

Studying Annihilation Distributions

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I tried to fit the distributions the radial distribution of the anti-hydrogen annihilation with analytic models. This should improve the results, avoiding statistical fluctuations: The models are listed below:

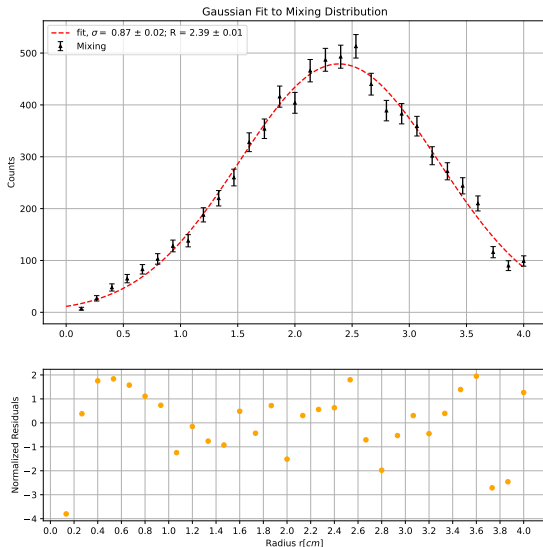
- Pdf Mixing: the Normal distribution.
- Pdf Uwlosses: Rayleigh distribution $\frac{r}{\sigma^2} e^{-\frac{r^2}{2\sigma^2}}$.
- Pdf Cosmic: $k \cdot x$.

The factor k is the normalization constant. The Mixing, UW losses and cosmic data are fitted and the result are shown in the following slides.



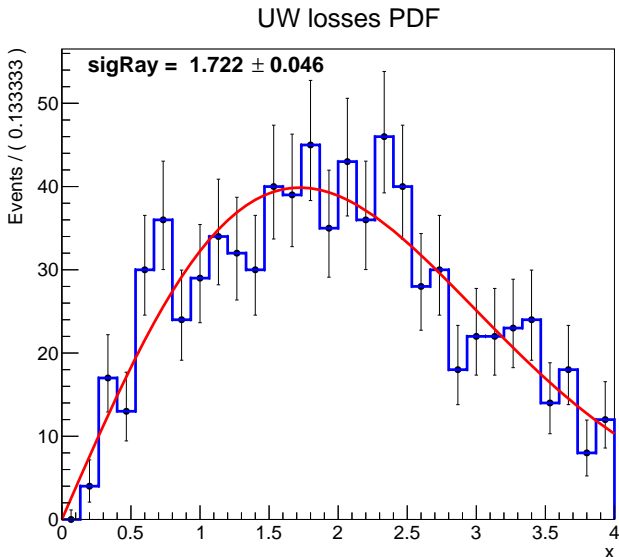
MIXING

Mixing dataset represents almost pure data of anti-hydrogen annihilation on the walls. The radius distribution is fitted with a Gaussian.



UWlosses

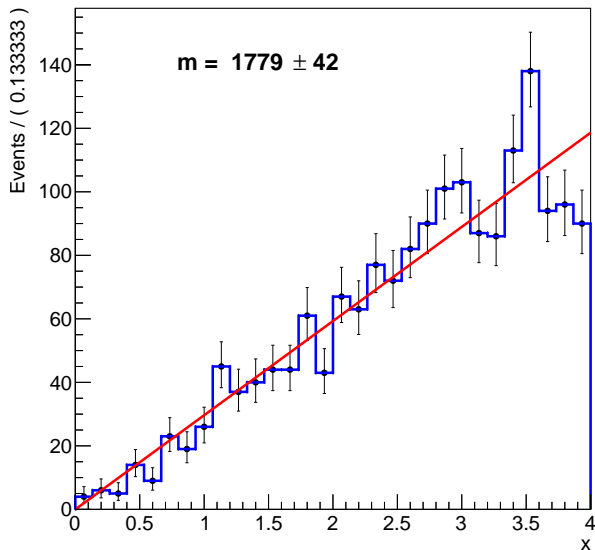
The microwave losses represent an almost pure anti-hydrogen sample of annihilation events due to residual gas inside the trap.



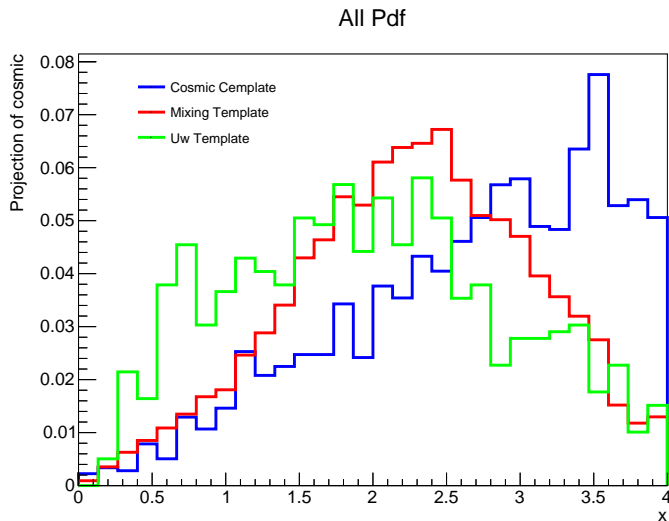
Cosmic

The cosmic distribution is obtained from dataset without anti-hydrogen.

Cosmic PDF



Pdfs normalized plotted together



Radial Density

The histogram in r variable doesn't account for the different area of the bin which is $2\pi r \cdot dr$. So it is useful to divide per $2\pi r$ to obtain the radial density of the events.

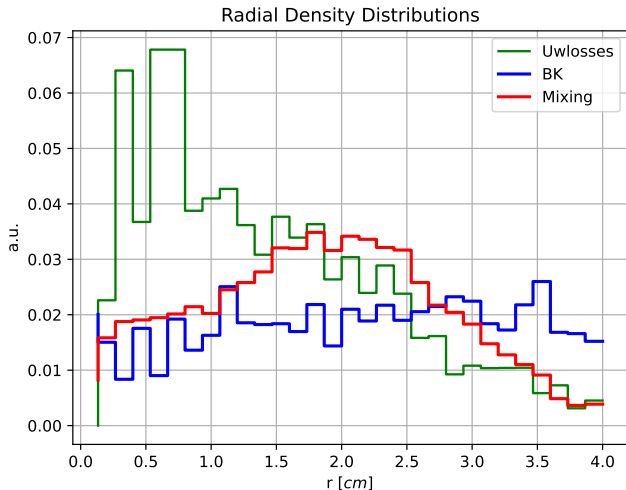


Figure: Radial density Pdf for f4 dataset

Toy simulation.

To study the accuracy of the algorithm to reconstruct the various parameter, we have developed a "toy" simulation tool. The model to generate the data is:

$$Pdf_{total} = a \cdot Gauss_{mix} + b \cdot Rayleigh + c \cdot linearModel_{cosmic} \quad (1)$$

where a, b, c represent the "weights" of the various contributions to the Pdf used to generate the data. The number of annihilation is indicated as N_{sample} . Once the data are generated, they are fitted with the model:

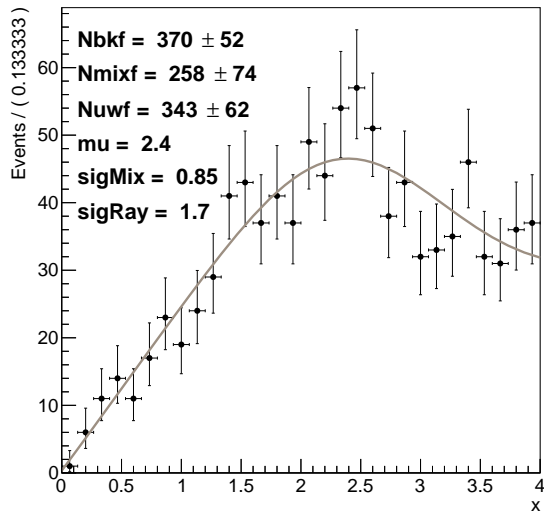
$$Pdf_{fit} = Nfit_{mix} \cdot Gauss_{mix} + Nfit_{uw} \cdot Rayleigh + Nfit_{bk} \cdot linearModel_{cosmic} \quad (2)$$

The parameters of the fit are $Nfit_{mix}$, $Nfit_{uw}$ and $Nfit_{bk}$. The "true value" are defined as:

- $Ngen_{mix} = a \cdot N_{sample}$
- $Ngen_{uw} = b \cdot N_{sample}$
- $Ngen_{bk} = c \cdot N_{sample}$

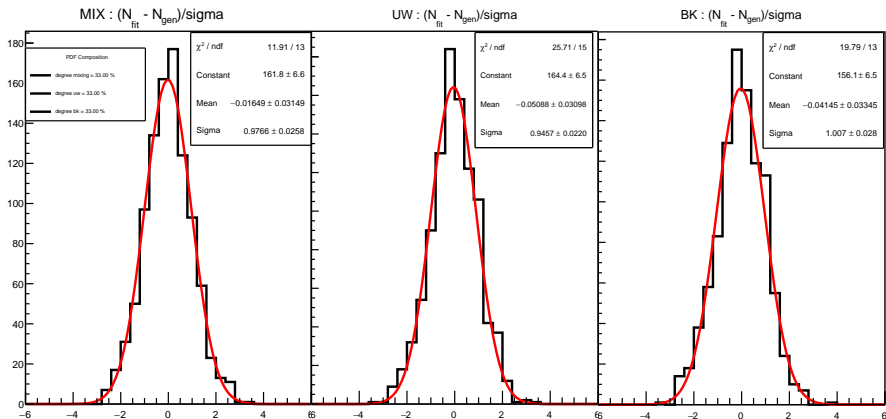
Example of fit, Toy: $N_{\text{sample}} = 1000$, $a = 33\%$, $b = 33\%$, $c = 33\%$

Fit Toy Model



Toy: $N_{\text{sample}} = 1000$, $a = 33\%$, $b = 33\%$, $c = 33\%$

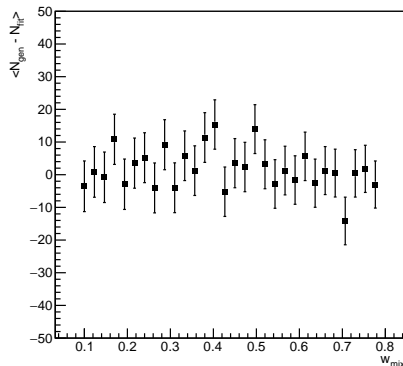
In this plot we have fixed the weight of each distribution to 33%, with $N_{\text{sample}} = 1000$ and $N_{\text{trials}} = 1000$. This first plot is made to ensure that the algorithm is able to reconstruct the parameters, and check the presence of a bias. The variable of the histograms are: $\frac{N_{\text{fit}} - N_{\text{gen}}}{\sigma_{\text{fit}}}$. The distributions are normal, the fit is behaving as expected.



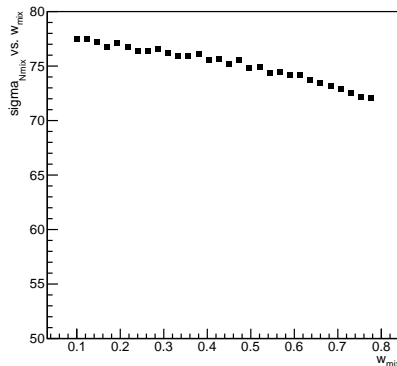
weight variation a for mix.

Now we study how or if the coefficients of the fit $Nfit_{mix}$, $Nfit_{uw}$ and $Nfit_{bk}$ vary with the increment of the weight a . At fixed $c = 10\%$, a is raised from 10% to 80% and b is decreased accordingly.

MIX: $N_{gen} - N_{fit}$ averaged over 100 trials



Graph



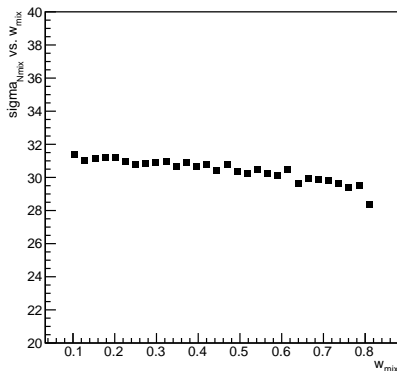
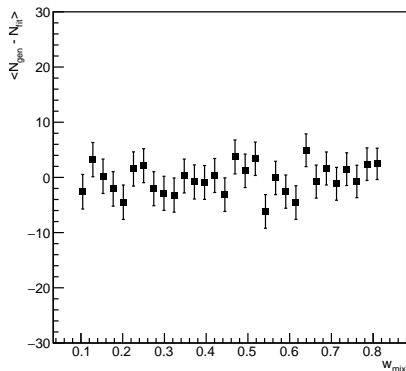
The number events is always $N_{sample} = 1000$. For each value of the weight a we iterate 100 times ($N_{trials} = 100$) to study the reconstructed coefficients with the variation of the weights.



$N = 165$.

Now we have done the same plot with $N = 165$, the same amount of data in `r68465_uw_exp_freq4.vertex.csv` after applying *cut1*. The value of c is fixed to reproduce the number of expected events from background ($c = 6\%$).

MIX: $N_{\text{gen}} - N_{\text{fit}}$ averaged over 100 trials

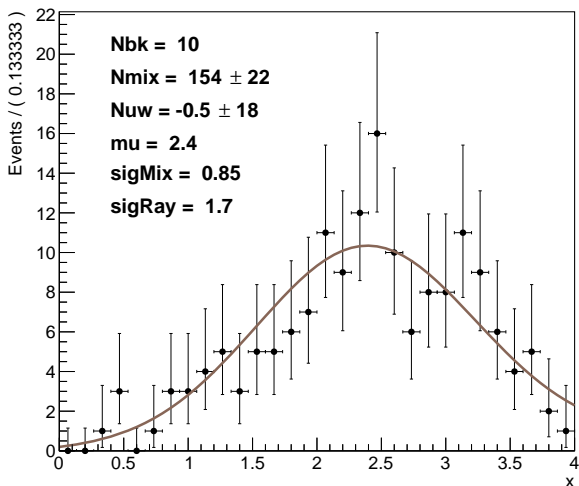


Fit to data.

Pdf = Gaussian (Mixing) + Rayleigh (Uwlosses) + linear model (cosmic fixed).

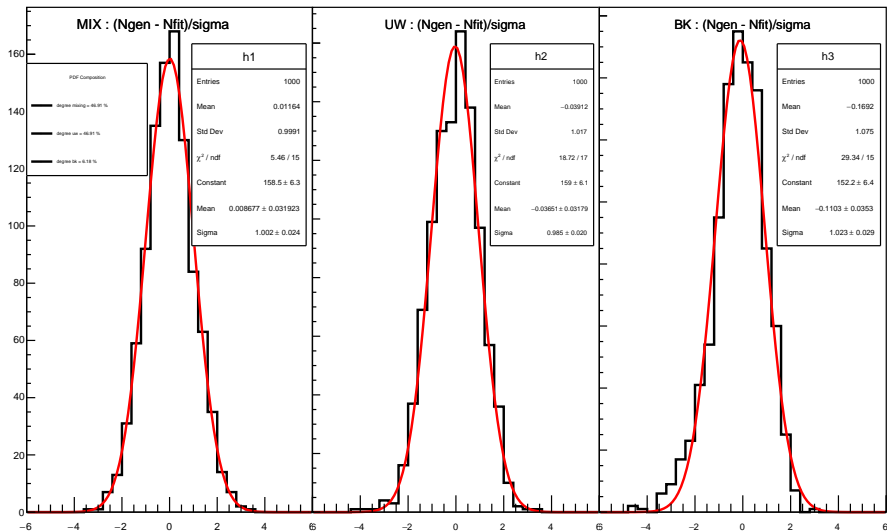
Data taken from: r68465_uw_exp_freq4.vertex.csv

Analytic Fit



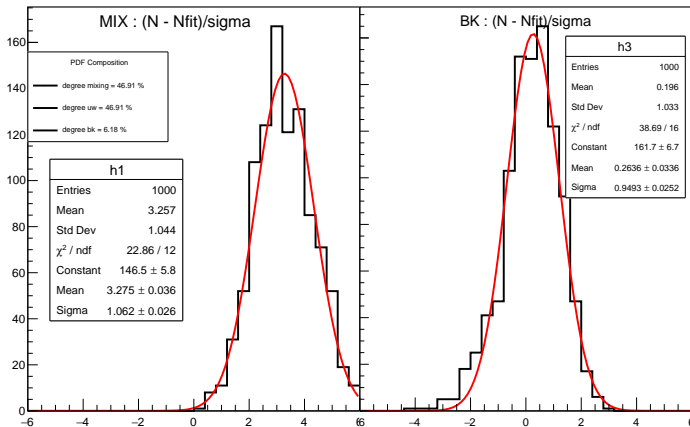
ADDITIONAL MATERIAL

$N_{mix} - N_{fit}$ for $a = 46\%$, $b = 46\%$, $c = 6\%$.



N_{uw} parameter of the fit model fixed

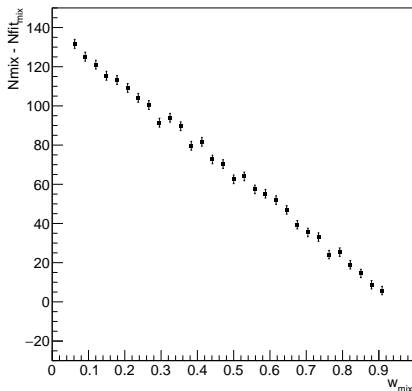
The Toy simulation is tested fixing the N_{uw} parameter of the fit model to 0. In the following plot the weight are $a = 46\%$, $b = 46\%$, $c = 6\%$, where c is fixed in such a way to reproduce the number of expected background events in `r68465_uw_exp_freq4.vertex.csv`, which correspond to 6% of the total events.



N_{uw} parameter of the fit model fixed

We study the bias $N_{mix} - N_{reconstructed}$ with the parameter N_{uw} of the fit model fixed to 0. For small value of w_{mix} , corresponding to small contribution of *Mixing* (and, conversely, a significant contribution of *Uwlosses* pdf) we observe a large bias.

N_{mix} Generated - reconstructed averaged over 100 trials



Graph

