

ADRIAN KUKLA

Qs 2.1 Activation Function

a) $g(-x) = \frac{-x}{1+|-x|} = \frac{-x}{1+|x|}$ ADRIAN KUKLA HW2 904056948 -g(x) = -x = g(-x) Hence g(x) is centered of zero. $g'(x) = \frac{1}{(1-x)^2} - 0$ The gradient indicates that it is vanishing for large values of IX

904056948 ADRIAN KUKLA HW2 Qs 3.1 Gradient Descent

Take derivative of objective function. So,

Let O(w) = 5 (w ct) + (w w w), \(\nabla \in Cw(\tau) \) + \(2 \) \(\lambda \) \(\lambda \) $\nabla_{\omega} D(\omega) = \nabla_{\beta} (\omega^{(t)}) + \lambda_{\beta} (\omega - \omega^{(t)}) = 0$ $\omega_{\beta} (\omega^{(t)}) = 0$ $\omega_{\beta} ($ Matches the gradient descentiformula for update where n= 2 The update rule corresponds to minimizing the first order taylor approximation plus an 12 proximity penalty where the gradient descent step is n = 1 learning rate in gradient descent. They're invoisely proportional

HW2 9540 56948 AURIAN KUKLA $\frac{3.2}{3.2}$ EC Prove $\frac{1}{2}$ $\frac{1}{2}$ That, when - w* 112= 11 w(+)-w*-n v+112 by definition = $|| w^{(t)} - w^{*}||^{2} - 2\eta \langle w^{(t)} - w^{*}|V_{t} \rangle + \eta^{2} ||V_{t}||^{2} ||V_{t}||^{2} ||V_{t}||^{2} - 2||V_{t}||^{2} ||V_{t}||^{2} |$ => <\w(+) -w*,v+>= 2n [11w(+)-w*112-11w(++1)-w*112]+ 2n 11v+112 $\Rightarrow \sum_{t=1}^{T} \langle w^{(t)} - w^{*} | v_{t} \rangle = 1 \sum_{t=1}^{T} (-1/-) + \frac{n}{2} \sum_{t=1}^{T} ||v_{t}||^{2}$ $=> \frac{1}{1-1} < \omega^{(1)} - \omega^{*} |V_{+}> = 1 (|V_{+}\omega^{(1)} - \omega^{*}||^{2} - |V_{+}\omega^{(1)}||^{2} + \frac{1}{N} \leq |V_{+}||^{2}$ By assumption $\omega^{(1)} = 0 \quad \forall = |V_{+}\omega^{(1)}||^{2}$ A450 11 w (T+1) ~ w* 112 >0 Hence, 11000 - w*112 - 110000 - w* 112 < 1100012 $\frac{1}{T} < \sqrt{\frac{(t)}{2\eta}} - \sqrt{\frac{1}{2\eta}} = \frac{1}{2\eta} + \frac{1}{2\eta} = \frac{1}{2\eta} = \frac{1}{2\eta} + \frac{1}{2\eta} = \frac{1}{2\eta} + \frac{1}{2\eta} = \frac{1}{2\eta} + \frac{1}{2\eta} = \frac{1}{2\eta} + \frac{1}{2\eta} = \frac{$ > Finally

904056948 ADRIAN KUKLA HW2 Q3,3 EC As f is convex we gensen's inequality where $f(\varpi x + (1-\varpi)y) \leq \varpi f(x) + (1-\varpi)f(y)$, $G \leq \varpi \leq 1$ Henre, $f(\varpi) \leq \frac{1}{2} \leq 1$ $\Rightarrow \int (\overline{\omega}) - f(w^*) \leq \frac{4}{7} \sum_{t=1}^{T} \left[f(w^{(t)}) - f(w^*) \right]$ => f(w)-f(w*) \left\ \frac{1}{7} \text{Zt=1} \left\ \w(t) - w*, \nabla f(w(t)) \right\), by first order comexity couditi / Part 1 7 Part 25 Use 3,2 Lemma Hence, T $= \frac{1}{2} \times \frac$ $\frac{B^2}{2(B/\rho F)T} = \frac{B \cdot p}{2TT} \qquad \frac{B}{B \cdot p} = \frac{B \cdot p}{B \cdot p} = \frac{B \cdot p}{2TT}$ $\Rightarrow \frac{B \cdot p}{2TT} + \frac{B \cdot p}{2TT} = \frac{B \cdot p}{2TT} \qquad \frac{B \cdot p}{TT} \qquad \frac{B \cdot$ O (TT) Convergence rate

904056928 HW2 ADRIAN KUKLA Q4 Automatic Differentiation

a) wy -> cos(wx) - (wy)

wa -> cos(wx) - (wy)

wa -> fy (wy, wx) 102 > h (·) \rightarrow $\left(\pm \right) \rightarrow \left(2 \left(\omega_{1}, \omega_{2} \right) \right)$ W1 > , Sque (.)2- [X] $\begin{cases} 1 & (1,2) > \cos(1)\cos(2) = 0.54 \times -0.416z - 0.225 \\ \sqrt{(2)} = 7 = 2 = 0.8807 \\ \sqrt{(1,2)} = -0.225 + 0.8807 = 0.656 \\ \sqrt{(1,2)} = -0.225 + 2 = 3.0986 \\ \sqrt{(1,2)} = -0.225 + 2 = 3.0986 \end{cases}$ $\frac{2}{2} \simeq \begin{cases} \frac{2}{2} (1.01,2) - \frac{1}{2} (1.2) \simeq 4.35 \\ \frac{1}{2} \simeq \frac{1}{2} (1.2,01) - \frac{1}{2} (1.2) \simeq 1.33 \\ \frac{1}{2} \simeq \frac{1}{2} (1.2,01) - \frac{1}{2} (1.2) \simeq 1.33 \end{cases}$ 0.35 -0.3 4.35 1.33 {(w)}

HW2 904056948 ADRIAN KUKLA - - sin (wy) cos (wz) = 0.35 $\frac{2l_{1}}{2l_{1}} = -\sin(\omega_{1})\cos(\omega_{2}) = 0.35$ $\frac{2l_{1}}{2l_{1}} = -\cos(\omega_{1})\sin(\omega_{2}) + \sigma(\omega_{1})(1-\sigma(\omega_{2}) = -0.34)$ $\frac{2l_{1}}{2l_{2}} = \frac{1}{\omega_{1}+\omega_{2}} + \frac{1}{2}\omega_{1}\omega_{2} = \frac{1}{4}, 33$ $\frac{\partial w_1}{\partial k_2} = \frac{1}{w_1 + w_2} = 1.33$ $\begin{array}{c|cccc}
7 & (\omega) = & 0.35 & -0.34 \\
4.33 & 1.33
\end{array}$ d) Backward mode yields the same result as the forward mode for a function f: 12 > 12 . It uses the chain rule to differentiate w. t. t. intermediate functions to derive same result $1(\omega) = \begin{bmatrix} 0.35 & -0.39 \\ 4.33 & 1.33 \end{bmatrix}$ Yes I love it -automatic differentiation eliminates manual derivative calculations.

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O 5

C) Means that CNNs are very good at analysing compute vision related tasks. So convolutions are shift equivariant and honce this means that convolutional layers can detect features independent of their position in spatial or time space. This avoids redundant parameter learning across positions,

Equivariance ensures robustness to translations which improves performance on tasks where the alignment of inputs varies like motion detection in videos or deject recognition.

ABO CNNs can reduce number of parameters compared to just a fully connected layer thanks to the shift equivariance property.

For 3 D videos 30 convolutions are used.

ADRIAN KUKLA HWZ 904056948 Q6 A1(w) = 1/2(w-2) = VA/4/w-2 Azle) = 1/2(w+1)2 >> VAzle)= w+1 when word - n V [sampled term] Aple) where moves in direction - (16-2)
Aple) where moves in director - (6+1) Select W=0 Select w=0At at w=0 $V_{A_1}(0)=-2$ Evaluate $\int (2n) < \int (0)$ $\int (2n)=\int (2n) + 2\pi$ $\int (2n)=\int (2n) + 2\pi$ $\int (2n)=\int (2n)=\int (2n) + 2\pi$ Hence $\int (2n) < \int (0)$ hence $\int (2n) < \int (0)$ hence $\int (2n) < \int (0)$ hence A2 at w=0 \(\nabla_2(0) = 1 at w > 0 $v \neq 2 = 0$ $v \neq 0$ vHence for w=0 if Az is sampled the next iterations will increase the overall function of. SGD is NOT quaranteed to decrease overall loss function. Hane.

Adrian Kukla

CS7643 HW2

Question 7

a)

Key contributions

Paper shows that deep neural networks can perfectly fit random labels.

Shows that explicit regularization like dropout or weight decay are neither necessary nor sufficient for explaining generalization. The paper suggests that is it <u>not</u> likely that regularization techniques are the main reason for generalization.

Shows that any depth 2-layer networks of linear size with ReLU activations can represent any labelling of the training data (any function) which shows that deep neural nets have very high capacity for learning.

Shows that SGD implicitly regularizes solutions which leads to generalization. SGD even with unchanged parameters can optimize weights to fit random patterns perfectly even when there is no relationship between labels and the associated images.

Strengths

Authors of the paper refer to works of multiple other authors/papers to provide some context.

Work of authors challenges conventional wisdom rather than conforming to the status quo – which can spur more research and innovations.

Study does conduct robust experiments on a number of different types of neural nets with and without regularization to evaluate their hypothesis. Combines empirical findings with ground neural network theory.

Weaknesses

No explanation about why some networks generalize better than others.

Doesn't offer any solutions or techniques to improve understanding of generalization.

Doesn't offer alternatives to classical and established measures.

b)

Personal takeaways

My understanding was that overfitting tends to occur when number of parameters is higher than number of samples – however this paper provides a counter to my previous understanding. Moreover, I thought that explicit regularization techniques like dropout or weight decay is necessary for generalization, whereas the paper shows that they're not. Changing the model architecture appropriately can vastly improve generalization without use of explicit regularization terms.

Interesting that the paper ruled out common measures like VC dimensions, Rademacher complexity as potential explanations for generalization performance. The paper suggests that

new theoretical frameworks should be explored which are outside of the commonly accepted measures.

Moreover, potential future research would be to evaluate what common properties of models that were trained by SGD to analyse how these models generalize well without the need for explicit regularization.