

# Chapter 16. Operator Overloading

*There are some things that I kind of feel torn about, like operator overloading. I left out operator overloading as a fairly personal choice because I had seen too many people abuse it in C++.*

—James Gosling, creator of Java<sup>1</sup>

In Python, you can compute compound interest using a formula written like this:

```
interest = principal * ((1 + rate) ** periods - 1)
```

Operators that appear between operands, like `1 + rate`, are *infix operators*. In Python, the infix operators can handle any arbitrary type. Thus, if you are dealing with real money, you can make sure that `principal`, `rate`, and `periods` are exact numbers—instances of the Python `decimal.Decimal` class—and that formula will work as written, producing an exact result.

But in Java, if you switch from `float` to `BigDecimal` to get exact results, you can't use infix operators anymore, because they only work with the primitive types. This is the same formula coded to work with `BigDecimal` numbers in Java:

```
BigDecimal interest = principal.multiply(BigDecimal.ONE.add(rate)
                                .pow(periods).subtract(BigDecimal.ONE));
```

It's clear that infix operators make formulas more readable. Operator overloading is necessary to support infix operator notation with user-defined or extension types, such as NumPy arrays. Having operator overloading in a high-level, easy-to-use language was probably a key reason for the huge success of Python in data science, including financial and scientific applications.

In [“Emulating Numeric Types” \(Chapter 1\)](#) we saw some trivial implementations of operators in a bare-bones `Vector` class. The `__add__` and `__mul__` methods in [Example 1-2](#) were written to show how special

methods support operator overloading, but there are subtle problems in their implementations that we overlooked. Also, in [Example 11-2](#), we noted that the `Vector2d.__eq__` method considers this to be `True`: `Vector(3, 4) == [3, 4]`—which may or not make sense. We will address these matters in this chapter, as well as:

- How an infix operator method should signal it cannot handle an operand
- Using duck typing or goose typing to deal with operands of various types
- The special behavior of the rich comparison operators (e.g., `==`, `>`, `<=`, etc.)
- The default handling of augmented assignment operators such as `+=`, and how to overload them

## What’s New in This Chapter

Goose typing is a key part of Python, but the `numbers` ABCs are not supported in static typing, so I changed [Example 16-11](#) to use duck typing instead of an explicit `isinstance` check against `numbers.Real`.<sup>2</sup>

I covered the `@` matrix multiplication operator in the first edition of *Fluent Python* as an upcoming change when 3.5 was still in alpha. Accordingly, that operator is no longer in a side note, but is integrated in the flow of the chapter in [“Using @ as an Infix Operator”](#). I leveraged goose typing to make the implementation of `__matmul__` safer than the one in the first edition, without compromising on flexibility.

[“Further Reading”](#) now has a couple of new references—including a blog post by Guido van Rossum. I also added mentions of two libraries that showcase effective use of operator overloading outside the domain of mathematics: `pathlib` and `Scapy`.

## Operator Overloading 101

Operator overloading allows user-defined objects to interoperate with infix operators such as `+` and `|`, or unary operators like `-` and `~`. More generally, function invocation (`()`), attribute access (`.`), and item

access/slicing ( `[]` ) are also operators in Python, but this chapter covers unary and infix operators.

Operator overloading has a bad name in some circles. It is a language feature that can be (and has been) abused, resulting in programmer confusion, bugs, and unexpected performance bottlenecks. But if used well, it leads to pleasurable APIs and readable code. Python strikes a good balance among flexibility, usability, and safety by imposing some limitations:

- We cannot change the meaning of the operators for the built-in types.
- We cannot create new operators, only overload existing ones.
- A few operators can't be overloaded: `is`, `and`, `or`, `not` (but the bitwise `&`, `|`, `~`, can).

In [Chapter 12](#), we already had one infix operator in `Vector`: `==`, supported by the `__eq__` method. In this chapter, we'll improve the implementation of `__eq__` to better handle operands of types other than `Vector`. However, the rich comparison operators (`==`, `!=`, `>`, `<`, `>=`, `<=`) are special cases in operator overloading, so we'll start by overloading four arithmetic operators in `Vector`: the unary `-` and `+`, followed by the infix `+` and `*`.

Let's start with the easiest topic: unary operators.

## Unary Operators

*The Python Language Reference*, [“6.5. Unary arithmetic and bitwise operations”](#) lists three unary operators, shown here with their associated special methods:

`-`, implemented by `__neg__`

Arithmetic unary negation. If `x` is `-2` then `-x == 2`.

`+`, implemented by `__pos__`

Arithmetic unary plus. Usually `x == +x`, but there are a few cases when that's not true. See [“When x and +x Are Not Equal”](#) if you're curious.

`~`, implemented by `__invert__`

Bitwise not, or bitwise inverse of an integer, defined as  $\sim x == -(x+1)$ . If  $x$  is 2 then  $\sim x == -3$ .<sup>3</sup>

The “[Data Model](#)” chapter of *The Python Language Reference* also lists the `abs()` built-in function as a unary operator. The associated special method is `__abs__`, as we’ve seen before.

It’s easy to support the unary operators. Simply implement the appropriate special method, which will take just one argument: `self`. Use whatever logic makes sense in your class, but stick to the general rule of operators: always return a new object. In other words, do not modify the receiver (`self`), but create and return a new instance of a suitable type.

In the case of `-` and `+`, the result will probably be an instance of the same class as `self`. For unary `+`, if the receiver is immutable you should return `self`; otherwise, return a copy of `self`. For `abs()`, the result should be a scalar number.

As for `~`, it’s difficult to say what would be a sensible result if you’re not dealing with bits in an integer. In the *pandas* data analysis package, the tilde negates boolean filtering conditions; see “[Boolean indexing](#)” in the *pandas* documentation for examples.

As promised before, we’ll implement several new operators on the `Vector` class from [Chapter 12. Example 16-1](#) shows the `__abs__` method we already had in [Example 12-16](#), and the newly added `__neg__` and `__pos__` unary operator methods.

#### **Example 16-1. `vector_v6.py`: unary operators `-` and `+` added to [Example 12-16](#)**

```
def __abs__(self):
    return math.hypot(*self)

def __neg__(self):
    return Vector(-x for x in self) ❶

def __pos__(self):
    return Vector(self) ❷
```

- ❶ To compute `-v`, build a new `Vector` with every component of `self` negated.

- ② To compute `+v`, build a new `Vector` with every component of `self`.

Recall that `Vector` instances are iterable, and the `Vector.__init__` takes an iterable argument, so the implementations of `__neg__` and `__pos__` are short and sweet.

We'll not implement `__invert__`, so if the user tries `~v` on a `Vector` instance, Python will raise `TypeError` with a clear message: “bad operand type for unary ~: 'Vector'.”

The following sidebar covers a curiosity that may help you win a bet about unary `+` someday.

---

#### WHEN X AND +X ARE NOT EQUAL

Everybody expects that `x == +x`, and that is true almost all the time in Python, but I found two cases in the standard library where `x != +x`.

The first case involves the `decimal.Decimal` class. You can have `x != +x` if `x` is a `Decimal` instance created in an arithmetic context and `+x` is then evaluated in a context with different settings. For example, `x` is calculated in a context with a certain precision, but the precision of the context is changed and then `+x` is evaluated. See [Example 16-2](#) for a demonstration.

**Example 16-2.** A change in the arithmetic context precision may cause `x` to differ from `+x`

```
>>> import decimal
>>> ctx = decimal.getcontext() ❶
>>> ctx.prec = 40 ❷
>>> one_third = decimal.Decimal('1') / decimal.Decimal('3') ❸
>>> one_third ❹
Decimal('0.33333333333333333333333333333333333333333333333333')
>>> one_third == +one_third ❺
True
>>> ctx.prec = 28 ❻
>>> one_third == +one_third ❼
False
>>> +one_third ❽
Decimal('0.33333333333333333333333333333333333333333333333333')
```

❶ Get a reference to the current global arithmetic context.

- ❷ Set the precision of the arithmetic context to 40.
- ❸ Compute  $1/3$  using the current precision.
- ❹ Inspect the result; there are 40 digits after the decimal point.
- ❺ `one_third == +one_third` is `True`.
- ❻ Lower precision to 28—the default for `Decimal` arithmetic.
- ❼ Now `one_third == +one_third` is `False`.
- ❽ Inspect `+one_third`; there are 28 digits after the `'.'` here.

The fact is that each occurrence of the expression `+one_third` produces a new `Decimal` instance from the value of `one_third`, but using the precision of the current arithmetic context.

You can find the second case where `x != +x` in the [collections.Counter documentation](#). The `Counter` class implements several arithmetic operators, including infix `+` to add the tallies from two `Counter` instances. However, for practical reasons, `Counter` addition discards from the result any item with a negative or zero count. And the prefix `+` is a shortcut for adding an empty `Counter`, therefore it produces a new `Counter`, preserving only the tallies that are greater than zero. See [Example 16-3](#).

**Example 16-3. Unary `+` produces a new `Counter` without zeroed or negative tallies**

```
>>> ct = Counter('abracadabra')
>>> ct
Counter({'a': 5, 'r': 2, 'b': 2, 'd': 1, 'c': 1})
>>> ct['r'] = -3
>>> ct['d'] = 0
>>> ct
Counter({'a': 5, 'b': 2, 'c': 1, 'd': 0, 'r': -3})
>>> +ct
Counter({'a': 5, 'b': 2, 'c': 1})
```

As you can see, `+ct` returns a counter where all tallies are greater than zero.

Now, back to our regularly scheduled programming.

---

# Overloading + for Vector Addition

The `Vector` class is a sequence type, and the section [“3.3.6. Emulating container types”](#) in the “Data Model” chapter of the official Python documentation says that sequences should support the `+` operator for concatenation and `*` for repetition. However, here we will implement `+` and `*` as mathematical vector operations, which are a bit harder but more meaningful for a `Vector` type.

---

## TIP

If users want to concatenate or repeat `Vector` instances, they can convert them to tuples or lists, apply the operator, and convert back—thanks to the fact that `Vector` is iterable and can be constructed from an iterable:

```
>>> v_concatenated = Vector(list(v1) + list(v2))
>>> v_repeated = Vector(tuple(v1) * 5)
```

---

Adding two Euclidean vectors results in a new vector in which the components are the pairwise additions of the components of the operands. To illustrate:

```
>>> v1 = Vector([3, 4, 5])
>>> v2 = Vector([6, 7, 8])
>>> v1 + v2
Vector([9.0, 11.0, 13.0])
>>> v1 + v2 == Vector([3 + 6, 4 + 7, 5 + 8])
True
```

What happens if we try to add two `Vector` instances of different lengths? We could raise an error, but considering practical applications (such as information retrieval), it's better to fill out the shortest `Vector` with zeros. This is the result we want:

```
>>> v1 = Vector([3, 4, 5, 6])
>>> v3 = Vector([1, 2])
>>> v1 + v3
Vector([4.0, 6.0, 5.0, 6.0])
```



Given these basic requirements, we can implement `__add__` like in [Example 16-4](#).

**Example 16-4.** `Vector.__add__` method, take #1

```
# inside the Vector class

def __add__(self, other):
    pairs = itertools.zip_longest(self, other, fillvalue=0.0) ❶
    return Vector(a + b for a, b in pairs) ❷
```

❶ `pairs` is a generator that produces tuples `(a, b)`, where `a` is from `self`, and `b` is from `other`. If `self` and `other` have different lengths, `fillvalue` supplies the missing values for the shortest iterable.

❷ A new `Vector` is built from a generator expression, producing one addition for each `(a, b)` from `pairs`.

Note how `__add__` returns a new `Vector` instance, and does not change `self` or `other`.

---

**WARNING**

Special methods implementing unary or infix operators should never change the value of the operands. Expressions with such operators are expected to produce results by creating new objects. Only augmented assignment operators may change the first operand (`self`), as discussed in [“Augmented Assignment Operators”](#).

---

[Example 16-4](#) allows adding `Vector` to a `Vector2d`, and `Vector` to a tuple or to any iterable that produces numbers, as [Example 16-5](#) proves.

**Example 16-5.** `Vector.__add__` take #1 supports non-`Vector` objects, too

```
>>> v1 = Vector([3, 4, 5])
>>> v1 + (10, 20, 30)
Vector([13.0, 24.0, 35.0])
>>> from vector2d_v3 import Vector2d
```

```
>>> v2d = Vector2d(1, 2)
>>> v1 + v2d
Vector([4.0, 6.0, 5.0])
```

Both uses of `+` in [Example 16-5](#) work because `__add__` uses `zip_longest(...)`, which can consume any iterable, and the generator expression to build the new `Vector` merely performs `a + b` with the pairs produced by `zip_longest(...)`, so an iterable producing any number of items will do.

However, if we swap the operands ([Example 16-6](#)), the mixed-type additions fail.

**Example 16-6.** `Vector.__add__` take #1 fails with non-`Vector` left operands

```
>>> v1 = Vector([3, 4, 5])
>>> (10, 20, 30) + v1
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
TypeError: can only concatenate tuple (not "Vector") to tuple
>>> from vector2d_v3 import Vector2d
>>> v2d = Vector2d(1, 2)
>>> v2d + v1
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
TypeError: unsupported operand type(s) for +: 'Vector2d' and 'Vector'
```

To support operations involving objects of different types, Python implements a special dispatching mechanism for the infix operator special methods. Given an expression `a + b`, the interpreter will perform these steps (also see [Figure 16-1](#)):

1. If `a` has `__add__`, call `a.__add__(b)` and return result unless it's `NotImplemented`.
2. If `a` doesn't have `__add__`, or calling it returns `NotImplemented`, check if `b` has `__radd__`, then call `b.__radd__(a)` and return result unless it's `NotImplemented`.
3. If `b` doesn't have `__radd__`, or calling it returns `NotImplemented`, raise `TypeError` with an *unsupported operand types* message.

---

**TIP**

The `__radd__` method is called the “reflected” or “reversed” version of `__add__`. I prefer to call them “reversed” special methods.<sup>4</sup>

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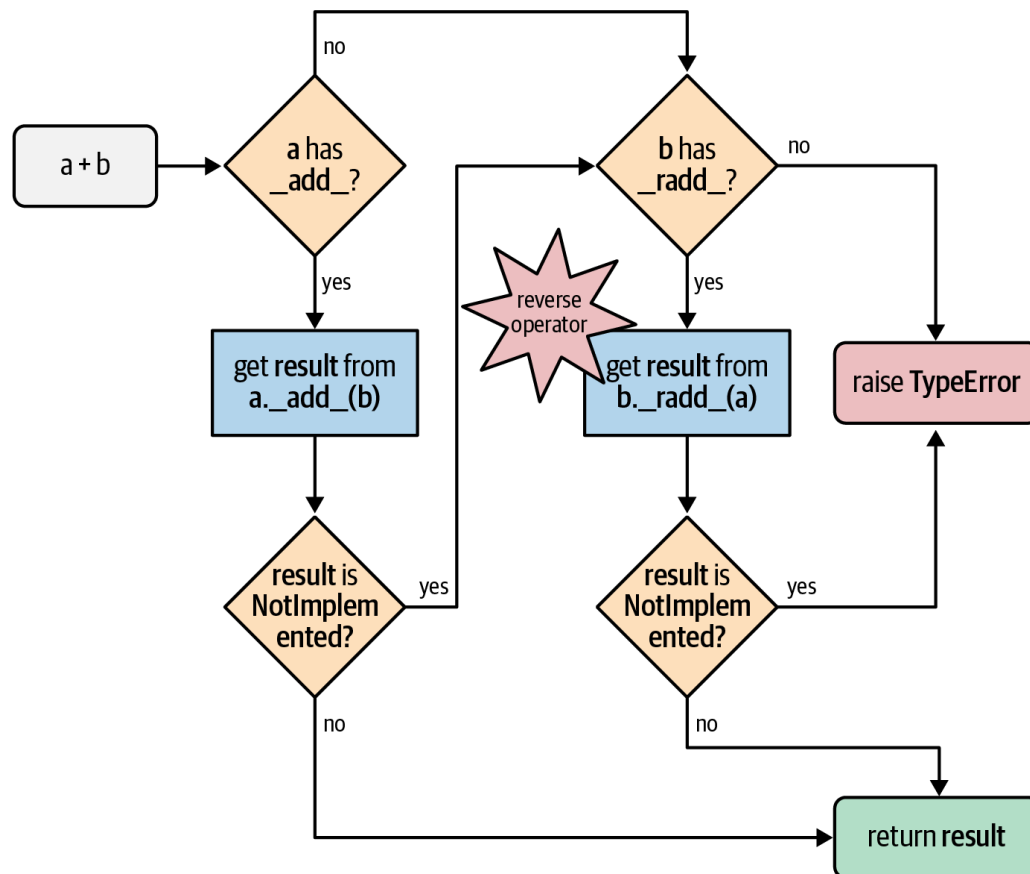


Figure 16-1. Flowchart for computing `a + b` with `__add__` and `__radd__`.

Therefore, to make the mixed-type additions in [Example 16-6](#) work, we need to implement the `Vector.__radd__` method, which Python will invoke as a fallback if the left operand does not implement `__add__`, or if it does but returns `NotImplemented` to signal that it doesn’t know how to handle the right operand.

---

**WARNING**

Do not confuse `NotImplemented` with `NotImplementedError`. The first, `NotImplemented`, is a special singleton value that an infix operator special method should return to tell the interpreter it cannot handle a given operand. In contrast, `NotImplementedError` is an exception that stub methods in abstract classes may raise to warn that subclasses must implement them.

---

The simplest implementation of `__radd__` that works is shown in

[Example 16-7](#).

**Example 16-7. The `Vector` methods `__add__` and `__radd__`**

```
# inside the Vector class

def __add__(self, other): ❶
    pairs = itertools.zip_longest(self, other, fillvalue=0.0)
    return Vector(a + b for a, b in pairs)

def __radd__(self, other): ❷
    return self + other
```

❶ No changes to `__add__` from [Example 16-4](#); listed here because `__radd__` uses it.

❷ `__radd__` just delegates to `__add__`.

Often, `__radd__` can be as simple as that: just invoke the proper operator, therefore delegating to `__add__` in this case. This applies to any commutative operator; `+` is commutative when dealing with numbers or our vectors, but it's not commutative when concatenating sequences in Python.

If `__radd__` simply calls `__add__`, here is another way to achieve the same effect:

```
def __add__(self, other):
    pairs = itertools.zip_longest(self, other, fillvalue=0.0)
    return Vector(a + b for a, b in pairs)

__radd__ = __add__
```

The methods in [Example 16-7](#) work with `Vector` objects, or any iterable with numeric items, such as a `Vector2d`, a `tuple` of integers, or an `array` of floats. But if provided with a noniterable object, `__add__` raises an exception with a message that is not very helpful, as in [Example 16-8](#).

**Example 16-8. `Vector.__add__` method needs an iterable operand**

```
>>> v1 + 1
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "vector_v6.py", line 328, in __add__
    pairs = itertools.zip_longest(self, other, fillvalue=0.0)
TypeError: zip_longest argument #2 must support iteration
```

Even worse, we get a misleading message if an operand is iterable but its items cannot be added to the `float` items in the `Vector`. See [Example 16-9](#).

**Example 16-9.** `Vector.__add__` method needs an iterable with numeric items

```
>>> v1 + 'ABC'
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "vector_v6.py", line 329, in __add__
    return Vector(a + b for a, b in pairs)
  File "vector_v6.py", line 243, in __init__
    self._components = array(self.typecode, components)
  File "vector_v6.py", line 329, in <genexpr>
    return Vector(a + b for a, b in pairs)
TypeError: unsupported operand type(s) for +: 'float' and 'str'
```

I tried to add `Vector` and a `str`, but the message complains about `float` and `str`.

The problems in Examples [16-8](#) and [16-9](#) actually go deeper than obscure error messages: if an operator special method cannot return a valid result because of type incompatibility, it should return `NotImplemented` and not raise `TypeError`. By returning `NotImplemented`, you leave the door open for the implementer of the other operand type to perform the operation when Python tries the reversed method call.

In the spirit of duck typing, we will refrain from testing the type of the `other` operand, or the type of its elements. We'll catch the exceptions and return `NotImplemented`. If the interpreter has not yet reversed the operands, it will try that. If the reverse method call returns `NotImplemented`, then Python will raise `TypeError` with a standard error message like “unsupported operand type(s) for +: *Vector* and *str*.”

The final implementation of the special methods for `Vector` addition is in [Example 16-10](#).

**Example 16-10. `vector_v6.py`: operator + methods added to `vector_v5.py` ([Example 12-16](#))**

```
def __add__(self, other):
    try:
        pairs = itertools.zip_longest(self, other, fillvalue=0.0)
        return Vector(a + b for a, b in pairs)
    except TypeError:
        return NotImplemented

def __radd__(self, other):
    return self + other
```

Note that `__add__` now catches a `TypeError` and returns `NotImplemented`.

---

**WARNING**

If an infix operator method raises an exception, it aborts the operator dispatch algorithm. In the particular case of `TypeError`, it is often better to catch it and `return NotImplemented`. This allows the interpreter to try calling the reversed operator method, which may correctly handle the computation with the swapped operands, if they are of different types.

---

At this point, we have safely overloaded the `+` operator by writing `__add__` and `__radd__`. We will now tackle another infix operator: `*`.

## Overloading `*` for Scalar Multiplication

What does `Vector([1, 2, 3]) * x` mean? If `x` is a number, that would be a scalar product, and the result would be a new `Vector` with each component multiplied by `x`—also known as an elementwise multiplication:

```
>>> v1 = Vector([1, 2, 3])
>>> v1 * 10
Vector([10.0, 20.0, 30.0])
```

```
>>> 11 * v1
Vector([11.0, 22.0, 33.0])
```

---

**NOTE**

Another kind of product involving `Vector` operands would be the dot product of two vectors—or matrix multiplication, if you take one vector as a  $1 \times N$  matrix and the other as an  $N \times 1$  matrix. We will implement that operator in our `Vector` class in [“Using @ as an Infix Operator”](#).

---

Back to our scalar product, again we start with the simplest `__mul__` and `__rmul__` methods that could possibly work:

```
# inside the Vector class

def __mul__(self, scalar):
    return Vector(n * scalar for n in self)

def __rmul__(self, scalar):
    return self * scalar
```

Those methods do work, except when provided with incompatible operands. The `scalar` argument has to be a number that when multiplied by a float produces another float (because our `Vector` class uses an array of floats internally). So a complex number will not do, but the scalar can be an `int`, a `bool` (because `bool` is a subclass of `int`), or even a `fractions.Fraction` instance. In [Example 16-11](#), the `__mul__` method does not make an explicit type check on `scalar`, but instead converts it into a float, and returns `NotImplemented` if that fails. That’s a clear example of duck typing.

### Example 16-11. `vector_v7.py`: operator \* methods added

```
class Vector:
    typecode = 'd'

    def __init__(self, components):
        self._components = array(self.typecode, components)

# many methods omitted in book listing, see vector_v7.py
# in https://github.com/fluentpython/example-code-2e
```

```

def __mul__(self, scalar):
    try:
        factor = float(scalar)
    except TypeError: ❶
        return NotImplemented ❷
    return Vector(n * factor for n in self)

def __rmul__(self, scalar):
    return self * scalar ❸

```

- ❶ If `scalar` cannot be converted to `float` ...
- ❷ ...we don't know how to handle it, so we return `NotImplemented` to let Python try `__rmul__` on the `scalar` operand.
- ❸ In this example, `__rmul__` works fine by just performing `self * scalar`, delegating to the `__mul__` method.

With [Example 16-11](#), we can multiply `Vectors` by scalar values of the usual, and not so usual, numeric types:

```

>>> v1 = Vector([1.0, 2.0, 3.0])
>>> 14 * v1
Vector([14.0, 28.0, 42.0])
>>> v1 * True
Vector([1.0, 2.0, 3.0])
>>> from fractions import Fraction
>>> v1 * Fraction(1, 3)
Vector([0.3333333333333333, 0.6666666666666666, 1.0])

```

Now that we can multiply `Vector` by scalars, let's see how to implement `Vector` by `Vector` products.



#### NOTE

In the first edition of *Fluent Python*, I used goose typing in [Example 16-11](#): I checked the `scalar` argument of `__mul__` with `isinstance(scalar, numbers.Real)`. Now I avoid using the `numbers` ABCs because they are not supported by PEP 484, and using types at runtime that cannot also be statically checked seems a bad idea to me.

Alternatively, I could have checked against the `typing.SupportsFloat` protocol that we saw in [“Runtime Checkable Static Protocols”](#). I chose duck typing in that example because I think fluent Pythonistas should be comfortable with that coding pattern.

On the other hand, `__matmul__` in [Example 16-12](#) is a good example of goose typing, new in this second edition.

---

## Using @ as an Infix Operator

The @ sign is well-known as the prefix of function decorators, but since 2015, it can also be used as an infix operator. For years, the dot product was written as `numpy.dot(a, b)` in NumPy. The function call notation makes longer formulas harder to translate from mathematical notation to Python,<sup>5</sup> so the numerical computing community lobbied for [PEP 465—A dedicated infix operator for matrix multiplication](#), which was implemented in Python 3.5. Today, you can write `a @ b` to compute the dot product of two NumPy arrays.

The @ operator is supported by the special methods `__matmul__`, `__rmatmul__`, and `__imatmul__`, named for “matrix multiplication.” These methods are not used anywhere in the standard library at this time, but are recognized by the interpreter since Python 3.5, so the NumPy team—and the rest of us—can support the @ operator in user-defined types. The parser was also changed to handle the new operator (`a @ b` was a syntax error in Python 3.4).

These simple tests show how @ should work with `Vector` instances:

```
>>> va = Vector([1, 2, 3])
>>> vz = Vector([5, 6, 7])
>>> va @ vz == 38.0 # 1*5 + 2*6 + 3*7
True
```

```
>>> [10, 20, 30] @ vz
380.0
>>> va @ 3
Traceback (most recent call last):
...
TypeError: unsupported operand type(s) for @: 'Vector' and 'int'
```

[Example 16-12](#) shows the code of the relevant special methods.

### Example 16-12. vector\_v7.py: operator @ methods

```
class Vector:
    # many methods omitted in book listing

    def __matmul__(self, other):
        if (isinstance(other, abc.Sized) and ❶
            isinstance(other, abc.Iterable)):
            if len(self) == len(other): ❷
                return sum(a * b for a, b in zip(self, other)) ❸
            else:
                raise ValueError('@ requires vectors of equal length.')
        else:
            return NotImplemented

    def __rmatmul__(self, other):
        return self @ other
```

- ❶ Both operands must implement `__len__` and `__iter__` ...
- ❷ ...and have the same length to allow...
- ❸ ...a beautiful application of `sum`, `zip`, and generator expression.

---

#### NEW ZIP() FEATURE IN PYTHON 3.10

The `zip` built-in accepts a `strict` keyword-only optional argument since Python 3.10. When `strict=True`, the function raises `ValueError` when the iterables have different lengths. The default is `False`. This new strict behavior is in line with Python's *fail fast* philosophy. In [Example 16-12](#), I'd replace the inner `if` with a `try/except ValueError` and add `strict=True` to the `zip` call.

---

[Example 16-12](#) is a good example of *goose typing* in practice. If we tested the `other` operand against `Vector`, we'd deny users the flexibility of using lists or arrays as operands to `@`. As long as one operand is a `Vector`, our `@` implementation supports other operands that are instances of `abc.Sized` and `abc.Iterable`. Both of these ABCs implement the `__subclasshook__`, therefore any object providing `__len__` and `__iter__` satisfies our test—no need to actually subclass those ABCs or even register with them, as explained in [“Structural Typing with ABCs”](#). In particular, our `Vector` class does not subclass either `abc.Sized` or `abc.Iterable`, but it does pass the `isinstance` checks against those ABCs because it has the necessary methods.

Let's review the arithmetic operators supported by Python, before diving into the special category of [“Rich Comparison Operators”](#).

## Wrapping-Up Arithmetic Operators

Implementing `+`, `*`, and `@`, we saw the most common patterns for coding infix operators. The techniques we described are applicable to all operators listed in [Table 16-1](#) (the in-place operators will be covered in [“Augmented Assignment Operators”](#)).

Table 16-1. Infix operator method names (the in-place operators are used for augmented assignment; comparison operators are in [Table 16-2](#))

Operator	Forward	Reverse	In-place	Description
+	<code>__add__</code>	<code>__radd</code>	<code>__iadd</code>	Addition or concatenation
	—	—	—	
-	<code>__sub__</code>	<code>__rsub</code>	<code>__isub</code>	Subtraction
	—	—	—	
*	<code>__mul__</code>	<code>__rmul</code>	<code>__imul</code>	Multiplication or repetition
	—	—	—	
/	<code>__true</code> <code>div__</code>	<code>__rtru</code> <code>ediv__</code>	<code>__itru</code> <code>ediv__</code>	True division
//	<code>__floo</code> <code>rdiv__</code>	<code>__rflo</code> <code>ordiv_</code>	<code>__iflo</code> <code>ordiv_</code>	Floor division
		—	—	
%	<code>__mod__</code>	<code>__rmod</code>	<code>__imod</code>	Modulo
	—	—	—	
<code>divmod</code> ( )	<code>__divm</code> <code>od__</code>	<code>__rdiv</code> <code>mod__</code>	<code>__idiv</code> <code>mod__</code>	Returns tuple of floor division quotient and modulo
<code>**</code> , <code>pow</code> ( )	<code>__pow__</code>	<code>__rpow</code>	<code>__ipow</code>	Exponentiation <sup>a</sup>
	—	—	—	
@	<code>__matm</code> <code>ul__</code>	<code>__rmat</code> <code>mul__</code>	<code>__imat</code> <code>mul__</code>	Matrix multiplication
&	<code>__and__</code>	<code>__rand</code>	<code>__iand</code>	Bitwise and
	—	—	—	
	<code>__or__</code>	<code>__ror__</code>	<code>__ior__</code>	Bitwise or
		—	—	

Operator	Forward	Reverse	In-place	Description
<code>^</code>	<code>__xor__</code> <code>—</code>	<code>__rxor</code> <code>—</code>	<code>__ixor</code> <code>—</code>	Bitwise xor
<code>&lt;&lt;</code>	<code>__lshi</code> <code>ft__</code>	<code>__rlsh</code> <code>ift__</code>	<code>__ilsh</code> <code>ift__</code>	Bitwise shift left
<code>&gt;&gt;</code>	<code>__rshi</code> <code>ft__</code>	<code>__rrsh</code> <code>ift__</code>	<code>__irsh</code> <code>ift__</code>	Bitwise shift right

**a** `pow` takes an optional third argument, `modulo`: `pow(a, b, modulo)`, also supported by the special methods when invoked directly (e.g., `a.__pow__(b, modulo)`).

The rich comparison operators use a different set of rules.

## Rich Comparison Operators

The handling of the rich comparison operators `==`, `!=`, `>`, `<`, `>=`, and `<=` by the Python interpreter is similar to what we just saw, but differs in two important aspects:

- The same set of methods is used in forward and reverse operator calls. The rules are summarized in [Table 16-2](#). For example, in the case of `==`, both the forward and reverse calls invoke `__eq__`, only swapping arguments; and a forward call to `__gt__` is followed by a reverse call to `__lt__` with the arguments swapped.
- In the case of `==` and `!=`, if the reverse method is missing, or returns `NotImplemented`, Python compares the object IDs instead of raising `TypeError`.

Table 16-2. Rich comparison operators: reverse methods invoked when the initial method call returns `NotImplemented`

Group	Infix operator	Forward method call	Reverse method call	Fallback
Equality	<code>a == b</code>	<code>a.__eq__(b)</code>	<code>b.__eq__(a)</code>	Return <code>id(a) == id(b)</code>
	<code>a != b</code>	<code>a.__ne__(b)</code>	<code>b.__ne__(a)</code>	Return <code>not (a == b)</code>
Ordering	<code>a &gt; b</code>	<code>a.__gt__(b)</code>	<code>b.__lt__(a)</code>	Raise <code>TypeError</code>
	<code>a &lt; b</code>	<code>a.__lt__(b)</code>	<code>b.__gt__(a)</code>	Raise <code>TypeError</code>
	<code>a &gt;= b</code>	<code>a.__ge__(b)</code>	<code>b.__le__(a)</code>	Raise <code>TypeError</code>
	<code>a &lt;= b</code>	<code>a.__le__(b)</code>	<code>b.__ge__(a)</code>	Raise <code>TypeError</code>

Given these rules, let’s review and improve the behavior of the `Vector.__eq__` method, which was coded as follows in *vector\_v5.py* ([Example 12-16](#)):

```
class Vector:
    # many lines omitted

    def __eq__(self, other):
        return (len(self) == len(other) and
                all(a == b for a, b in zip(self, other)))
```

That method produces the results in [Example 16-13](#).

**Example 16-13. Comparing a `Vector` to a `Vector`, a `Vector2d`, and a tuple**

```

>>> va = Vector([1.0, 2.0, 3.0])
>>> vb = Vector(range(1, 4))
>>> va == vb ❶
True
>>> vc = Vector([1, 2])
>>> from vector2d_v3 import Vector2d
>>> v2d = Vector2d(1, 2)
>>> vc == v2d ❷
True
>>> t3 = (1, 2, 3)
>>> va == t3 ❸
True

```

- ❶ Two `Vector` instances with equal numeric components compare equal.
- ❷ A `Vector` and a `Vector2d` are also equal if their components are equal.
- ❸ A `Vector` is also considered equal to a `tuple` or any iterable with numeric items of equal value.

The result in [Example 16-13](#) is probably not desirable. Do we really want a `Vector` to be considered equal to a `tuple` containing the same numbers? I have no hard rule about this; it depends on the application context. The “Zen of Python” says:

*In the face of ambiguity, refuse the temptation to guess.*

Excessive liberality in the evaluation of operands may lead to surprising results, and programmers hate surprises.

Taking a clue from Python itself, we can see that `[1, 2] == (1, 2)` is `False`. Therefore, let’s be conservative and do some type checking. If the second operand is a `Vector` instance (or an instance of a `Vector` subclass), then use the same logic as the current `__eq__`. Otherwise, return `NotImplemented` and let Python handle that. See [Example 16-14](#).

**Example 16-14. `vector_v8.py`: improved `__eq__` in the `Vector` class**

```

def __eq__(self, other):
    if isinstance(other, Vector): ❶

```

```

        return (len(self) == len(other) and
                all(a == b for a, b in zip(self, other)))
    else:
        return NotImplemented ❷

```

❶ If the `other` operand is an instance of `Vector` (or of a `Vector` subclass), perform the comparison as before.

❷ Otherwise, return `NotImplemented`.

If you run the tests in [Example 16-13](#) with the new `Vector.__eq__` from [Example 16-14](#), what you get now is shown in [Example 16-15](#).

**Example 16-15. Same comparisons as [Example 16-13](#): last result changed**

```

>>> va = Vector([1.0, 2.0, 3.0])
>>> vb = Vector(range(1, 4))
>>> va == vb ❶
True
>>> vc = Vector([1, 2])
>>> from vector2d_v3 import Vector2d
>>> v2d = Vector2d(1, 2)
>>> vc == v2d ❷
True
>>> t3 = (1, 2, 3)
>>> va == t3 ❸
False

```

❶ Same result as before, as expected.

❷ Same result as before, but why? Explanation coming up.

❸ Different result; this is what we wanted. But why does it work?  
Read on...

Among the three results in [Example 16-15](#), the first one is no news, but the last two were caused by `__eq__` returning `NotImplemented` in [Example 16-14](#). Here is what happens in the example with a `Vector` and a `Vector2d`, `vc == v2d`, step-by-step:

1. To evaluate `vc == v2d`, Python calls `Vector.__eq__(vc, v2d)`.



2. `Vector.__eq__(vc, v2d)` verifies that `v2d` is not a `Vector` and returns `NotImplemented`.
3. Python gets the `NotImplemented` result, so it tries `Vector2d.__eq__(v2d, vc)`.
4. `Vector2d.__eq__(v2d, vc)` turns both operands into tuples and compares them: the result is `True` (the code for `Vector2d.__eq__` is in [Example 11-11](#)).

As for the comparison `va == t3`, between `Vector` and `tuple` in [Example 16-15](#), the actual steps are:

1. To evaluate `va == t3`, Python calls `Vector.__eq__(va, t3)`.
2. `Vector.__eq__(va, t3)` verifies that `t3` is not a `Vector` and returns `NotImplemented`.
3. Python gets the `NotImplemented` result, so it tries `tuple.__eq__(t3, va)`.
4. `tuple.__eq__(t3, va)` has no idea what a `Vector` is, so it returns `NotImplemented`.
5. In the special case of `==`, if the reversed call returns `NotImplemented`, Python compares object IDs as a last resort.

We don't need to implement `__ne__` for `!=` because the fallback behavior of `__ne__` inherited from `object` suits us: when `__eq__` is defined and does not return `NotImplemented`, `__ne__` returns that result negated.

In other words, given the same objects we used in [Example 16-15](#), the results for `!=` are consistent:

```
>>> va != vb
False
>>> vc != v2d
False
>>> va != (1, 2, 3)
True
```

The `__ne__` inherited from `object` works like the following code—except that the original is written in C:<sup>6</sup>

```
def __ne__(self, other):
    eq_result = self == other
```

```

    if eq_result is NotImplemented:
        return NotImplemented
    else:
        return not eq_result

```

After covering the essentials of infix operator overloading, let's turn to a different class of operators: the augmented assignment operators.

## Augmented Assignment Operators

Our `Vector` class already supports the augmented assignment operators `+=` and `*=`. That's because augmented assignment works with immutable receivers by creating new instances and rebinding the lefthand variable.

[Example 16-16](#) shows them in action.

**Example 16-16. Using `+=` and `*=` with `Vector` instances**

```

>>> v1 = Vector([1, 2, 3])
>>> v1_alias = v1 ❶
>>> id(v1) ❷
4302860128
>>> v1 += Vector([4, 5, 6]) ❸
>>> v1 ❹
Vector([5.0, 7.0, 9.0])
>>> id(v1) ❺
4302859904
>>> v1_alias ❻
Vector([1.0, 2.0, 3.0])
>>> v1 *= 11 ❼
>>> v1 ❽
Vector([55.0, 77.0, 99.0])
>>> id(v1)
4302858336

```

❶ Create an alias so we can inspect the `Vector([1, 2, 3])` object later.

❷ Remember the ID of the initial `Vector` bound to `v1`.

❸ Perform augmented addition.

- ④ The expected result...
- ⑤ ...but a new `Vector` was created.
- ⑥ Inspect `v1_alias` to confirm the original `Vector` was not altered.
- ⑦ Perform augmented multiplication.
- ⑧ Again, the expected result, but a new `Vector` was created.

If a class does not implement the in-place operators listed in [Table 16-1](#), the augmented assignment operators work as syntactic sugar: `a += b` is evaluated exactly as `a = a + b`. That's the expected behavior for immutable types, and if you have `__add__`, then `+=` will work with no additional code.

However, if you do implement an in-place operator method such as `__iadd__`, that method is called to compute the result of `a += b`. As the name says, those operators are expected to change the lefthand operand in place, and not create a new object as the result.

---

**WARNING**

The in-place special methods should never be implemented for immutable types like our `Vector` class. This is fairly obvious, but worth stating anyway.

---

To show the code of an in-place operator, we will extend the `BingoCage` class from [Example 13-9](#) to implement `__add__` and `__iadd__`.

We'll call the subclass `AddableBingoCage`. [Example 16-17](#) is the behavior we want for the `+` operator.

**Example 16-17. The `+` operator creates a new `AddableBingoCage` instance**

```
>>> vowels = 'AEIOU'
>>> globe = AddableBingoCage(vowels) ❶
>>> globe.inspect()
('A', 'E', 'I', 'O', 'U')
>>> globe.pick() in vowels ❷
```

```

True
>>> len(globe.inspect()) ❸
4
>>> globe2 = AddableBingoCage('XYZ') ❹
>>> globe3 = globe + globe2
>>> len(globe3.inspect()) ❺
7
>>> void = globe + [10, 20] ❻
Traceback (most recent call last):
...
TypeError: unsupported operand type(s) for +: 'AddableBingoCage' and 'list'

```

- ❶ Create a `globe` instance with five items (each of the `vowels`).
- ❷ Pop one of the items, and verify it is one of the `vowels`.
- ❸ Confirm that the `globe` is down to four items.
- ❹ Create a second instance, with three items.
- ❺ Create a third instance by adding the previous two. This instance has seven items.
- ❻ Attempting to add an `AddableBingoCage` to a `list` fails with `TypeError`. That error message is produced by the Python interpreter when our `__add__` method returns `NotImplemented`.

Because an `AddableBingoCage` is mutable, [Example 16-18](#) shows how it will work when we implement `__iadd__`.

**Example 16-18. An existing `AddableBingoCage` can be loaded with `+=` (continuing from [Example 16-17](#))**

```

>>> globe_orig = globe ❶
>>> len(globe.inspect()) ❷
4
>>> globe += globe2 ❸
>>> len(globe.inspect())
7
>>> globe += ['M', 'N'] ❹
>>> len(globe.inspect())
9
>>> globe is globe_orig ❺

```

```

True
>>> globe += 1 ❹
Traceback (most recent call last):
...
TypeError: right operand in += must be 'Tombola' or an iterable

```

- ❶ Create an alias so we can check the identity of the object later.
- ❷ `globe` has four items here.
- ❸ An `AddableBingoCage` instance can receive items from another instance of the same class.
- ❹ The righthand operand of `+=` can also be any iterable.
- ❺ Throughout this example, `globe` has always referred to the same object as `globe_orig`.
- ❻ Trying to add a noniterable to an `AddableBingoCage` fails with a proper error message.

Note that the `+=` operator is more liberal than `+` with regard to the second operand. With `+`, we want both operands to be of the same type (`AddableBingoCage`, in this case), because if we accepted different types, this might cause confusion as to the type of the result. With the `+=`, the situation is clearer: the lefthand object is updated in place, so there's no doubt about the type of the result.

---

#### TIP

I validated the contrasting behavior of `+` and `+=` by observing how the `list` built-in type works. Writing `my_list + x`, you can only concatenate one `list` to another `list`, but if you write `my_list += x`, you can extend the lefthand `list` with items from any iterable `x` on the righthand side. This is how the `list.extend()` method works: it accepts any iterable argument.

---

Now that we are clear on the desired behavior for `AddableBingoCage`, we can look at its implementation in [Example 16-19](#). Recall that `BingoCage`, from [Example 13-9](#), is a concrete subclass of the `Tombola` ABC from [Example 13-7](#).

### Example 16-19. bingoaddable.py: AddableBingoCage extends

BingoCage to support + and +=

```
from tombola import Tombola
from bingo import BingoCage


class AddableBingoCage(BingoCage): ❶

    def __add__(self, other):
        if isinstance(other, Tombola): ❷
            return AddableBingoCage(self.inspect() + other.inspect())
        else:
            return NotImplemented

    def __iadd__(self, other):
        if isinstance(other, Tombola):
            other_iterable = other.inspect() ❸
        else:
            try:
                other_iterable = iter(other) ❹
            except TypeError: ❺
                msg = ('right operand in += must be '
                       "'Tombola' or an iterable")
                raise TypeError(msg)
        self.load(other_iterable) ❻
        return self ❼
```

- ❶ AddableBingoCage extends BingoCage.
- ❷ Our `__add__` will only work with an instance of `Tombola` as the second operand.
- ❸ In `__iadd__`, retrieve items from `other`, if it is an instance of `Tombola`.
- ❹ Otherwise, try to obtain an iterator over `other`.<sup>7</sup>
- ❺ If that fails, raise an exception explaining what the user should do. When possible, error messages should explicitly guide the user to the solution.
- ❻ If we got this far, we can load the `other_iterable` into `self`.

- ❶ Very important: augmented assignment special methods of mutable objects must return `self`. That's what users expect.

We can summarize the whole idea of in-place operators by contrasting the `return` statements that produce results in `__add__` and `__iadd__` in [Example 16-19](#):

`__add__`

The result is produced by calling the constructor `AddableBingoCage` to build a new instance.

`__iadd__`

The result is produced by returning `self`, after it has been modified.

To wrap up this example, a final observation on [Example 16-19](#): by design, no `__radd__` was coded in `AddableBingoCage`, because there is no need for it. The forward method `__add__` will only deal with right-hand operands of the same type, so if Python is trying to compute `a + b`, where `a` is an `AddableBingoCage` and `b` is not, we return `NotImplemented`—maybe the class of `b` can make it work. But if the expression is `b + a` and `b` is not an `AddableBingoCage`, and it returns `NotImplemented`, then it's better to let Python give up and raise `TypeError` because we cannot handle `b`.

---

#### TIP

In general, if a forward infix operator method (e.g., `__mul__`) is designed to work only with operands of the same type as `self`, it's useless to implement the corresponding reverse method (e.g., `__rmul__`) because that, by definition, will only be invoked when dealing with an operand of a different type.

---

This concludes our exploration of operator overloading in Python.

## Chapter Summary

We started this chapter by reviewing some restrictions Python imposes on operator overloading: no redefining of operators in the built-in types

themselves, overloading limited to existing operators, with a few operators left out (`is`, `and`, `or`, `not`).

We got down to business with the unary operators, implementing `__neg__` and `__pos__`. Next came the infix operators, starting with `+`, supported by the `__add__` method. We saw that unary and infix operators are supposed to produce results by creating new objects, and should never change their operands. To support operations with other types, we return the `NotImplemented` special value—not an exception—allowing the interpreter to try again by swapping the operands and calling the reverse special method for that operator (e.g., `__radd__`). The algorithm Python uses to handle infix operators is summarized in the flowchart in [Figure 16-1](#).

Mixing operand types requires detecting operands we can't handle. In this chapter, we did this in two ways: in the duck typing way, we just went ahead and tried the operation, catching a `TypeError` exception if it happened; later, in `__mul__` and `__matmul__`, we did it with an explicit `isinstance` test. There are pros and cons to these approaches: duck typing is more flexible, but explicit type checking is more predictable.

In general, libraries should leverage duck typing—opening the door for objects regardless of their types, as long as they support the necessary operations. However, Python's operator dispatch algorithm may produce misleading error messages or unexpected results when combined with duck typing. For this reason, the discipline of type checking using `isinstance` calls against ABCs is often useful when writing special methods for operator overloading. That's the technique dubbed *goose typing* by Alex Martelli—which we saw in [“Goose Typing”](#). Goose typing is a good compromise between flexibility and safety, because existing or future user-defined types can be declared as actual or virtual subclasses of an ABC. In addition, if an ABC implements the `__subclasshook__`, then objects pass `isinstance` checks against that ABC by providing the required methods—no subclassing or registration required.

The next topic we covered was the rich comparison operators. We implemented `==` with `__eq__` and discovered that Python provides a handy implementation of `!=` in the `__ne__` inherited from the `object` base class. The way Python evaluates these operators along with `>`, `<`, `>=`, and `<=` is slightly different, with special logic for choosing the reverse



method, and fallback handling for `==` and `!=`, which never generate errors because Python compares the object IDs as a last resort.

In the last section, we focused on augmented assignment operators. We saw that Python handles them by default as a combination of plain operator followed by assignment, that is: `a += b` is evaluated exactly as `a = a + b`. That always creates a new object, so it works for mutable or immutable types. For mutable objects, we can implement in-place special methods such as `__iadd__` for `+=`, and alter the value of the lefthand operand. To show this at work, we left behind the immutable `Vector` class and worked on implementing a `BingoCage` subclass to support `+=` for adding items to the random pool, similar to the way the `list` built-in supports `+=` as a shortcut for the `list.extend()` method. While doing this, we discussed how `+` tends to be stricter than `+=` regarding the types it accepts. For sequence types, `+` usually requires that both operands are of the same type, while `+=` often accepts any iterable as the righthand operand.

## Further Reading

Guido van Rossum wrote a good defense of operator overloading in [“Why operators are useful”](#). Trey Hunner blogged [“Tuple ordering and deep comparisons in Python”](#), arguing that the rich comparison operators in Python are more flexible and powerful than programmers may realize when coming from other languages.

Operator overloading is one area of Python programming where `isinstance` tests are common. The best practice around such tests is goose typing, covered in [“Goose Typing”](#). If you skipped that, make sure to read it.

The main reference for the operator special methods is the [“Data Model” chapter](#) of the Python documentation. Another relevant reading is [“9.1.2.2. Implementing the arithmetic operations”](#) in the `numbers` module of *The Python Standard Library*.

A clever example of operator overloading appeared in the `pathlib` package, added in Python 3.4. Its `Path` class overloads the `/` operator to build filesystem paths from strings, as shown in this example from the documentation:

```
>>> p = Path('/etc')
>>> q = p / 'init.d' / 'reboot'
>>> q
PosixPath('/etc/init.d/reboot')
```

Another nonarithmetic example of operator overloading is in the [Scapy](#) library, used to “send, sniff, dissect, and forge network packets.” In Scapy, the `/` operator builds packets by stacking fields from different network layers. See [“Stacking layers”](#) for details.

If you are about to implement comparison operators, study `functools.total_ordering`. That is a class decorator that automatically generates methods for all rich comparison operators in any class that defines at least a couple of them. See the [functools module docs](#).

If you are curious about operator method dispatching in languages with dynamic typing, two seminal readings are [“A Simple Technique for Handling Multiple Polymorphism”](#) by Dan Ingalls (member of the original Smalltalk team), and [“Arithmetic and Double Dispatching in Smalltalk-80”](#) by Kurt J. Hebel and Ralph Johnson (Johnson became famous as one of the authors of the original *Design Patterns* book). Both papers provide deep insight into the power of polymorphism in languages with dynamic typing, like Smalltalk, Python, and Ruby. Python does not use double dispatching for handling operators as described in those articles. The Python algorithm using forward and reverse operators is easier for user-defined classes to support than double dispatching, but requires special handling by the interpreter. In contrast, classic double dispatching is a general technique you can use in Python or any object-oriented language beyond the specific context of infix operators, and in fact Ingalls, Hebel, and Johnson use very different examples to describe it.

The article, [“The C Family of Languages: Interview with Dennis Ritchie, Bjarne Stroustrup, and James Gosling”](#), from which I quoted the epigraph for this chapter, appeared in *Java Report*, 5(7), July 2000, and *C++ Report*, 12(7), July/August 2000, along with two other snippets I used in this chapter’s “Soapbox” (next). If you are into programming language design, do yourself a favor and read that interview.



James Gosling, quoted at the start of this chapter, made the conscious decision to leave operator overloading out when he designed Java. In that same interview ([“The C Family of Languages: Interview with Dennis Ritchie, Bjarne Stroustrup, and James Gosling”](#)) he says:

*Probably about 20 to 30 percent of the population think of operator overloading as the spawn of the devil; somebody has done something with operator overloading that has just really ticked them off, because they’ve used like + for list insertion and it makes life really, really confusing. A lot of that problem stems from the fact that there are only about half a dozen operators you can sensibly overload, and yet there are thousands or millions of operators that people would like to define—so you have to pick, and often the choices conflict with your sense of intuition.*

Guido van Rossum picked the middle way in supporting operator overloading: he did not leave the door open for users creating new arbitrary operators like `<=>` or `: - )`, which prevents a Tower of Babel of custom operators, and allows the Python parser to be simple. Python also does not let you overload the operators of the built-in types, another limitation that promotes readability and predictable performance.

Gosling goes on to say:

*Then there’s a community of about 10 percent that have actually used operator overloading appropriately and who really care about it, and for whom it’s actually really important; this is almost exclusively people who do numerical work, where the notation is very important to appealing to people’s intuition, because they come into it with an intuition about what the + means, and the ability to say “a + b” where a and b are complex numbers or matrices or something really does make sense.*

Of course, there are benefits to disallowing operator overloading in a language. I’ve seen the argument that C is better than C++ for systems programming because operator overloading in C++ can make costly operations seem trivial. Two successful modern languages that compile to binary executables made opposite choices: Go doesn’t have operator overloading, but [Rust does](#).

But overloaded operators, when used sensibly, do make code easier to read and write. It's a great feature to have in a modern high-level language.

## A Glimpse at Lazy Evaluation

If you look closely at the traceback in [Example 16-9](#), you'll see evidence of the *lazy* evaluation of generator expressions. [Example 16-20](#) is that same traceback, now with callouts.

**Example 16-20.** Same as [Example 16-9](#)

```
>>> v1 + 'ABC'
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "vector_v6.py", line 329, in __add__
    return Vector(a + b for a, b in pairs) ❶
  File "vector_v6.py", line 243, in __init__
    self._components = array(self.typecode, components) ❷
  File "vector_v6.py", line 329, in <genexpr>
    return Vector(a + b for a, b in pairs) ❸
TypeError: unsupported operand type(s) for +: 'float' and 'str'
```

- ❶ The `Vector` call gets a generator expression as its `components` argument. No problem at this stage.
- ❷ The `components` genexp is passed to the `array` constructor. Within the `array` constructor, Python tries to iterate over the genexp, causing the evaluation of the first item `a + b`. That's when the `TypeError` occurs.
- ❸ The exception propagates to the `Vector` constructor call, where it is reported.

This shows how the generator expression is evaluated at the latest possible moment, and not where it is defined in the source code.

In contrast, if the `Vector` constructor was invoked as `Vector([a + b for a, b in pairs])`, then the exception would happen right there, because the list comprehension tried to build a `list` to be passed as the argument to the `Vector()` call. The body of `Vector.__init__` would not be reached at all.

[Chapter 17](#) will cover generator expressions in detail, but I did not want to let this accidental demonstration of their lazy nature go unnoticed.

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- 1 Source: [“The C Family of Languages: Interview with Dennis Ritchie, Bjarne Stroustrup, and James Gosling”](#).
- 2 The remaining ABCs in Python’s standard library are still valuable for goose typing and static typing. The issue with the `numbers` ABCs is explained in [“The numbers ABCs and Numeric Protocols”](#).
- 3 See [https://en.wikipedia.org/wiki/Bitwise\\_operation#NOT](https://en.wikipedia.org/wiki/Bitwise_operation#NOT) for an explanation of the bitwise not.
- 4 The Python documentation uses both terms. The [“Data Model” chapter](#) uses “reflected,” but [“9.1.2.2. Implementing the arithmetic operations”](#) in the `numbers` module docs mention “forward” and “reverse” methods, and I find this terminology better, because “forward” and “reversed” clearly name each of the directions, while “reflected” doesn’t have an obvious opposite.
- 5 See [“Soapbox”](#) for a discussion of the problem.
- 6 The logic for `object.__eq__` and `object.__ne__` is in function `object_richcompare` in [Objects/typeobject.c](#) in the CPython source code.
- 7 The `iter` built-in function will be covered in the next chapter. Here I could have used `tuple(other)`, and it would work, but at the cost of building a new `tuple` when all the `.load(...)` method needs is to iterate over its argument.

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