

Session 6.3

13) $2(n!)^2$

For each place $2k$, there are $n-2k$ women to choose from. For each $2k-1$ there are $n-(2k-1)$ men to choose from. This gives a total of $(n!)^2$ possibilities. Since we can order women and men on both (even, odd) and (odd, even), we have a total $2(n!)^2$ permutations.

34) ~~$C(15, 4) \cdot C(26, 2)$~~

$$C(15, 4) \cdot C(21, 2) = \frac{15 \cdot 14 \cdot 13 \cdot 12}{4!} \cdot \frac{21 \cdot 20}{2} = \frac{1365}{1} \cdot 210 = 286650$$

First we pick 4 women to ensure the criteria is met. Then we pick the remaining two members from the pool.

Session 6.4

4) $\frac{13!}{8!5!} = 1287$

$$\begin{aligned} 9) (2x + (-3y))^{200} &= \sum_{j=0}^{200} \binom{200}{j} 2x^{200-j} \cdot (-3y)^j \\ &\Rightarrow \binom{200}{99} \cdot 2^{101} \cdot (-3)^{99} \\ &= \frac{200!}{101!99!} \cdot 2^{101} \cdot 3^{99} \end{aligned}$$

12) $\binom{11}{k}, k = 0, 1, \dots, 11$

Section 6.5

$$6) \quad 3^5 = \underline{\underline{243}}$$

$$14) \quad x_1 + x_2 + x_3 + x_4 = 17$$



$$\binom{17+2}{4-1} = \binom{19}{3} = \frac{19!}{3!16!} = \frac{19 \cdot 18 \cdot 17}{6}$$

$$= \underline{\underline{969}}$$

30)

$$n = 11$$

$$n_1 = 1$$

$$n_2 = 4$$

$$n_3 = 4$$

$$n_4 = 2$$

$$p = \frac{11!}{1!4!4!2!} = \frac{11!}{24 \cdot 24 \cdot 2} = \underline{\underline{34650}}$$

54)

$$\left. \begin{array}{ccc} 5 & 0 & 0 \\ 4 & 1 & 0 \\ 3 & 1 & 1 \\ 3 & 2 & 0 \\ 2 & 2 & 1 \end{array} \right\} \underline{\underline{5}}$$

Section 6.6

$$5a) \quad \underline{\underline{2134}}$$

$$5b) \quad \underline{\underline{12534}}$$