CSE 12 — Basic Data Structures and Object-Oriented Design Lecture 13

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Announcements

- Quiz 13 due Monday @ 8am
- Survey 5 due tonight @ 11:59pm
- PA5 due Wednesday @ 11:59pm

Topics

Guich

- Partition/Sort
- Questions on Lecture 13?

Quicksort: Another magical (recursive) algorithm

https://www.youtube.com/watch?v=ywWBy6J5gz8

	14	4	9	12	15	8	19	2
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Select a **pivot** element:

14	4	9	(12)	15	8	19	2

"Partition" the elements in the array (smaller or equal to pivot, larger or equal to pivot)

2	4	9	8	15	12	19	14
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Magically sort the smaller elements and the larger elements (Quicksort)

```
Partition (numbers, lowIndex, highIndex)
Quicksort (numbers, lowIndex, highIndex) {
                                                                  // Pick middle element as pivot
   if (lowIndex >= highIndex) {
                                                               midpoint = lowIndex + (highIndex - lowIndex) / 2
      return
                                                                  pivot = numbers[midpoint]
                                                                  done = false
   lowEndIndex = Partition(numbers, lowIndex, highIndex)
                                                                  while (!done) {
   Quicksort (numbers, lowIndex, lowEndIndex)
                                                                     // Increment lowIndex while numbers[lowIndex] < pivot
   Quicksort(numbers, lowEndIndex + 1, highIndex)
                                                                     while (numbers[lowIndex] < pivot) {
                                                                        lowIndex += 1
                                                                     // Decrement highIndex while pivot < numbers[highIndex]</pre>
                                                                     while (pivot < numbers[highIndex]) {
                                                                        highIndex -= 1
                                                                     // If zero or one elements remain, then all numbers are
                                                                     // partitioned. Return highIndex.
                                                                     if (lowIndex >= highIndex) {
       There are many ways to partition!
                                                                        done = true
                                                                     else {
                                                                        // Swap numbers[lowIndex] and numbers[highIndex]
                                                                        temp = numbers[lowIndex]
                                                                        numbers[lowIndex] = numbers[highIndex]
                                                                        numbers[highIndex] = temp
                                                                        // Update lowIndex and highIndex
                                                                        lowIndex += 1
                                                                        highIndex -= 1
                                                                  return highIndex
```

```
Quick sort
sort {12, 4, 9, 3, 15, 8, 19, 2}
bu INder = 0
high INdex = 7
midpoint = 3
pivot = 3
```

```
// Pick middle element as pivot
midpoint = lowIndex + (highIndex - lowIndex) / 2
pivot = numbers[midpoint]
done = false
while (!done) {
   // Increment lowIndex while numbers[lowIndex] < pivot
   while (numbers[lowIndex] < pivot) {</pre>
      lowIndex += 1
   // Decrement highIndex while pivot < numbers[highIndex]</pre>
   while (pivot < numbers[highIndex]) {
      highIndex -= 1
   // If zero or one elements remain, then all numbers are
   // partitioned. Return highIndex.
   if (lowIndex >= highIndex) {
      done = true
   else {
      // Swap numbers[lowIndex] and numbers[highIndex]
      temp = numbers[lowIndex]
      numbers[lowIndex] = numbers[highIndex]
      numbers[highIndex] = temp
      // Update lowIndex and highIndex
      lowIndex += 1
      highIndex -= 1
return highIndex
```

Partition (numbers, lowIndex, highIndex) {

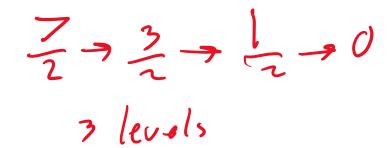
Quick Sort Details

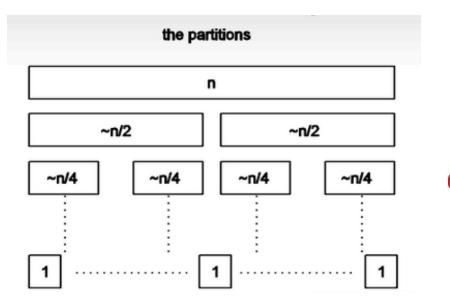
- 1. We always pick the middle location as pivot
- 2. The data we sort is {2, 3, 1, 5, 4, 6, 7}

After the first split, what is the order of elements in the list that was <= pivot?

- **5** A. 1234
- B. 2314
- C. 4321
- D. 3412
- **2** E. None of the above

Quick Sort: Using a "good" pivot





How many levels will there be if you choose a pivot that divides the list in

half?

A. 1

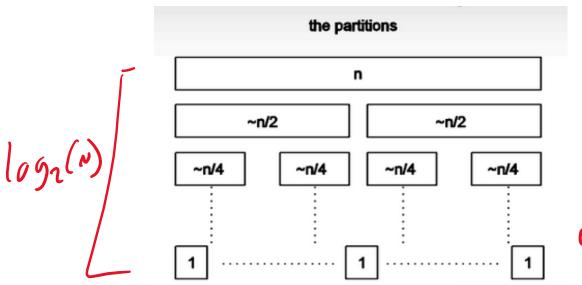
B. log(N)

C. N

N*log(N)

 $E. N^2$

Quick Sort: Using a "good" pivot



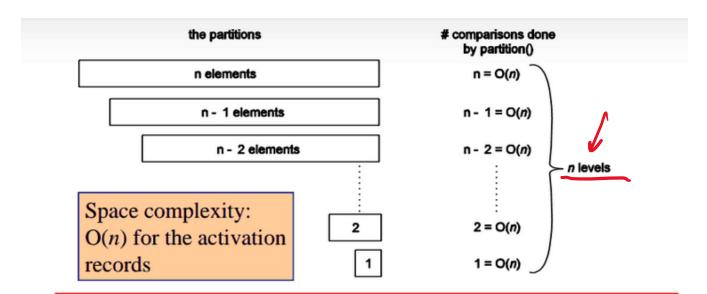
If the time to partition on each level takes N comparisons, how long does Quicksort take with a good partition?

- A. O(1)
- B. O(log(N))
- C. O(N)
- D.) O(N*log(N))
- E. $O(N^2)$

Which of these choices would be the *worst* choice for the pivot?

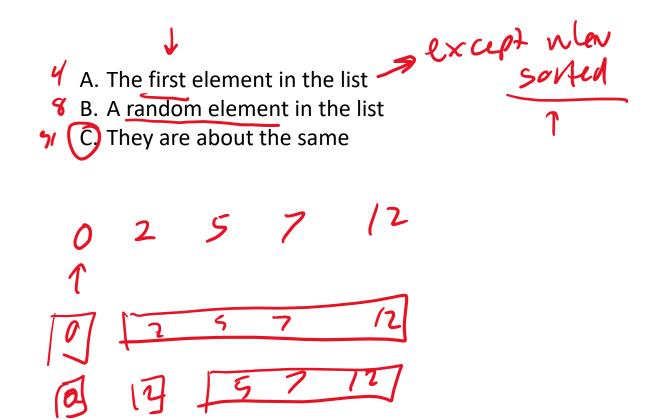
MUK The minimum element in the list B. The last element in the list C. The first element in the list D. A random element in the list

Quick sort with a bad pivot



If the pivot always produces one empty partition and one with n-1 elements, there will be n levels, each of which requires O(n) comparisons: $O(n^2)$ time complexity

Which of these choices is a better choice for the pivot?



QuickSort – Draw the picture of sort()

```
public class Sort {
public static void swap(String[] array, int i1, int i2) {
  String temp = array[i1];
  array[i1] = array[i2];
  array[i2] = temp;
 public static int partition(String[] array, int low, int high) {
  int pivotStartIndex = high - 1;
  String pivot = array[pivotStartIndex];
  int smallerBefore = low, largerAfter = high - 2;
  while (smallerBefore <= largerAfter) {
   if (array[smallerBefore].compareTo(pivot) < 0) {
    smallerBefore += 1:
   else {
    swap(array, smallerBefore, largerAfter);
    largerAfter -= 1:
  swap(array, smallerBefore, pivotStartIndex);
  return smallerBefore:
```

```
public static void qsort(String[] array, int low, int high) {
  if (high - low \leq 1) { return; }
  int splitAt = partition(array, low, high);
  qsort(array, low, splitAt);
  qsort(array, splitAt + 1, high);
 public static void sort(String∏array) {
  qsort(array, 0, array.length);
main() {
 String[] str = \{"f", "b", "a", "e", "d", "c" \};
 int | result = Sort.sort(str);
 System.out.println(Arrays.deepToString(result));
```