

CSE 12 – Basic Data Structures and Object-Oriented Design

Lecture 17

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Topics

- Questions on Lecture 17?
- Linear Probing

Hash Table – draw the picture (Separate Chaining)

N : # of elements hashed in the table
 M : size of table

```
int getIndex(String k) {  
    return k.length;  
}
```

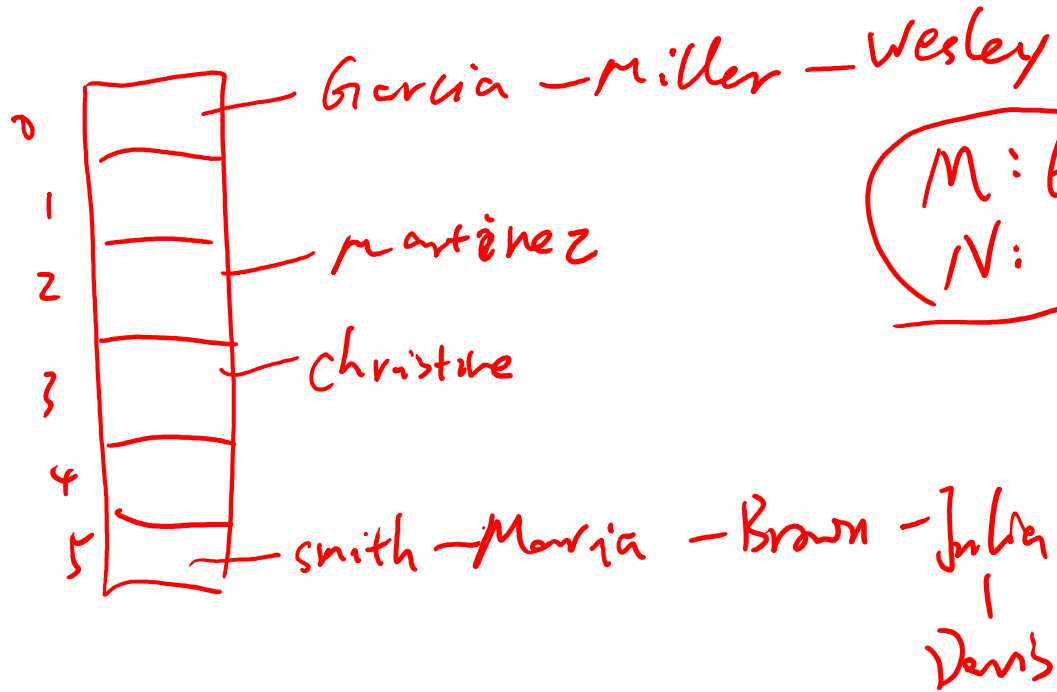
$$\frac{N}{M}$$

load factor

of buckets – 6

(i.e. the size of the array)

```
set("Smith", 1);  
set("Maria", 2);  
set("Christine", 3);  
set("Brown", 4);  
set("Julia", 5);  
set("Garcia", 6);  
set("Miller", 7);  
set("Davis", 8);  
set("Wesley", 9);  
set("Martinez", 10);
```



```
int getIndex(String k) {
    return k.length;
}
```

load $\alpha = 1.67$

```
set("Smith", 1);
set("Maria", 2);
set("Christine", 3);
set("Brown", 4);
set("Julia", 5);
set("Garcia", 6);
set("Miller", 7);
set("Davis", 8);
set("Wesley", 9);
set("Martinez", 10);
```

Hash Table – draw the picture (Separate Chaining)

```
int getIndex(String k) {  
    return k.length;  
}
```

of buckets – 4

(i.e. the size of the array)

expandCapacity() called in **set()**

LoadFactor – 2

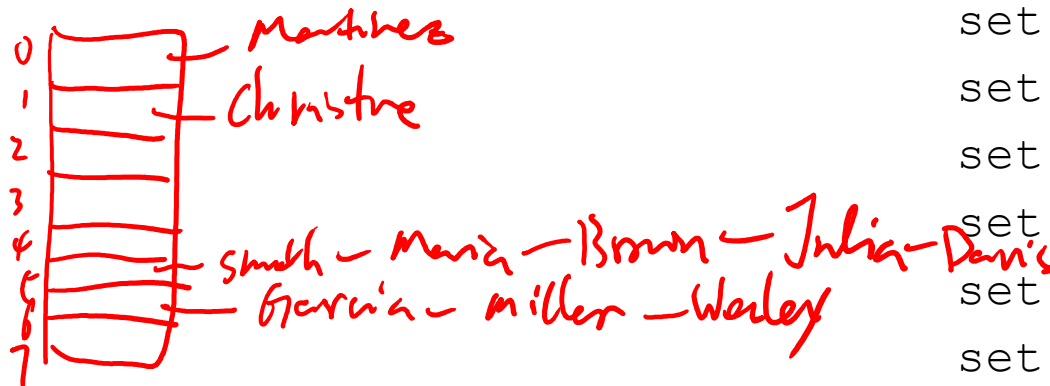
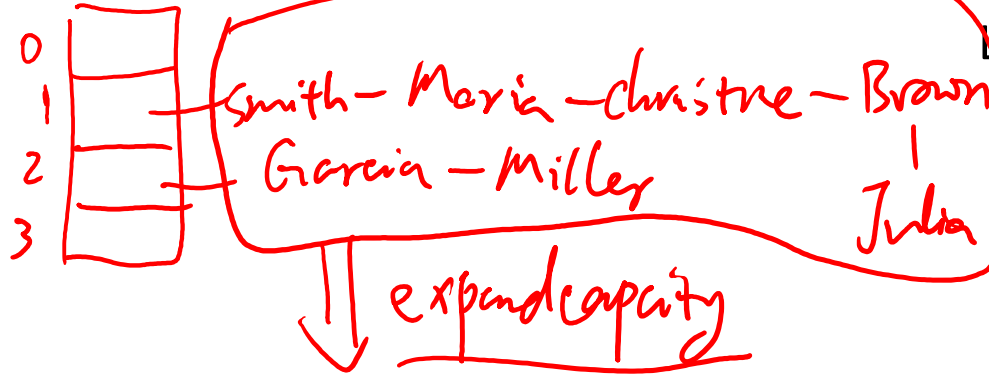
```
set("Smith", 1);  
set("Maria", 2);  
set("Christine", 3);  
set("Brown", 4);  
set("Julia", 5);  
set("Garcia", 6);  
set("Miller", 7);  
set("Davis", 8);  
set("Wesley", 9);  
set("Martinez", 10);
```

```
int getIndex(String k) {
    return k.length;
}
```

of buckets = 4

loadFactor = 2

very bad



```
set("Smith", 1);
set("Maria", 2);
set("Christine", 3);
set("Brown", 4);
set("Julia", 5);
set("Garcia", 6);
set("Miller", 7);
set("Davis", 8);
set("Wesley", 9);
set("Martinez", 10);
```

Hash Table – draw the pictures (Linear Probing)

```
int getIndex(String k) {  
    return k.length();  
}
```

of buckets – 4

(i.e. the size of the array)

expandCapacity() called in set()

LoadFactor – .75

```
set("Smith", 1);  
set("Maria", 2);  
set("Christine", 3);  
set("Brown", 4);  
set("Julia", 5);  
set("Garcia", 6);  
set("Miller", 7);  
set("Davis", 8);  
set("Wesley", 9);  
set("Martinez", 10);
```

0	
1	Smith
2	Maria
3	

0	Julia	
1	Christine	
2		
3		
4		
5	Smith	←
6	Maria	←
7	Brown	

Caching

0	
1	
2	
3	
4	
5	Julia
6	Smith
7	Maria
8	Christine
9	Christine
10	Garcia
11	Miller
12	Davis
13	Wesley
14	Martinez
15	

```

int getIndex(String k) { Search
    return k.length();
}
    
```

Search (Brown) / delete (Brown)
Search (Garcia)


of buckets - 4

expandCapacity() called in set()

LoadFactor .75

set("Smith", 1);
 set("Maria", 2);
 set("Christine", 3);
 set("Brown", 4);
 set("Julia", 5);
 set("Garcia", 6);
 set("Miller", 7);
 set("Davis", 8);
 set("Wesley", 9);
 set("Martinez", 10);

linear probing
creates cluster



Amortized analysis *∴ for worst case analysis*

- Reasoning: worst case scenario analysis assumes that worst case input happens all the time but it may not be true.
- Approach: Assume worst case but look at the whole picture

Example: insert into the end of arrays

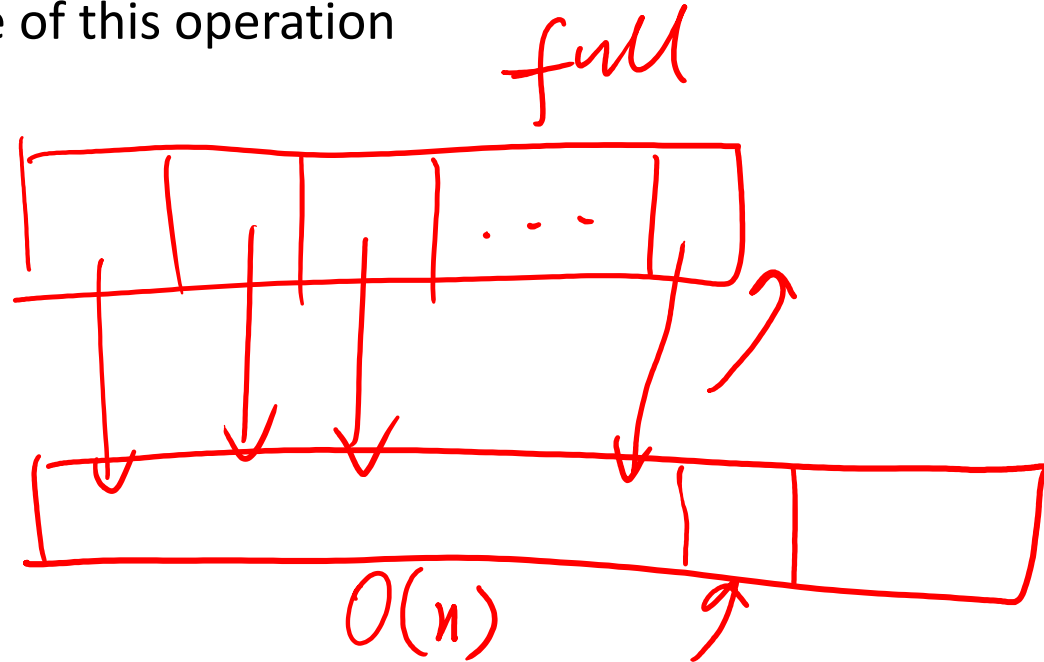
What is the worst case runtime of this operation

A: $O(1)$

B: $O(n)$

C: $O(\log n)$

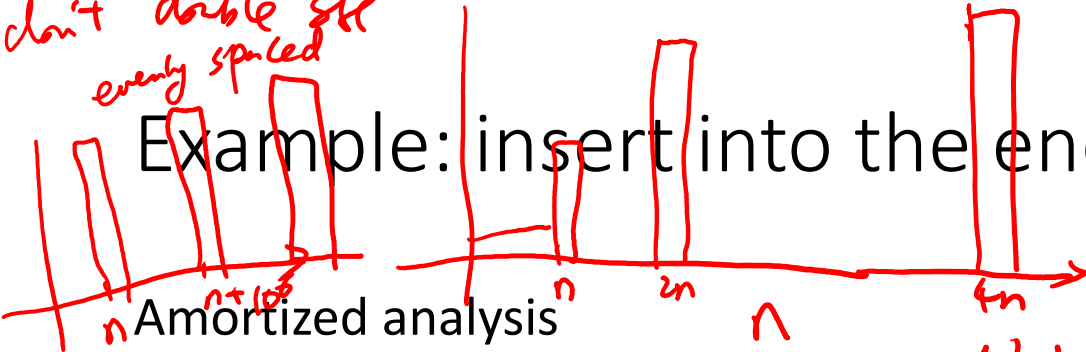
D: I forgot what O is....



don't double size
evenly spaced

Example: insert into the end of arrays

$$2n+2-1$$



$$\text{cost} \rightarrow \frac{n + (n+1)}{2}$$



empty

all the actions that leads to worst case

$$= \frac{(n+1)^2}{2} - \frac{1}{n+1}$$

① insert or delete



1

② - - - -



1

⋮

③ $\frac{n}{2}$ $\frac{n+1}{2}$



1



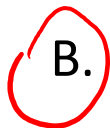
n+1



Hashing - insert

If we insert an element in the hash table, what is the worst case runtime? We consider expanding capacity and rehashing after load factor is reached.

A. $O(1)$

 B. $O(n)$

C. $O(\log n)$

Hashing - insert

If we insert an element in the hash table, what is the worst case runtime? We consider expanding capacity and rehashing after load factor is reached.

- A. $O(1)$
- B. $O(n)$
- C. $O(\log n)$

Would separate chaining or linear probing matter?

- A. Yes
- ☒ B. No

Amortized analysis of Hashing - insert



We assume that we double the size of table when we rehash. What is the amortized analysis result?

