## **Bestimates**

# Final project for Math 390 Data Science at Queens College

May 24, 2019

By Adriana Sham

In collaboration with:

**Burhan Haanif** 

Diego Astudillo

Sakib Salim

Vincent Miceli

#### **Abstract**

We use sophisticated algorithms to predict the value of individual coops and condos. We contend that these estimates are far more accurate and efficient than zillow's predictions and Multiple Listing Services (mlsi).

We identify the most significant features of apartment dynamically, supplement the data set to smooth over missing data, and run our data in several algorithms that feature select, validate, and ship a model useful toward the goal of estimating future prices.

#### 1. Introduction

Machine learning is based on the study of algorithms and statistical models, using computer systems to create algorithms and statistical models to gradually improve their performance in specific tasks. The process of applying machine learning to real world problems is called predictive analysis.

In this project, a predicting model is used estimate the selling price of aparments in Queens, NY area; this project pointedly studies the condominium and coops. It utilizes the raw data listed on Multiple Listing Services, for coops and condominiums that are sold during the year of 2016 to 2017 which consists of n = 2230 (observations) and p = 55 (features).

In the model training process, it uses  $D = x_n$ ,  $y_n$  to train the predictive model, to get the *yhats* (the output). Three different algorithms are used to make a model for the sale price of the apartments: Linear, Regression Tree, and Random Forests Modeling.

Our group used Google's vitual machine to obtain better estimates, and bu doing so it allowed us to make more iterations in the algorithms.

### 2. The Data

The raw data that was utilized in tho make the model was harvested from Multiple Listing Services. The data set was harvested with MTurk and it is a raw download from their website. It is mainly zip codes from mainland Queens, leaving out the Rockaways, a peninsula near JFK airport that is geographically distinct from the rest of the neighborhoods, with a total of 55 zipcodes from Queens, NY. The raw size of the dataset is n x p which is 2230 x 55. However, some of the irrelevant features were excluded in order to improve the dataset.

The raw dataset began with 55 features and it was cut down to 25 features, because 30 of them were irrelevant. The features that were kept in the original data are:

The population of interest is the entire the coops and condos that are sold in Queens. This dataset partly represents the population of interest because this is a fairly small sample size of Queens. Certain zipcodes have just a few observations in comparison to the other zipcodes that have a larger size of obsevations.

External sources were not use in this project, but we featurization was done using the provided dataset. There are dangers of extrapolation because the prediction of this data can only predict on the zipcodes bedrrom, bathrroms, within the range provided and not outside of that and that might make extrapolation anything outside of the range of these feature. Now that out model is predicting for studios, one, two, three bedrooms home, using the same model to predict home that have over 3 bedrooms would be extrapolation. In our dataset there are outliers, for example the house that worth close to \$1M or in the total taxes that ranges from \$11 to \$9300. It does not take account on weird cases, it will predict poorly on them.

#### 2.2. Featurization

There were 55 features at the beginning and only 24 features were kept, and they are:

approx\_year\_built: interger; prewar built would be concrete walls, and brick outside, old elevators and modern ones that are built would be wood community\_district\_num: interger; determines school districts coop\_condo: factor; appartments that are either coops or condos. coops are those that have more community charges, you don't own the appartment, however, you own a stock in the cooporation that owns the building. In order to buy coops you have to be aproved by the coorperation board. Coops also have less fredom in renting or subletting. Co-ops are also cheaper then condos. In Comparison to co\_ops a person actully owns the apartment, and has the freedom to make the changes in the floor plans and almost 2x as expensive dining\_room\_type: factor; this was factorial and was combo, formal or other garage\_exists: factor; existence of garage in the coop/condo kitchen\_type: factor; the feature was factorial but we made it into two different kinds "eat in" and "efficeny" or none num\_bedrooms: interger; number of bedrroms in the coop/condo num\_floors\_in\_building: interger; number of floors in the coop/condo num\_full\_bathrooms: interger; number of full bathrooms in the coop/condo num\_total\_rooms: interger; number of total rooms in the coop/condo

parking\_charges: factor; the charge for the parking space in the coop/condo <code>pct\_tax\_deductibl</code>: interger; the percentage of reducable taxable income sq\_footage: interger; the size of the apartment by square feet total\_taxes: factor; the property tax charged by the <code>local goverment</code> walk\_score: interger; it is the walk to the nearby stores

Within the 25 features, we created more features from raw data that help facilitate the model making process, such as:

pets\_allowed: cats\_allowed and dog\_allowed were combined into one column because they are collinear. montly charges: maintenance\_cost and common\_charges are combine into one column since they are mutually exclusive. price\_persqft: using listing\_price to divide by sqr\_footage, then dropping listing\_price and sqr\_footage lat: latitude of addresses from full\_address\_or\_zip\_code. We used the package ggmap to get the coordinates from the given feature full\_address\_or\_zip\_code, then we dropped the feature after using. lon: longitude of addresses from full\_address\_or\_zip\_code. We used the package ggmap to get the coordinates from the given feature full\_address\_or\_zip\_code, then we dropped the feature after using. Distance to the closest LIRR: we used ggmap to get the latitude and longitude of each LIRR station in Queens, then we ran a code to find the nearest distance of each coop/condo to the closest LIRR station.

we featurize some of the data in accordance to how we needed it in excel and in R such as deleting the dollar sign(\$) from some columns because Rwa sreading the column as a string, then we made as numeric, another exaple would be kitchen\_type we made into eaten and efficiency, etc.

# 2.3. Errors and Missingness

The dataset was full of NAs, misspelling and wrong entries. One of them was in the parking garage exists such as "eys", "yes", "underground", "Yes", we corrected them into "yes" through excel by replacing each misspelled entry and turning NAs into "no" assuming they have no garage. There were errors in the total\_taxes entries some of the entries for the taxes were uncertain such as entries under a \$1000 dollars. There were community district numbers that were missing and we used search engine to correct each entry.

In total\_taxes, the entries that were under a \$1000 dollars we decided to make it into NA's and let missforest fill the entries because total\_taxes lower than \$1000 did not make sense. Entries that have over 1000 entries of Nas, we decided not to impute them because it would give us an arbitrary number which might worsen our prediction. And most of the columns that contains NAs we used missForest to impute the data, so that we don't drop some of the important features.

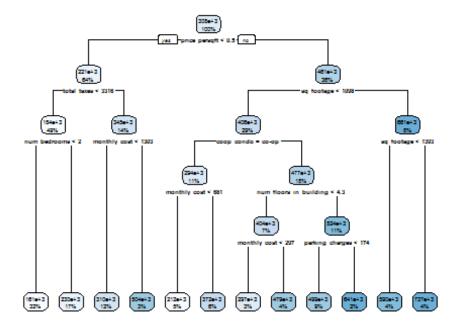
We also included a dummy matrix M, to take account of the NAs so that when running the regression the missingness would also be taken account, and see the effect on the regression line.

## 3. Modeling

Below are three different model to predict on prices. It shows which of the model gives the best result to ship to ship to the world. The dataset used n = 523 observations and the rest of the observation were dropped because they did not have the y (the output).

## 3.1 Regression Tree Modeling

The were only six variable used for spliting, they are coop/condo, sq\_footage, price\_per\_sq\_foot, parking\_charges, latitude, montly\_cost. The tree starts from the most important feature to start splitting which in this case is coop/condo because the feature that affect the price the most is coop/condo, then going down to the size of the apartment determine by sq\_footage, then by price\_per\_sq\_foot, parking\_charges, latitude, montly\_cost which is the montly maintenance charges by the apprtment.



## 3.2 Linear Modeling

We fitted a linear regression model using xs (features) and some of them were statistically signficant, which are coop\_condocondo, dining\_room\_typeformal, num\_bedrooms, num\_floors\_in\_building, num\_total\_rooms, parking\_charges, lat, monthly\_cost, price\_persqft, is\_missing\_community\_district\_num

 $R^2$  in sample = 84 is higher than out of sample, it is higher because it is prompt to overfitting. out of sample  $R^2$  = 85 is lower than in sample since since it is working with the testing set. To interpret the coefficients once we set everything in constant, once we

compare two naturally observed observations PRICE and coop/condo we can see that price will go up by \$172000 dollars. yet if we take in considerration latitude PRICE will increase to \$677900

This linear regression did well, but it could be done better using RandomForest. This is because the data is not completly linear, and therefore it is not yielding a desirable  $R^2$  and the RMSE is \$83215.95 which means that our linear model is sample estimates is plus or minus \$83215.95.

```
##
## Call:
## lm(formula = Ytrain ~ ., data = Xtrain)
##
## Residuals:
##
      Min
                1Q
                   Median
                               3Q
                                      Max
## -295653 -31899
                      2725
                             33423
                                   314214
##
## Coefficients:
                                      Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                     -3.794e+07 1.017e+07
                                                          -3.730 0.000220
## approx_year_built
                                     -3.775e+01 2.690e+02 -0.140 0.888450
## community_district_num
                                     2.001e+03 1.243e+03
                                                            1.610 0.108301
## coop_condocondo
                                     1.720e+05 1.977e+04
                                                            8.703 < 2e-16
## dining_room_typedining area
                                     1.950e+04 5.172e+04
                                                            0.377 0.706350
## dining_room_typeformal
                                     2.424e+04 9.331e+03
                                                            2.598 0.009733
## dining_room_typeother
                                     1.246e+04 1.221e+04
                                                            1.020 0.308268
## garage exists
                                     3.292e+03 1.023e+04
                                                            0.322 0.747841
## kitchen typeeat in
                                     5.448e+03
                                                1.092e+04
                                                            0.499 0.618207
## kitchen_typeefficiency
                                    -1.649e+04 1.078e+04
                                                           -1.530 0.126950
## num bedrooms
                                     3.235e+04 8.779e+03
                                                            3.685 0.000261
                                     2.363e+03 7.932e+02
                                                            2.980 0.003069
## num floors in building
## num_full_bathrooms
                                     1.706e+04
                                                5.152e+04
                                                            0.331 0.740723
## num half bathrooms
                                     2.510e+03
                                                3.594e+04
                                                            0.070 0.944363
## num_total_rooms
                                     2.179e+04
                                                5.748e+03
                                                            3.791 0.000174
## parking_charges
                                     3.950e+02 1.032e+02
                                                            3.827 0.000151
## pct tax deductibl
                                     5.616e+01 1.417e+03
                                                            0.040 0.968404
## sq_footage
                                     2.578e+01 1.316e+01
                                                            1.958 0.050927
## total_taxes
                                     7.102e+00 5.832e+00
                                                            1.218 0.224030
## walk score
                                    -5.797e+02 3.738e+02
                                                           -1.551 0.121804
## lat
                                     6.779e+05 1.472e+05
                                                            4.606 5.59e-06
## lon
                                    -1.359e+05 9.529e+04
                                                           -1.426 0.154661
## pets allowed
                                     5.998e+03
                                                7.596e+03
                                                            0.790 0.430213
## monthly cost
                                     1.630e+02 1.876e+01
                                                            8.688 < 2e-16
## price persqft
                                     4.754e+05 7.376e+04
                                                            6.445 3.44e-10
## is missing approx year built
                                                            0.400 0.689335
                                     1.324e+04 3.309e+04
## is_missing_community_district_num -2.695e+05
                                                7.382e+04
                                                           -3.651 0.000297
## is_missing_dining_room_type
                                     5.126e+02
                                                8.653e+03
                                                            0.059 0.952789
## is missing kitchen type
                                    -5.278e+03
                                                           -0.186 0.852252
                                                2.832e+04
## is_missing_num_floors_in_building 6.807e+02 9.305e+03
                                                            0.073 0.941719
## is missing num half bathrooms
                                     8.973e+02 1.691e+04
                                                            0.053 0.957718
```

```
## is missing parking charges
                                     -5.735e+03 8.255e+03 -0.695 0.487666
## is missing pct tax deductibl
                                      1.016e+04 9.496e+03
                                                             1.070 0.285327
## is_missing_sq_footage
                                      2.216e+03 7.544e+03
                                                             0.294 0.769094
## is_missing_total_taxes
                                      6.810e+02 1.000e+04
                                                             0.068 0.945737
## is missing monthly cost
                                     -7.148e+03 2.288e+04 -0.312 0.754886
##
                                     ***
## (Intercept)
## approx_year_built
## community_district_num
## coop condocondo
## dining_room_typedining area
                                     **
## dining_room_typeformal
## dining room typeother
## garage_exists
## kitchen_typeeat in
## kitchen_typeefficiency
                                     ***
## num_bedrooms
## num_floors_in_building
## num full bathrooms
## num_half_bathrooms
                                     ***
## num total rooms
                                     ***
## parking_charges
## pct_tax_deductibl
## sq_footage
## total taxes
## walk score
## lat
                                     ***
## lon
## pets_allowed
                                     ***
## monthly_cost
                                     ***
## price persqft
## is_missing_approx_year_built
## is_missing_community_district_num ***
## is missing dining room type
## is missing kitchen type
## is missing num floors in building
## is_missing_num_half_bathrooms
## is_missing_parking_charges
## is missing pct tax deductibl
## is_missing_sq_footage
## is_missing_total_taxes
## is missing monthly cost
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 70340 on 386 degrees of freedom
## Multiple R-squared: 0.855, Adjusted R-squared: 0.8418
## F-statistic: 65.03 on 35 and 386 DF, p-value: < 2.2e-16
```

### 3.3 Random Forest Modeling

Random forest is like a bunch of decision trees. When building these decision trees, each time a split in a tree is considered, a random sample of m predictors is chosen as split candidates from the full set of p predictors. The split is allowed to use only one of those m predictors. A fresh sample of m predictors is taken at each split, and typically we choose the number of predictors considered at each split is approximately equal to the square root of the total number of predictors.

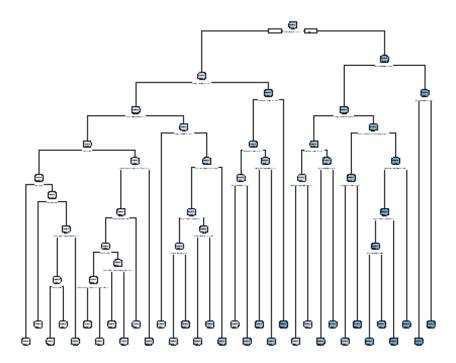
Random Forest is a non-parametric model. Where the function that is used to predict can be any function; the data decides on how the function looks like.

We believe random forest is the best because When the number of trees produced by random forests approaches infinity, theoretically, according to the large number theorem, it can be proved that the training error and the test error converge. In the actual process, since it is impossible to generate an infinite number of decision trees, the setting problem of the model parameters will affect the degree of over-fitting of the fitting results in the same running time.

I believe that coop\_condo, sq\_footage, and latitude have an effect on sale price that is truly causal. Whether the apartment is coop or condo is important because if it's a condominium then it means that it would predict higher sale price, and if it's a coop it would have a lower price. sq\_footage is the size of the house the bigger the house the more expensive its is sale price and latitude because the more north is the apartment the more expensive it is.

# 4. Performance Results (for Random Forest)

in sample  $R^2$  = 84 and out of sample  $R^2$  = 85 which is very close to out linear model. The RMSE is plus or minu \$70000. which is way better than the RMSE in the linear model. It is a \$13000 of difference. This is a valid estimate of model because the data was split into train and test set, and performing validation from the model created from the train set and tested it on the test set.



### 5. Discussion

While trying to use missForest to fill the NAs in the dataset. At first the y's in the training set was use to used the y's, giving was giving perfect x's the moment out of sample was done, were having bad results. Due to short amount of time given, this prediction is the best that we can have for now, if given time was longer our group would have done the forward stepwise to do feature selecting and have a better prediction model. I think our prediction is better than the listed estimates that Zillow has (with the given zipcodes) because the model that we carefully futurized. If we were given more time we would have also included distance from the apartment to midtown Manhattan.

### ##Code Appendix

```
pacman::p_load(dplyr, tidyr, ggplot2, magrittr, stringr, mlr)
housing_data = read.csv("housing_data_2016_2017.csv")
```

##Delete variables that we dont need

```
housing data %<>%
  select(-c(HITId, HITTypeId, Title, Description, Keywords, Reward, CreationT
ime, MaxAssignments,
                       RequesterAnnotation,
                                               AssignmentDurationInSeconds,
AutoApprovalDelayInSeconds, Expiration, NumberOfSimilarHITs, LifetimeInSecond
s, AssignmentId,
                   WorkerId,
                               AssignmentStatus,
                                                   AcceptTime, SubmitTime, Au
toApprovalTime,
                  ApprovalTime,
                                  RejectionTime,
                                                  RequesterFeedback,
eInSeconds, LifetimeApprovalRate,
                                     Last30DaysApprovalRate, Last7DaysApprova
lRate, URL, url, date of sale))
```

### **Clean Data**

```
housing data %<>%
  mutate( zip code = str extract(full address or zip code, "[0-9]{5}"))
housing data %<>%
  mutate(dogs allowed = ifelse(substr(housing data$dogs allowed, 1, 3) == "ye
s", 1, 0)) %>%
 mutate(cats_allowed = ifelse(substr(housing_data$cats_allowed, 1, 3) == "ye
s", 1, 0)) %>%
 mutate( pets_allowed = ifelse( cats_allowed + dogs_allowed > 0, 1, 0)) %>%
  mutate(coop condo = factor(tolower(coop condo)))
housing_data %<>%
  select(-c(dogs allowed, cats allowed, fuel type))
d = housing data
d %<>%
  mutate(maintenance cost = sjmisc::rec(maintenance cost, rec = "NA = 0; els
e = copy")) %<>%
  mutate(common charges = sjmisc::rec(common charges, rec = "NA = 0; else =
copy"))##recode from NA to 0.
# combine maintaince cost and common charges
d %<>%
  mutate( monthly_cost = common_charges + maintenance_cost)
d %<>%
 mutate(monthly_cost = sjmisc::rec(monthly_cost, rec = "0 = NA; else = copy
"))
## Garage exists conver it to binary
d %<>%
 mutate(garage exists = sjmisc::rec(garage exists, rec = "NA = 0; else = co
py")) ##recode from NA to 0.
d %<>%
  mutate(garage_exists = sjmisc::rec(garage_exists, rec = " eys = 1; UG = 1;
Underground = 1; yes = 1; Yes = 1; else = copy")) \#recode from NA to \emptyset.
d %<>%
  select(-c(maintenance_cost , common_charges, model_type))
```

```
d %<>%
  mutate( dining_room_type = as.factor(dining_room_type)) %>%
  mutate(garage_exists = as.character(garage_exists)) %>%
  mutate(garage_exists = as.numeric(garage_exists)) %>%
  mutate( parking_charges = as.character(parking_charges)) %>%
  mutate( parking_charges = as.numeric(parking_charges)) %>%
  mutate(sale_price = as.character(sale_price)) %>%
  mutate(sale_price = as.numeric(sale_price)) %>%
  mutate(total_taxes = as.character(total_taxes)) %>%
  mutate(total_taxes = as.numeric(total_taxes)) %>%
  mutate(price_persqft = listing_price_to_nearest_1000 / sq_footage)

## Warning: NAs introduced by coercion

## Warning: NAs introduced by coercion
```

#Added latitude and longitude features using ggmap

```
#Already run and included in the data
#pacman::p Load(ggmap)
#d %<>%
# mutate(lat = geocode(full_address or zip_code)$lat, lon = #geocode(full_ad
dress or zip code)$lon )
#geocoordinates for relevant LIRR stations
lirr coord = coord
## Error in eval(expr, envir, enclos): object 'coord' not found
RAD EARTH = 3958.8
degrees to radians = function(angle degrees){
  for(i in 1:length(angle degrees))
    angle_degrees[i] = angle_degrees[i]*pi/180
  return(angle degrees)
}
compute_globe_distance = function(destination, origin){
  destination rad = degrees to radians(destination)
  origin_rad = degrees_to_radians(origin)
  delta_lat = destination_rad[1] - origin_rad[1]
  delta lon = destination rad[2] - origin rad[2]
  h = (sin(delta_lat/2))^2 + cos(origin_rad[1]) * cos(destination_rad[1]) * (
sin(delta lon/2))^2
  central_angle = 2 * asin(sqrt(h))
  return(RAD_EARTH * central_angle)
#find the closest LIRR station and compute distance
shortest_lirr_distance = function(all_lirr_coords, house_coords){
  shortest dist = Inf
for (i in 1: nrow(all lirr coords)){
```

```
ith_lirr = c(all_lirr_coords$lat[i], all_lirr_coords$lon[i])
    new_dist = compute_globe_distance(ith_lirr, house_coords)
    if( new_dist < shortest_dist){
        shortest_dist = new_dist
      }
    }
    return(shortest_dist)
}
d %<>%
    rowwise() %>%
    mutate(shortest_dist = shortest_lirr_distance(lirr_coord, c(lat, lon)) )
## Error in nrow(all_lirr_coords): object 'lirr_coord' not found
#makes any other addresses redundant
d %<>%
    select(-c(zip_code, full_address_or_zip_code, listing_price_to_nearest_1000))
```

We are trying to predict sale\_price. So let's section our dataset:

```
####CREATE A COLUMN ID

d %<>%
    ungroup(d) %>%
    mutate(id = 1 : 2230)
d %<>%
    mutate(total_taxes = ifelse(d$total_taxes < 1000, NA, total_taxes))
real_y = data.frame(d$id, d$sale_price)
real_d = subset(d, (!is.na(d$sale_price)))
fake_d = subset(d, (is.na(d$sale_price)))
real_d$sale_price = NULL
fake_d$sale_price = NULL</pre>
```

#Split the data that has y into train and test sets

```
train_indices = sample(1 : nrow(real_d), nrow(real_d)*4/5)
training_data = real_d[train_indices, ]
testing_data = real_d[-train_indices, ]

X = rbind(training_data, testing_data, fake_d)

M = tbl_df(apply(is.na(X), 2, as.numeric))
colnames(M) = paste("is_missing_", colnames(X), sep = "")
```

#Some of these missing indicators are collinear because they share all the rows they are missing on. Let's filter those out:

```
M = tbl_df(t(unique(t(M))))
```

#Some featuers did not have missingness so let's remove them:

```
M \%<>\% select if(function(x){sum(x) > 0})
pacman::p load(missForest)
Ximp = missForest(data.frame(X), sampsize = rep(172, ncol(X)))$ximp
     missForest iteration 1 in progress...
## Warning in randomForest.default(x = obsX, y = obsY, ntree = ntree, mtry =
## mtry, : The response has five or fewer unique values. Are you sure you wan
## to do regression?
## done!
     missForest iteration 2 in progress...
## Warning in randomForest.default(x = obsX, y = obsY, ntree = ntree, mtry =
## mtry, : The response has five or fewer unique values. Are you sure you wan
t
## to do regression?
## done!
##
    missForest iteration 3 in progress...
## Warning in randomForest.default(x = obsX, y = obsY, ntree = ntree, mtry =
## mtry, : The response has five or fewer unique values. Are you sure you wan
## to do regression?
## done!
     missForest iteration 4 in progress...
##
## Warning in randomForest.default(x = obsX, y = obsY, ntree = ntree, mtry =
## mtry, : The response has five or fewer unique values. Are you sure you wan
## to do regression?
## done!
Ximp %<>%
  arrange(id)
Xnew = data.frame(cbind(Ximp, M, real_y))
Xnew %<>%
  mutate(price = d.sale_price) %>%
  select(-c(id, d.id, d.sale_price))
linear mod impute and missing dummies = lm(price ~ ., data = Xnew)
summary(linear_mod_impute_and_missing_dummies)
##
## Call:
```

```
## lm(formula = price ~ ., data = Xnew)
##
## Residuals:
##
       Min
                1Q
                   Median
                                 3Q
                                        Max
##
  -296854
           -36454
                       -20
                              36523
                                     332799
##
## Coefficients: (3 not defined because of singularities)
##
                                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                                  9.154e+06
                                      -3.664e+07
                                                             -4.003 7.23e-05
## approx year built
                                                               0.132 0.894659
                                       3.249e+01
                                                  2.453e+02
## community_district_num
                                       2.337e+03
                                                  1.169e+03
                                                               2.000 0.046099
                                                               8.208 1.98e-15
## coop_condocondo
                                       1.419e+05
                                                  1.729e+04
## dining room typedining area
                                                               0.297 0.766940
                                       1.559e+04
                                                  5.259e+04
## dining_room_typeformal
                                       2.332e+04
                                                  8.519e+03
                                                               2.738 0.006405
                                       1.297e+04
## dining_room_typeother
                                                  1.126e+04
                                                               1.152 0.249739
## garage_exists
                                       5.128e+02
                                                  9.017e+03
                                                               0.057 0.954675
## kitchen_typeeat in
                                      -2.854e+03
                                                  1.000e+04
                                                              -0.285 0.775535
## kitchen_typeefficiency
                                                  9.750e+03
                                      -1.767e+04
                                                              -1.813 0.070508
## num bedrooms
                                       4.236e+04
                                                  7.904e+03
                                                               5.359 1.29e-07
## num_floors_in_building
                                       2.535e+03
                                                  7.163e+02
                                                               3.539 0.000440
## num full bathrooms
                                       1.727e+04
                                                  5.242e+04
                                                               0.329 0.741999
## num_half_bathrooms
                                      -1.230e+04
                                                  3.258e+04
                                                              -0.377 0.706010
## num_total_rooms
                                       1.853e+04
                                                  5.175e+03
                                                               3.581 0.000376
## parking_charges
                                       3.493e+02
                                                  9.717e+01
                                                               3.595 0.000357
## pct tax deductibl
                                       4.671e+01
                                                  1.026e+03
                                                               0.046 0.963700
## sq footage
                                       3.027e+01
                                                  1.268e+01
                                                               2.386 0.017398
                                                  5.344e+00
## total taxes
                                       1.314e+01
                                                               2.458 0.014296
## walk_score
                                      -6.554e+02
                                                  3.382e+02
                                                              -1.938 0.053253
## lat
                                                  1.354e+05
                                                               4.822 1.90e-06
                                       6.530e+05
## lon
                                      -1.301e+05
                                                  8.466e+04
                                                              -1.537 0.125057
## pets_allowed
                                       1.112e+04
                                                  6.886e+03
                                                               1.615 0.106929
## monthly_cost
                                                               9.080 < 2e-16
                                       1.286e+02
                                                  1.416e+01
## price persqft
                                       5.546e+05
                                                  6.661e+04
                                                               8.326 8.36e-16
## is missing approx year built
                                       6.389e+03
                                                  3.368e+04
                                                               0.190 0.849625
## is_missing_community_district_num -2.312e+05
                                                  7.469e+04
                                                              -3.095 0.002080
## is missing dining room type
                                       5.110e+03
                                                  7.818e+03
                                                              0.654 0.513701
## is_missing_kitchen_type
                                      -1.343e+04
                                                  2.871e+04
                                                              -0.468 0.640234
## is_missing_num_bedrooms
                                              NA
                                                         NA
                                                                 NA
                                                                           NA
## is_missing_num_floors_in_building
                                      2.070e+03
                                                  8.315e+03
                                                               0.249 0.803508
## is_missing_num_half_bathrooms
                                                  1.407e+04
                                                              -0.867 0.386093
                                      -1.221e+04
## is_missing_num_total_rooms
                                              NA
                                                         NA
                                                                  NA
                                                                           NA
## is missing parking charges
                                      -2.146e+03
                                                  7.632e+03
                                                              -0.281 0.778657
## is_missing_pct_tax_deductibl
                                       1.291e+04
                                                  8.669e+03
                                                               1.489 0.137226
## is_missing_sq_footage
                                      -2.267e+03
                                                  6.700e+03
                                                              -0.338 0.735281
## is missing total taxes
                                       6.496e+02
                                                  9.155e+03
                                                              0.071 0.943463
## is missing monthly cost
                                      -2.973e+03
                                                  1.991e+04
                                                              -0.149 0.881388
## is_missing_price_persqft
                                              NA
                                                         NA
                                                                  NA
                                                                           NA
                                      ***
## (Intercept)
## approx year built
```

```
## community district num
                                     ***
## coop_condocondo
## dining_room_typedining area
## dining_room_typeformal
## dining_room_typeother
## garage_exists
## kitchen_typeeat in
## kitchen_typeefficiency
## num bedrooms
## num floors in building
## num_full_bathrooms
## num_half_bathrooms
                                     ***
## num total rooms
                                     ***
## parking_charges
## pct_tax_deductibl
## sq_footage
## total_taxes
## walk_score
## lat
## lon
## pets allowed
## monthly_cost
                                     ***
## price_persqft
## is missing approx year built
## is_missing_community_district_num **
## is_missing_dining_room_type
## is missing kitchen type
## is missing num bedrooms
## is_missing_num_floors_in_building
## is_missing_num_half_bathrooms
## is_missing_num_total_rooms
## is_missing_parking_charges
## is_missing_pct_tax_deductibl
## is missing sq footage
## is_missing_total_taxes
## is missing monthly cost
## is_missing_price_persqft
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 72110 on 492 degrees of freedom
     (1702 observations deleted due to missingness)
## Multiple R-squared: 0.8494, Adjusted R-squared:
## F-statistic: 79.28 on 35 and 492 DF, p-value: < 2.2e-16
```

#### **REMOVING MISSING Y SECTION**

```
Data = Xnew
### sale price is our imputed Y
Y = Data$price
```

```
Data %<>%
    filter(!is.na(price)) %>%
    select(-price)

Xtrain = Data[1:422, ]
Xtest = Data[423:528, ]

Ytrain = Y[1:422]
Ytest = Y[423:528]

dtrain = cbind(Xtrain, Ytrain) ## combine x train with y train, x test with y test
dtest = cbind(Xtest, Ytest)

Dropping colinear features
```

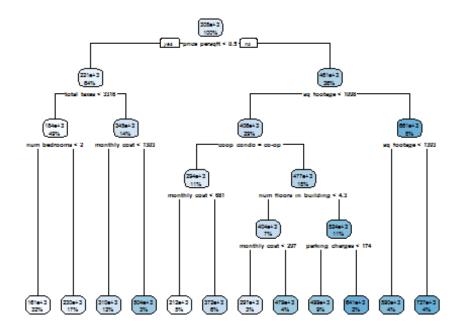
```
Xtrain %<>%
  select(-c(is_missing_num_total_rooms, is_missing_num_bedrooms, is_missing_p
rice_persqft))
```

Linear Regression

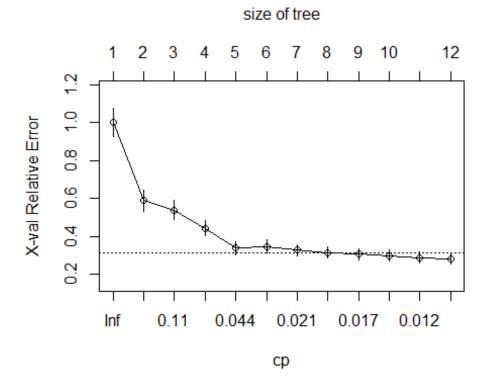
```
linear = lm(Ytrain ~ ., data = Xtrain)## simple linear model
summary(linear)
##
## Call:
## lm(formula = Ytrain ~ ., data = Xtrain)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -295653 -31899
                     2725
                            33423 314214
##
## Coefficients:
##
                                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    -3.794e+07 1.017e+07 -3.730 0.000220
## approx year built
                                    -3.775e+01 2.690e+02 -0.140 0.888450
## community_district_num
                                     2.001e+03 1.243e+03
                                                            1.610 0.108301
## coop_condocondo
                                     1.720e+05 1.977e+04
                                                            8.703 < 2e-16
## dining_room_typedining area
                                     1.950e+04 5.172e+04
                                                            0.377 0.706350
## dining_room_typeformal
                                     2.424e+04 9.331e+03
                                                            2.598 0.009733
                                     1.246e+04 1.221e+04
## dining_room_typeother
                                                            1.020 0.308268
## garage_exists
                                     3.292e+03 1.023e+04
                                                            0.322 0.747841
                                     5.448e+03 1.092e+04
## kitchen_typeeat in
                                                            0.499 0.618207
## kitchen_typeefficiency
                                    -1.649e+04 1.078e+04 -1.530 0.126950
## num_bedrooms
                                     3.235e+04 8.779e+03 3.685 0.000261
## num_floors_in_building
                                     2.363e+03 7.932e+02
                                                            2.980 0.003069
## num full bathrooms
                                     1.706e+04 5.152e+04
                                                            0.331 0.740723
## num_half_bathrooms
                                     2.510e+03 3.594e+04
                                                            0.070 0.944363
## num_total_rooms
                                     2.179e+04 5.748e+03 3.791 0.000174
```

```
## parking charges
                                       3.950e+02
                                                  1.032e+02
                                                              3.827 0.000151
## pct_tax_deductibl
                                       5.616e+01 1.417e+03
                                                              0.040 0.968404
## sq_footage
                                       2.578e+01
                                                 1.316e+01
                                                              1.958 0.050927
## total taxes
                                       7.102e+00 5.832e+00
                                                              1.218 0.224030
## walk_score
                                      -5.797e+02 3.738e+02
                                                             -1.551 0.121804
## lat
                                       6.779e+05
                                                  1.472e+05
                                                              4.606 5.59e-06
                                                             -1.426 0.154661
## lon
                                      -1.359e+05 9.529e+04
## pets_allowed
                                       5.998e+03
                                                 7.596e+03
                                                              0.790 0.430213
## monthly cost
                                       1.630e+02
                                                 1.876e+01
                                                              8.688 < 2e-16
## price persaft
                                       4.754e+05
                                                  7.376e+04
                                                              6.445 3.44e-10
## is missing approx year built
                                       1.324e+04
                                                  3.309e+04
                                                              0.400 0.689335
## is_missing_community_district_num -2.695e+05
                                                  7.382e+04
                                                             -3.651 0.000297
## is missing dining room type
                                                              0.059 0.952789
                                       5.126e+02
                                                  8.653e+03
## is_missing_kitchen_type
                                      -5.278e+03
                                                  2.832e+04
                                                             -0.186 0.852252
## is_missing_num_floors_in_building
                                                  9.305e+03
                                                              0.073 0.941719
                                      6.807e+02
## is_missing_num_half_bathrooms
                                       8.973e+02
                                                  1.691e+04
                                                              0.053 0.957718
## is missing parking charges
                                      -5.735e+03
                                                  8.255e+03
                                                             -0.695 0.487666
## is missing pct tax deductibl
                                                  9.496e+03
                                      1.016e+04
                                                              1.070 0.285327
## is missing sq footage
                                       2.216e+03
                                                  7.544e+03
                                                              0.294 0.769094
## is_missing_total_taxes
                                      6.810e+02
                                                  1.000e+04
                                                              0.068 0.945737
## is missing monthly cost
                                      -7.148e+03
                                                  2.288e+04 -0.312 0.754886
##
                                      ***
## (Intercept)
## approx_year_built
## community district num
## coop condocondo
## dining room typedining area
## dining_room_typeformal
## dining_room_typeother
## garage_exists
## kitchen_typeeat in
## kitchen_typeefficiency
                                      ***
## num bedrooms
## num_floors_in_building
## num_full_bathrooms
## num half bathrooms
                                      ***
## num total rooms
## parking_charges
                                      ***
## pct_tax_deductibl
## sq_footage
## total_taxes
## walk score
                                      ***
## lat
## lon
## pets allowed
                                      ***
## monthly_cost
                                      ***
## price_persqft
## is_missing_approx_year_built
## is_missing_community_district_num ***
## is_missing_dining_room_type
```

```
## is missing kitchen type
## is_missing_num_floors_in_building
## is_missing_num_half_bathrooms
## is_missing_parking_charges
## is_missing_pct_tax_deductibl
## is_missing_sq_footage
## is missing total taxes
## is missing monthly cost
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 70340 on 386 degrees of freedom
## Multiple R-squared: 0.855, Adjusted R-squared: 0.8418
## F-statistic: 65.03 on 35 and 386 DF, p-value: < 2.2e-16
yhat = predict(linear, Xtest)
e = yhat - Ytest
sqrt(sum(e^2) / nrow(Xtest))
## [1] 83215.95
#REGRESSION TREE
pacman::p load(rsample)#data spliting
pacman::p load(rpart) #performing reg tree
pacman::p_load(rpart.plot) #ploting reg tree
pacman::p_load(ipred) #bagging
pacman::p load(caret) #bagging
m1 = rpart(
 formula = Ytrain ~ .,
  data = Xtrain,
  method = "anova"
  )
rpart.plot(m1)
```



# plotcp(m1)



# summary(m1)

```
## Call:
## rpart(formula = Ytrain ~ ., data = Xtrain, method = "anova")
##
     n = 422
##
##
              CP nsplit rel error
                                      xerror
                                                   xstd
## 1
      0.42758149
                      0 1.0000000 1.0034864 0.07563004
## 2
      0.12824221
                      1 0.5724185 0.5888809 0.05677089
## 3
      0.09266116
                      2 0.4441763 0.5377683 0.05130348
## 4 0.07319492
                      3 0.3515151 0.4417798 0.04077420
## 5
      0.02585520
                      4 0.2783202 0.3364894 0.03348648
## 6 0.02291037
                      5 0.2524650 0.3462884 0.03336475
                      6 0.2295546 0.3283003 0.02936593
## 7
      0.01939333
## 8
     0.01776872
                      7 0.2101613 0.3146267 0.03040719
                      8 0.1923926 0.3055096 0.02989080
## 9
      0.01663924
## 10 0.01348814
                      9 0.1757533 0.2983826 0.03004550
## 11 0.01014447
                     10 0.1622652 0.2876490 0.02931209
## 12 0.01000000
                     11 0.1521207 0.2813368 0.02881401
##
## Variable importance
##
            price_persqft
                                    monthly cost
                                                              coop_condo
##
                       20
                                               15
                                                                       13
                                       sq_footage
##
        approx year built
                                                             total_taxes
##
                       12
                                                9
                                                                        8
##
          parking_charges
                                              lon
                                                            num_bedrooms
##
                                                5
                                                                        3
##
          num total rooms
                               pct_tax_deductibl community_district_num
##
                                                2
## num_floors_in_building
                                              lat
##
                                                1
##
## Node number 1: 422 observations,
                                        complexity param=0.4275815
     mean=308191.7, MSE=3.121006e+10
     left son=2 (268 obs) right son=3 (154 obs)
##
##
     Primary splits:
##
         price_persqft
                           < 0.5036155 to the left, improve=0.4275815, (0 mi
ssing)
##
                           splits as LR, improve=0.3754617, (0 missing)
         coop condo
##
         approx_year_built < 1970.5</pre>
                                       to the left, improve=0.3463094, (0 mi
ssing)
         total taxes
                           < 3389.792 to the left,
                                                      improve=0.3270625, (0 mi
##
ssing)
##
         num total rooms
                           < 4.5
                                        to the left, improve=0.2781774, (0 mi
ssing)
##
     Surrogate splits:
##
         coop condo
                           splits as LR, agree=0.848, adj=0.584, (0 split)
##
         approx_year_built < 1970.5
                                       to the left, agree=0.844, adj=0.571,
(0 split)
                           < 135.1167 to the left, agree=0.794, adj=0.435,
##
         parking_charges
(0 split)
         monthly_cost < 471.5 to the right, agree=0.789, adj=0.422,
```

```
(0 split)
         lon
                           < -73.87994 to the right, agree=0.744, adj=0.299,</pre>
##
(0 split)
##
## Node number 2: 268 observations,
                                       complexity param=0.09266116
     mean=220622.8, MSE=1.036057e+10
##
##
     left son=4 (207 obs) right son=5 (61 obs)
##
     Primary splits:
##
         total taxes
                         < 3316.375 to the left,
                                                   improve=0.4395279, (0 miss
ing)
         sq footage
                         < 940.6025
                                     to the left, improve=0.4138876, (0 miss
##
ing)
         monthly_cost
                                     to the left, improve=0.3937581, (0 miss
##
                         < 1019
ing)
##
         num total rooms < 4.5
                                     to the left, improve=0.3399684, (0 miss
ing)
##
         num bedrooms
                         < 1.5
                                     to the left, improve=0.3103121, (0 miss
ing)
##
     Surrogate splits:
##
         sq_footage
                                < 1050.357 to the left, agree=0.858, adj=0.
377, (0 split)
         monthly_cost
                                < 985.5
                                            to the left,
                                                          agree=0.851, adj=0.
##
344, (0 split)
##
         lat
                                < 40.77906 to the left, agree=0.832, adj=0.
262, (0 split)
         num total rooms
                                < 5.5
                                            to the left, agree=0.810, adj=0.
164, (0 split)
         num floors in building < 7.36
                                            to the left, agree=0.806, adj=0.
##
148, (0 split)
##
## Node number 3: 154 observations,
                                       complexity param=0.1282422
     mean=460584.3, MSE=3.092526e+10
##
     left son=6 (121 obs) right son=7 (33 obs)
##
     Primary splits:
##
         sq_footage
                           < 1098
                                       to the left,
                                                     improve=0.3546534, (0 mi
ssing)
##
         num total rooms
                           < 4.5
                                       to the left,
                                                     improve=0.3330176, (0 mi
ssing)
         num bedrooms
                           < 1.5
                                       to the left,
                                                     improve=0.3201549, (0 mi
##
ssing)
        total taxes
                           < 3690.024 to the left,
                                                     improve=0.3156214, (0 mi
##
ssing)
         approx year built < 1963.5
                                       to the left,
                                                     improve=0.2232692, (0 mi
##
ssing)
    Surrogate splits:
##
                                       to the left, agree=0.890, adj=0.485,
##
         total_taxes
                           < 4120.488
(0 split)
##
         num bedrooms
                           < 2.5
                                       to the left, agree=0.857, adj=0.333,
(0 split)
         monthly cost
                           < 1478.5
                                       to the left, agree=0.844, adj=0.273,
```

```
(0 split)
         num_total_rooms
                                       to the left, agree=0.805, adj=0.091,
##
                           < 5.5
(0 split)
         pct_tax_deductibl < 35.53167 to the right, agree=0.799, adj=0.061,</pre>
##
(0 split)
##
## Node number 4: 207 observations,
                                       complexity param=0.01663924
     mean=183990.5, MSE=3.585262e+09
##
##
     left son=8 (137 obs) right son=9 (70 obs)
##
     Primary splits:
##
         num_bedrooms
                                     to the left, improve=0.2952904, (0 miss
                         < 1.5
ing)
                                     to the left, improve=0.2228783, (0 miss
##
         monthly cost
                         < 764
ing)
##
         sq footage
                         < 940.6025
                                    to the left, improve=0.2185199, (0 miss
ing)
                         < 2953.945 to the left, improve=0.2160151, (0 miss
##
         total taxes
ing)
                                     to the left, improve=0.2120814, (0 miss
##
         num total rooms < 4.5
ing)
##
     Surrogate splits:
                                        to the left,
                                                      agree=0.874, adj=0.629,
##
         sq_footage
                            < 853
(0 split)
##
         num_total_rooms
                            < 3.5
                                        to the left, agree=0.845, adj=0.543,
(0 split)
##
         monthly cost
                            < 805.5
                                        to the left, agree=0.773, adj=0.329,
(0 split)
                                        to the left, agree=0.744, adj=0.243,
##
         total taxes
                            < 3140.35
(0 split)
         num half bathrooms < 0.965
                                        to the left, agree=0.691, adj=0.086,
##
(0 split)
##
## Node number 5: 61 observations,
                                      complexity param=0.0258552
     mean=344932.6, MSE=1.334551e+10
##
##
     left son=10 (50 obs) right son=11 (11 obs)
##
     Primary splits:
##
         monthly cost
                         < 1302.5
                                     to the left, improve=0.4183022, (0 miss
ing)
##
         sq footage
                         < 1102.955 to the left, improve=0.3724499, (0 miss
ing)
                                     to the left, improve=0.2772907, (0 miss
##
         total taxes
                         < 4024.79
ing)
                         < 0.4499131 to the left, improve=0.2409971, (0 miss
         price persaft
##
ing)
##
         parking_charges < 64.775</pre>
                                     to the left, improve=0.2147612, (0 miss
ing)
##
     Surrogate splits:
##
         num total rooms
                            < 6.5
                                        to the left, agree=0.885, adj=0.364,
(0 split)
                    < 1339.5 to the left, agree=0.869, adj=0.273,
         sq footage
```

```
(0 split)
        total taxes
                           < 4381.68
                                       to the left, agree=0.852, adj=0.182,
##
(0 split)
                                       to the right, agree=0.836, adj=0.091,
        num half bathrooms < 0.72
(0 split)
##
## Node number 6: 121 observations,
                                      complexity param=0.07319492
    mean=405892.4, MSE=2.159689e+10
##
     left son=12 (47 obs) right son=13 (74 obs)
##
     Primary splits:
                          splits as LR, improve=0.3689025, (0 missing)
##
        coop condo
                                    to the left, improve=0.2996678, (0 mi
##
        approx_year_built < 2004.5
ssing)
##
        price persqft
                          < 0.5847979 to the left, improve=0.2978430, (0 mi
ssing)
                                      to the left, improve=0.2590936, (0 mi
        num total rooms
                          < 3.5
ssing)
                                      to the left, improve=0.2478039, (0 mi
        sq_footage
                     < 679.415
##
ssing)
##
    Surrogate splits:
                               < 1971
                                          to the left, agree=0.884, adj=0.
##
        approx year built
702, (0 split)
        monthly_cost
                               < 514.5 to the right, agree=0.851, adj=0.
##
617, (0 split)
        price persqft
                              < 0.6130331 to the left, agree=0.818, adj=0.
532, (0 split)
        community district num < 27.5 to the right, agree=0.769, adj=0.
404, (0 split)
##
        pct_tax_deductibl < 48.45333 to the right, agree=0.752, adj=0.
362, (0 split)
                                    complexity param=0.01348814
## Node number 7: 33 observations,
    mean=661121.2, MSE=1.394647e+10
    left son=14 (17 obs) right son=15 (16 obs)
##
##
    Primary splits:
##
        sq_footage
                              < 1392.81 to the left, improve=0.3859944,</pre>
(0 missing)
##
        total_taxes
                               < 3874.715 to the left,
                                                         improve=0.3050610,
(0 missing)
        monthly_cost
                               < 1326
                                           to the left,
                                                         improve=0.2652581,
##
(0 missing)
##
        num bedrooms
                               < 2.5
                                           to the left,
                                                         improve=0.2378804,
(0 missing)
        num floors in building < 21.5
                                          to the left, improve=0.1998063,
##
(0 missing)
##
    Surrogate splits:
        total_taxes < 4366.515 to the left, agree=0.818, adj=0.625, (0 s
##
plit)
##
        monthly_cost < 1326
                                 to the left, agree=0.788, adj=0.562, (0 s
plit)
```

```
##
         num bedrooms < 2.5 to the left, agree=0.727, adj=0.438, (0 s
plit)
         lon
                       < -73.83932 to the right, agree=0.727, adj=0.438, (0 s
##
plit)
         price_persqft < 0.5384526 to the right, agree=0.727, adj=0.438, (0 s
##
plit)
##
## Node number 8: 137 observations
     mean=160732.4, MSE=1.951881e+09
##
## Node number 9: 70 observations
     mean=229509.8, MSE=3.651313e+09
##
##
## Node number 10: 50 observations
##
     mean=309887.8, MSE=7.481011e+09
##
## Node number 11: 11 observations
    mean=504227.3, MSE=9.045062e+09
##
##
## Node number 12: 47 observations,
                                       complexity param=0.02291037
     mean=293892.3, MSE=1.181581e+10
##
     left son=24 (23 obs) right son=25 (24 obs)
##
##
     Primary splits:
##
         monthly_cost
                         < 681
                                     to the left, improve=0.5433477, (0 miss
ing)
##
         sq footage
                         < 743.825
                                     to the left, improve=0.5232991, (0 miss
ing)
         total taxes
                                     to the left, improve=0.4687540, (0 miss
##
                         < 2752.269
ing)
         num total rooms < 3.5
                                     to the left, improve=0.4296906, (0 miss
##
ing)
##
         num bedrooms
                         < 0.5
                                     to the left, improve=0.3338656, (0 miss
ing)
##
     Surrogate splits:
                           < 743.825
                                       to the left, agree=0.894, adj=0.783,
##
         sq_footage
(0 split)
##
         total taxes
                           < 3129.924 to the left, agree=0.872, adj=0.739,</pre>
(0 split)
                           < 3.5
                                       to the left, agree=0.766, adj=0.522,
##
         num total rooms
(0 split)
                           < 0.5539046 to the left, agree=0.745, adj=0.478,
##
         price_persqft
(0 split)
                                       to the right, agree=0.723, adj=0.435,
##
         pct tax deductibl < 43.415</pre>
(0 split)
##
## Node number 13: 74 observations,
                                       complexity param=0.01939333
##
     mean=477027.5, MSE=1.478183e+10
##
     left son=26 (29 obs) right son=27 (45 obs)
##
     Primary splits:
##
         num_floors_in_building < 4.285</pre>
to the left, improve=0.2335069,
```

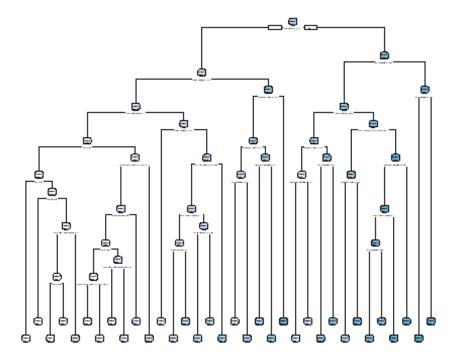
```
(0 missing)
                                < 211
                                             to the left,
                                                           improve=0.2193306,
##
         monthly_cost
(0 missing)
         total taxes
                                < 2143
                                             to the left,
                                                           improve=0.2122442,
##
(0 missing)
         approx_year_built
                                < 2006.5
                                             to the left,
                                                           improve=0.2079009,
##
(0 missing)
##
         parking charges
                                < 174.5133 to the left,
                                                           improve=0.1971597,
(0 missing)
     Surrogate splits:
##
##
         price_persqft
                                < 0.5718783 to the left,
                                                           agree=0.730, adj=0.
310, (0 split)
##
         total taxes
                                < 2143
                                             to the left,
                                                           agree=0.716, adj=0.
276, (0 split)
         parking_charges
                                < 114.89
                                             to the left,
                                                           agree=0.703, adj=0.
##
241, (0 split)
         community_district_num < 24.5</pre>
                                             to the left, agree=0.676, adj=0.
172, (0 split)
                                             to the right, agree=0.676, adj=0.
##
         pct tax deductibl
                                < 46.875
172, (0 split)
## Node number 14: 17 observations
     mean=589941.2, MSE=3.455467e+09
##
##
## Node number 15: 16 observations
##
     mean=736750, MSE=1.399019e+10
##
## Node number 24: 23 observations
##
     mean=212043.5, MSE=3.314759e+09
##
## Node number 25: 24 observations
##
     mean=372330.8, MSE=7.389972e+09
##
## Node number 26: 29 observations,
                                        complexity param=0.01776872
     mean=403842.7, MSE=1.358682e+10
##
##
     left son=52 (12 obs) right son=53 (17 obs)
##
     Primary splits:
##
         monthly_cost < 297
                                  to the left, improve=0.5939465, (0 missing
)
##
         kitchen_type splits as LRL-, improve=0.2566576, (0 missing)
##
         total_taxes < 2087.5
                                  to the left, improve=0.2457086, (0 missing
)
                                  to the left, improve=0.2435420, (0 missing
##
         sq footage
                      < 698.275
)
##
         num bedrooms < 1.5
                                  to the left, improve=0.2292115, (0 missing
)
##
     Surrogate splits:
##
         num bedrooms
                                     to the left, agree=0.793, adj=0.500, (0
                         < 1.5
split)
         num total rooms < 3.5 to the left, agree=0.793, adj=0.500, (0
##
```

```
split)
         sq_footage
                         < 669.49
                                      to the left, agree=0.793, adj=0.500, (0
##
split)
                         < 0.6518208 to the right, agree=0.793, adj=0.500, (0
         price persaft
##
split)
         total_taxes
                         < 2306.5
                                      to the left, agree=0.759, adj=0.417, (0
##
split)
##
                                        complexity param=0.01014447
## Node number 27: 45 observations,
     mean=524191.1, MSE=9.875883e+09
##
     left son=54 (37 obs) right son=55 (8 obs)
##
##
     Primary splits:
                           < 174.1833 to the left, improve=0.3006410, (0 mi
##
         parking charges
ssing)
##
         monthly cost
                           < 630.5
                                        to the left,
                                                      improve=0.2754588, (0 mi
ssing)
         approx_year_built < 2005.5</pre>
##
                                        to the left,
                                                      improve=0.2286395, (0 mi
ssing)
##
         total taxes
                           < 3674.215 to the left,
                                                      improve=0.1941959, (0 mi
ssing)
                                        to the left, improve=0.1876615, (0 mi
##
         sq footage
                           < 878.5
ssing)
     Surrogate splits:
##
##
         price_persqft
                                 < 0.8290999 to the left, agree=0.956, adj=0.
750, (0 split)
                                 < -73.92553 to the right, agree=0.933, adj=0.</pre>
##
         lon
625, (0 split)
##
         approx_year_built
                                             to the left, agree=0.889, adj=0.
                                 < 2009.5
375, (0 split)
         community_district_num < 29.5</pre>
                                             to the left, agree=0.867, adj=0.
250, (0 split)
                                             to the right, agree=0.867, adj=0.
         sq footage
                                 < 591
##
250, (0 split)
##
## Node number 52: 12 observations
    mean=296920.8, MSE=1.016437e+10
##
##
## Node number 53: 17 observations
     mean=479316.9, MSE=2.236462e+09
##
##
## Node number 54: 37 observations
     mean=498854.1, MSE=6.488097e+09
##
##
## Node number 55: 8 observations
    mean=641375, MSE=8.843234e+09
yhat = predict(m1, Xtest)
e = yhat - Ytest
sqrt(sum(e^2)/106)
```

```
## [1] 111454.6

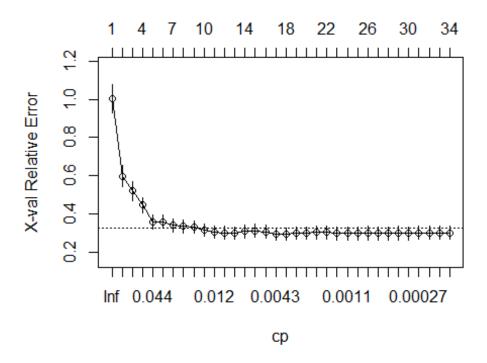
m2 <- rpart(
    formula = Ytrain ~ .,
    data = Xtrain,
    method = "anova",
    control = list(cp = 0, xval = 10)
)

rpart.plot(m2)</pre>
```



plotcp(m2)

### size of tree



```
yhat = predict(m2, Xtest)
e = yhat - Ytest
sqrt(sum(e^2)/106)
## [1] 107028.4
jpeg(file = "save_m2.jpeg")
###Tuning
m3 <- rpart(
    formula = Ytrain ~ .,
    data
            = Xtrain,
    method = "anova",
    control = list(minsplit = 10, maxdepth = 12, xval = 10)
)
yhat = predict(m3, Xtest)
e = yhat - Ytest
sqrt(sum(e^2)/106)
## [1] 111454.6
m3$cptable
##
              CP nsplit rel error
                                     xerror
## 1
      0.42758149
                      0 1.0000000 1.0033581 0.07572629
## 2 0.12824221
                      1 0.5724185 0.6290791 0.05820362
## 3 0.09266116
                      2 0.4441763 0.5672022 0.05401394
```

```
## 4 0.07319492
                      3 0.3515151 0.4550638 0.04217392
                      4 0.2783202 0.3534294 0.03651200
## 5 0.02585520
## 6 0.02291037
                      5 0.2524650 0.3043492 0.02887121
## 7 0.01939333
                      6 0.2295546 0.3147219 0.02938829
                     7 0.2101613 0.3044802 0.02975724
## 8 0.01776872
## 9 0.01663924
                     8 0.1923926 0.3003660 0.02986459
## 10 0.01348814
                     9 0.1757533 0.2768037 0.02751636
## 11 0.01014447
                     10 0.1622652 0.2655842 0.02747896
                     11 0.1521207 0.2619472 0.02733595
## 12 0.01000000
# function to get optimal cp
get_cp <- function(x) {</pre>
        <- which.min(x$cptable[, "xerror"])</pre>
 min
  cp <- x$cptable[min, "CP"]</pre>
}
# function to get minimum error
get_min_error <- function(x) {</pre>
 min <- which.min(x$cptable[, "xerror"])</pre>
  xerror <- x$cptable[min, "xerror"]</pre>
}
optimal_tree <- rpart(</pre>
    formula = Ytrain ~ .,
            = Xtrain,
    data
    method = "anova",
    control = list(minsplit = 11, maxdepth = 8, cp = 0.01)
    )
pred <- predict(optimal_tree, newdata = Xtrain)</pre>
RMSE(pred = pred, obs = Ytrain)
## [1] 68903.54
```

#### ##RANDOM FORESTS

```
m1 <- randomForest(
  formula = Ytrain ~ .,
  data = Xtrain
)

m1

##

## Call:
## randomForest(formula = Ytrain ~ ., data = Xtrain)

##

Type of random forest: regression
##

Number of trees: 500

## No. of variables tried at each split: 10
##</pre>
```

```
Mean of squared residuals: 4408749600
##
##
                       % Var explained: 85.87
which.min(m1$mse)
## [1] 159
# RMSE of this optimal random forest
sqrt(m1$mse[which.min(m1$mse)])
## [1] 65665.63
features <- setdiff(names(Xtrain), Ytrain)</pre>
set.seed(1989)
m2 <- tuneRF(
 X
           = Xtrain,
      = Ytrain,
 ntreeTry = 500,
 mtryStart = 5,
  stepFactor = 1.5,
 improve = 0.01,
trace = FALSE # to not show real-time progress
## -0.03910721 0.01
## 0.03347455 0.01
## 0.03056411 0.01
## 0.01855087 0.01
```

