Community detection on the Wikipedia hyperlink graph

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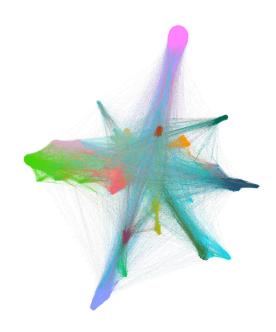
January 25, 2018





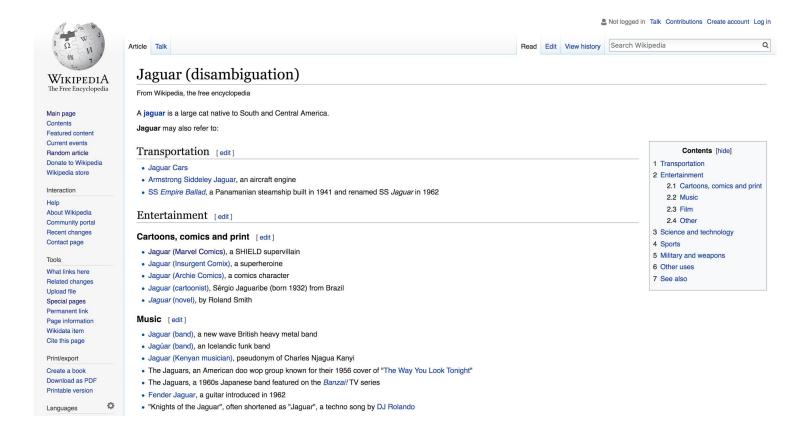
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1) Data Acquisition

Disambiguation pages



Wikipedia API

```
In [1]: import wikipedia
In [2]: wikipedia.page('Jaguar (disambiguation)')
        /usr/local/lib/python3.5/dist-packages/bs4/ init .py:181: UserWarning: No parser was explicitly specified, so I'm u
        sing the best available HTML parser for this system ("lxml"). This usually isn't a problem, but if you run this code
        on another system, or in a different virtual environment, it may use a different parser and behave differently.
        The code that caused this warning is on line 193 of the file /usr/lib/python3.5/runpy.py. To get rid of this warning,
        change code that looks like this:
         BeautifulSoup(YOUR MARKUP))
        to this:
         BeautifulSoup(YOUR MARKUP, "1xml")
          markup type=markup type))
        DisambiguationError
                                                  Traceback (most recent call last)
        <ipython-input-2-23d0ceef0c05> in <module>()
        ---> 1 wikipedia.page('Jaguar (disambiguation)')
        /usr/local/lib/python3.5/dist-packages/wikipedia/wikipedia.py in page(title, pageid, auto suggest, redirect, preload)
                        # if there is no suggestion or search results, the page doesn't exist
            274
            275
                        raise PageError(title)
                  return WikipediaPage(title, redirect=redirect, preload=preload)
        --> 276
            277
                  elif pageid is not None:
                    return WikipediaPage(pageid=pageid, preload=preload)
            278
```

Strategy

- Start from root node 'Jaguar (disambiguation)'
- Explore neighbors (first nodes)
- Explore neighbors of first nodes (second nodes)
- Get inner connections

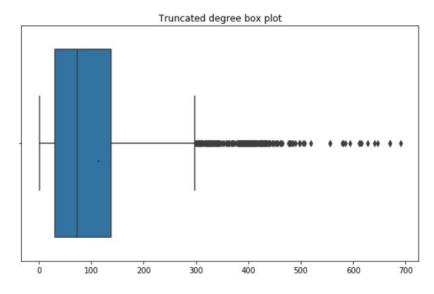


- Title
- Neighbors
- Categories (need to be cleaned from "All wikipedia pages with ... "
- URL



Principal properties of the collected network

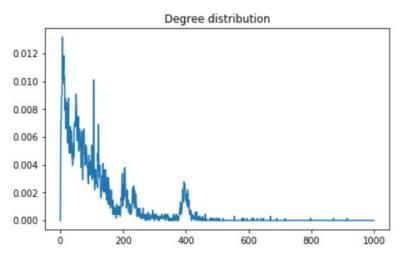
| Property | Value |
|-------------------------------------|-----------|
| Nodes | 6830 |
| Edges | 367483 |
| Clustering coefficient | 0.643 |
| Size of the largest giant component | 6830/6830 |
| Diameter | 5 |
| Average degree | 107.5 |

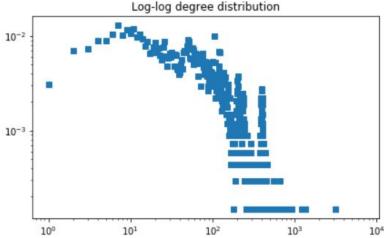


2) Modelisation of the network

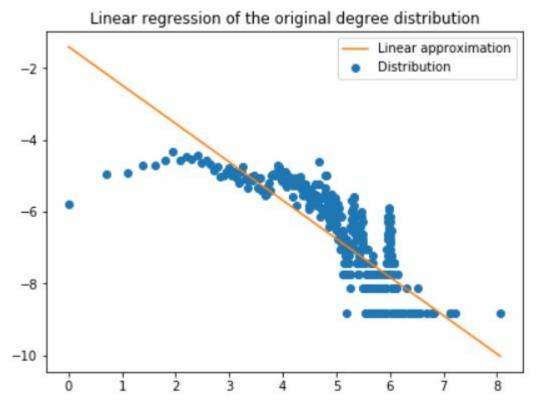
Find a simple network with similar properties

- Approximate the number of nodes/edges, the degree distribution, the clustering coefficient and the giant components
- The degree distribution is very complicated and noisy
- The log-log plot suggests a power law distribution





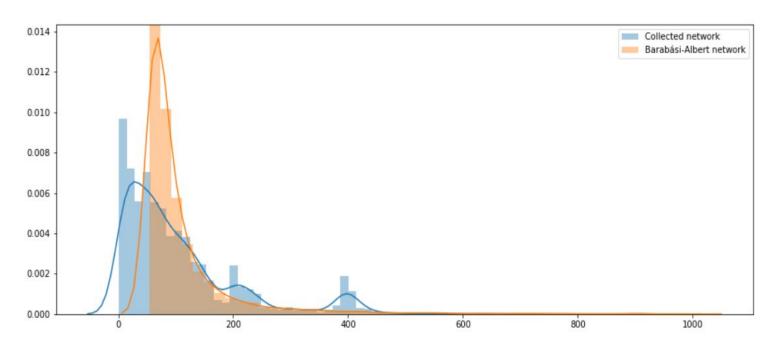
Regression of the degree distribution



- A linear regression can be used to find the power law coefficient
- $y = 1.0693 \times x 1.405$
- $R^2 \simeq 0.627$
- The value of R^2 is not very high but the power law seems to be a good approximation anyway.

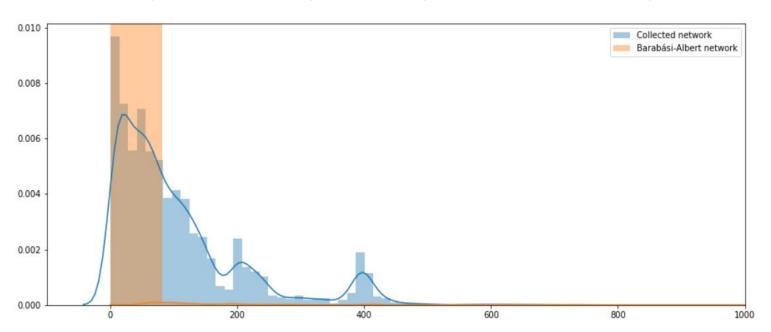
Barabási-Albert model

- The Barabási-Albert graph allows to get a power law distribution with an exponent of 3
- We would prefer a coefficient closer to the one calculated (~1.0693)



Creation of a power law network

- No perfect method to get exactly the wanted coefficient
- Generating a sequence of degrees following the desired law and linking them iteratively



Summary of the properties

| | Nodes | Edges | Distribution fit | Clustering coefficient | Giant components |
|---------------------|-------|--------|------------------|------------------------|------------------|
| Original | 6830 | 367483 | X | 0.643 | 6830/6830 |
| Erdős–Rényi | 6830 | 368697 | Bad | 0.016 | 6830/6830 |
| Barabási-Albe rt | 6830 | 365904 | Pretty good | 0.048 | 6830/6830 |
| Self-made power law | 6830 | 24675 | Pretty bad | 0.452 | 6826/683 |

- None of the model perfectly fits all the properties
- It seems like the Barabási-Albert network gives the most encouraging results
 - => preferential attachment

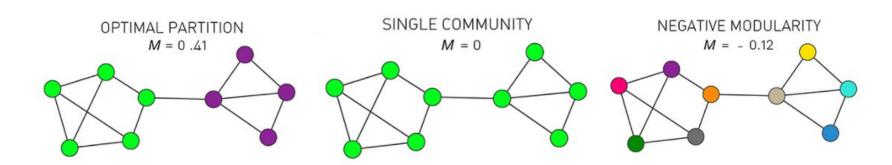
3.a) Community detection: Louvain Algorithm

Louvain Algorithm

- Optimization algorithm for maximizing the modularity of the network

Modularity

Measure of division of a network into modules (communities)



Louvain Algorithm

Start with a weighted network of N nodes, N different communities

Step I:

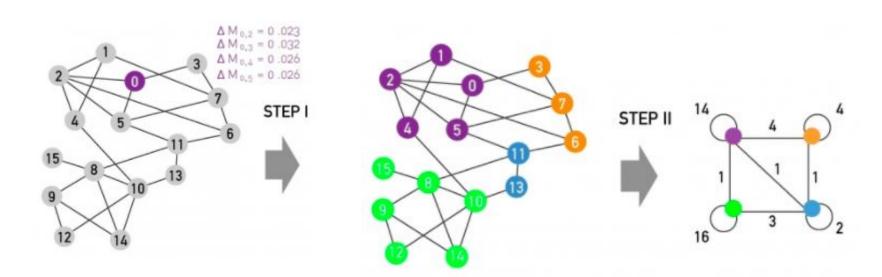
 For each node i evaluate the gain in modularity if we place node i in the community of one of its neighbors j

Step II:

- Construct a new network with communities as nodes
- New weights are the sum of weights on links between communities

Louvain algorithm

- Forces small communities into a larger one



Results

Modularity of the resulting partition

- High modularity 0.7878
- Network has community structures
- Number of communities: 17

Topics for community

```
Community 2/17 (561 pages):

('Jaguar vehicles', 44)

('Ford Motor Company', 43)

('Rear-wheel-drive vehicles', 40)

('Motor vehicle manufacturers of the United Kingdom', 36)

('Defunct motor vehicle manufacturers of England', 33)

('Car manufacturers of the United Kingdom', 30)

('Sports car manufacturers', 29)

('Former defence companies of the United Kingdom', 29)

('Car brands', 29)

('Defunct motor vehicle manufacturers of the United Kingdom', 28)
```

Alphabetical Order

Aircrafts

American Footbal

Animals / mammals

Apple inc.

British ships

Cars

Comics and fictional characters

Electronics

Car racing

Luxury in Britain

Mexican soccer

Music instruments

Rugby

Social science

Songwriters

Weapons

3.b) Community detection : Spectral Clustering

Spectral clustering algorithm

- Compute the graph Laplacian ${f L}={f D}$ ${f A}$ or ${f L}_{
 m norm}={f D}^{-1/2}{f L}{f D}^{-1/2}$
- Compute the first k eigenvalues and eigenvectors
- Gives a n x k matrix (k first eigenvectors)
- Each row can be seen as an embedding of a node in \mathbb{R}^k

- Clusterize those n points of \mathbb{R}^k to get the labels

First try: apply on natural graph

- Edges when there are links
- Weights all equal to 1

Poor results:

- Giant community with 99% of the nodes

'1, 1, 0, 0, 0, 1, 1, 2, 0, 0, 1, 6809, 1, 1, 1, 4, 1, 2, 2, 1, 1'

Better idea : apply a kernel

$$\arg \min_{y_1,...,y_N} \sum_{i \sim j} \mathbf{W}(i,j) \|y_i - y_j\|_2^2$$



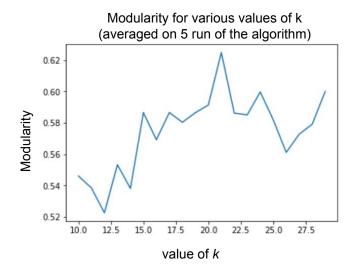
- Compute all distances (costly: θ (|edges| + |nodes|log|nodes|))
- Create a new complete graph
- $\mathbf{W}(u, v) = \exp\left(\frac{-d^2(u, v)}{\sigma^2}\right)$ (gaussian kernel)

Sparsify?

Choose k?

The same k returned by Louvain ?

- Elbow rule? Difficult to apply, high variance in the modularity (on average 0.035 of variance).



Results

- Modularity of the resulting partition : 0.62 ± 0.026

(reminder of louvain: 0.7878)

- Same communities are detected:
 - Some are doubled (ship incidents three times)
 - One is finer (electronics split in computer hardware and video games)

Interpretation of the results:

- Communities can be extracted just from the link structure

Louvain better results in term of modularity

- Spectral clustering more costly but finer partition

4) Time to Visualize

Networkx

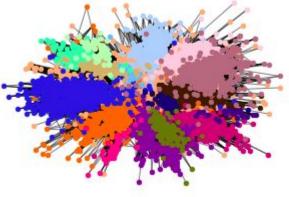
Initial state

Benefits:

- Easy to implement

Drawbacks:

- Provides basic options for visualization
- Layouts don't provide enough information



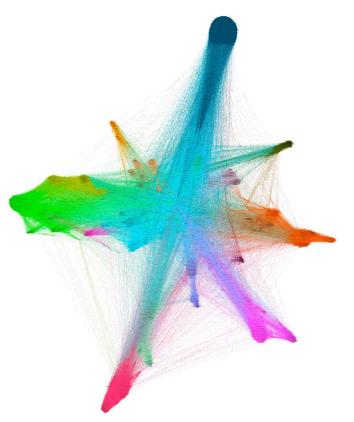
Spring layout



Fruchterman Reingold layout

Spectral layout

Gephi

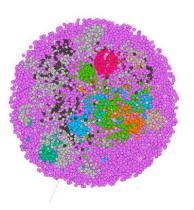


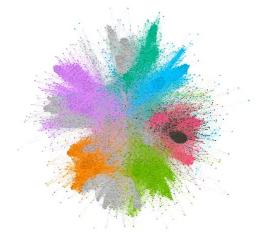
Benefits:

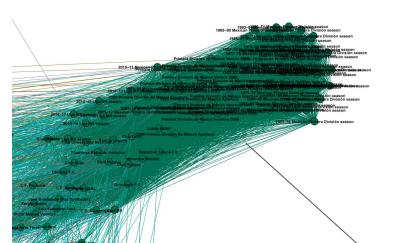
Customizing layouts and partitions

Drawbacks:

- Slow
- Limited interactivity
- No Jupyter notebook support







Gephi



Animals

Arcitizationec fox American de Singresied cat

Singresied cat

Electrical de Singresied Control de Singresied cat

Electrical de Singresied Control de Sin

padger II brower integrated Taxonomic Information System ctacled Band Potent ferret ed wolf Encyclopedia of Life

Change and paretage Biotechnology Information

DogMargay

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2014-12 Montan Primera Division Primera 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Primera División de México Invier
                                                            2013-14 Liga MX season
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Primera División de México Apertura
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Deportivo Toluca F.C.
```

Cougar

xonomy (biology)Giant otter ly wolf American mink Ocelot

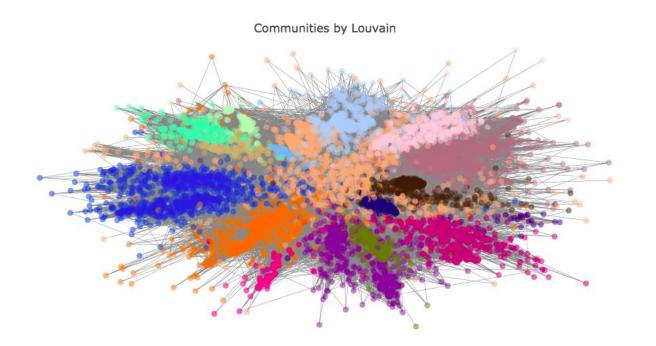
American black bear Coyote

inniped Sea otter

accoon

Mexican football

Plotly



Benefits:

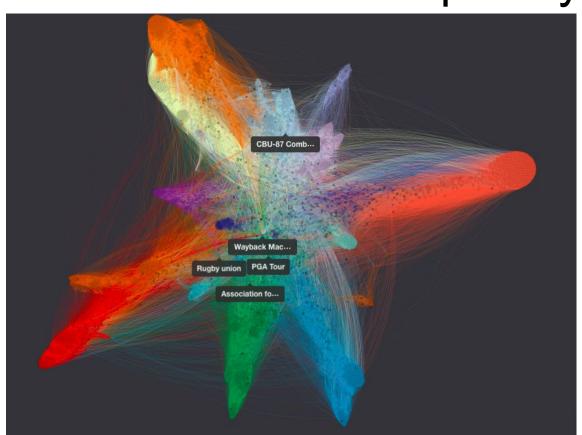
- Allows interactivity
- WebGL support

Drawbacks:

- Still laggy

Plotly interactive graph

Graphistry



Benefits:

- Fast
- Allows interactivity in real time
- Customizing plots
- Support for multiple python network modules

Drawbacks:

Not really intuitive

Conclusion

Conclusion

- The clustering we made proved that we can extract categories only from structural considerations
- Louvain algorithm seems to provide better results : faster and better modularity

Further work

 Measure properly the fit of the community detection with the categories of the nodes. How?

Implement a natural language processing pipeline on those categories in order to extract topics

Additional slides

Modularity

Measure of division of a network into modules (communities)

Hypothesis: Randomly wired networks lack an inherent community structure

$$M = \sum_{c=1}^{nc} \left[\frac{L_c}{L} - \left(\frac{k_c}{2L} \right)^2 \right]$$

L – number of links in network

 L_c – number of links within C_c community

 k_c – degree of the nodes in C_c community

Modularity

Higher when

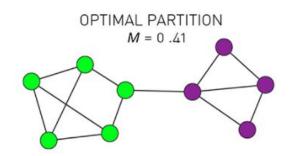
- number of edges in the communities high
- number of edges between the communities low

Zero when

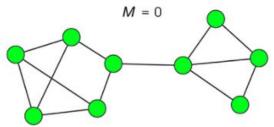
All nodes belong to one community

Negative when

Each node belongs to separate community







NEGATIVE MODULARITY

