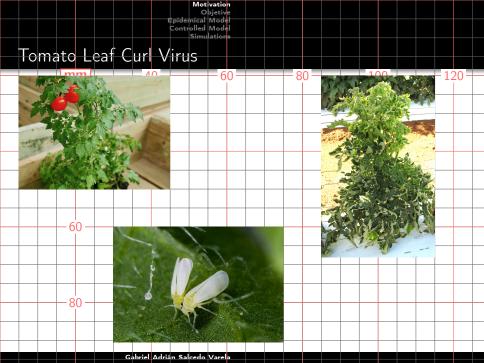
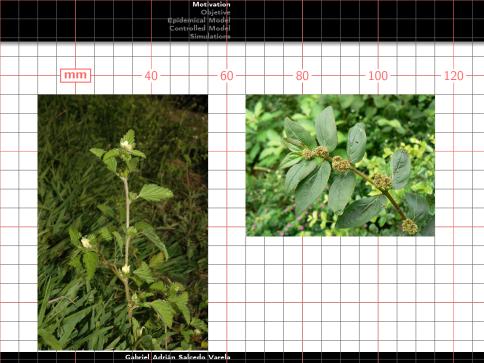
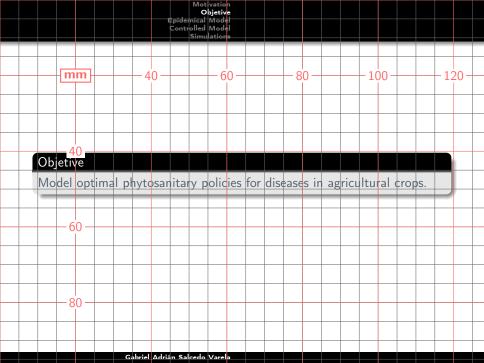
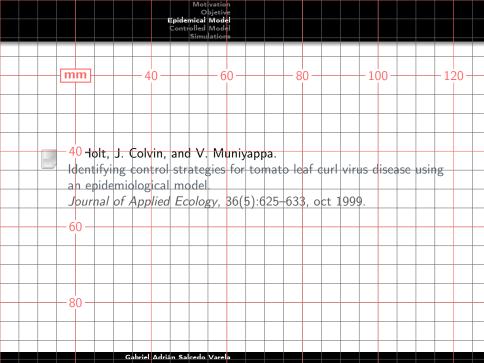


Contents    mm				Ol Epidemical Controlled Simu	ojetive Model Model ations					
1 Motivation 2 Objetive 3 Epidemical Mode 4 Controlled Model     Plant mode 5 Simulations	Со									
2 Objetive  3 Epidemical Model  4 Controlled Model  Plant model  5 Simulations		mm	40 -		- 60 <del></del>	8	80	100	120-	
3 Epidemical Model  4 Controlled Model  Plant model  5 Simulations		<b>Motivation</b>	1							
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Plant model     Simulations										
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Gábriel Adrián Salcedo Varela			Gabriel Adri	án Salcedo	Varela					



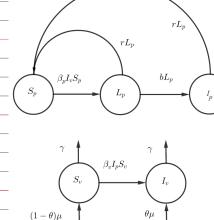








- infection by infeted plants and vectors,
- output and input for
- plants and vectors.



Motivation

Epidemical Model Controlled Mode

## Others Controls

#### **Cultural Control**

- physical barriers.
- planting dates.
- removal of
- host plant

## Biological control

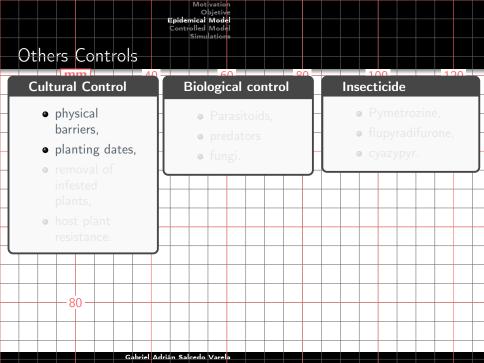
- Parasitoids.
- predators • fungi.
  - X. I. Yuan.

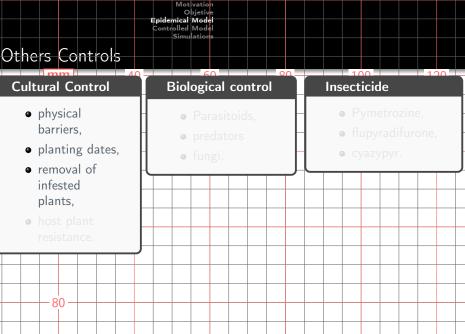
# Insecticide

60 90 100 120

- Pymetrozine,
- flupyradifurone,
- cyazypyr.
- R. E. Shun-xiang, W. A. Zhen-zhong, Q. I. Bao-li, The pest status of bemisla tabaci in china and
- non-chemical control strategies\* Insect Science, 8(3):279-288, 2001.
- H. A. Smith and M. C. Giurcanu. New Insecticides for Management of Tomato Yellow Leaf Curl, a Virus

Vectored by the Silverleaf Whitefly, Bemisla tabaci. Journal of Insect \$cience, 14(1):4-7, jan 2014.





physical

barriers.

 removal of infested plants, host plant



#### **Cultural Control**

- physical barriers,
- planting dates,
- removal of infested plants,
- host plant resistance.

## Biological control

- Parasitoids,
- predators
- fungi.

## Insecticide

- Pymetrozine,
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  - cyazypyr.

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## Others Controls

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- removal of infested plants,
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  - predators
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40

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- host plant resistance.

## Biological control

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  - predators
  - fungi.

#### Insecticide

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- flupyradifurone,
- cyazypyr.



40

## Others Controls

#### **Cultural Control**

- physical barriers.
- planting dates,
- removal of infested plants,
- host plant

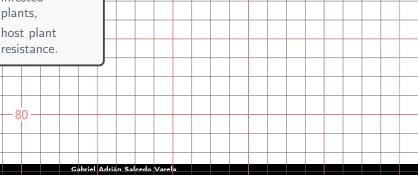
## Biological control

- Parasitoids.
  - predators
  - fungi.

#### Insecticide

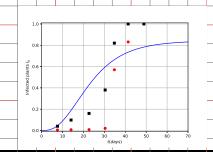
60 00 100 120

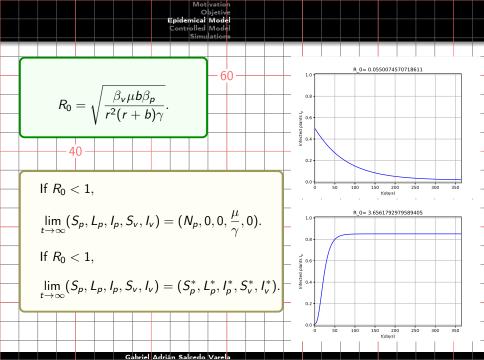
- Pymetrozine,
- flupyradifurone,
- cyazypyr.



$$\begin{split} \frac{dS_{p}}{dt} &= -\beta_{p}S_{p}I_{v} + r(L_{p} + I_{p}), \\ \frac{dL_{p}}{dt} &= \beta_{p}S_{p}I_{v} - bL_{p} - rL_{p}, \\ \frac{dI_{p}}{dt} &= bL_{p} - rI_{p}, \\ \frac{dS_{v}}{dt} &= -\beta_{v}S_{v}I_{p} - \gamma S_{v} - (1 - \theta)\mu, \\ \frac{dI_{v}}{dt} &= \beta_{v}S_{v}I_{p} - \gamma I_{v} - \theta\mu, \\ S_{p}(0) &= S_{p_{0}}, L_{p}(0) = L_{p_{0}}, I_{p}(0) = I_{p_{0}}, \\ S_{v}(0) &= S_{v_{0}}, I_{v}(0) = I_{v_{0}}. \end{split}$$

Par. Value Descrip. 0.1 plant latent rate 0.01 plant remove rate 0.075 plant infectious rate 0.06vector die or depar rate 0.3 mmigration rate nfected vectors arrival 0.003 vector infected rate





		Mot	vatio	n
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Plant model

## Plant Model with control

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$$\frac{dt}{dt}$$

$$-bL_p - (r$$

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		J(L	$_{1},$ $_{L}$	2, L	(3) =		7	$A_1I_p$	(t)	+ ,	$A_2L$	$_{p}(t)$	+	$A_3I$	$_{v}(t)$	) +	$c_1 u$	$_{1}(t)$	$)^{2} +$	- <i>c</i> <sub>2</sub>	u <sub>2</sub> (	$t)^2$	12	.0
su	bje	ct t	0			− C3	u <sub>3</sub> (	t)~	dt,															
			_ 1	   																				
			-4		$\frac{dS_p}{dt}$	=	_	$\beta_p S$	$_{p}I_{v}$	+ (	r +	$u_1$	$L_p$	+(	r+	u <sub>2</sub> )	$I_p$ ,							
					,,																			
					$\frac{dL_p}{dt}$	=	$\beta_{p}$	$S_p$	/ <sub>v</sub> –	bL	p —	(r	+ <i>u</i>	<sub>1</sub> )L	ο,									
			6		dI				,															
			<del></del> 6	y-	$\frac{dI_p}{dt}$	=	bL	-p <sup>—</sup>	- (r	+ 1	12)1	p,												
					$dS_v$	_		BS	. ,	_ (	~ _	- IIa	) 5	_ (	1 _	θ)	, ,							
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			<del>-</del> 8		$\frac{dI_v}{dt}$	=	$\beta_{\nu}$	$S_{v}$	, –	$(\gamma$	+ ι	13)[	, –	$\theta\mu$ ,										
			_ 0	П																				
				Ţ	$S_p($	0)	=	$S_{p_0}$	$, L_{p}$	,(0)		$L_{p_0}$	$I_p($	0) =	$= I_p$	<sub>o</sub> , S	$_{v}(0$	) =	$S_{v_0}$	$I_{v}$	(0)	= /	v <sub>0</sub> •	
						G	abriel	Adriá	n Sa	cedo	Vare	a												

 $T\in (0,\infty)$  be fixed. Consider the control system:

$$\begin{cases} \dot{x}(s) = f(s, u(s), x(s)) \ s \in [t_0, T], \\ x(t_0) = x_0, \end{cases}$$

with terminal state constraint  $x(T; t_0, x_0, u(\cdot)) \in M,$ 

$$1 \dots M \subset \mathbb{D}^n : C \dots$$

where  $M \subseteq \mathbb{R}^n$  is fixed.

 $M: \mathbb{R}_+ \to 2^{\mathbb{R}^n}$  is a moving target in  $\mathbb{R}^n$  if for any  $t \in \mathbb{R}_+$ , M(t) is a measurable.

del Plant model del ons

$$J(t_0,x_0;u(\cdot))=\int_{t_0}^{T}g(s,u(s),x(s))ds+h(T,x(T))\equiv J^T(t_0,x_0,u(\cdot)).$$

**Problem** 
$$(OC)^T$$

Given  $(t_0,x_0)\in\mathbb{R}_+ imes\mathbb{R}^n$  with  $ilde{\mathcal{U}}^M_{\mathbf{x_0}}[t_0,T]
eq\emptyset$ , find a  $ar{u}(\cdot)\in ilde{\mathcal{U}}^M_{\mathbf{x_0}}[t_0,T]$ 

Given 
$$(t_0,x_0)\in\mathbb{R}_+$$
 such that

$$J^{T}(t_0,x_0;\bar{u}(\cdot))=\inf_{u(\cdot)\in\tilde{\mathcal{U}}_{x_0}^{M}[t_0,T]}J^{T}(t_0,x_0;u(\cdot)).$$

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 $\omega: \mathbb{R}_+ \times \mathbb{R}_+ \to \mathbb{R}_+$  increasing, and  $\omega(r,0) = \emptyset$  for every  $r \geq 0$ .

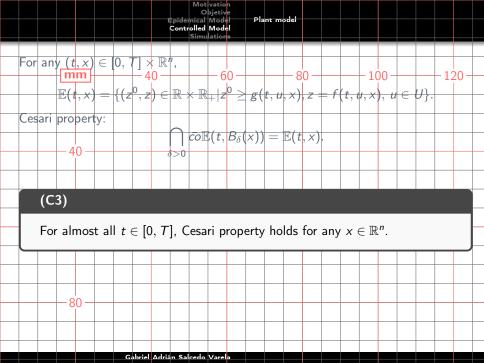
## (C1)

$$f: \mathbb{R}_+ \times U \times \mathbb{R}^n \to \mathbb{R}^n$$
 is measurable, satisfies a lipchitz condition in  $x$ , and  $|f(t, u, 0)| \leq L$ , for every  $(t, u) \in \mathbb{R}_+ \times U$ .

$$g:\mathbb{R}_+ imes U imes \mathbb{R}^n o \mathbb{R}$$
 and  $h:\mathbb{R}^n o \mathbb{R}$  are measurable, and

$$|g(s, u, x_1) - g(s, u, x_2)| + |h(x_1) - h(x_2)| \le \omega(|x_1| \vee |x_2|, |x_1 - x_2|)$$

for every  $(s,u) \in \mathbb{R}_+ \times U, x_1, x_2 \in \mathbb{R}^n$ .



#### Existence Theorem

Let (C1)-(C3) hold. Let  $M \subseteq \mathbb{R}^n$  be a non-empty closed set. Let  $(t_0, x_0) \in [0, T] \times \mathbb{R}^n$  be given and  $\tilde{\mathcal{U}}_x^M[t_0, T] \neq \emptyset$ . Then problem  $(OC)^T$  admits at least one optimal pair.



## Pontryagin's Maximum Principle

If  $u^*(t)$  and  $x^*(t)$  are optimal for the problem  $(OC)^T$ , then there exists a piecewise differentiable adjoint variable  $\lambda(t)$  such that

$$H(t,x^*(t),u(t),\lambda(t)) \leq H(t,x^*(t),u^*(t),\lambda(t))$$

for all controls u at each time t, where the Hamiltonian H is

$$H = g(t, x(t), u(t)) + \lambda(t)f(t, x(t), u(t)),$$

and

$$\lambda'(t) = -\frac{\partial H(t, x^*(t), u^*(t), \lambda(t))}{\partial x},$$
$$\lambda(T) = 0.$$

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		Ster	2.	Us	ing	the	in	tial	CO	ndit	ion	<i>X</i> <sub>1</sub>	= x	$r(t_0)$	) =	a a	nd	the	val	ues		
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