,>	L"exa"	L"E"

Rational Constant

Rational Constant Concept

Description

A Rational Constant is a holder class for a compile-time value of a rational type. Every Rational Constant is also a nullary Metafunction, returning itself. A rational constant object is implicitly convertible to the corresponding run-time value of the rational type.

Expression requirements

In the following table and subsequent specifications, r is a model of Rational Constant.

Expression	Туре	Complexity
r::tag	rational_c_tag	Constant time
r::value_type	A rational type	Constant time
r::num_type	An integral type	Constant time
r::den_type	An integral type	Constant time
r::num	An Integral constant expression	Constant time
r::den	An Integral constant expression	Constant time
r::type	Rational Constant	Constant time
r::value_type const c=r()		Constant time



Expression semantics

Expression	Semantics
r::tag	r's tag type; r::tag::value is r's conversion rank.
r::value_type	A cv-unqualified type of r()
r::num_type	A cv-unqualified type of r::num
r::den_type	A cv-unqualified type of r::den
r::num	The numerator of the rational constant
r::den	The denominator of the rational constant
r::type	equal_to <n::type,n>::value == true.</n::type,n>
r::value_type const c=r()	r::value_type const c=r::value_type(r::num,r::den)

Models

• ratio<>

Header <boost/ratio/mpl/rational_constant.hpp>

This header includes all the rational constant related header files

```
#include <boost/ratio/mpl/rational_c_tag.hpp>
#include <boost/ratio/mpl/numeric_cast.hpp>
#include <boost/ratio/mpl/arithmetic.hpp>
#include <boost/ratio/mpl/comparison.hpp>
```

Header <boost/ratio/mpl/rational_c_tag.hpp>

```
namespace boost {
namespace mpl {
    struct rational_c_tag : int_<10> {};
}
}
```

Header <boost/ratio/mpl/numeric_cast.hpp>

```
namespace boost {
namespace mpl {
    template<> struct numeric_cast< integral_c_tag,rational_c_tag >;
}
}
```



mpl::numeric_cast<> Specialization

A Integral Constant is seen as a ratio with numerator the Integral Constant value and denominator 1.

```
template<> struct numeric_cast< integral_c_tag,rational_c_tag >
{
   template< typename N > struct apply
        : ratio< N::value, 1 >
   {
   };
};
```

Header <boost/ratio/mpl/arithmetic.hpp>

This header includes all the rational constant arithmetic MPL specializations.

```
#include <boost/ratio/mpl/plus.hpp>
#include <boost/ratio/mpl/minus.hpp>
#include <boost/ratio/mpl/times.hpp>
#include <boost/ratio/mpl/divides.hpp>
#include <boost/ratio/mpl/negate.hpp>
#include <boost/ratio/mpl/abs.hpp>
#include <boost/ratio/mpl/sign.hpp>
#include <boost/ratio/mpl/gcd.hpp>
#include <boost/ratio/mpl/gcd.hpp>
#include <boost/ratio/mpl/lcm.hpp>
```

Header <boost/ratio/mpl/plus.hpp>

```
namespace boost {
namespace mpl {
    template<>
       struct plus_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::plus_impl<> Specialization

The specialization relays on the ratio_add template class.

Header <boost/ratio/mpl/minus.hpp>

```
namespace boost {
namespace mpl {
    template<>
    struct minus_impl< rational_c_tag,rational_c_tag >;
}
}
```



mpl::minus_impl<> Specialization

The specialization relays on the ratio_subtract template class.

Header <boost/ratio/mpl/times.hpp>

```
namespace boost {
namespace mpl {
    template<>
    struct times_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::times_impl<> Specialization

The specialization relays on the ratio_multiply template class.

Header <boost/ratio/mpl/divides.hpp>

```
namespace boost {
namespace mpl {
   template<>
    struct divides_impl< rational_c_tag,rational_c_tag >;
}
}
```

mpl::divides_impl<> Specialization

The specialization relays on the ratio_divide template class.



Header <boost/ratio/mpl/gcd.hpp>

```
namespace boost {
namespace mpl {
   template<>
    struct gcd_impl< rational_c_tag,rational_c_tag >;
}
}
```

mpl::gcd_impl<> Specialization

The specialization relays on the ratio_gcd template class.

Header <boost/ratio/mpl/lcm.hpp>

```
namespace boost {
namespace mpl {
    template<>
       struct lcm_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::lcm_impl<> Specialization

The specialization relays on the ratio_lcm template class.

Header <boost/ratio/mpl/negate.hpp>

```
namespace boost {
namespace mpl {
    template<>
       struct negate_impl< rational_c_tag >;
}
```

mpl::negate_impl<> Specialization

The specialization relays on the ratio_negate template class.



```
template<>
struct negate_impl< rational_c_tag >
{
   template< typename R > struct apply
        : ratio_negate<R>
   {
    };
};
```

Header <boost/ratio/mpl/abs.hpp>

```
namespace boost {
namespace mpl {
    template<>
    struct abs_impl< rational_c_tag >;
}
```

mpl::abs_impl<> Specialization

The specialization relays on the ratio_abs template class.

Header <boost/ratio/mpl/sign.hpp>

```
namespace boost {
namespace mpl {
   template<>
    struct sign_impl< rational_c_tag >;
}
```

mpl::sign_impl<> Specialization

The specialization relays on the ratio_sign template class.

Header <boost/ratio/mpl/comparison.hpp>

This header includes all the rational constant comparison MPL specializations.



```
#include <boost/ratio/mpl/equal_to.hpp>
#include <boost/ratio/mpl/not_equal_to.hpp>
#include <boost/ratio/mpl/less.hpp>
#include <boost/ratio/mpl/less_equal.hpp>
#include <boost/ratio/mpl/greater.hpp>
#include <boost/ratio/mpl/greater_equal.hpp>
```

Header <boost/ratio/mpl/equal_to.hpp>

```
namespace boost {
namespace mpl {
    template<>
    struct equal_to_impl< rational_c_tag,rational_c_tag >;
}
}
```

mpl::equal_to_impl<> Specialization

The specialization relays on the ratio_equal template class.

Header <boost/ratio/mpl/not_equal_to.hpp>

```
namespace boost {
namespace mpl {
    template<>
        struct not_equal_to_impl< rational_c_tag,rational_c_tag >;
}
}
```

mpl::not_equal_to_impl<> Specialization

The specialization relays on the ratio_not_equal template class.



Header <boost/ratio/mpl/less.hpp>

```
namespace boost {
namespace mpl {
   template<>
    struct less_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::less_impl<> Specialization

The specialization relays on the ratio_less template class.

Header <boost/ratio/mpl/less_equal.hpp>

```
namespace boost {
namespace mpl {
    template<>
    struct less_equal_impl< rational_c_tag,rational_c_tag >;
}
}
```

mpl::less_equal_impl<> Specialization

The specialization relays on the ratio_less_equal template class.

Header <boost/ratio/mpl/greater.hpp>

```
namespace boost {
namespace mpl {
    template<>
        struct greater_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::greater_impl<> Specialization

The specialization relays on the ${\tt ratio_greater}$ template class.



Header <boost/ratio/mpl/greater_equal.hpp>

```
namespace boost {
namespace mpl {
   template<>
    struct greater_equal_impl< rational_c_tag,rational_c_tag >;
}
```

mpl::greater_equal_impl<> Specialization

The specialization relays on the ratio_greater_equal template class.



Appendices

Appendix A: History

Version 2.1.0, Febreary 1, 2014 - 1.56

New Features:

- #XXXX Add ratio_power.
- #XXXX Add IEC binary prefixes.

Version 2.0.1, Febreary 1, 2013 - 1.53

Fixes:

• #7616 br_mul::nan - warning C4293: '<<' : shift count negative or too big, undefined behavior`.

Version 2.0.0, November 1, 2012 - 1.52

Features:

• Replace the short_name and long_name functions by symbol and prefix functions respectively.

Deprecated:

The ratio_string<>::short_name and ratio_string<>::long_name are deprecated. Use ratio_string<>::symbol and ratio_string<>::prefix respectively. These functions be removed in 1.55.

Fixes:

• #7478 Compiles fails with compilers supporting char16_t and char32_t fails if the library doesn't provides std::u16string and std::u32string.

Version 1.0.3, August 1, 2012 - 1.51

Fixes:

• #7075 Workaround for error: the type of partial specialization template parameter constant "n1" depends on another template parameter.

Version 1.0.2, April 1, 2012 - 1.50

Fixes:

• #6498 boost::ratio won't compile with default settings.

Version 1.0.1, Jan 8, 2011

Features:

• Added MPL Rational Constant and the associated numeric metafunction specializations.

Version 1.0.0, Jan 2, 2011

· Moved ratio to trunk.



· Documentation revision.

Version 0.2.1, September 27, 2010

Fixes:

· Removal of LLVM adapted files due to incompatible License issue.

Version 0.2.0, September 22, 2010

Features:

• Added ratio_string traits.

Fixes:

• ratio_less overflow avoided following the algorithm from libc++.

Test:

• A more complete test has been included adapted from the test of from libc++/ratio.

Version 0.1.0, September 10, 2010

Features:

• Ratio has been extracted from Boost.Chrono.

Appendix B: Rationale

Why ratio needs CopyConstruction and Assignment from ratios having the same normalized form

Current N3000 doesn't allows to copy-construct or assign ratio instances of ratio classes having the same normalized form.

This simple example

```
ratio<1,3> r1;
ratio<3,9> r2;
r1 = r2; // (1)
```

fails to compile in (1). Other example

```
ratio<1,3> r1;
ratio_subtract<ratio<2,3>,ratio<1,3> > r2=r1; // (2)
```

The type of ratio_subtract<ratio<2,3>,ratio<1,3> > could be ratio<3,9> so the compilation could fail in (2). It could also be ratio<1,3> and the compilation succeeds.

Why ratio needs the nested normalizer typedef type

The current resolution of issue LWG 1281 acknowledges the need for a nested type typedef, so Boost.Ratio is tracking the likely final version of std::ratio.



Appendix C: Implementation Notes

How does Boost.Ratio try to avoid compile-time rational arithmetic overflow?

When the result is representable, but a simple application of arithmetic rules would result in overflow, e.g. ratio_multiply<ratio<INTMAX_MAX,2>,ratio<2,INTMAX_MAX>> can be reduced to ratio<1,1>, but the direct result of ratio<INTMAX_MAX*2, INT-MAX_MAX*2> would result in overflow.

Boost.Ratio implements some simplifications in order to reduce the possibility of overflow. The general ideas are:

- The num and den ratio<> fields are normalized.
- Use the gcd of some of the possible products that can overflow, and simplify before doing the product.
- Use some equivalences relations that avoid addition or subtraction that can overflow or underflow.

The following subsections cover each case in more detail.

ratio_add

In

```
(n1/d1)+(n2/d2)=(n1*d2+n2*d1)/(d1*d2)
```

either n1*d2+n2*d1 or d1*d2 can overflow.

```
( (n1 * d2) + (n2 * d1) )
------(d1 * d2)
```

Dividing by gcd(d1,d2) on both num and den

```
( (n1 * (d2/gcd(d1,d2))) + (n2 * (d1/gcd(d1,d2))) )
------
((d1 * d2) / gcd(d1,d2))
```

Multiplying and diving by gcd(n1,n2) in numerator

Factorizing gcd(n1,n2)

Regrouping



```
( gcd(n1,n2) *
  ( ((n1/gcd(n1,n2)) * (d2/gcd(d1,d2))) + ((n2/gcd(n1,n2)) * (d1/gcd(d1,d2))) )
)
( (d1 / gcd(d1,d2)) * d2 )
```

Dividing by (d1 / gcd(d1,d2))

```
( ( gcd(n1,n2) / (d1 / gcd(d1,d2)) ) *
  ( ((n1/gcd(n1,n2)) * (d2/gcd(d1,d2))) + ((n2/gcd(n1,n2)) * (d1/gcd(d1,d2))) )
)
d2
```

Dividing by d2

```
( gcd(n1,n2) / (d1 / gcd(d1,d2)) ) *
( ((n1/gcd(n1,n2)) * (d2/gcd(d1,d2))) + ((n2/gcd(n1,n2)) * (d1/gcd(d1,d2))) / d2 )
```

This expression correspond to the multiply of two ratios that have less risk of overflow as the initial numerators and denominators appear now in most of the cases divided by a gcd.

For ratio_subtract the reasoning is the same.

ratio_multiply

In

```
(n1/d1)*(n2/d2)=((n1*n2)/(d1*d2))
```

either n1*n2 or d1*d2 can overflow.

Dividing by gcc(n1,d2) numerator and denominator

```
(((n1/gcc(n1,d2))*n2)
-----(d1*(d2/gcc(n1,d2))))
```

Dividing by gcc(n2,d1)

```
((n1/gcc(n1,d2))*(n2/gcc(n2,d1)))
------
((d1/gcc(n2,d1))*(d2/gcc(n1,d2)))
```

And now all the initial numerator and denominators have been reduced, avoiding the overflow.

For ratio_divide the reasoning is similar.

ratio_less

In order to evaluate

```
(n1/d1) < (n2/d2)
```

without moving to floating-point numbers, two techniques are used:



• First compare the sign of the numerators.

If sign(n1) < sign(n2) the result is true.

If sign(n1) == sign(n2) the result depends on the following after making the numerators positive

· When the sign is equal the technique used is to work with integer division and modulo when the signs are equal.

Let call Qi the integer division of ni and di, and Mi the modulo of ni and di.

```
ni = Qi * di + Mi and Mi < di
```

Form

```
((n1*d2)<(d1*n2))
```

we get

Developing

Dividing by d1*d2

```
Q1 + (M1/d1) < Q2 + (M2/d2)
```

If Q1=Q2 the result depends on

```
(M1/d1) < (M2/d2)
```

If M1==0==M2 the result is false

If M1=0 M2!=0 the result is true

If M1!=0 M2==0 the result is false

If M1!=0 M2!=0 the result depends on

```
(d2/M2) < (d1/M1)
```

If Q1!=Q2, the result of

```
Q1 + (M1/d1) < Q2 + (M2/d2)
```

depends only on Q1 and Q2 as Qi are integers and (Mi/di) <1 because Mi<di.

if Q1>Q2, Q1==Q2+k, k>=1



but the difference between two numbers between 0 and 1 can not be greater than 1, so the result is false.

if
$$Q2>Q1$$
, $Q2==Q1+k$, $k>=1$

which is always true, so the result is true.

The following table recapitulates this analisys

ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q1	Q2	M1	M2	Result
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q1	Q2	!=0	!=0	Q1 < Q2
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	0	0	false
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	0	!=0	true
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	!=0	0	false
ratio <n1,d1></n1,d1>	ratio <n2,d2></n2,d2>	Q	Q	!=0	!=0	ratio_less <ra- tio<d2,m2>, ra- tio<d1 m1="">></d1></d2,m2></ra-

Appendix D: FAQ

Appendix E: Acknowledgements

The library code was derived from Howard Hinnant's time2_demo prototype. Many thanks to Howard for making his code available under the Boost license. The original code was modified by Beman Dawes to conform to Boost conventions.

time2_demo contained this comment:

Much thanks to Andrei Alexandrescu, Walter Brown, Peter Dimov, Jeff Garland, Terry Golubiewski, Daniel Krugler, Anthony Williams.

Howard Hinnant, who is the real author of the library, has provided valuable feedback and suggestions during the development of the library. In particular, The ratio_io.hpp source has been adapted from the experimental header <ratio_io> from Howard Hinnant.

The acceptance review of Boost.Ratio took place between October 2nd and 11th 2010. Many thanks to Anthony Williams, the review manager, and to all the reviewers: Bruno Santos, Joel Falcou, Robert Stewart, Roland Bock, Tom Tan and Paul A. Bristol.

Thanks to Andrew Chinoff and Paul A. Bristol for his help polishing the documentation.

Appendix F: Tests

In order to test you need to run

bjam libs/ratio/test

You can also run a specific suite of test by doing



cd libs/chrono/test
bjam ratio

ratio

Name	kind	Description	Result	Ticket
typedefs.pass	run	check the num/den are correct for the pre- defined typedefs	Pass	#
ratio.pass	run	check the num/den are correctly simplified	Pass	#
ratio1.fail	compile-fails	The template argument D shall not be zero	Pass	#
ratio2.fail	compile-fails	the absolute values of the template arguments N and D shall be repres- entable by type int- max_t	Pass	#
ratio3.fail	compile-fails	the absolute values of the template arguments N and D shall be repres- entable by type int- max_t	Pass	#

comparison

Name	kind	Description	Result	Ticket
ratio_equal.pass	run	check ratio_equal metafunction class	Pass	#
ratio_not_equal.pass	run	check ratio_not_equal metafunction class	Pass	#
ratio_less.pass	run	check ratio_less metafunction class	Pass	#
ratio_less_equal.pass	run	check ratio_less_equal metafunction class	Pass	#
ratio_greater.pass	run	check ratio_greater metafunction class	Pass	#
ratio_greater_equal.pass	run	check ratio_great- er_equal metafunction class	Pass	#



arithmetic

Name	kind	Description	Result	Ticket
ratio_add.pass	run	check ratio_add metafunction class	Pass	#
ratio_subtract.pass	run	check ratio_subtract metafunction class	Pass	#
ratio_multiply.pass	run	check ratio_multiply metafunction class	Pass	#
ratio_divide.pass	run	check ratio_divide metafunction class	Pass	#
ratio_add.fail	compile-fails	check ratio_add over- flow metafunction class	Pass	#
ratio_subtract.fail	compile-fails	check ratio_subtract underflow metafunction class	Pass	#
ratio_multiply.fail	compile-fails	check ratio_multiply overflow metafunction class	Pass	#
ratio_divide.fail	compile-fails	check ratio_divide overflow metafunction class	Pass	#

Appendix G: Tickets

Ticket	Description	Resolution	State
1	result of metafunctions ratio_multiply and ratio_divide were not normalized ratios.	Use of the nested ratio typedef type on ratio arithmetic operations.	Closed
2	INTMAX_C is not always defined.	Replace INTMAX_C by BOOST_INTMAX_C until boost/cstdint.hpp ensures INTMAX_C is always defined.	Closed
3	MSVC reports a warning instead of an error when there is an integral constant overflow.	manage with MSVC reporting a warning instead of an error when there is an integral constant overflow.	Closed
4	ration_less overflow on cases where it can be avoided.	Change the algorithm as implemented in libc++.	Closed



Appendix H: Future Plans

For later releases

- Use template aliases on compiler providing it.
- Implement multiple arguments ratio arithmetic.

