

# CSE 12 – Basic Data Structures and Object-Oriented Design

## Lecture 10

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# Announcements

- Quiz 10 due Monday @ 8am
- Survey 4 due Friday @ 11:59pm
- PA3 due tonight @ 11:59pm
- Exam 1 on Friday (no class)
  - Released @ 8am on Friday
  - Closes @ 10am on Saturday
  - More details on Piazza

} 26 hour

↳ 60 minutes  
↳ no make ups

Lectures  
→ 1-8

# Topics

- Questions on Lecture 10?
- Big O

Questions on Lecture 10?

Let  $f(n) = 100$

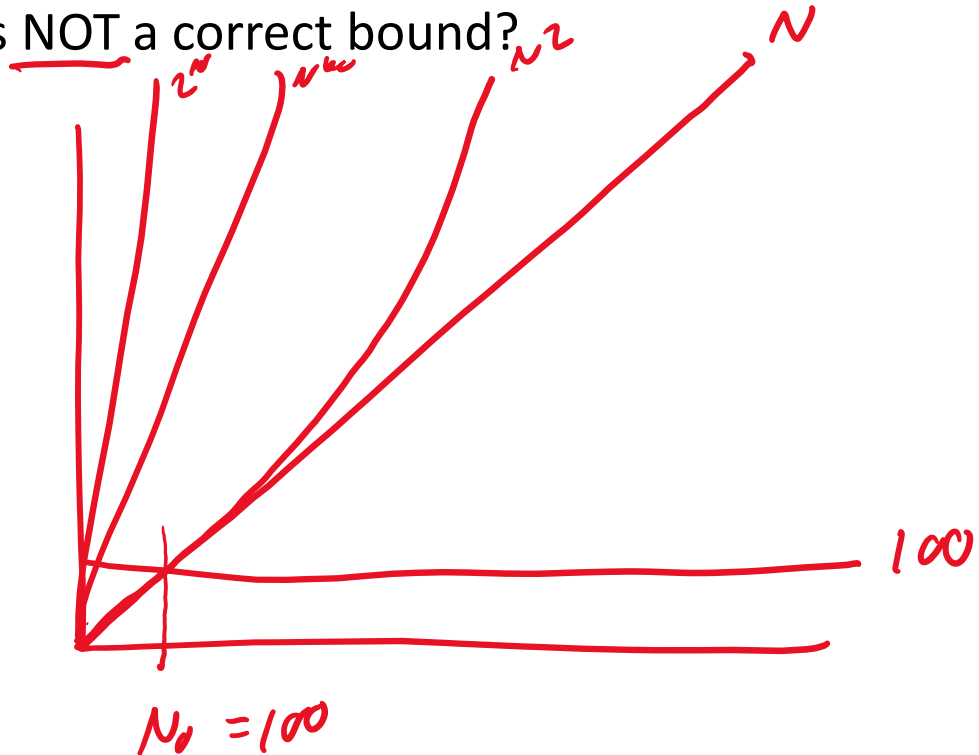
$$f(n) \leq c + g(n)$$

$N_0$

$O(f(n))$

- Which of the following is NOT a correct bound?

- 4 A.  $f(n)$  is  $O(2^n)$
- 0 B.  $f(n)$  is  $O(n^2)$
- 2 C.  $f(n)$  is  $O(n)$
- 4 D.  $f(n)$  is  $O(n^{100})$
- 37 **E.** None of these



For each function in the list below, it is related to the function below it by  $O$ , and the reverse is **not** true. That is,  $n$  is  $O(n^2)$  but  $n^2$  is **not**  $O(n)$ .

- $f(n) = 1/(n^2)$
- •  $f(n) = 1/n$
- •  $f(n) = 1$
- $f(n) = \log(n)$
- $f(n) = \sqrt{n}$
- •  $f(n) = n$  ✓
- •  $f(n) = n^2$  ✓
- $f(n) = n^3$  ✓
- $f(n) = n^4$
- • ... and so on for constant polynomials ...
- $f(n) = 2^n$
- $f(n) = n!$
- $f(n) = n^n$

upper bound  
 $O(f(n))$

$$f(n) \leq C \cdot g(n)$$

$n$   
 $n^2$   
 $n^3$

Let  $f(n) = 3n^3 + 2n + 7$

$\leq$

$$\frac{3n^3 + 2n^3 + 7n^3}{12n^3}$$

• Which of the following is a correct bound?

2 ~~A.~~  $f(n)$  is  $O(\log(n))$

0 ~~B.~~  $f(n)$  is  $O(n^2)$

0 ~~C.~~  $f(n)$  is  $O(n)$

so 3 D.  $f(n)$  is  $O(n^3)$

3 E. None of these

$$\leq \frac{12}{1} + \frac{n^3}{1}$$

$$N = O^?$$

```
void printAllElementOfArray(int[] arr) {
    for (int i = 0; i < arr.length; i++) {
        printf("%d\n", arr[i]);
    }
}
```

$$\rightarrow 1 + (n+1) + n + n$$

$$P(N) = 3N + 2$$

- Which of the following is a correct bound?

$$3N + 2N = 5N$$

$$g(N) = N$$

$$C \approx 5$$

$$N_0 = 2$$

- 0 A.  $f(n)$  is  $O(\log(n))$  X
- 1 B.  $f(n)$  is  $O(n^2)$  ✓
- 20 C.  $f(n)$  is  $O(n)$  ✓
- 0 D.  $f(n)$  is  $O(n^3)$  ✓
- nb E. More than one of these



```

void printAllPossibleOrderedPairs(int arr[]) {
    for (int i = 0; i < arr.length; i++) {
        for (int j = 0; j < arr.length; j++) {
            printf("%d = %d\n", arr[i], arr[j]);
        }
    }
}

```

$$1 + (n+1) + n + \dots$$

$$N (1 + (n+1) + n + n + \dots)$$

$$2 + 2n + n(2 + 3n)$$

• Which of the following is a correct bound?

$$f(n) = 3n^2 + 2n + 2n + 2$$

1 A.  $f(n)$  is  $O(\log(n))$  X

4 B.  $f(n)$  is  $O(n^2)$  ✓

0 C.  $f(n)$  is  $O(n)$  X

2 D.  $f(n)$  is  $O(n^3)$  ✓

47 (E) More than one of these

$$C = 3 \quad g(n) = n^2$$

$$N_0 = 4$$



```

int fibonacci(int num) {
    if (num <= 1) return num;
    return fibonacci(num - 2) + fibonacci(num - 1);
}

```

*fibonacci(5)*

*↓  
15 times*

*↑  
N*

*↑  
N*

- Which of the following is a correct bound?

*2<sup>N</sup> → 32*

*35* **A.**  $f(n)$  is  $O(2^n)$

*1* B.  $f(n)$  is  $O(n^2)$  *25*

*2* C.  $f(n)$  is  $O(n)$  *5*

*2* D.  $f(n)$  is  $O(n^3)$  *125*

*4* E. More than one of these