

CSE 12 – Basic Data Structures and Object-Oriented Design

Lecture 13

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Announcements

- Quiz 13 due Wednesday @ 9am
- Survey 5 due Friday @ 11:59pm
- PA4 due Wednesday @ 11:59pm

Topics

- Partition/Sort
- Questions on Lecture 13?

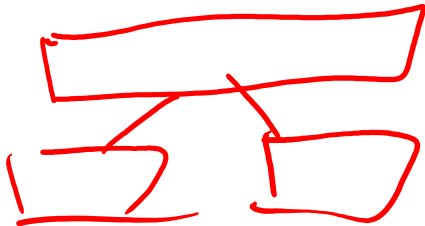
```

public class SortFast {

    public static String s(int[] arr) { return Arrays.toString(arr); }

    public static int[] combine(int[] part1, int[] part2) {
        int index1 = 0, index2 = 0;
        int[] combined = new int[part1.length + part2.length];
        while(index1 < part1.length && index2 < part2.length) {
            if(part1[index1] < part2[index2]) {
                combined[index1 + index2] = part1[index1];
                index1 += 1;
            }
            else {
                combined[index1 + index2] = part2[index2];
                index2 += 1;
            }
        }
        while(index1 < part1.length) {
            combined[index1 + index2] = part1[index1]; index1 += 1;
        }
        while(index2 < part2.length) {
            combined[index1 + index2] = part2[index2]; index2 += 1;
        }
        System.out.println(s(part1) + " + " + s(part2) + " -> " + s(combined));
        return combined;
    }
}

```



```

public static int[] sortC(int[] arr) {
    if(arr.length <= 1) { return arr; }
    else {
        int[] part1 = Arrays.copyOfRange(arr, 0, arr.length / 2);
        int[] part2 = Arrays.copyOfRange(arr, arr.length / 2, arr.length);

        System.out.println(s(arr) + " -> " + s(part1) + " + " + s(part2));

        int[] sortedPart1 = sortC(part1);
        int[] sortedPart2 = sortC(part2);

        int[] sorted = combine(sortedPart1, sortedPart2);

        return sorted;
    }
}

```

```

public static void main(String[] args) {
    int[] result = SortFast.sortC(new int[] {34, 93, 12, 49, 69, 25, 39});
    System.out.println(SortFast.s(result));
}

```

$[34, 93, 12, 49, 69, 25, 39] \rightarrow [34, 93, 12] + [49, 69, 25, 39]$

$[34, 93, 12] \rightarrow [34] + [93, 12]$

$[93, 12] \rightarrow [93] + [12]$

$[93] + [12] \rightarrow [12, 93]$

$[34] + [12, 93] \rightarrow [12, 34, 93]$

Quicksort: Another magical (recursive) algorithm

<https://www.youtube.com/watch?v=ywWBy6J5gz8>

14	4	9	12	15	8	19	2
----	---	---	----	----	---	----	---

Select a **pivot** element:

14	4	9	12	15	8	19	2
----	---	---	----	----	---	----	---

“Partition” the elements in the array (**smaller or equal to pivot**, larger or equal to pivot)

2	4	9	8	15	12	19	14
---	---	---	---	----	----	----	----

Magically sort the smaller elements and the larger elements (Quicksort)

2	4	8	9	12	15	19	21
---	---	---	---	----	----	----	----

```

Quicksort(numbers, lowIndex, highIndex) {
    if (lowIndex >= highIndex) {
        return
    }

    lowEndIndex = Partition(numbers, lowIndex, highIndex)
    Quicksort(numbers, lowIndex, lowEndIndex)
    Quicksort(numbers, lowEndIndex + 1, highIndex)
}

```

There are many ways to partition!

```

Partition(numbers, lowIndex, highIndex) {
    // Pick middle element as pivot
    midpoint = lowIndex + (highIndex - lowIndex) / 2
    pivot = numbers[midpoint]

    done = false
    while (!done) {
        // Increment lowIndex while numbers[lowIndex] < pivot
        while (numbers[lowIndex] < pivot) {
            lowIndex += 1
        }

        // Decrement highIndex while pivot < numbers[highIndex]
        while (pivot < numbers[highIndex]) {
            highIndex -= 1
        }

        // If zero or one elements remain, then all numbers are
        // partitioned. Return highIndex.
        if (lowIndex >= highIndex) {
            done = true
        }
        else {
            // Swap numbers[lowIndex] and numbers[highIndex]
            temp = numbers[lowIndex]
            numbers[lowIndex] = numbers[highIndex]
            numbers[highIndex] = temp

            // Update lowIndex and highIndex
            lowIndex += 1
            highIndex -= 1
        }
    }

    return highIndex
}

```

avoid overflow

Quick sort

0 1 2 3 4 5 6 7
sort {12, 4, 9, 3, 15, 8, 19, 2}
low high

length : 8

pivot : 3

2, 4, 9, 3, 15, 8, 19, 12

↑ low high

2, 3, 9, 4, 15, 8, 19, 12

high

↑ low

return 1

```
Partition(numbers, 0lowIndex, 7highIndex) {  
    // Pick middle element as pivot  
    midpoint = lowIndex + (highIndex - lowIndex) / 2  
    pivot = numbers[midpoint]  
  
    done = false  
    while (!done) {  
        // Increment lowIndex while numbers[lowIndex] < pivot  
        while (numbers[lowIndex] < pivot) {  
            lowIndex += 1  
        }  
  
        // Decrement highIndex while pivot < numbers[highIndex]  
        while (pivot < numbers[highIndex]) {  
            highIndex -= 1  
        }  
  
        // If zero or one elements remain, then all numbers are  
        // partitioned. Return highIndex.  
        if (lowIndex >= highIndex) {  
            done = true  
        }  
        else {  
            // Swap numbers[lowIndex] and numbers[highIndex]  
            temp = numbers[lowIndex]  
            numbers[lowIndex] = numbers[highIndex]  
            numbers[highIndex] = temp  
  
            // Update lowIndex and highIndex  
            lowIndex += 1  
            highIndex -= 1  
        }  
    }  
  
    return highIndex  
}
```

Quick Sort Details

1. We always pick the middle location as pivot
2. The data we sort is {2, 3, 1, 5, 4, 6, 7}

After the first split, what is the order of elements in the list that was \leq pivot?

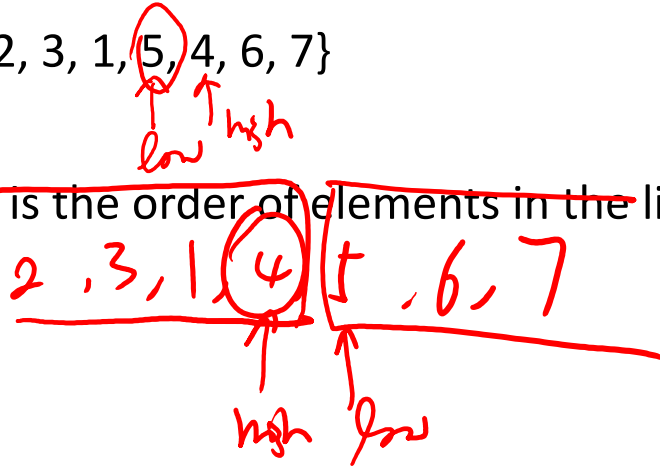
A. 1 2 3 4

B. 2 3 1 4

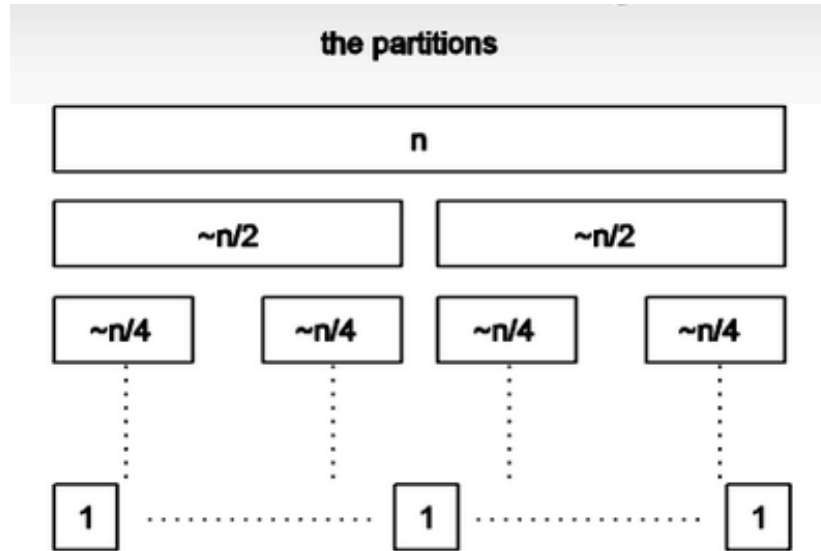
C. 4 3 2 1

D. 3 4 1 2

E. None of the above



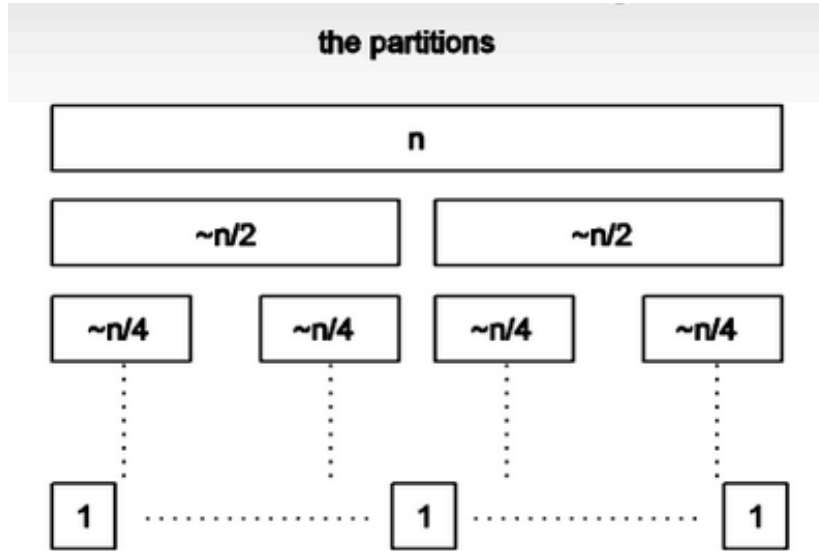
Quick Sort: Using a “good” pivot



How many levels will there be if you choose a pivot that divides the list in half?

- A. 1
- B. $\log(N)$
- C. N
- D. $N \cdot \log(N)$
- E. N^2

Quick Sort: Using a “good” pivot



If the time to partition on each level takes N comparisons, how long does Quicksort take with a good partition?

- A. $O(1)$
- B. $O(\log(N))$
- C. $O(N)$
- D. $O(N \cdot \log(N))$**
- E. $O(N^2)$

Which of these choices would be the *worst* choice for the pivot?

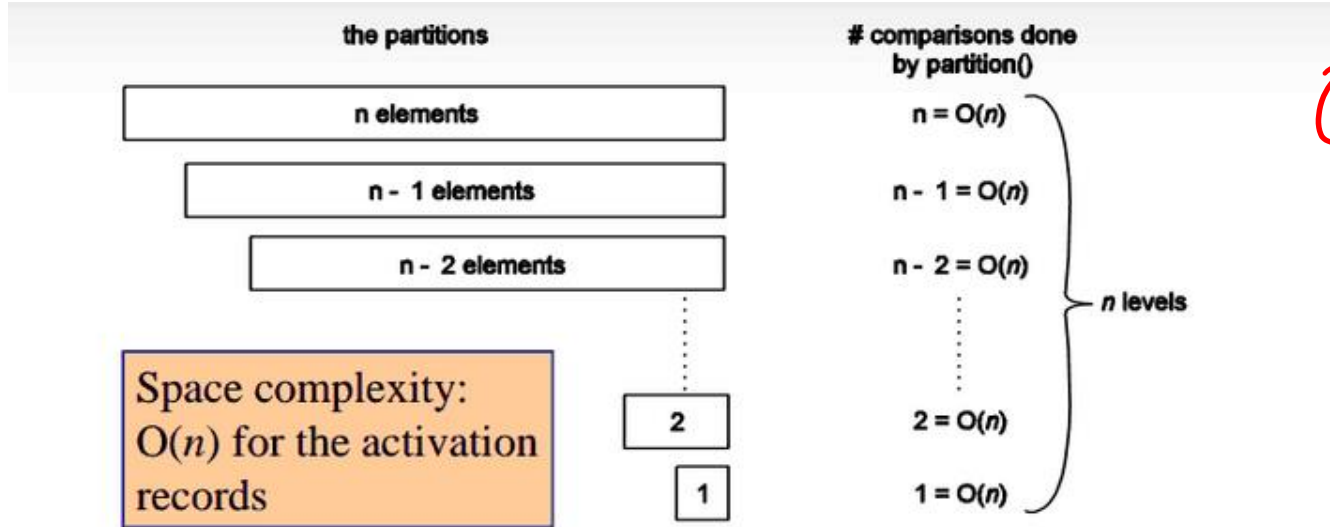
- A. The minimum element in the list
- B. The last element in the list
- C. The first element in the list
- D. A random element in the list

2, 3, 1, 4, 5, 7, 6

1 2 3 . . .

2 7, 3 . . . 6

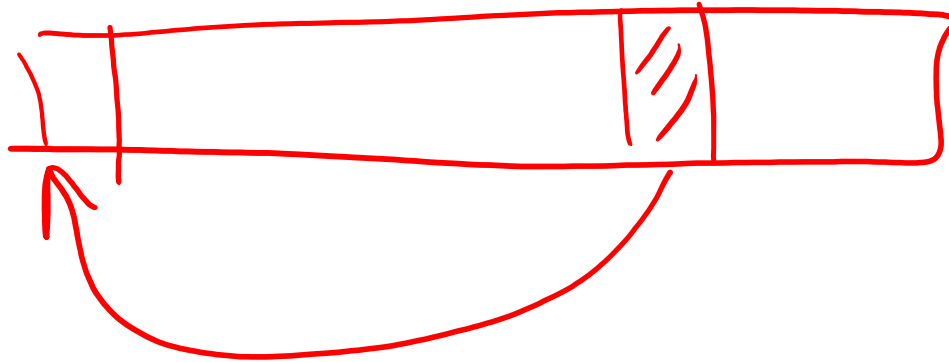
Quick sort with a bad pivot



If the pivot always produces one empty partition and one with $n - 1$ elements, there will be n levels, each of which requires $O(n)$ comparisons: $O(n^2)$ time complexity

Which of these choices is a better choice for the pivot?

- A. The first element in the list
- ☒ B. A random element in the list (avoid worst-case)
- C. They are about the same



```
public class Sort {  
    public static void swap(String[] array, int i1, int i2) {  
        String temp = array[i1];  
        array[i1] = array[i2];  
        array[i2] = temp;  
    }  
    public static int partition(String[] array, int low, int high){  
        int pivotStartIndex = high - 1 random loc;  
        String pivot = array[pivotStartIndex];  
        int smallerBefore = low, largerAfter = high - 2;  
  
        while (smallerBefore <= largerAfter) {  
            if (array[smallerBefore].compareTo(pivot) < 0) {  
                smallerBefore += 1;  
            }  
            else {  
                swap(array, smallerBefore, largerAfter);  
                largerAfter -= 1;  
            }  
        }  
  
        swap(array, smallerBefore, pivotStartIndex);  
        return smallerBefore;  
    }  
}  
  
    public static void qsort(String[] array, int low, int high) {  
        if (high - low <= 1) { return; }  
        int splitAt = partition(array, low, high);  
        qsort(array, low, splitAt);  
        qsort(array, splitAt + 1, high);  
    }  
  
    public static void sort(String[] array) {  
        qsort(array, 0, array.length);  
    }  
  
    main() {  
        String[] str = {"f", "b", "a", "e", "d", "c"};  
        int[] result = Sort.sort(str);  
        System.out.println(Arrays.deepToString(result));  
    }
```