

Projection Taxonomy

COMP 557

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Review

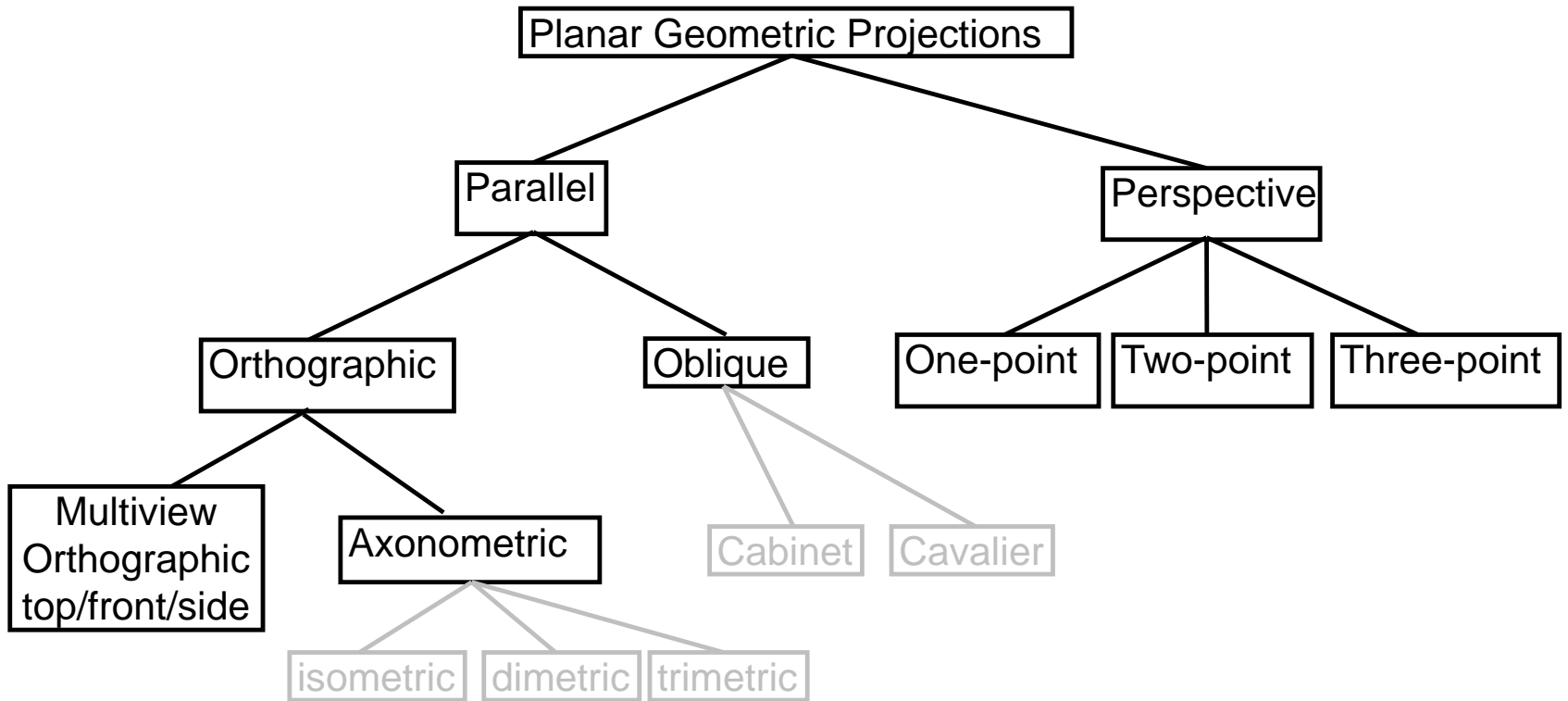
- What goes where on projection?
- gluPerspective and glFrustum
- Frustum applications
 - Tiled rendering, anaglyphs, depth of field, shifted perspective
- History of projection
- Depth Cues

Recall: Ray Generation vs. Projection

- Viewing in ray tracing
 - start with image point
 - compute ray that projects to that point
 - do this using geometry
- Viewing by projection
 - start with 3D point
 - compute image point that it projects to
 - do this using transforms
- Both provide planar projection

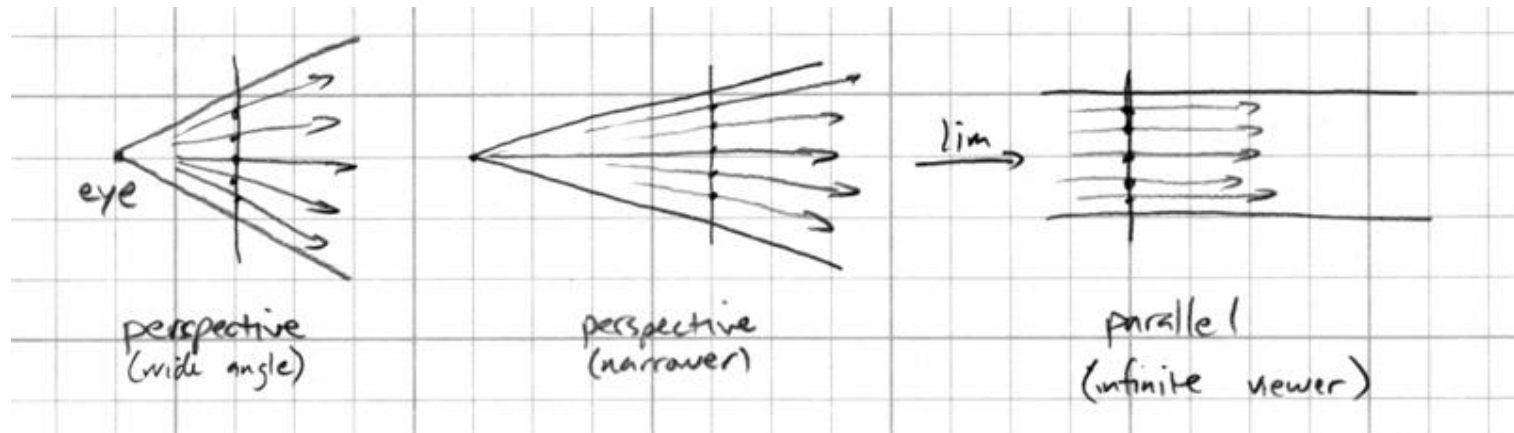
Taxonomy of Classical Projections

- Emphasis on cube-like objects
 - traditional in mechanical and architectural drawing



Parallel Projection

- Viewing rays are parallel rather than diverging
 - like a perspective camera that's far away



Multiview Orthographic

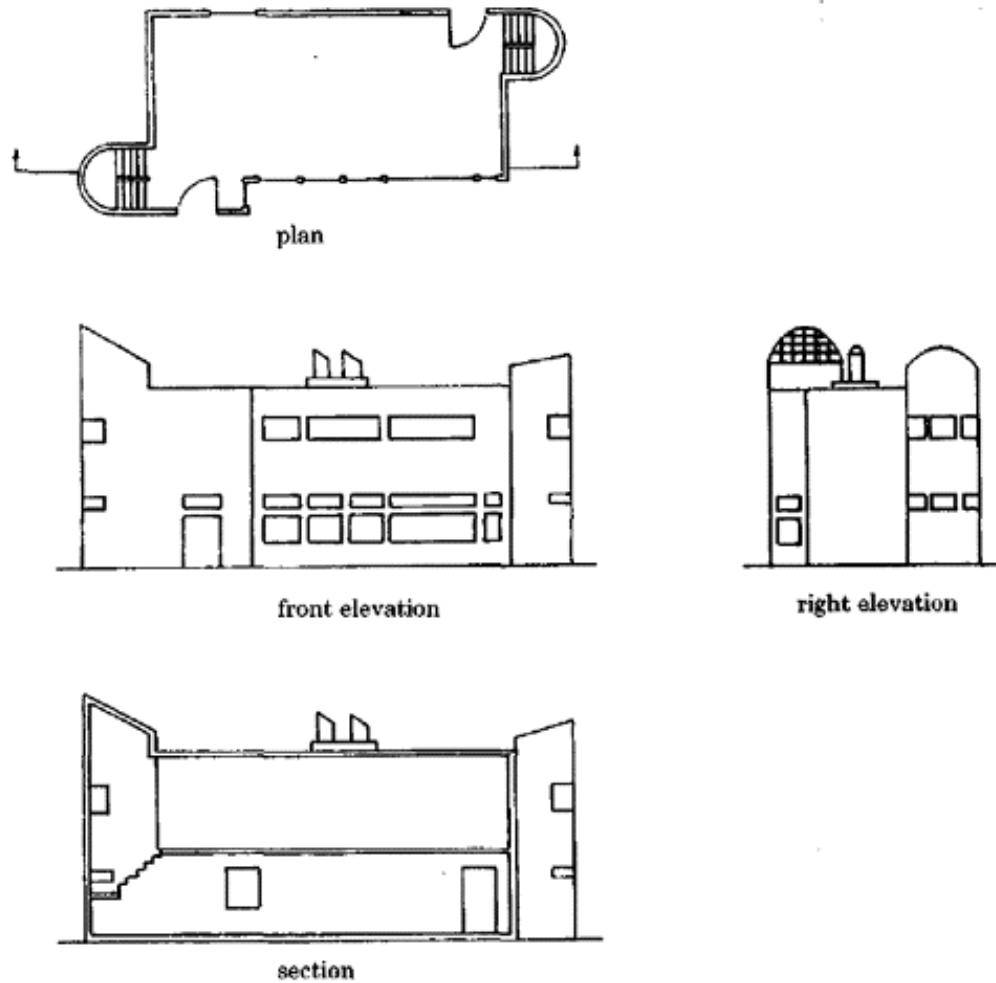
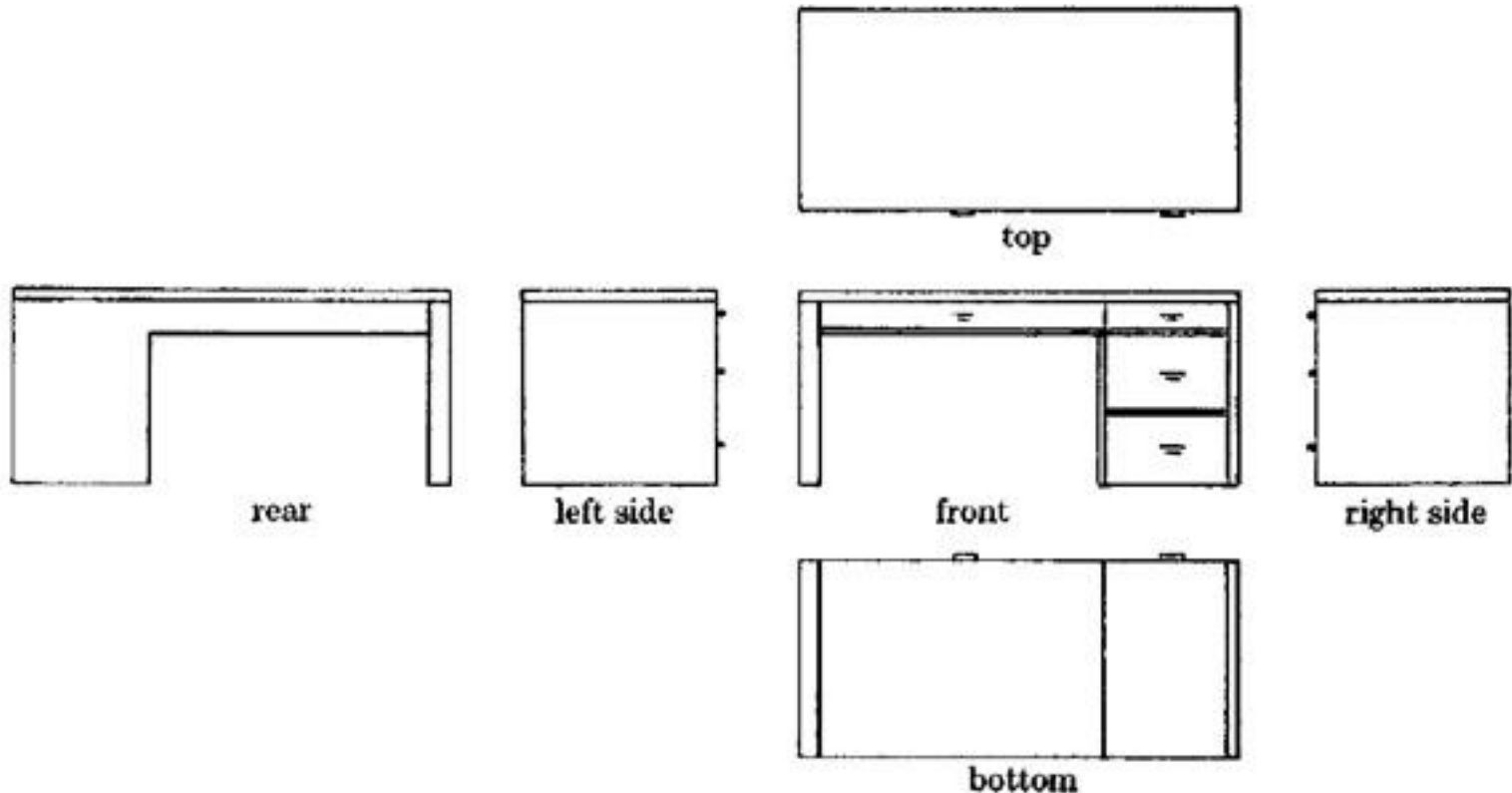
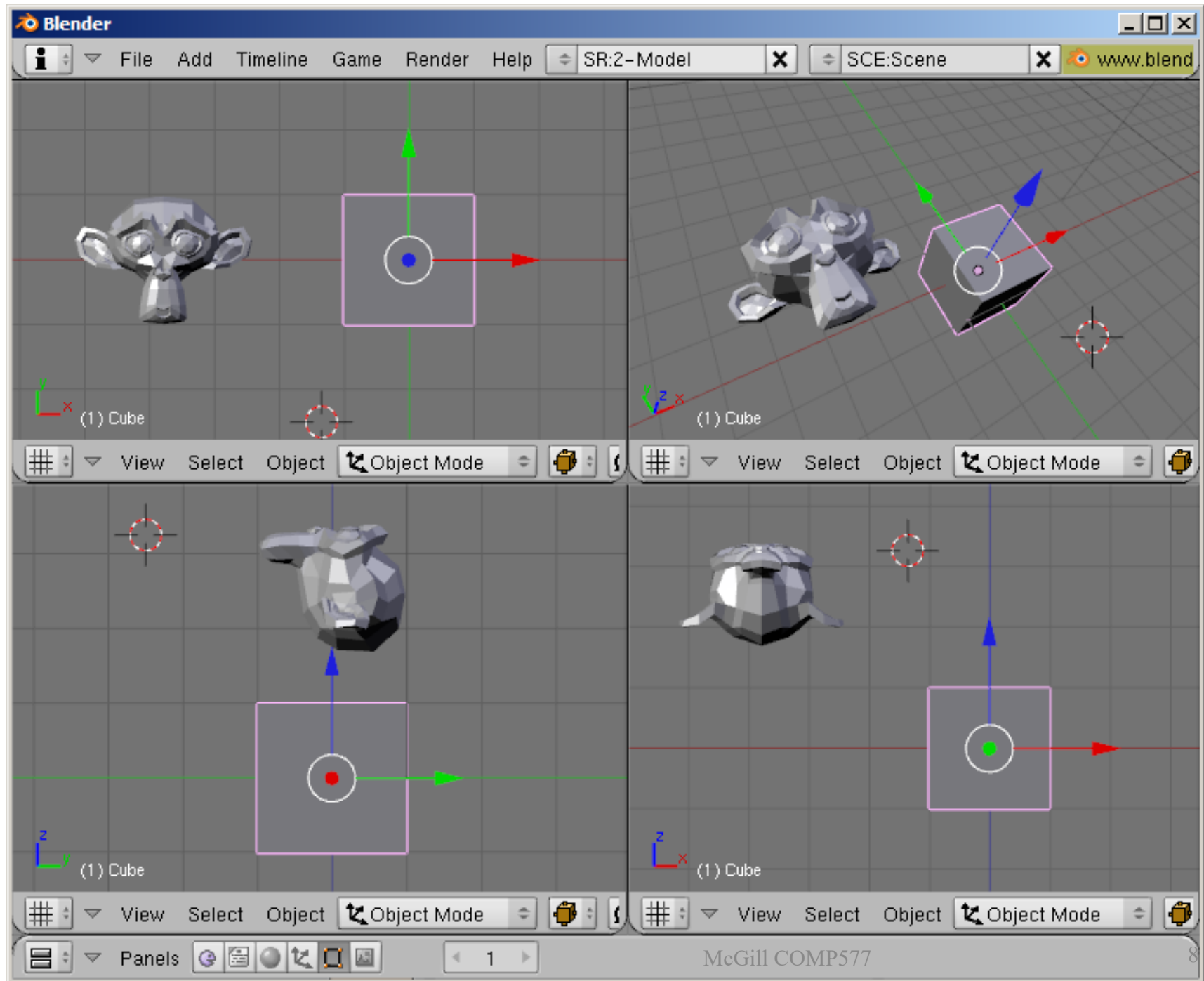


FIGURE 2-1. Multiview orthographic projection: plan, elevations, and section of a building.

Multiview Orthographic

- Projection plane parallel to a coordinate plane
- Projection direction perpendicular to projection plane

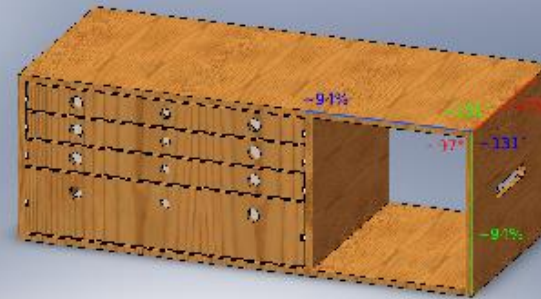




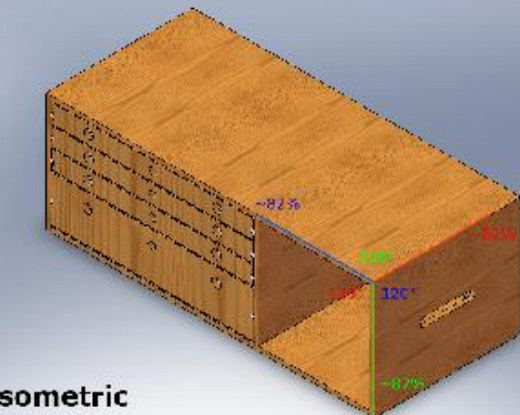
Off-axis parallel

axonometric: projection plane perpendicular to projection direction but not parallel to coordinate planes

Trimetric

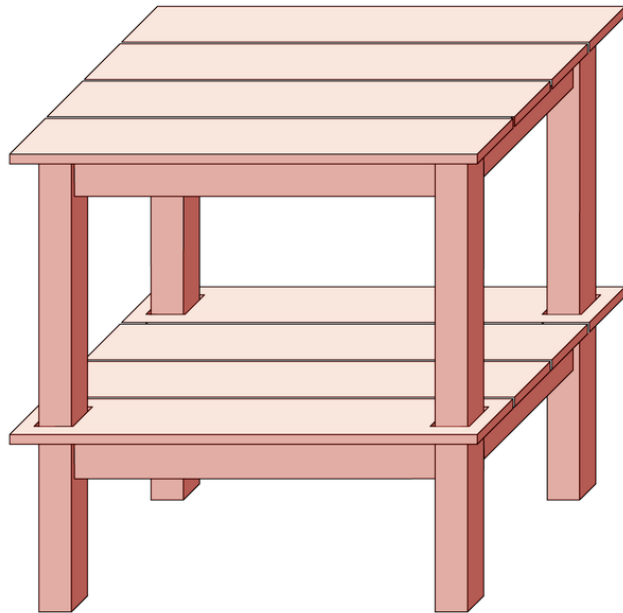


Dimetric



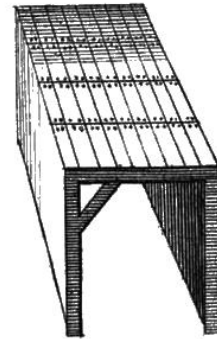
Isometric

Oblique Parallel Projection

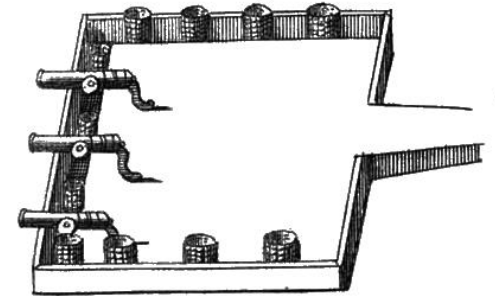


Cabinet, $\frac{1}{2}$ length in z

Gallery



Battery

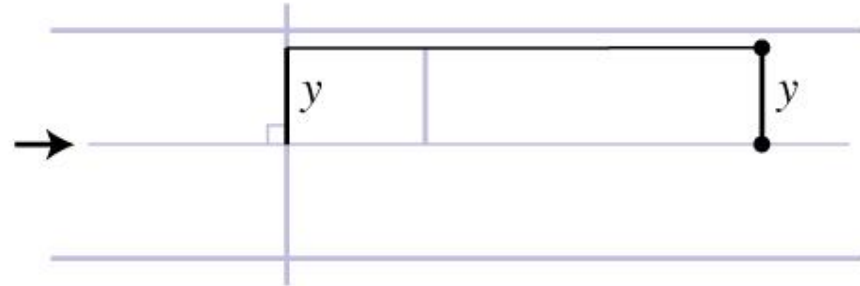


Cavalier... same length in all dimensions

oblique: projection plane parallel to a coordinate plane but not perpendicular to projection direction.

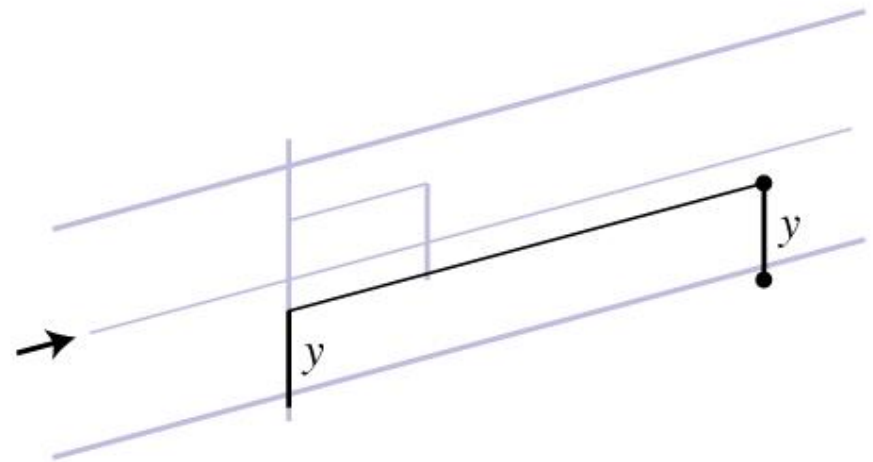
Orthographic Projection

- In graphics, we associate axonometric with orthographic
 - projection plane perpendicular to projection direction
 - image height determines size of objects in image

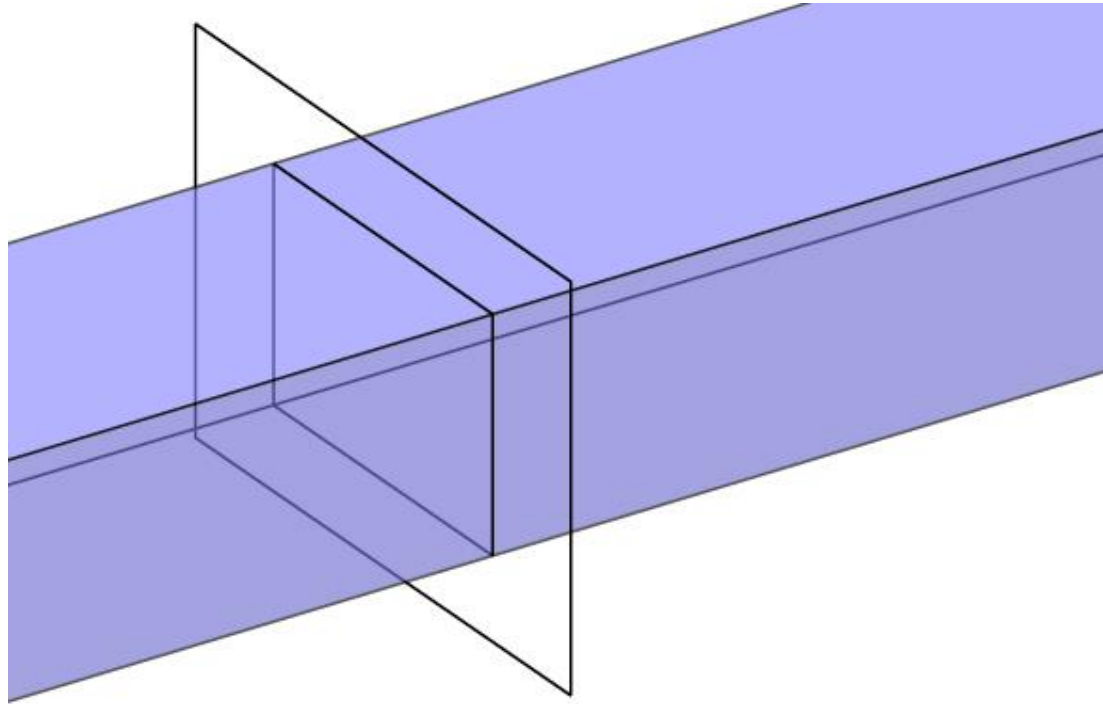


Oblique projection

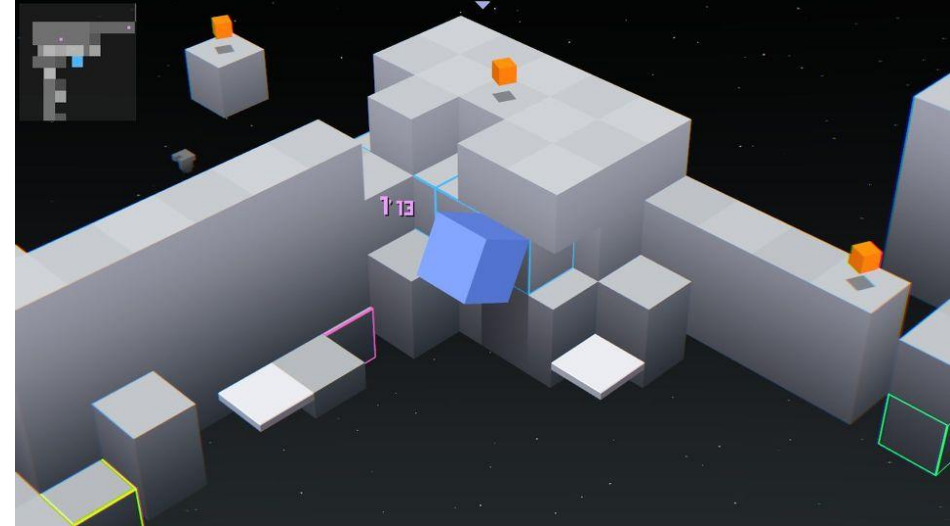
- View direction no longer coincides with projection plane normal (one more parameter)
 - objects at different distances still same size
 - objects are shifted in the image depending on their depth



Orthographic View Volume



Recall: view volume is specified by left right top and bottom

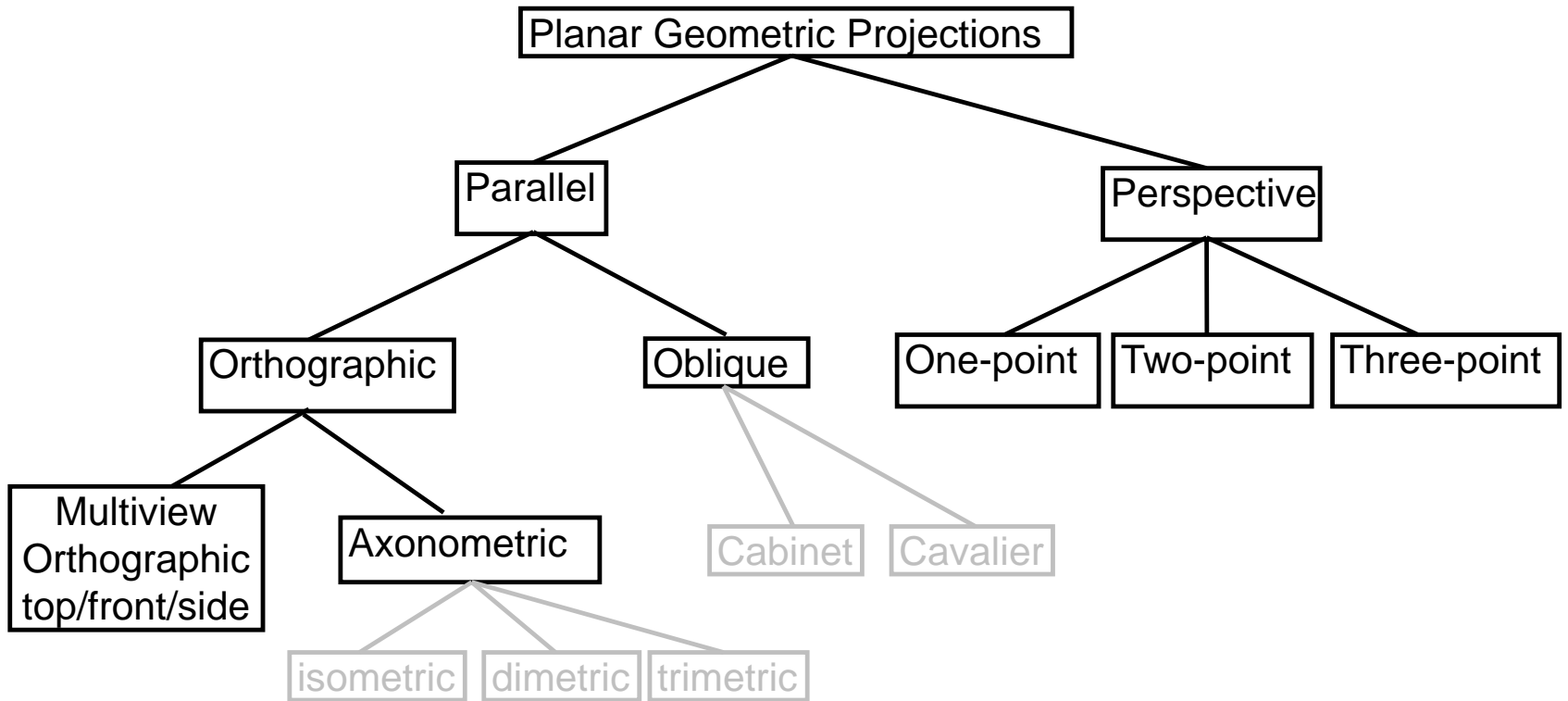


Parallel projections in video games?



Taxonomy of Classical Projections

- Emphasis on cube-like objects
 - traditional in mechanical and architectural drawing

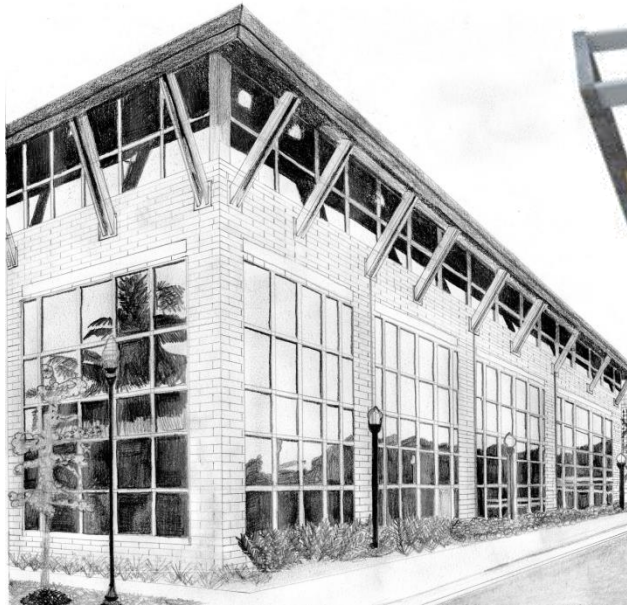


Perspective

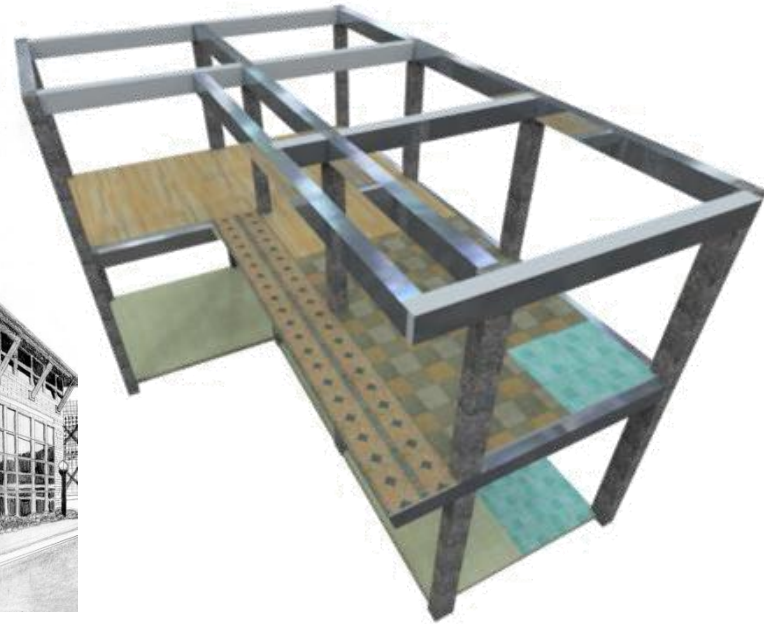
one-point: projection plane parallel to a coordinate plane (to two coordinate axes)



two-point: projection plane parallel to one coordinate axis

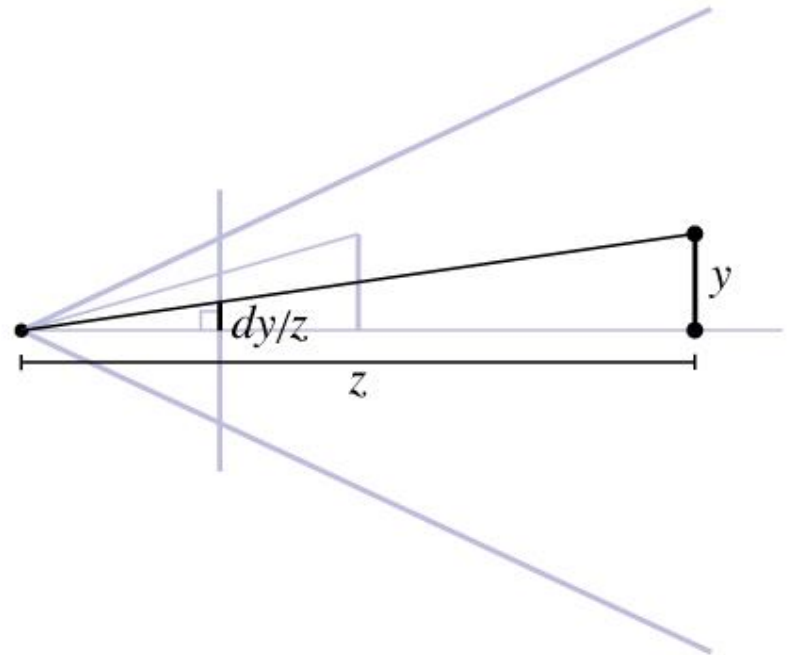


three-point: projection plane not parallel to a coordinate axis



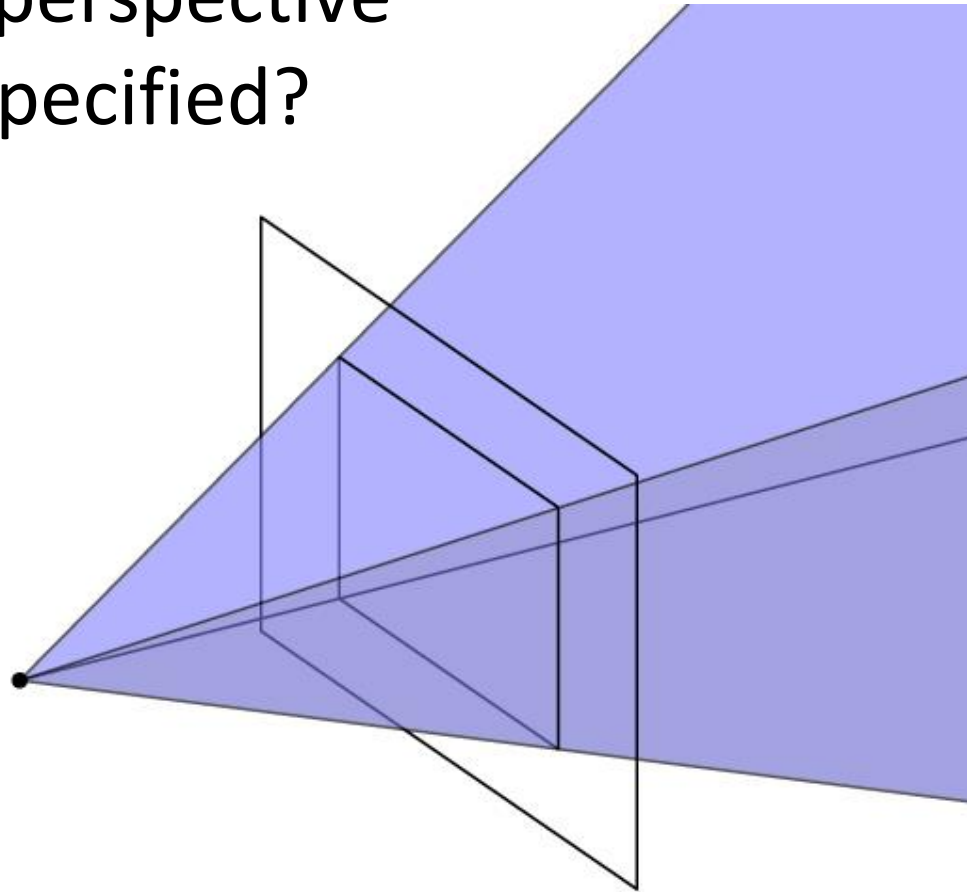
Perspective projection (normal)

- Perspective is projection by lines through a point; “normal” = plane perpendicular to view direction
 - magnification determined by:
 - image height
 - object depth
 - image plane distance
 - $FOV = 2 \operatorname{atan}(h / (2d))$
 - $y' = d y / z$
 - “normal” case corresponds to common types of cameras



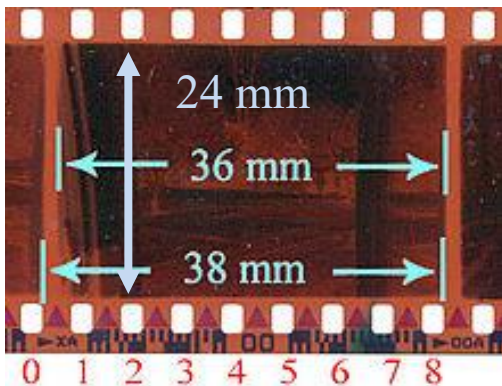
View volume: perspective

- Recall: how is perspective view volume specified?



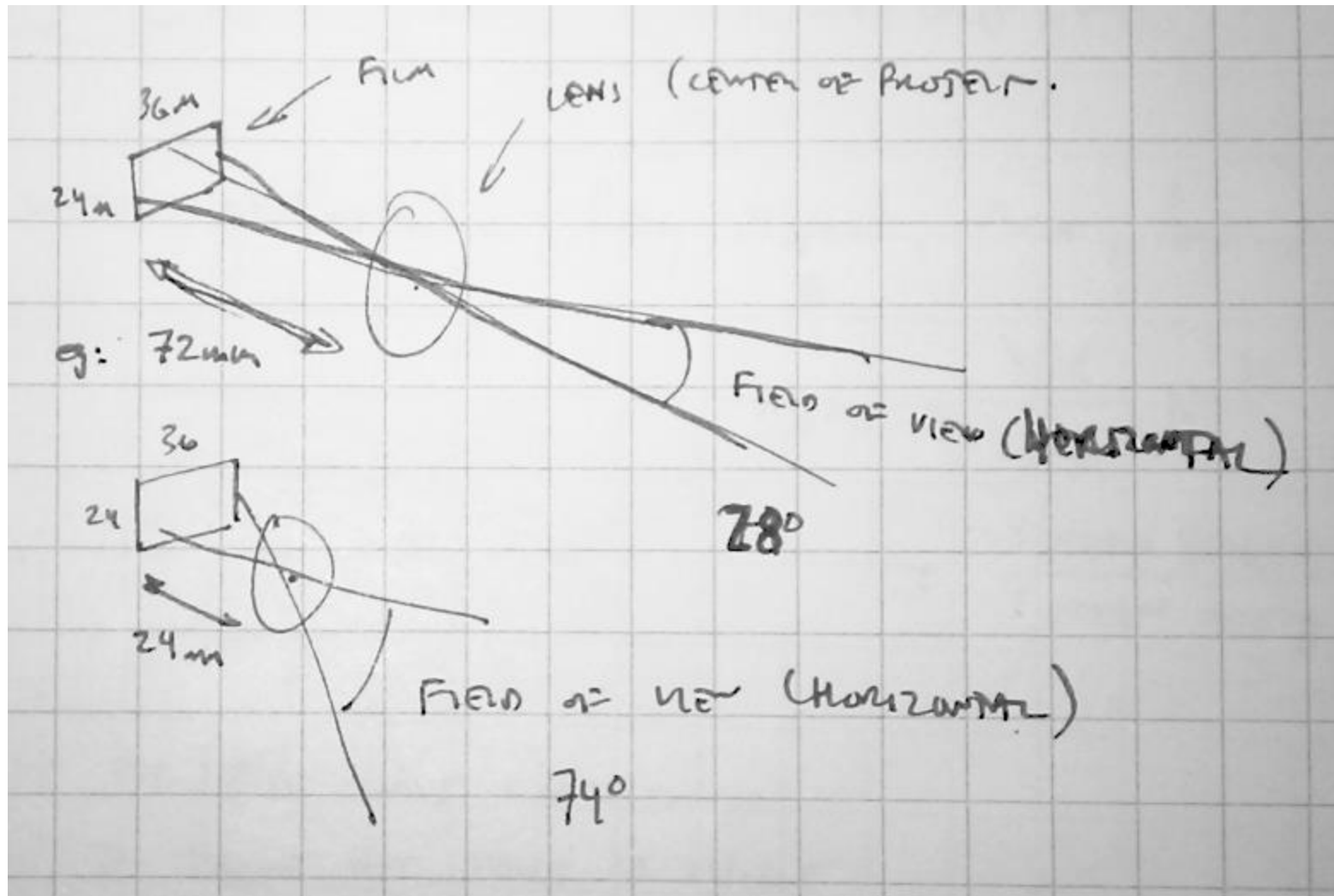
Field of view (or f.o.v.)

- The angle between the rays corresponding to opposite edges of a perspective image
 - Easy to compute only for “normal” perspective
 - Must decide to measure vertical, horizontal, or diagonal
- In cameras, determined by focal length
 - This is confusing because it depends on film image size
 - For still photography, 35mm format: 36 x 24 mm image



- 18mm = — super-wide angle
- 28mm = — wide angle
- 50mm = — “normal”
- 100mm = — narrow angle (“telephoto”)





Field of view

- Determines “strength” of perspective effects



close viewpoint
wide angle
prominent foreshortening



far viewpoint
narrow angle
little foreshortening

[Ansel Adams]

19mm



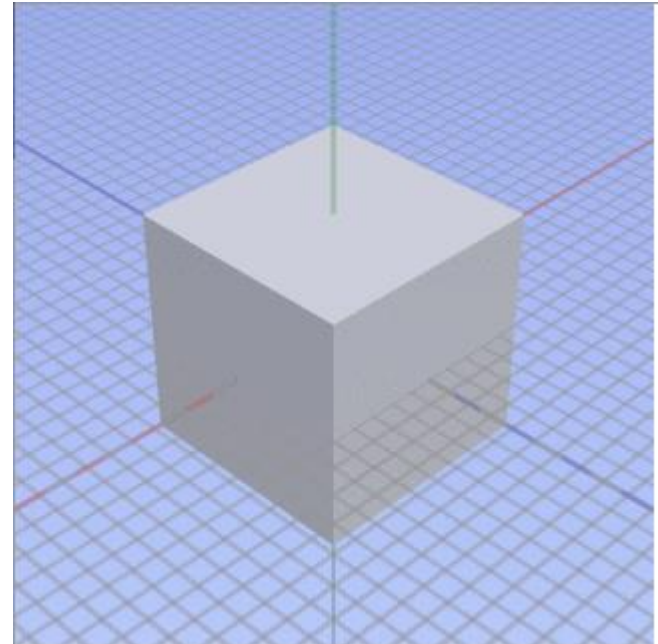
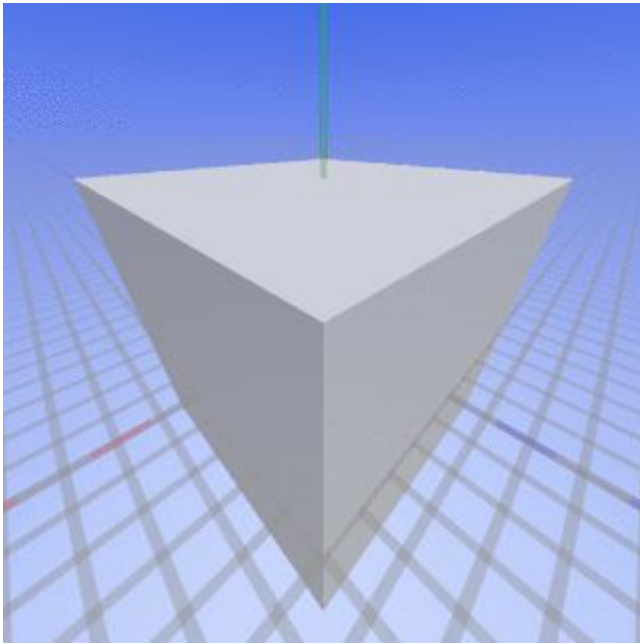
Choice of field of view

- In photography, wide angle lenses are specialty tools
 - “hard to work with”
 - easy to create weird-looking perspective effects
- In graphics, you can type in whatever f.o.v. you want
 - Don’t be one of those people that type in big numbers unless you really mean it!



[Ken Perlin]

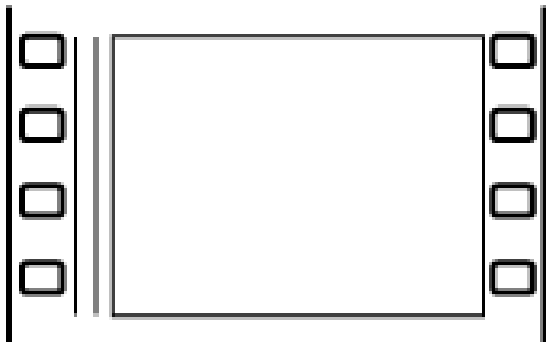
Perspective Distortions





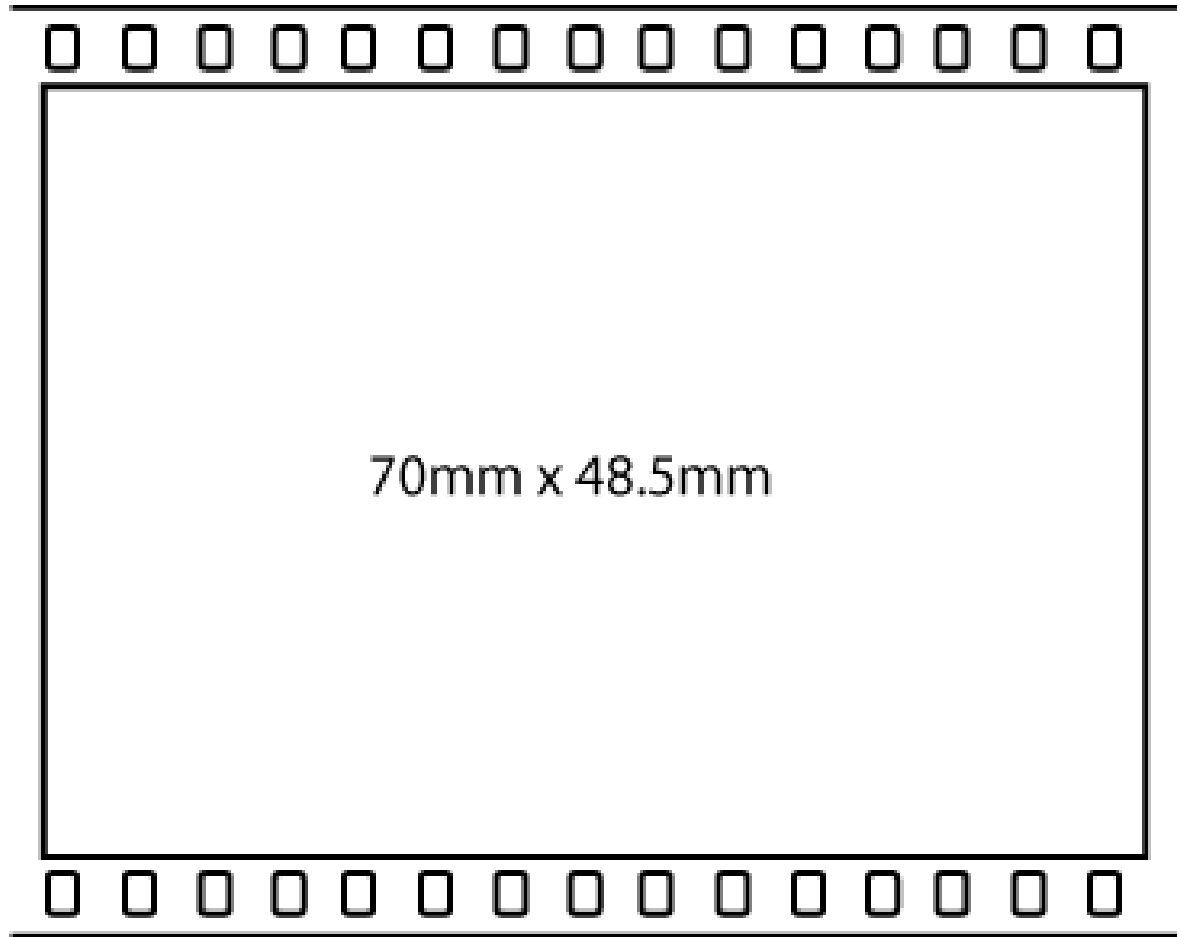
Brief aside...

21.95mm x 18.6mm



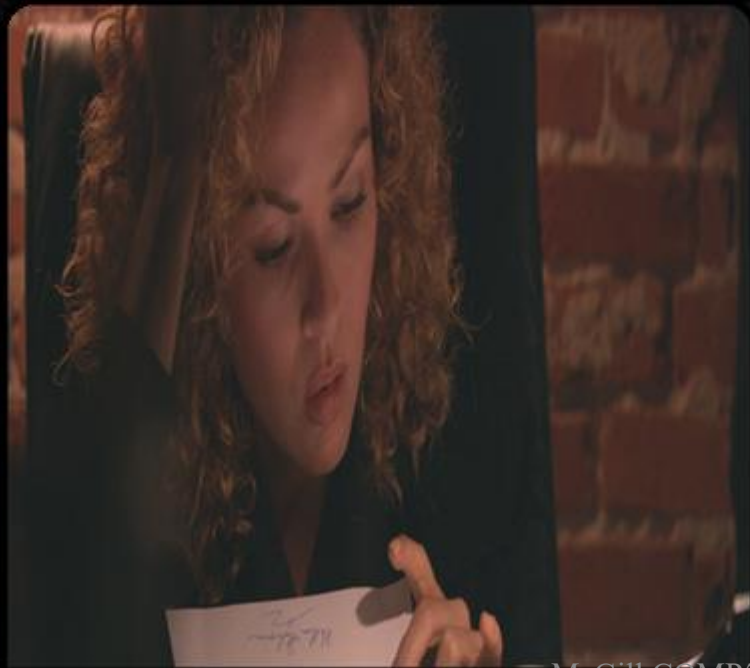
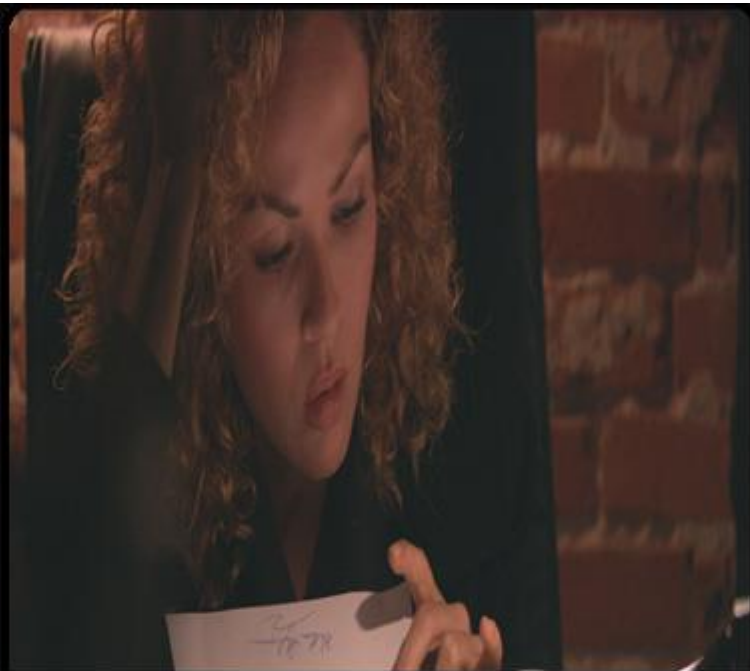
35mm
Academy Format

70mm x 48.5mm



70mm
IMAX Format

Widescreen
anamorphic
e.g., CinemaScope



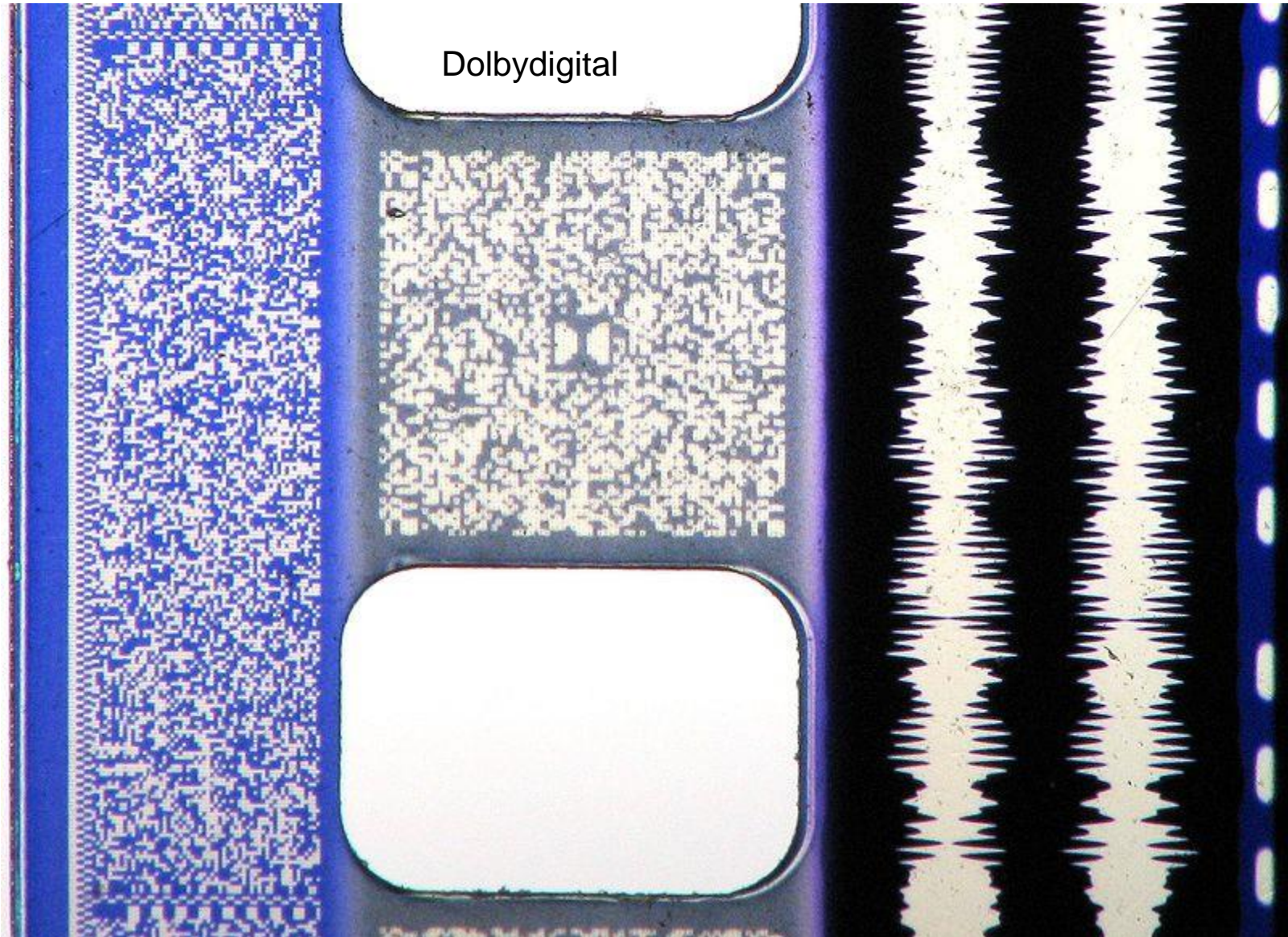
SDDS

(sony dynamic digital sound)

Analog optical

DTS

time code









ANAMORPHIC VINTAGE OVAL BOKEH FILTER+ FLARE/STREAK

GET A VINTAGE LOOK TO YOUR VIDEOS



1.33 or 4:3

Standard aspect ratio
and
standard-definition video

1.66:1

Aspect ratio used for
most European theatrical
showings

1.78:1 or 16:9

Standard aspect ratio for
high-definition video

1.85:1

Aspect ratio used for most
U.S. theatrical showings
since the 1960s

2.40:1

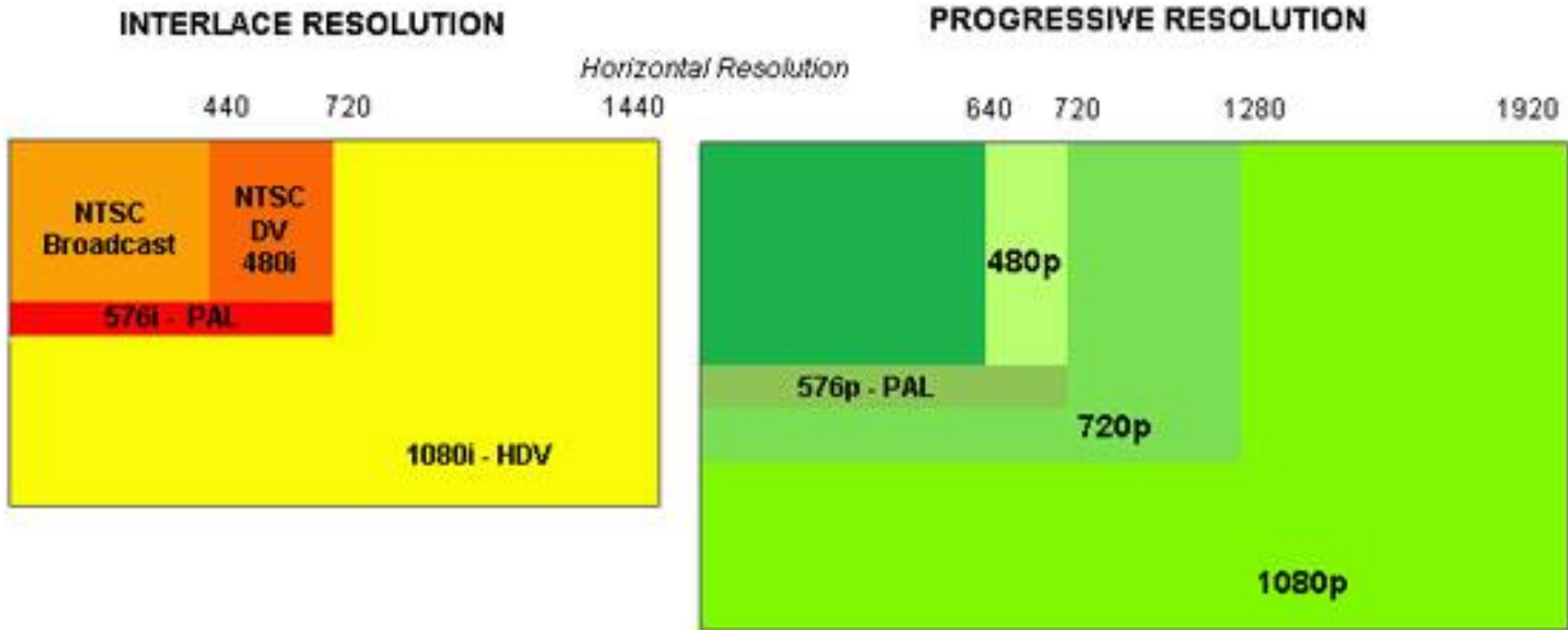
Aspect ratio of current anamorphic
(wide-screen) showings

2.75:1

Aspect ratio of Ultra-Panavision 70

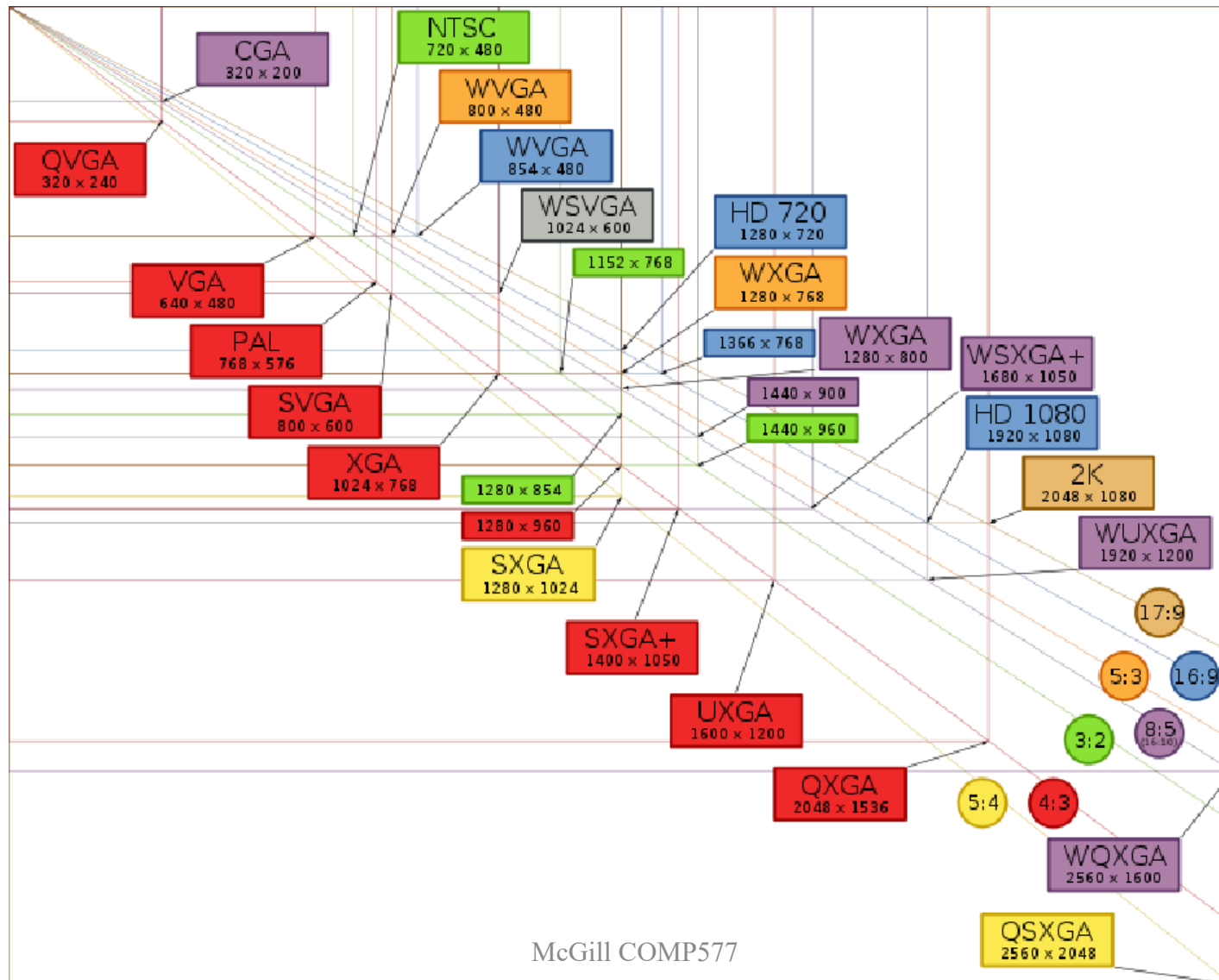
McGill COMP577

Common Resolutions



Resolutions and Aspect Ratios

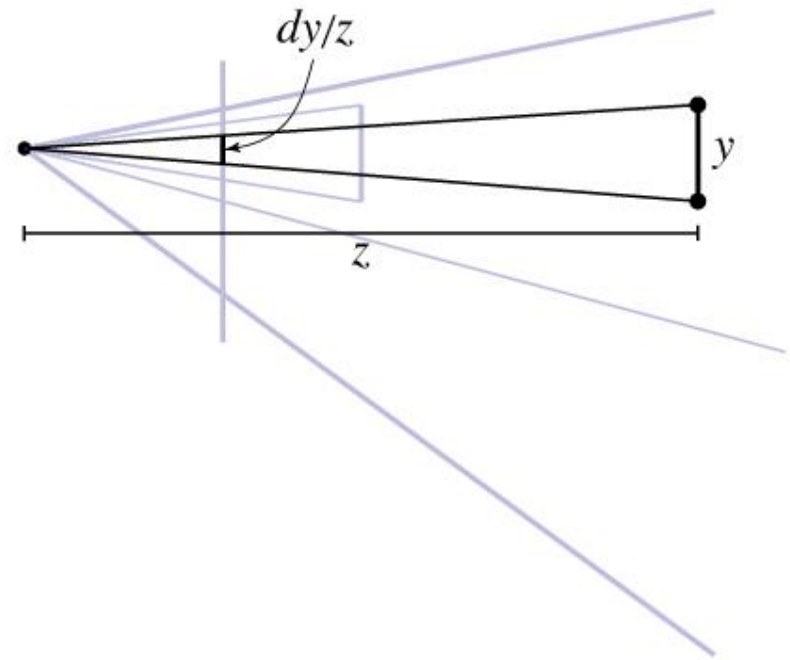
Square Pixels?



Back to projections...

Shifted perspective projection

- Perspective but with projection plane not perpendicular to view direction
 - additional parameter: projection plane normal
 - exactly equivalent to cropping out an *off-center* rectangle from a larger “normal” perspective
 - corresponds to *view camera* in photography



Why shifted perspective?

- Control convergence of parallel lines
- Standard example: architecture
 - buildings are taller than you, so you look up
 - top of building is farther away, so it looks smaller
- Solution: make projection plane parallel to facade
 - top of building is the same distance *from the projection plane*
- Same perspective effects can be achieved using post-processing
 - (though not the focus effects)
 - choice of *which* rays vs. arrangement of rays in image



camera tilted up: converging vertical lines



lens shifted up: parallel vertical lines

Specifying perspective projections

- Many ways to do this
 - common: from, at, up, v.f.o.v. (but not for shifted)
- One way:
 - viewpoint, view direction, up
 - establishes location and orientation of viewer
 - view direction is the direction of the center ray
 - image width, image height, projection distance
 - establishes size and location of image rectangle
 - image plane normal
 - can be different from view direction to get shifted perspective

Non-planar Projections...

Non-planar Projections...

(panoramas, environment maps, etc.)







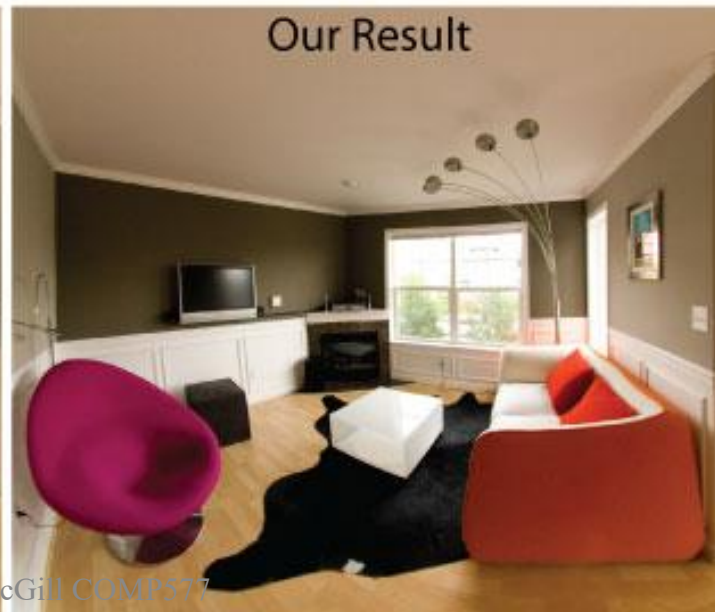






Optimizing Content-Preserving Projections for Wide-Angle Images

Robert Carroll, Maneesh Agrawala, Aseem Agarwala, SIGGRAPH 2009





Perspective



Mercator



Stereographic



Our Result



RYAN: Render Your Animation Nonlinearly Projected,
P. Coleman & K. Singh
NPAR 04

