#### SANDIP FOUNDATION'S

# Sandip Institute of Technology and Research Centre, Nashik



# LABORATORY MANUAL

# FINITE ELEMENT ANALYSIS

(Course Code: 402044A)

**Final Year of Mechanical Engineering** 

(2015 Course)

A. Y. 2018-2019

Semester I
DEPAREMENT OF MECHANICAL ENGINEERING

# **CAD CAM LABORATORY**

# LABORATORY MANUAL

for

Final year Mechanical Engineering

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# Department of Mechanical Engineering

Sandip Institute of Technology and Research Centre, Mahiravani, Nashik 422213.

# Vision and Mission of the Department of Mechanical Engineering

#### **VISION**

 To achieve excellence in the domain of mechanical engineering by inculcating a culture of learning and research

#### **MISSION**

- To nurture the students of Mechanical Engineering to be competent, motivated and ethical professionals.
- To foster research, innovation and entrepreneurship skills leading to employable and self-reliant technocrats.
- To groom the socio-techno potential for up-liftment of society.

Programme Educational Objectives (PEOs)			
PEO1	To apply knowledge in Mechanical Engineering to improve lives and livelihoods of human beings through a successful career in industry and other related fields.		
PEO2	To develop technologist and innovators for addressing social, technical and business challenges.		
PEO3	To demonstrate personal growth by pursuing higher studies, professional development courses, and /or engineering certification.		
Programme Specific Outcomes (PSOs)			
PSO1	<b>Professional skills</b> – Graduates will engage in higher studies, research and other continuous professional development activities.		
PSO2	<b>Problem solving skills</b> – Graduate will demonstrate the ability to provide solutions to social, technical and business challenges.		
PSO3	Successful career and Entrepreneurship – Graduate will demonstrate the ability to cater the needs of mechanical industries.		



# Department of Mechanical Engineering

Sandip Institute of Technology and Research Centre, Mahiravani, Nashik 422213

#### PROGRAMME OUTCOMES (POs)

Engineering Graduates will be able to:			
P01	Engineering Knowledge - apply knowledge of mathematics, science and engineering to solve the real life problems in Mechanical systems.[I]		
P02	<b>Problem Analysis</b> – identify, formulate and solve Mechanical Engineering problems in thermal, manufacturing and machine design and conduct new experiments.[I]		
P03	<b>Design/development of Solutions</b> – design systems like thermal, robotics, mechatronics and machines within realistic constraints. [III]		
P04	Conduct investigations of complex problems – design and conduct experiments to interpret data and analyse the results.[I,IIII]		
P05	<b>Modern Tool Usage</b> – to develop awareness and work on emerging technologies like CAD/CAM software's, Robotics.[II]		
P06	The engineer and society – understand the impact of an engineer in general and Mechanical Engineering knowledge for welfare of society in particular.[I,II,III]		
P07	Environment and Sustainability – develop or modify eco-friendly and highly reliable as well as sustainable systems.[I,III]		
P08	Ethics – take professional decision with a sense of ethical responsibility. [I]		
P09	Individual and team work – function effectively as an individual and as a member or leader in multidisciplinary and/or cross cultural teams. [I]		
P10	Communication – communicate effectively for achievements of goals. [I,II]		
P11	<b>Project Management and Finance</b> – execute disciplinary and interdisciplinary projects in day-to-day life. [I,II]		
P12	Life-Long Learning – to imbibe habit of lifelong learning. [II,III]		

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**Performing a Typical ANSYS Analysis** 

The ANSYS program has many finite element analysis capabilities, ranging from a simple,

linear, static analysis to a complex, nonlinear, transient dynamic analysis. The analysis guide

manuals in the ANSYS documentation set describe specific procedures for performing

analyses for different engineering disciplines.

A typical ANSYS analysis has three distinct steps:

Build the model.

Apply loads and obtain the solution.

Review the results.

**Building a Model** 

Building a finite element model requires more of an ANSYS user's time than any other part

of the analysis. First, you specify a job name and analysis title. Then, you use the PREP7

preprocessor to define the element types, element real constants, material properties, and the

model geometry.

Specifying a Job name and Analysis Title

This task is not required for an analysis, but is recommended.

**Defining the Job name** 

The job name is a name that identifies the ANSYS job. When you define a job name for an

analysis, the job name becomes the first part of the name of all files the analysis creates. (The

extension or suffix for these files' names is a file identifier such as .DB.) By using a job name

for each analysis, you insure that no files are overwritten. If you do not specify a job name,

all files receive the name FILE or file, depending on the operating system.

Command(s): /FILNAME

**GUI: Utility Menu>File>Change Job name** 

**Defining Element Types** 

The ANSYS element library contains more than 100 different element types. Each element

type has a unique number and a prefix that identifies the element category: BEAM4,

PLANE77, SOLID96, etc. The following element categories are available

The element type determines, among other things:

- The degree-of-freedom set (which in turn implies the discipline-structural, thermal, magnetic, electric, quadrilateral, brick, etc.)
- Whether the element lies in two-dimensional or three-dimensional space.

For example, BEAM4, has six structural degrees of freedom (UX, UY, UZ, ROTX, ROTY, ROTZ), is a line element, and can be modeled in 3-D space. PLANE77 has a thermal degree of freedom (TEMP), is an eight-node quadrilateral element, and can be modeled only in 2-D space.

#### **Defining Element Real Constants**

Element real constants are properties that depend on the element type, such as cross-sectional properties of a beam element. For example, real constants for BEAM3, the 2-D beam element, are area (AREA), moment of inertia (IZZ), height (HEIGHT), shear deflection constant (SHEARZ), initial strain (ISTRN), and added mass per unit length (ADDMAS). Not all element types require real constants, and different elements of the same type may have different real constant values.

As with element types, each set of real constants has a reference number, and the table of reference number versus real constant set is called the *real constant table*. While defining the elements, you point to the appropriate real constant reference number using the **REAL** command

## (Main Menu> Preprocessor>Create>Elements>Elem Attributes).

#### **Defining Material Properties**

Most element types require material properties. Depending on the application, material properties may be:

- Linear or nonlinear
- Isotropic, orthotropic, or anisotropic
- Constant temperature or temperature-dependent.

As with element types and real constants, each set of material properties has a material reference number. The table of material reference numbers versus material property sets is called the *material table*. Within one analysis, you may have multiple material property sets (to correspond with multiple materials used in the model). ANSYS identifies each set with a unique reference number.

#### Main Menu > Preprocessor> Material Props > Material Models.

#### **Creating the Model Geometry**

Once you have defined material properties, the next step in an analysis is generating a finite element model-nodes and elements-that adequately describes the model geometry.

There are two methods to create the finite element model: solid modeling and direct generation.

With solid modeling, you describe the geometric shape of your model, and then instruct the ANSYS program to automatically mesh the geometry with nodes and elements. You can control the size and shape of the elements that the program creates. With *direct generation*, you "manually" define the location of each node and the connectivity of each element. Several convenience operations, such as copying patterns of existing nodes and elements, symmetry reflection, etc. are available.

## **Apply Loads and Obtain the Solution**

In this step, you use the SOLUTION processor to define the analysis type and analysis options, apply loads, specify load step options, and initiate the finite element solution. You also can apply loads using the PREP7 preprocessor.

#### **Applying Loads**

The word loads as used in this manual includes boundary conditions (constraints, supports, or boundary field specifications) as well as other externally and internally applied loads. Loads in the ANSYS program are divided into six categories:

- DOF Constraints
- Forces
- Surface Loads
- Body Loads
- Inertia Loads
- Coupled-field Loads

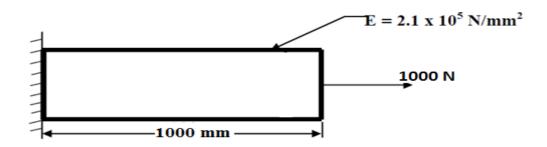
You can apply most of these loads either on the solid model (keypoints, lines, and areas) or the finite element model (nodes and elements).

Two important load-related terms you need to know are load step and substep. A *load step* is simply a configuration of loads for which you obtain a solution. In a structural analysis, for example, you may apply wind loads in one load step and gravity in a second load step. Load steps are also useful in dividing a transient load history curve into several segments.

# PART-A

#### Problem 1.1: Bar of Constant Cross-section Area

Consider the bar shown in figure below. Young's modulus is  $2.1 \times 10^5 \text{N/mm}^2$  and Area is  $500 \text{mm}^2$ . Determine the Nodal Displacement, Stress in each element, Reaction forces.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL h method- ok
- 2. Element type Add/Edit/Delete Add Link 3D Finit stn 180 ok close.
- 3. Real constants Add ok real constant set no 1 c/s area 500 ok.
- 4. Material Properties material models Structural Linear Elastic Isotropic EX 2.1e5 PRXY 0.27 ok close.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS–1000 (x value w.r.t first node) ok (second node is created).
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 ok (elements are created through nodes).
- 7. Loads Define loads apply Structural Displacement on Nodes- pick node 1 apply –DOFs to be constrained All DOF ok. Loads –
- 8. Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom FX Force/Moment value 1000 (+ve value) ok.
- 9. Solve current LS ok (Solution is done is displayed) close.
- 10. Element table Define table Add 'Results data item' By Sequence num LS LS1 ok.
- 11. Plot results contour plot –Element table item to be plotted LS,1, avg common nodes- yes average- ok.
- 12. List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).

- 13. Plot results- nodal solution-ok-DOF solution- x component of displacement-ok.
- 14. Animation: PlotCtrls Animate Deformed shape def+undeformed ok.

<u>Ana</u>	<u>lvtica</u>	l appro	ach:
	-		

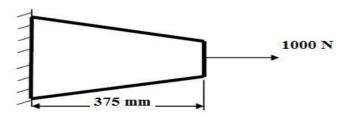
Calculation:	
Displacement:	
Stress:	
Reaction force:	

	ANSYS	Theoretical
Deformation		
Stress		
Reaction		

# **Problem 1.2: Bars of Tapered Cross section Area**

Consider the Tapered bar shown in figure below. Determine the Nodal Displacement, Stress in each element, Reaction forces

 $E = 2 \times 10^5 \text{ N/mm}^2$ , Area at root,  $A_1 = 1000 \text{ mm}^2$ , Area at the end,  $A_2 = 500 \text{ mm}^2$ .



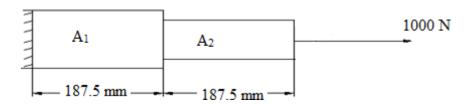
Solution: The tapered bar is modified into 2 elements as shown below with modified area of cross section.

$$(A_1 + A_2)/2 = (1000+500)/2 = 750 \text{ mm}^2$$

$$A_1 = (1000+750)/2 = 875 \text{ mm}^2$$

$$A_2 = (500 + 750)/2 = 625 \text{ mm}^2$$

$$L_1 = 187.5 \text{ mm } \& L_2 = 187.5 \text{ mm}$$



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method– ok
- 2. Element type Add/Edit/Delete Add link, 3D Finit stn 180 ok- close.
- 3. Real constants Add ok real constant set no 1 cross-sectional AREA1 875 apply-ok
- 4. Add ok real constant set no 2 cross-sectional AREA 2 625-ok
- 5. Material Properties material models Structural Linear Elastic Isotropic EX 2e5 –PRXY 0.3 ok close.
- 6. Modeling Create keypoints– In Active CS, =0, Y=0 Apply (first key point is created) location in active CS, X= 187.5, Y=0, apply (second key point is created) location in active CS X=375, Y=0(third key point is created) -ok.
- 7. Modeling-Create lines-straight lines-pick key points 1 & 2-ok- pick key points 2 & 3-ok

- 8. Meshing-mesh attributes-picked lines (pick the lines)-ok-material no= 1, real constants set no = 1, element type no =1, link 1, element section= none defined-pick the other line-ok-material number 2-define material id 2- real constants set no = 2, element type no =2-element section= none defined-ok.
- 9. Meshing-size controls-manual size-lines-all lines- no of element divisions=10(yes)-ok
- 10. Meshing-mesh tool-mesh-pick the lines-ok (the color changes to light blue)
- 11. Loads Define loads apply Structural Displacement on key points- pick key point 1 apply –DOFs to be constrained ALL DOF, displacement value=0 ok.
- 12. Loads Define loads apply Structural Force/Moment on key points- pick last key point apply direction of For/Mom FX Force/Moment value 1000 (+ve value) ok.
- 13. Solve current LS ok (Solution is done is displayed) close.
- 14. Element table Define table Add 'Results data item' By Sequence num LS LS1 ok.
- 15. Plot results contour plot –Element table item to be plotted LS,1, avg common nodes- yes average- ok.
- 16. List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 17. Plot results- nodal solution-ok-DOF solution- x component of displacement-ok.
- 18. Animation: PlotCtrls Animate Deformed shape def+undeformed-ok.

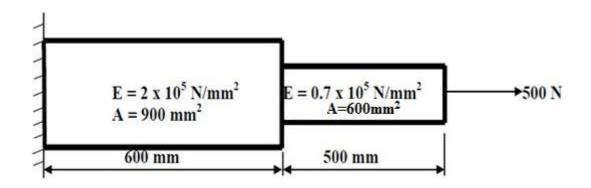
**Analytical approach:** 

Calculation:
Displacement:
tress:
eaction force:

	ANSYS	Theoretical
D.C.		
Deformation		
Ctmagg		
Stress		
Reaction		

# **Problem 1.3: Stepped Bar**

Consider the stepped bar shown in figure below. Determine the Nodal Displacement, Stress in each element, Reaction forces.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add link, 3D Finit stn 180 ok- close.
- Real constants Add ok real constant set no 1 cross-sectional AREA 1 900
   apply-ok
- 4. Add ok real constant set no 2 cross-sectional AREA 2 600-ok
- Material Properties material models Structural Linear Elastic Isotropic EX
   2e5 –PRXY 0.3- material- new material-define material id=2- Structural Linear
   Elastic Isotropic EX 0.7e5 –PRXY 0.3- ok close.
- 6. Modeling Create key points– In Active CS, =0, Y=0 Apply (first key point is created) location in active CS, X= 600, Y=0, apply (second key point is created) location in active CS X=1100, Y=0(third key point is created) -ok.
- 7. Modeling-Create lines-straight lines-pick key points 1 & 2-ok- pick key points 2 & 3-ok
- 8. Meshing-mesh attributes-picked lines (pick the lines)-ok-material no= 1, real constants set no = 1, element type no =1, link 1, element section= none defined-pick the other line-ok-material number 2-define material id 2- real constants set no = 2, element type no =2-element section= none defined-ok.
- 9. Meshing-size controls-manual size-lines-all lines- no of element divisions=10(yes)-ok
- 10. Meshing-mesh tool-mesh-pick the lines-ok (the color changes to light blue)
- 11. Loads Define loads apply Structural Displacement on key points- pick key point 1 apply –DOFs to be constrained ALL DOF, displacement value=0 ok.

- 12. Loads Define loads apply Structural Force/Moment on key points- pick last key point apply direction of For/Mom FX Force/Moment value 500 (+ve value) ok.
- 13. Solve current LS ok (Solution is done is displayed) close.
- 14. Element table Define table Add 'Results data item' By Sequence num LS LS1 ok.
- 15. Plot results contour plot –Element table item to be plotted LS,1, avg common nodes- yes average- ok.
- 16. List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 17. Plot results- nodal solution-ok-DOF solution- x component of displacement-ok.
- 18. Animation: PlotCtrls Animate Deformed shape def+undeformed-ok.

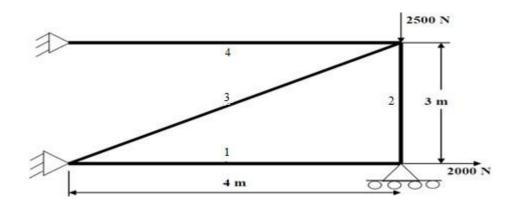
# **Analytical approach:**

ANSYS Results:	
Reaction force:	
Stress in each element:	
Displacement:	
Calculation:	

	ANSYS	Theoretical
Deformation		
Deformation		
Ctmaga		
Stress		
D .:		
Reaction		

# 2. TRUSSES

**Problem 2.1:** Consider the four bar truss shown in figure. For the given data, find Stress in each element, Reaction forces, Nodal displacement. E = 210 GPa,  $A = 0.1 \text{ m}^2$ .



- 1. Ansys Main Menu Preferences-select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add Link 3D Finit stn 180 ok close.
- 3. Real constants Add ok real constant set no 1 c/s area 0.1 ok close.
- 4. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– Ok close.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS– 4 (x value w.r.t first node) apply (second node is created) x,y,z location in CS 4, 3 (x, y value w.r.t first node) apply (third node is created) 0, 3 (x, y value w.r.t first node) ok (forth node is created).
- 6. Create–Elements–Elem Attributes Material number 1 Real constant set number 1 ok
- 7. Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3 apply pick 3 & 1 apply pick 3 & 4 ok (elements are created through nodes).
- Loads Define loads apply Structural Displacement on Nodes pick node 1
   4 apply DOFs to be constrained All DOF ok on Nodes pick node 2 apply DOFs to be constrained UY ok.
- 9. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom FX Force/Moment value 2000 (+ve value) ok Structural –
- 10. Force/Moment on Nodes- pick node 3 apply direction of For/Mom FY –

Force/Moment value -2500 (-ve value) - ok.

- 11. Solve current LS ok (Solution is done is displayed) close.
- 12. Element table Define table Add 'Results data item' By Sequence num LS LS1 ok.
- 13. Plot results contour plot –Element table item to be plotted LS,1, avg common nodes- yes average- ok.
- 14. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 15. Plot results- nodal solution-ok-DOF solution- Y component of displacement-ok.
- 16. Animation: PlotCtrls Animate Deformed shape def+undeformed-ok.

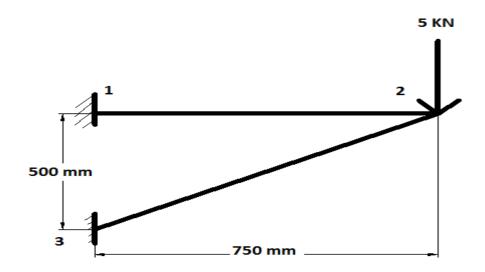
### **RESULT:**

# **Analytical approach:**

Calculation:	
Displacement:	
Stress:	
Reaction force: _	

	ANSYS	Theoretical
Deformation		
Beromanon		
Stress		
Reaction		

**Problem 2.2:** Consider the two bar truss shown in figure. For the given data, find Stress in each element, Reaction forces, Nodal displacement. E = 210 GPa,  $A = 0.1 \text{ m}^2$ .



- 1. Ansys Main Menu Preferences-select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add Link 3D Finit stn 180 ok close.
- 3. Real constants Add ok real constant set no 1 c/s area 0.1 ok close.
- 4. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– Ok close.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS– 0.75 (x value w.r.t first node) apply (second node is created) x,y,z location in CS –(0, -0.5),(x, y value w.r.t first node) ok (third node is created
- Create–Elements–Elem Attributes Material number 1 Real constant set number 1 ok
- 7. Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3— ok (elements are created through nodes).
- 8. Loads Define loads apply Structural Displacement on Nodes pick node 1 &3 apply DOFs to be constrained All DOF ok
- 9. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom FY Force/Moment value 5000 (-ve value)
- 10. Solve current LS ok (Solution is done is displayed) close.
- 11. Element table Define table Add 'Results data item' By Sequence num LS LS1 ok.
- 12. Plot results contour plot –Element table item to be plotted LS,1, avg common

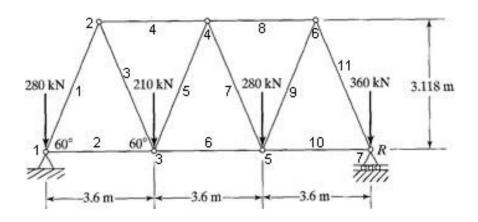
- nodes- yes average- ok.
- 13. List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 14. Plot results- nodal solution-ok-DOF solution- Y component of displacement-ok.
- 15. Animation: PlotCtrls Animate Deformed shape def+undeformed-ok.

# **Analytical approach:**

Calculation:	
Displacement:	
Stress:	
Reaction force:	

	ANSYS	Theoretical
Deformation		
Stress		
Reaction		

**Problem 2.3:** Determine the nodal deflections, reaction forces, and stress for the truss system shown below (E = 200GPa, A = 3250mm2).

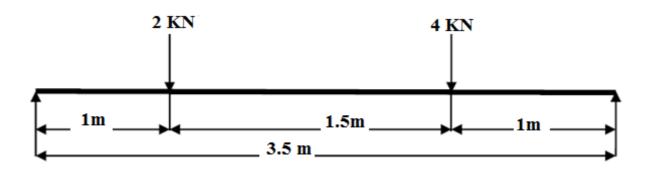


	ANSYS	Theoretical
Deformation		
Stress		
Reaction		

## 3. BEAMS

# **Problem 3.1: Simply Supported Beam**

Compute the Shear force and bending moment diagrams for the beam shown and find the maximum deflection. Assume rectangular c/s area of 100 mm \* 100mm, Young's modulus of 210 MPa, Poisson's ratio 0.27.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node BEAM 188– ok- close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 2.10e5– PRXY 0.27 ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) -enter b=100, h=100- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS–1000 (x value w.r.t first node) apply (second node is created) 2500 (x value w.r.t first node) apply(third node is created)- x,y,z location in CS-3500 (x value w.r.t first node)-ok.
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3 apply pick 3 & 4 ok (elements are created through nodes).
- 7. Loads Define loads apply Structural Displacement on Nodes- pick node 1 & 4 apply –DOFs to be constrained all DOF ok.
- 8. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply –direction of For/Mom FY Force/Moment value -2000(-ve value) ok- Force/Moment on Nodes- pick node 3 apply –direction of For/Mom FY Force/Moment value -4000(-ve value) ok.

- 9. Solve current LS ok (Solution is done is displayed) close.
- 10. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.
- 11. Stress: Plot Results Contour plot Nodal solution stress vonmises stress ok.
- 12. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 13. Plot results contour plot Line Element Results Elem table item at node I SMIS6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS3 Elem table item at node J SMIS16 ok (bending moment diagram will be displayed).
- 15. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- NOTE: For Shear Force Diagram use the combination SMISC 6 & SMISC 19, for Bending Moment Diagram use the combination SMISC 3 & SMISC 16.
- 16. Animation: PlotCtrls Animate Deformed results DOF solution USUM ok.

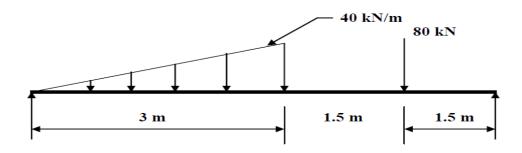
**Analytical approach:** 

Calculation:	
Displacement:	_
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
Shear force		
Bending moment		
Stress		

# Problem 3.2: Simply Supported Beam with uniformly varying load.

Compute the Shear force and bending moment diagrams for the beam shown and find the maximum deflection. Assume rectangular c/s area of 100 mm \* 100 mm, Young's modulus of  $2.1 \times 10^5 \text{ N/mm}^2$ , Poisson's ratio= 0.27.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method- ok
- 2. Element type Add/Edit/Delete Add BEAM 2 nodes Beam 188 ok close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 2.1e5– PRXY 0.27 –ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=100, h=100- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS–3000 (x value w.r.t first node) apply (second node is created) 4500 (x value w.r.t first node) –apply (third node is created) 6000 (x value w.r.t first node) ok (forth node is created).
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3 apply pick 3 & 4 ok (elements are created through nodes).
- 7. Loads Define loads apply Structural Displacement on Nodes- pick node 1 & 4 apply –DOFs to be constrained all DOF ok.
- 8. Loads Define loads apply Structural Pressure on Beams pick element between nodes 1 & 2–apply–pressure value at node I– 0 (value)– pressure value at node J 40000–ok.
- 9. Loads Define loads apply Structural Force/Moment on Nodes- pick node 3 apply direction of For/Mom FY Force/Moment value (-80000) (-ve value) ok.
- 10. Solve current LS ok (Solution is done is displayed) close.

- 11. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.
- 12. Stress: Plot Results Contour plot Nodal solution stress von mises stress ok.
- 13. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 15. Plot results contour plot Line Element Results Elem table item at node I SMIS3 Elem table item at node J SMIS16 ok (bending moment diagram will be displayed).
- 16. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 17. Animation: PlotCtrls Animate Deformed results DOF solution deformed + undeformed ok.

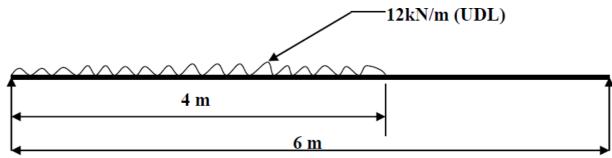
Analytical approach:

mary treat approach	
Calculation:	
Deflection:	
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
Shear force		
Bending moment		
Stress		

# Problem 3.3: Simply Supported Beam with Uniformally distributed load.

Compute the Shear force and bending moment diagrams for the beam shown and find the maximum deflection. Assume rectangular c/s area of 0.1 m \* 0.1 m, Young's modulus of 210



GPa, Poisson's ratio 0.27.

- 1. Ansys Main Menu Preferences-select STRUCTURAL ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node 188 ok- close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– PRXY 0.27 –ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=100, h=100- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS–4 (x value w.r.t first node) apply (second node is created) 6 (x value w.r.t first node) ok (third node is created).
- 6. Create Nodes Fill between Nds pick 1 & 2 apply number of nodes to fill 7 startingnode no 4 ok.
- 7. Create Elements Auto numbered Thru Nodes pick 1 & 4 apply– pick 4 & 5 apply– pick 5 & 6 apply– pick 6 & 7 apply– pick 7 & 8 apply– pick 8 & 9 apply pick 9 & 10 apply– pick 10 & 2 apply pick 2 & 3 ok (elements are created through nodes).
- 8. Loads Define loads apply Structural Displacement on Nodes- pick node 1 & 3 apply DOFs to be constrained UY ok.
- 9. Loads Define loads apply Structural Pressure on Beams pick all elements betweennodes 1 & 2 apply pressure value at node I 12000 pressure value at node J 12000 ok.
- 10. Solve current LS ok (Solution is done is displayed) close.
- 11. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.

- 12. Stress: Plot Results Contour plot Nodal solution stress von mises stress ok.
- 13. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS 6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 15. Plot results contour plot Line Element Results Elem table item at node I SMIS
   3 Elem table item at node J SMIS 16 ok (bending moment diagram will be displayed).
- 16. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 17. PlotCtrls Animate Deformed results DOF solution USUM ok.

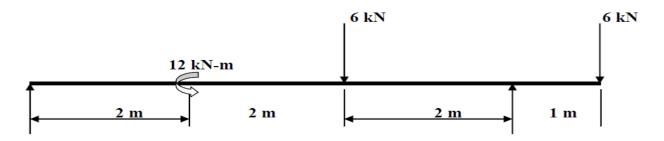
#### **Analytical approach:**

Calculation:	
Deflection:	
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
Shear force		
Bending moment		
Stress		

# Problem 3.4: Beam with moment and overhung

Compute the Shear force and bending moment diagrams for the beam shown and find the maximum deflection. Assume rectangular c/s area of 0.2 m \* 0.3 m, Young's modulus of 210 GPa, Poisson's ratio 0.27.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method- ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node 188 ok close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– PRXY 0.27 –ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=200, h=300- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS– 2 (x value w.r.t first node) apply (second node is created) 4 (x value w.r.t first node) –apply (third node is created) 6 (x value w.r.t first node) apply (forth node is created) 7 (x value w.r.t first node) ok (fifth node is created).
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3 apply pick 3 & 4 apply pick 4 & 5 ok (elements are created through nodes).
- 7. Loads Define loads apply Structural Displacement on Nodes- pick node 1 & 4 –apply –DOFs to be constrained UY ok.
- 8. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom MZ Force/Moment value 12000 (anticlockwise, +ve value) apply –pick node 3 apply direction of For/Mom FY Force/Moment value -6000 (-ve value) –apply pick node 5 apply direction of For/Mom FY Force/Moment value -6000 (-ve value) ok.
- 9. Solve current LS ok (Solution is done is displayed) close.
- 10. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.

- 11. Stress: Plot Results Contour plot Nodal solution stress von mises stress ok.
- 12. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 13. Plot results contour plot Line Element Results Elem table item at node I SMIS6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS3 Elem table item at node J SMIS16 ok (bending moment diagram will be displayed).
- 15. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).
- 16. Animation: PlotCtrls Animate Deformed results DOF solution deformed + undeformed ok.

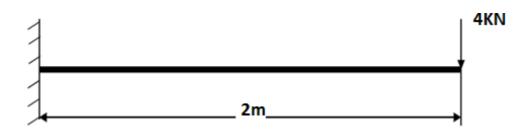
### **Analytical approach:**

Calculation:	
Deflection:	
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
SFD		
BMD		
Stress		

#### **Problem 3.5: Cantilever Beam**

Compute the Shear force and bending moment diagrams for the beam shown and find the maximum deflection. Assume rectangular c/s area of 0.2 m \* 0.3 m, Young's modulus of 210 GPa, Poisson's ratio 0.27.



- 1. Ansys Main Menu Preferences-Select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node Beam 188 ok- close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– PRXY 0.27 –ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=200, h=300- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS–2 (x value w.r.t first node) ok (second node is created).
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 ok (elements are created through nodes).
- 7. Loads Define loads apply Structural Displacement on Nodes- pick node 1 apply –
- 8. DOFs to be constrained ALL DOF ok.
- 9. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom FY Force/Moment value –( -40000) (-ve value) ok.
- 10. Solve current LS ok (Solution is done is displayed) close.
- 11. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.
- 12. Stress: Plot Results Contour plot Nodal solution stress von mises stress ok.

- 13. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 15. Plot results contour plot Line Element Results Elem table item at node I SMIS3 Elem table item at node J SMIS16 ok (bending moment diagram will be displayed).
- 16. Reaction forces: List Results reaction solution items to be listed All items ok (reaction forces will be displayed with the node numbers).

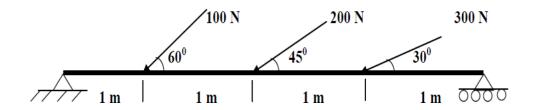
# **Analytical approach:**

Calculation:	
Deflection:	
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
SFD		
BMD		
Stress		

# **Problem 3.6: Beam with angular loads**

Compute the Shear force and bending moment diagrams for the beam shown in fig such that one end hinged and at the other end is having roller support and find the maximum deflection. Assume rectangular c/s area of 0.2 m \* 0.3 m, Young's modulus of 210 GPa, Poisson's ratio 0.27.



- 1. Ansys Main Menu Preferencesselect STRUCTURAL ok
- 2. Element type Add/Edit/Delete Add BEAM 2node 188 ok close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 210e9– PRXY 0.27 –ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=200, h=300- preview-ok.
- 5. Modeling Create Nodes In Active CS Apply (first node is created) x,y,z location in CS– 1 (x value w.r.t first node) apply (second node is created) 2 (x value w.r.t first node) apply (third node is created) 3 (x value w.r.t first node) apply (forth node is created) 4 (x value w.r.t first node) ok (fifth node is created).
- 6. Create Elements Auto numbered Thru Nodes pick 1 & 2 apply pick 2 & 3 apply pick 3 & 4 apply pick 4 & 5 ok (elements are created through nodes).
- 7. Create Nodes Rotate nodes CS by angles pick node 2 apply about nodal z-axis 60 apply pick node 3 apply about nodal z-axis 45 apply pick node 4 apply about nodal z-axis 30 ok.
- 8. Loads Define loads apply Structural Displacement on Nodes- pick node 1 apply –DOFs to be constrained UX & UY apply pick node 5 apply DOFs to be constrained –UY ok.
- 9. Loads Define loads apply Structural Force/Moment on Nodes- pick node 2 apply direction of For/Mom FX Force/Moment value -100 (-ve value) apply pick node 3 apply direction of For/Mom FX Force/Moment value -200 (-ve

- value) apply pick node 4 apply direction of For/Mom FX Force/Moment value 300 (-ve value) ok.
- 10. Solve current LS ok (Solution is done is displayed) close.
- 11. Displacement: Plot Results Contour plot Nodal solution DOF solution displacement vector sum ok.
- 12. Stress: Plot Results Contour plot Nodal solution stress von mises stress ok.
- 13. Element table Define table Add 'Results data item' By Sequence num SMISC –SMISC, 6 apply, By Sequence num SMISC SMISC, 19 apply, By Sequence num –SMISC SMISC, 3 apply, By Sequence num SMISC SMISC, 16 ok close.
- 14. Plot results contour plot Line Element Results Elem table item at node I SMIS6 Elem table item at node J SMIS19 ok (Shear force diagram will be displayed).
- 15. Plot results contour plot Line Element Results Elem table item at node I SMIS3 Elem table item at node J SMIS16 ok (bending moment diagram will be displayed).

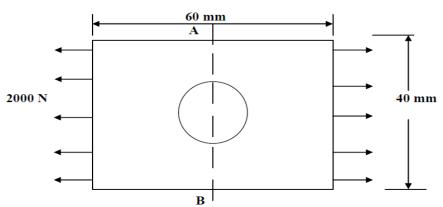
#### **Analytical approach:**

Calculation:	
Deflection:	
Shear force:	
Bending moment:	
Stress:	

	ANSYS	Theoretical
Deflection		
Shear force		
Bending moment		
Stress		

# Stress analysis of a rectangular plate with circular hole

**Problem 4.1:** In the plate with a hole under plane stress, find deformed shape of the hole and determine the maximum stress distribution along A-B (you may use t = 1 mm). E = 210GPa, t = 1 mm, Poisson's ratio = 0.3, Dia. of the circle = 10 mm, Analysis assumption – plane



stress with thickness is used.

- 1. Ansys Main Menu Preferences-Select STRUCTURAL-h method ok
- 2. Element type Add/Edit/Delete Add Solid Quad 4 node 42 ok option element behavior K3 Plane stress with thickness ok close.
- 3. Real constants Add ok real constant set no 1 Thickness 1 ok.
- 4. Material Properties material models Structural Linear Elastic Isotropic EX 2.1e5 –PRXY 0.3 ok close.
- 5. Modeling –Create Area Rectangle by dimensions X1, X2, Y1, Y2 0, 60, 0, 40 ok.
- 6. Create Area Circle solid circle X, Y, radius 30, 20, 5 ok.
- 7. Operate Booleans Subtract Areas pick area which is not to be deleted (rectangle) apply pick area which is to be deleted (circle) ok.
- 8. Meshing Mesh Tool Mesh Areas Quad Free Mesh pick all ok. Mesh Tool Refine pick all Level of refinement 3 ok.
- 9. Loads Define loads apply Structural Displacement on Nodes select box drag the left side of the area apply DOFs to be constrained ALL DOF ok.
- 10. Loads Define loads apply Structural Force/Moment on Nodes select box drag the right side of the area apply direction of For/Mom FX Force/Moment value 2000 (+ve value) ok.
- 11. Solve current LS ok (Solution is done is displayed) close.

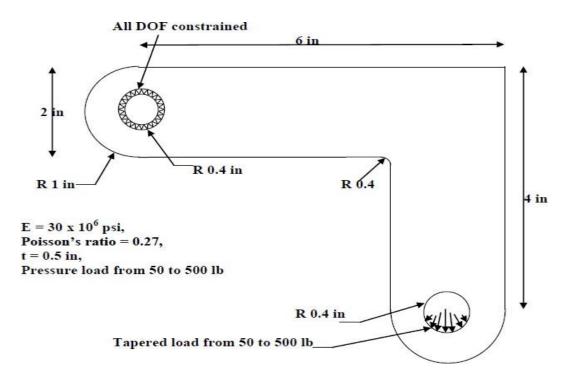
- 12. Deformed shape-Plot Results Deformed Shape def+undeformed ok.
- 13. Plot results contour plot Element solu Stress Von Mises Stress ok (the stress distribution diagram will be displayed).

# **Analytical approach:**

Calculation:

	ANSYS	Theoretical
Deformation		
Stress		

**Problem 4.2:** The corner angle bracket is shown below. The upper left hand pin-hole is constrained around its entire circumference and a tapered pressure load is applied to the bottom of lower right hand pin-hole. Compute Maximum displacement, Von-Mises stress.



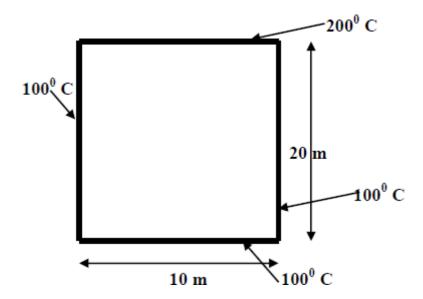
- 1. Ansys Main Menu Preferencesselect STRUCTURAL ok
- 2. Element type Add/Edit/Delete Add Solid Quad 8 node 82 ok option element behavior K3 Plane stress with thickness ok close.
- 3. Real constants Add ok real constant set no 1 Thickness 0.5 ok.
- 4. Material Properties material models Structural Linear Elastic Isotropic EX 30e6 –PRXY 0.27 ok close.
- 5. Modeling Create Area Rectangle by dimensions X1, X2, Y1, Y2 0, 6, 0, 2 apply –Create Area Rectangle by dimensions X1, X2, Y1, Y2 4, 6, -2, 2 ok. Create Area –Circle solid circle X, Y, radius 0, 1, 1 apply X, Y, radius 5, -2, 1 ok.
- 6. Operate Booleans Add Areas pick all.
- 7. Create Lines Line fillet pick the two lines where fillet is required apply fillet radius 0.4 ok. Create Areas Arbitrary by lines pick filleted lines ok. Operate Booleans –
- 8. Add Areas pick all. Create Area Circle solid circle X, Y, radius 0, 1, 0.4

- apply -X, Y, radius 5, -2, 0.4 ok.
- 9. Operate Booleans Subtract Areas pick area which is not to be deleted (bracket)
   apply pick areas which is to be deleted (pick two circles) ok.
- 10. Meshing Mesh Tool Mesh Areas Quad Free Mesh pick all ok. Mesh Tool Refine– pick all Level of refinement 3 ok.
- 11. Loads Define loads apply Structural Displacement on Lines select the inner lines of the upper circle apply DOFs to be constrained ALL DOF ok.
- 12. Loads Define loads apply Structural Pressure on Lines Pick line defining bottom left part of the circle apply load PRES value 50 optional PRES value 500 ok. Structural Pressure on Lines Pick line defining bottom right part of the circle apply load PRES value 500 optional PRES value 50 ok.
- 13. Solve current LS ok (Solution is done is displayed) close.
- 14. Plot Results Deformed Shape def+undeformed ok.
- 15. Plot results contour plot Element solu. Stress Von Mises Stress ok (the stress distribution diagram will be displayed).
- 16. PlotCtrls Animate Deformed shape def+undeformed-ok.

## PART B

#### THERMAL ANALYSIS

**Problem 5.1:** Solve the 2-D heat conduction problem for the temperature distribution within the rectangular plate. Thermal conductivity of the plate, KXX=401 W/(m-K).

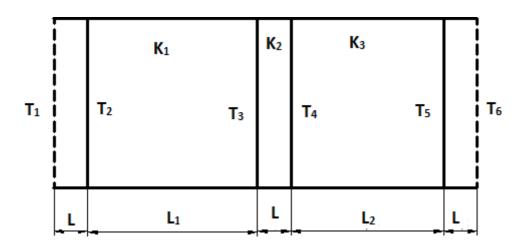


- 1. Ansys Main Menu Preferences-select THERMAL- h method– ok
- 2. Element type Add/Edit/Delete Add Solid Quad 4 node 55 ok option elementbehavior K3 Plane stress with thickness ok close.
- 3. Material Properties material models Thermal Conductivity Isotropic KXX 401.
- 4. Modeling Create Area Rectangle by dimensions X1, X2, Y1, Y2 0, 10, 0, 20 ok.
- 5. Meshing Mesh Tool Mesh Areas Quad Free Mesh pick all ok. Mesh Tool Refine pick all Level of refinement 3 ok.
- 6. Loads Define loads apply Thermal Temperature on Lines select 1000 C lines apply DOFs to be constrained TEMP Temp value 1000 C ok.
- 7. Loads Define loads apply Thermal Temperature on Lines select 1000 C lines –
- 8. Solve current LS ok (Solution is done is displayed) close.
- 9. Read results-last set-ok

- 10. List results-nodal solution-select temperature-ok
- 11. Observe the nodal solution per node.
- 12. From the menu bar-plot ctrls-style-size and shape-display of the element-click on real constant multiplier=0.2, don't change other values-ok.
- 13. Plot results-contour plot-nodal solution-temperature-deformed shape only-ok
- 14. Element table-define table-add-enter user label item=HTRANS, select by sequence no SMISC, 1-ok-close.
- 15. Element table-list table-select HTRANS-ok

## **RESULT:**

**Problem 5.2:** A furnace wall is made up of silica brick ( $K=1.5W/m^{\circ}C$ ) and outside magnesia brick ( $K=4.9 \text{ W/m}^{\circ}C$ ) each 10cm thick. The inner and outer surfaces are exposed to fluids at temperatures of  $820^{\circ}C$  and  $110^{\circ}C$  respectively. The contact resistance is  $0.001m^{2\circ}C/W$ . The heat transfer coefficient for inner and outer surfaces is equal to  $35 \text{ W/m}^{2}K$ . Find the heat flow through the wall per unit area per unit time and temperature distribution across the wall. Area=  $1m^{2}$ .



Given:  $K_1=1.5W/m^{\circ}C$ ,  $K_2=1$  W/m°C,  $K_3=4.9$  W/m°C,  $h_1=h_4=35$  W/m²K,  $T1=820^{\circ}C$ ,  $T6=110^{\circ}C$ ,  $L1=L_2=10$  cm & L=1mm.

- 1. Preferences-thermal-h method-ok
- 2. Preprocessor-Element type-add/edit/delete-add-link, 3d conduction 33,element type reference N0.=1-apply-link, convection 34 element type reference no.2=2-ok-close
- 3. Real constant- add/edit/delete-add-real constant set no=1-C/S area =1-ok-close.
- 4. Real constant- add/edit/delete-add-real constant set no=2-C/S area =1-ok-close.
- 5. Material properties-material model-thermal conductivity-isotropic-KXX=1.5-ok. From the define material model behavior menu bar-material new model Enter define material id=2-ok

Thermal-conductivity-isotropic- $K_{xx}$ =1-ok

Define material id=3-ok

Thermal-conductivity-isotropic-K<sub>xx</sub>=4.9-ok

Define material id=4-ok-convection or film coefficient HF= 35, close Modeling-create-nodes-in active CS

Enter node no=1,x=0,y=0,z=0-apply

Enter node no=2, X=0.001, Y=0, Z=0-apply

Enter node no=3, X=0.101, Y=0, Z=0-apply

Enter node no=4, X=0.102, Y=0, Z=0-apply

Enter node no=5, X=0.202, Y=0, Z=0-apply

Enter node no=6, X=0.203, Y=0, Z=0-ok.

Modeling-create-element-element attributes

Enter element type no=2 LINK 34 (convection)

Material no=4 (convection or film coefficient)

Real constant set no=2 (convection)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 1 & 2-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=1 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 2 & 3-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=2 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 3 & 4-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=3 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 4 & 5-ok.

Modeling-create-element-element attributes

Enter element type no=2 LINK 34 (Convection)

Material no=4 (convection or film coefficient)

Real constant set no=2 (convection)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 5 & 6-ok.

Observe the straight line.

From the menu bar select plot controls-Numbering-Plot numbering control and select element/attributes numbering=element no and don't change other attributes-ok

- 6. Solution- Analysis type-new analysis-steady state-ok.
- Solution-define loads-apply-thermal-temperature-on nodes-pick the first nodes-ok-temperature-load-temperature value=820<sup>o</sup> C-apply.
- Define load-apply-thermal-temperature-on nodes-pick the last node-ok, select temperature-load temperature value=110° C-ok.
- Solution- solve-current LS-ok.
   Solution is done-close.
- 7. Read results-last set-ok
- 8. List results-nodal solution-select temperature-ok
- 9. Observe the nodal solution per node.
- 10. From the menu bar-plot ctrls-style-size and shape-display of the element-click on real constant multiplier=0.2, don't change other values-ok.
- 11. Plot results-contour plot-nodal solution-temperature-deformed shape only-ok
- 12. Element table-define table-add-enter user label item=HTRANS, select by sequence no SMISC, 1-ok-close.
- 13. Element table-list table-select HTRANS-ok

#### **RESULT:**

#### **Analytical approach:**

Calculation:

	ANSYS	Theoretical
Nodal temperature		
$T_1$		
$T_2$		
$T_3$		
$\mathrm{T}_4$		
$T_5$		
$T_6$		
Heat flux		

**Problem 5.3:** The exterior wall of a building is constructed of four materials, 12mm thick gypsum board, 75mm thick fibre glass insulation, 20mm thick plywood and 20mm thick hardboard. The inside and outside air temperatures are 20°C and -10°C respectively. The convective heat transfer coefficients on the inner and outer surfaces of the wall are 6W/m<sup>2</sup> °C and 10 W/m<sup>2</sup> °C respectively. Determine the heat flux and the temperature distribution. Take K for gypsum=0.176W/m°C, K for fibre glass=0.036W/m°C, K for plywood=0.115 W/m°C and K for hardboard=0.215 W/m°C. Area= 1m<sup>2</sup>.

T <sub>1</sub>	т	<sub>2</sub> T	з Т	T <sub>4</sub> 1	Г <sub>5</sub> Т	6 <b>T</b> 7
	<b>h</b> ₁	<b>K</b> 1	K <sub>2</sub>	Кз	<b>K</b> 4	h <sub>6</sub>
·		L <sub>1</sub>	L <sub>2</sub>	L3	. L4	

- 1. Preferences-thermal-h method-ok
- 2. Element type-add/edit/delete-add-link, 3d conduction 33,element type reference N0.=1-apply-link, convection 34 element type reference no.2=2-ok-close
- 3. Real constant- add/edit/delete-add-real constant set no=1-C/S area =1-ok-close.
- 4. Real constant- add/edit/delete-add-real constant set no=2-C/S area =1-ok-close.
- 5. Material properties-material model-convection film coefficient-enter HF=6-ok
  From the define material model behaviour menu bar-material new model
  Enter define material id=2-ok

Thermal-conductivity-isotropic-K<sub>xx</sub>=0.176-ok

Define material id=3-ok

Thermal-conductivity-isotropic- $K_{xx}$ =0.036-ok

Define material id=4-ok

Thermal-conductivity-isotropic-K<sub>xx</sub>=0.115-ok

Define material id=5-ok

Thermal-conductivity-isotropic-K<sub>xx</sub>=0.215-ok

Define material id=6-convection or film coefficient HF= 10, close

Modeling-create-nodes-in active CS

Enter node no=1,x=0,y=0,z=0-apply

Enter node no=2, X=0.001, Y=0, Z=0-apply

Enter node no=3, X=0.013, Y=0, Z=0-apply

Enter node no=4, X=0.088, Y=0, Z=0-apply

Enter node no=5, X=0.108, Y=0, Z=0-apply

Enter node no=6, X=0.128, Y=0, Z=0-apply

Enter node no=7, X=0.129, Y=0, Z=0-ok

Modeling-create-element-element attributes

Enter element type no=2 LINK 34 (convection)

Material no=1 (convection or film coefficient)

Real constant set no=2 (convection)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 1 & 2-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=2 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 2 & 3-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33(Conduction)

Material no=3 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 3 & 4-ok

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=4 (conduction)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 4 & 5-ok.

Modeling-create-element-element attributes

Enter element type no=1 LINK 33 (Conduction)

Material no=5 (convection or film coefficient)

Real constant set no=1 (conduction)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 5 & 6-ok.

Modeling-create-element-element attributes

Enter element type no=2 LINK 34 (convection)

Material no=6 (convection or film coefficient)

Real constant set no=2 (convection)-ok

Modeling-create-element-auto numbered-through node-pick the nodes 6 & 7-ok

Observe the straight line.

From the menu bar select plot controls-Numbering-Plot numbering control and select element/attributes numbering=element no and don't change other attributes-ok

- 6. Solution- Analysis type-new analysis-steady state-ok.
- Solution-define loads-apply-thermal-temperature-on nodes-pick the first nodes-ok-temperature-load-temperature value=20<sup>0</sup> C-apply.
- Define load-apply-thermal-temperature-on nodes-pick the last node-ok, select temperature-load temperature value=-10<sup>0</sup> C-ok.
- Solution- solve-current LS-ok.
   Solution is done-close.
- 7. Read results-last set-ok
- 8. List results-nodal solution-select temperature-ok
- 9. Observe the nodal solution per node.
- 10. From the menu bar-plot ctrls-style-size and shape-display of the element-click on real constant multiplier=0.2, don't change other values-ok.
- 11. Plot results-contour plot-nodal solution-temperature-deformed shape only-ok
- 12. Element table-define table-add-enter user label item=HTRANS, select by sequence no SMISC, 1-ok-close.
- 13. Element table-list table-select HTRANS-ok

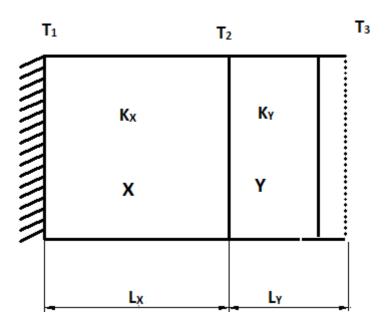
RESUL	$\mathbf{T}$	:
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# **Analytical approach:**

Calculation:

	ANSYS	Theoretical
Nodal temperature		
$T_1$		
$T_2$		
$T_3$		
$\mathrm{T}_4$		
$T_5$		
$T_6$		
$T_7$		
Heat flux		

**Problem 5.4:** A plane wall 'X' (K=75W/mK) is 60 mm thick and has volumetric heat generation of  $1.5 \times 10^6 \text{W/m}^3$ . It is insulated on one side while the other side is in contact with the surface of another wall 'Y' (K=150W/mK) which is 30mm thick and has no heat generation. The free surface of wall 'Y' is exposed to a cooling fluid at  $20^0\text{C}$  with a convection coefficient of 950 W/m<sup>2</sup>K. Find steady state temperatures at salient points across the composite wall. Area=  $1\text{m}^2$ .



- 1. Preferences-Thermal-h method-ok
- 2. Element type-add/edit/delete- add-solid, quad 4node 55-enter reference number=1-select options-element behaviour, K<sub>3</sub>= plane thickness-ok
- 3. Real constants- add/edit/delete-add- enter real constant set no. 1, thickness=2-ok-close
- 4. Material properties-Material models-material number 1-thermal-conductivity-isotropic-KXX=75-ok.
- 5. From the menu bar select material-new model-enter material no. ID 2=2-select
- 6. Material model no.2- thermal-conductivity-isotropic-KXX=150-ok.
- 7. Modeling-create-areas-rectangles-by dimensions- $X_1$ =0,  $X_2$ =0.06,  $Y_1$ =0, $Y_2$ =0.03-apply-  $X_1$ =0.06,  $X_2$ =0.09,  $Y_1$ =0, $Y_2$ =0.03-OK Modeling-operate-Boolean-glue-areas-pick the material-ok
- 8. Meshing-size controls-manual size-picked lines-pick the first vertical line, middle line and the last vertical line-ok-number of element divisions-2-apply Meshing-size controls-manual size-picked lines-pick the first rectangle top and

bottom lines-number of element divisions=60-apply

Meshing-size controls-manual size-picked lines-pick the top and bottom lines of second rectangle-number of element divisions=30-ok.

Meshing-mesh areas- free-pick all-ok.

- 9. Solution-Analysis type-new analysis-steady state-ok
- ➤ define loads-apply-thermal-heat generated on areas-pick the first rectangle-ok
- ➤ define loads-apply-thermal-heat generated on areas-apply Hgen on areas as constant value- load Hgen value=1.5e6
- ➤ define loads-apply-thermal-convection-on lines-pick the back corner line-ok-enter film coefficient=950-bulk temperature=20°C (Don't change other attributes)-ok
- ➤ define loads-apply-thermal-heat flux-on lines-pick the front corner line-ok-enter heat flux=0-ok
- 10. Solution-solve-current LS-ok-close
- 11. Read results-last set-ok
- 12. List results-nodal solution-select temperature-ok
- 13. Observe the nodal solution per node.
- 14. From the menu bar-plot ctrls-style-size and shape-display of the element-click on real constant multiplier=0.2, don't change other values-ok.
- 15. Plot results-contour plot-nodal solution-temperature-deformed shape only-ok

#### **RESULT:**

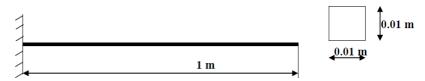
#### **Analytical approach:**

Calculation:

	ANSYS	Theoretical
Nodal temperature		
$T_1$		
$T_2$		
$T_3$		

**Problem 6.1:** Modal Analysis of Cantilever beam for natural frequency determination.

Modulus of elasticity = 200GPa, Density = 7800 Kg/m3.



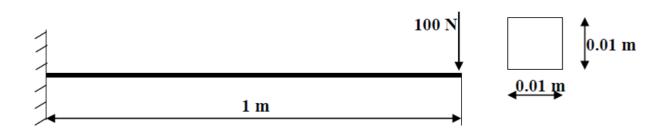
- 1. Ansys Main Menu Preferences-select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node 188– ok- close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 200e9– PRXY 0.27 Density 7800 ok close.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=0.01, h=0.01- preview-ok.
- 5. Modeling Create Keypoints in Active CS x,y,z locations 0,0 apply x,y,z locations 1,0 ok (Keypoints created).
- 6. Create Lines lines in Active Coord pick keypoints 1 and 2 ok.
- Meshing Size Cntrls ManualSize Lines All Lines element edge length 0.1
   ok. Mesh– Lines Pick All ok.
- 8. Solution Analysis Type New Analysis Modal ok.
- 9. Solution Analysis Type Subspace Analysis options no of modes to extract 5 no of modes to expand 5 ok (use default values) ok.
- 10. Solution Define Loads Apply Structural Displacement On Keypoints Pick firstkeypoint apply DOFs to be constrained ALL DOF ok.
- 11. Solve current LS ok (Solution is done is displayed) close.
- 12. Result Summary
- 13. Read Results First Set
- 14. Plot Results Deformed Shape def+undeformed ok.
- 15. PlotCtrls Animate Deformed shape def+undeformed-ok.
- 16. Read Results Next Set
- 17. Plot Results Deformed Shape def+undeformed ok.
- 18. PlotCtrls Animate Deformed shape def+undeformed-ok

## **RESULT:**

**Analytical solution:** 

## Problem 6.2: Fixed- fixed beam subjected to forcing function

Conduct a harmonic forced response test by applying a cyclic load (harmonic) at the end of the beam. The frequency of the load will be varied from 1 - 100 Hz. Modulus of elasticity = 200GPa, Poisson's ratio = 0.3, Density = 7800 Kg/m3.



- 1. Ansys Main Menu Preferences-select STRUCTURAL- h method ok
- 2. Element type Add/Edit/Delete Add BEAM 2 node BEAM 188 ok close.
- 3. Material Properties material models Structural Linear Elastic Isotropic EX 200e9– PRXY 0.3 Density 7800 ok.
- 4. Sections-Beams-common sections- sub type- rectangle (1<sup>st</sup> element) enter b=100, h=100- preview-ok.
- 5. Modeling Create Keypoints in Active CS x,y,z locations 0,0 apply x,y,z locations 1,0 ok (Keypoints created).
- 6. Create Lines lines in Active Coord pick keypoints 1 and 2 ok.
- Meshing Size Cntrls ManualSize Lines All Lines element edge length 0.1
   ok. Mesh– Lines Pick All ok.
- 8. Solution Analysis Type New Analysis Harmonic ok.
- 9. Solution Analysis Type Subspace Analysis options Solution method FULL DOF printout format Real + imaginary ok (use default values) ok.
- 10. Solution Define Loads Apply Structural Displacement On Keypoints Pick firstkeypoint apply DOFs to be constrained ALL DOF ok.
- 11. Solution Define Loads Apply Structural Force/Moment On Keypoints Pick secondnode apply direction of force/mom FY Real part of force/mom 100 imaginary part of force/mom 0 ok.
- 12. Solution Load Step Opts Time/Frequency Freq and Substps... Harmonic frequency range– 0 100 number of substeps 100 B.C stepped ok.
- 13. Solve current LS ok (Solution is done is displayed) close.

## 14. TimeHistPostpro

Select 'Add' (the green '+' sign in the upper left corner) from this window - Nodal solution -DOF solution - Y component of Displacement - ok. Graphically select node 2- ok.

Select 'List Data' (3 buttons to the left of 'Add') from the window.

Time History Variables' window click the 'Plot' button, (2 buttons to the left of 'Add')

Utility Menu – PlotCtrls – Style – Graphs – Modify Axis – Y axis scale – Logarithmic

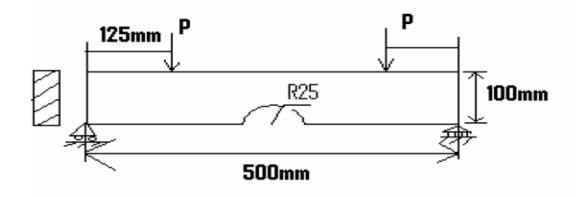
–ok. Utility Menu – Plot – Replot.

This is the response at node 2 for the cyclic load applied at this node from 0 - 100 Hz.

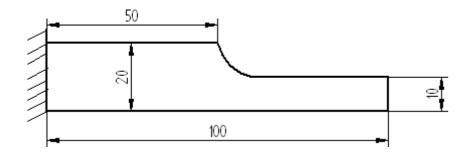
## **RESULT:**

# **ADDITIONAL PROBLEMS**

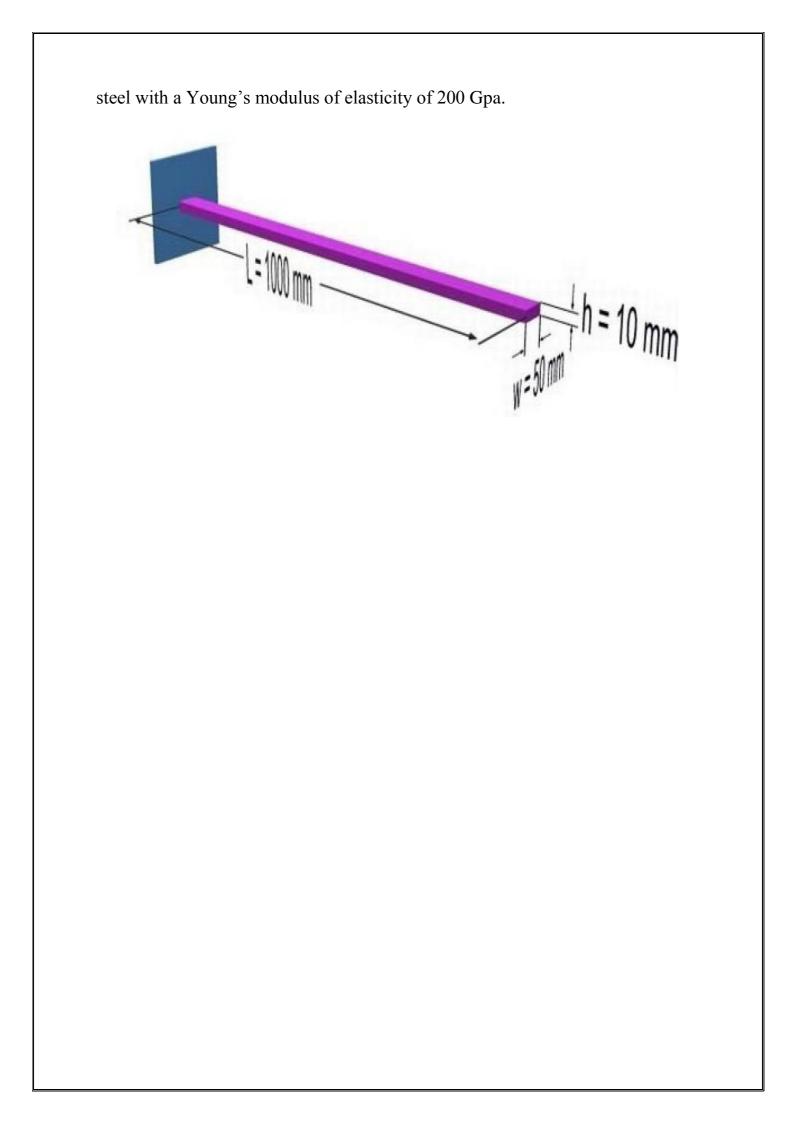
1. Calculate the stresses and displacement for the plate shown below. Let the load be P = 100N applied at equal distance from both ends and E = 3e7 N/mm2.

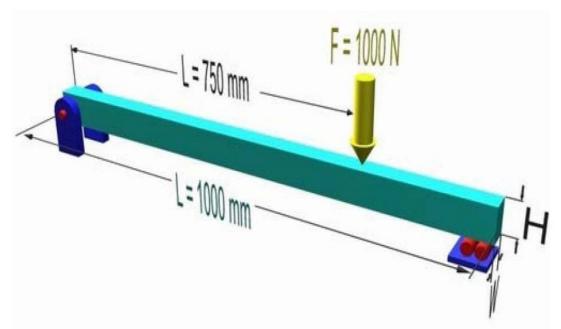


- 2. Current passes through a stainless steel wire of 2.5 mm diameter (k=200 W/mK) causing volumetric heat generation of 26.14X108 W/m3 .the wire is submerged in a fluid maintained at 500 C and convective heat transfer coefficient at the wire surface is 4000W/m2 K . Find the steady state temperature at the centre and at the surface of the wire.
- 3. Calculate the maximum value of Von-misses stresses in the stepped beam with a rounded plate as shown in the figure. Where Young's modulus, E=210Gpa, Poisson's ratio is 0.3 and the beam thickness is 10mm, the element size is 2mm



4. Loads will not be applied to the beam shown below in order to observe the deflection caused by the weight of the beam itself. The beam is to be made of





5. A beam has a force of 1000N applied as shown below. The purpose of this optimization problem is to minimize the weight of the beam without exceeding the allowable stress. It is necessary to find the cross sectional dimensions of the beam in order to minimize the weight of the beam. However, the width and height of the beam cannot be smaller than 10mm. The maximum stress anywhere in the beam cannot exceed 200 MPa. The beam is to be made of steel with a modulus of elasticity of 200 GPa.

## **VIVA QUESTIONS & ANSWERS**

#### 1. Theories of failures

- a. Maximum Principal Stress Theory- A material in complex state of stress fails, when the maximum principal stress in it reaches the value of stress at elastic limit in simple tension.
- b. **Maximum Shear Stress Theory** A material in complex state of stress fails when the maximum shearing stress in it reaches the value of shearing stress at elastic limit in uniaxial tension test.
- c. **Maximum Principal Strain Theory**-Failure in a complex system occurs when the maximum strain in it reaches the value of the strain in uniaxial stress at elastic limit.
- d. **Maximum Strain Energy Theory** A material in complex state of stress fails when the maximum strain energy per unit volume at a point reaches the value of strain energy per unit volume at elastic limit in simple tension test.
- e. **Maximum Distortion Energy Theory**-This theory is also known as Von-Mises criteria for failure of elastic bodies. According to this theory part of strain energy causes only changes in volume of the material and rest of it causes distortion. At failure the energy causing distortion per unit volume is equal to the distortion energy per unit volume in uniaxial state of stress at elastic limit.

#### 2. What is factor of safety?

The maximum stress to which any member is designed is much less than the ultimate stress and this stress is called working stress. The ratio of ultimate stress to working stress is called factor of safety.

3. What is Endurance limit?

The max stress at which even a billion reversal of stress cannot cause failure of the material is called endurance limit.

4. Define: Modulus of rigidity, Bulk modulus

**Modulus of rigidity**: It is defined as the ratio of shearing stress to shearing strain within elastic limit.

**Bulk modulus**: It is defined as the ratio of identical pressure 'p' acting in three mutually perpendicular directions to corresponding volumetric strain.

5. What is proof resilience?

The maximum strain energy which can be stored by a body without undergoing

permanent deformation is called proof resilience.

6. What is shear force diagram?

A diagram in which ordinate represent shear force and abscissa represents the position of the section is called SFD.

7. What is bending moment diagram?

A diagram in which ordinate represents bending moment and abscissa represents the position of the section is called BMD.

- 8. Assumptions in simple theory of bending.
  - a. The beam is initially straight and every layer of it is free to expand or contract.
  - b. The material is homogeneous and isotropic.
  - c. Young's modulus is same in tension and compression.
  - d. Stresses are within elastic limit.
  - e. Plane section remains plane even after bending.
  - f. The radius of curvature is large compared to depth of beam.
- 9. State the three phases of finite element method.

Preprocessing, Analysis & Post processing

10. What are the h and p versions of finite element method?

Both are used to improve the accuracy of the finite element method. In h version, the order of polynomial approximation for all elements is kept constant and the numbers of elements are increased. In p version, the numbers of elements are maintained constant and the order of polynomial approximation of element is increased.

11. What is the difference between static analysis and dynamic analysis?

Static analysis: The solution of the problem does not vary with time is known as static analysis.E.g.: stress analysis on a beam.

Dynamic analysis: The solution of the problem varies with time is known as dynamic analysis.E.g.: vibration analysis problem.

12. What are Global coordinates?

The points in the entire structure are defined using coordinates system is known as global coordinate system.

13. What are natural coordinates? A natural coordinate system is used to define any point

inside the element by a set of dimensionless number whose magnitude never exceeds unity. This system is very useful in assembling of stiffness matrices.

#### 14. What is a CST element?

Three node triangular elements are known as constant strain triangular element. It has 6 unknown degrees of freedom called u1, v1, u2, v2, u3, v3. The element is called CST because it has constant strain throughout it.

#### 15. Define shape function.

In finite element method, field variables within an element are generally expressed by the following approximate relation:

 $\Phi$  (x,y) = N<sub>1</sub>(x,y)  $\Phi$ 1+ N<sub>2</sub>(x,y)  $\Phi$ 2+N<sub>3</sub>(x,y)  $\Phi$ 3+N<sub>4</sub>(x,y)  $\Phi$ 4 where  $\Phi$ 1,  $\Phi$ 2,  $\Phi$ 3 and  $\Phi$ 4 are the values of the field variables at the nodes and N1, N2, N3 and N4 are interpolation function. N1, N2, N3, N4 are called shape functions because they are used to express the geometry or shape of the element.

#### 16. What are the characteristics of shape function?

The characteristics of the shape functions are as follows:

- The shape function has unit value at one nodal point and zero value at the other nodes.
- The sum of shape functions is equal to one.

## 17. Why polynomials are generally used as shape function?

- Differentiation and integration of polynomials are quite easy.
- The accuracy of the results can be improved by increasing the order of the polynomial.
- It is easy to formulate and computerize the finite element equations.

#### 18. State the properties of a stiffness matrix.

The properties of the stiffness matrix [K] are:

- It is a symmetric matrix.
- The sum of the elements in any column must be equal to zero.
- It is an unstable element, so the determinant is equal to zero.

#### 19. What are the difference between boundary value problem and initial value problem?

The solution of differential equation obtained for physical problems which satisfies some specified conditions known as boundary conditions. If the solution of differential

equation is obtained together with initial conditions then it is known as initial value problem. If the solution of differential equation is obtained together with boundary conditions then it is known as boundary value problem.

#### 20. What is meant by plane stress?

Plane stress is defined as a state of stress in which the normal stress ( $\alpha$ ) and the shear stress directed perpendicular to plane are zero.

#### 21. Define plane strain.

Plane strain is defined to be a state of strain in which the strain normal to the xy plane and the shear strains are assumed to be zero.

#### 22. Define Quasi-static response.

When the excitations are varying slowly with time then it is called quasi-static response.

## 23. What is a sub parametric element?

If the number of nodes used for defining the geometry is less than the number of nodes used for defining the displacements is known as sub parametric element.

## 24. What is a super parametric element?

If the number of nodes used for defining the geometry is more than the number of nodes used for defining the displacements is known as sub parametric element.

#### 25. What is meant by isoparametric element?

If the number of nodes used for defining the geometry is same as number of nodes used for defining the displacements then it is called parametric element.

#### 26. What is the purpose of isoparametric element?

It is difficult to represent the curved boundaries by straight edges finite elements. A large number of finite elements may be used to obtain reasonable resemblance between original body and assemblage. In order to overcome this drawback, iso parametric elements are used i.e for problems involving curved boundaries, a family of elements 'isoparametric elements' are used.

## 27. What are isotropic and orthotropic materials?

A material is isotropic if its mechanical and thermal properties are the same in all directions. Isotropic materials can have homogeneous or non-homogeneous microscopic structures.

Orthotropic materials: A material is orthotropic if its mechanical or thermal properties are

unique and independent in three mutually perpendicular directions.

## 28. What is discretization?

Discretization is the process of dividing given problem into several small elements, connected with nodes.

## 29. Steps in FEM

- Discretization
- Selection of the displacement models
- Deriving element stiffness matrices
- Assembly of overall equations/ matrices
- Solution for unknown displacements
- Computations for the strains/stresses