

Notes about A1 trasverse asymmetry experiment

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The aim of these notes is to describe each parts of the analysis of the experiment A1 about the mesurement of the transverse asymmetry. The focus will be on the code of the program used to extract the physical asymmetry and the data collected by the detectors (from now on called detector A and B):

Structure of the Event Differently from the classic experiment of particle physics, in this experiment an Event is considered the amount of data collected by the two detectors over a temporal window that is 20 ms long. The data collected by the two detectors are the counts of scattered electron by a thin target of carbon and lead (10 mm for carbon and 5 mm for lead). The target respect the convention that his lenght is under 10% of the radiation lenght (to avoid double scattering events). Mami (*Mainzer Microtron*) is an accelerator that produce a continuos beam of electrons that is sent towards two different experiment (A1 and A2 collaborations). The energy at which Mami works for the experiment will be 0,57 GeV. The Cross section of the electrons with such amount of energy is dominated by elastic scattering. The physical quantity to measure is the asymmetry between the number of scattered electrons, using incident electrons with two different polarity state (\uparrow and \downarrow) transverse polarized with respect to the scattering plane.

$$asym = \frac{A_+ - A_-}{A_+ + A_-} \text{ (expected } \sim -20 \text{ ppm, } Q = 0,2 \text{ GeVc}^{-1}) \quad (1)$$

This quantity is computed for each event, that is diveded in 4 different sub-events. The polarity for each event can be of type $+, -, +$ or $-, +, -, +$, and is produced at the first stage of the accelerator, using circular polarized light to produce the polarized transverse beam. The polarization pattern is randomly selected using a De Bruijn sequence implemented using an arduino (*add photo and explanation*). The percentage of polarization for the beam is roughly 80%, and the reconstructed asymmetry should be scaled correctly by this factor. The counts are collected by two detectors, which are made, respectively, of three and nine pmts coupled to a fused silica bar.

1 Reconstruct the asymmetry

It's possible to obtain a raw exstimation of the asymmetry directly taking the average over all the asymmetry computed for each event. However this raw asymmetry needs to be corrected for variations in the beam that affect the measurement. The counts of the pmts can be slightly different due to the variation of the position of the beam on the target, the variations of the incident angles, the uncertain associated with the energy and the current of the beam. All this quantity can influence the asymmetry measured by the pmts, considering also that the expected asymmetry is in the order of ten part per million, and small asymmetry introduced by fluctuations on the beam parameters are not negligible. Correcting the false asymmetries that rise from those uncertainties is a tough task, and it's more easy to adopt a different strategy. Knowing that the beam parameters produced by Mami are quite stable over the time, we can assume a linear model as the following:

$$Asym = A_{physical} \cdot P + \delta_I + A_x \delta x + A_y \delta y + A_{\theta_x} \delta \theta_x + A_{\theta_y} \delta \theta_y + A_E \delta E \quad (2)$$

$A_{physical}$ is the aim of the experiment, A_x and A_y are the asymmetries induced by the variation of the posizion of the beam, A_{θ_x} and A_{θ_y} are the asymmetry associated to angles, A_E is the asymmetry associated to the beam energy. The relevant assumption is that, for small variation of the beam, the false asymmetry are

linearly dependent on the Beam uncertainties (that are $\delta x, \delta y, \delta\theta_x, \delta\theta_y, delta_E$), so a first order approximation seems valid. Collecting all the beam parameters for each sub-event allow the possibility to perform a linear fit to extract the physical asymmetry (the offset) and the false asymmetries. We will refer to these differences between the sub-events as correlated-differences.

2 Processing the Data

The RawData from each monitors are collected by the VFC, and need to be processed to obtain the physical quantity that are important for the analysis. (single and multichannel, synchronous voltage-to-frequency converters (AD7741)) were used for the Beam monitors. Data are obtained in the following way: an analog input signal is sent to the electronics, from $-V_{ref}$ to V_{ref} . The Output signal returned from the electronic is a square waves whose frequency is proportional to the input signal. The output frequency goes from $5\% f_{ref}$ to $45\% f_{ref}$ (with f_{ref} we are indicating the reference frequency of the VFC). For each monitors the measurements are about counting the number of pulses in the output signal, during a period of time that is roughly $20ms$. During the beam time the f_{ref} will be set to ~ 6 MHz, so a period of 20 ms correspond to a number of pulses of ~ 117000 . Following the logic of how the vfc are operating, we can derive the formula to convert the number of pulses that make up the data to the corresponding values in Volt.

$$V_{measured} = V_{range} \left(2 \frac{(N_{out} - 5\% \cdot Period)}{40\% \cdot Period} - 1 \right) \quad (3)$$

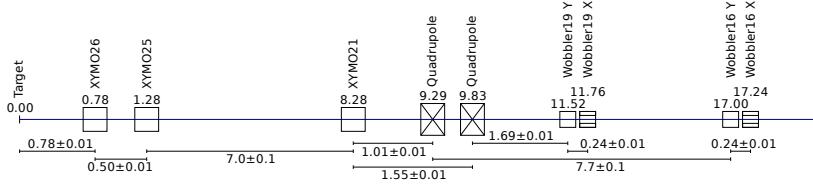
The number of output pulses is N_{out} , that goes from $5\% \cdot Period$ to $45\% \cdot Period$. The obtained values still are not physical values about the beam. We need to convert the Volt in physical quantity, as μm or μA . All the voltage values are converted in physical quantity using the following:

$$V_{phys} = (V_{measured} - offset) \cdot scale \quad (4)$$

all the factors needed for the conversion are obtained from dedicated calibration measurements during the beamtime. For the experiment, there are 11 monitors in total, which will measure the following quantity:

- **I21** and **I13** to measure the beam current.
- **E18** that measure the energy of the beam.
- **X21,Y21,X26,Y26,X25,Y26** to measure the position of the beam in the xy plane, with the convention that the beam is moving in the z direction.

For the beam line, and also for knowing the exact position of the monitors (needed to compute some values for the fit) it's useful to draw a scheme of the beam line here:



The position of the **X/Y** monitors in the figure (given in meters) are needed to compute:

- $x_{position}$ on the target
- $y_{position}$ on the target
- θ_x scattering x angle
- θ_y scattering y angle
- $E18$ energy of the Beam
- I Beam current

It is possible that those quantity are associated to false asymmetries that need to be corrected to obtain the physical transverse asymmetry we are interested to measure. To be precise the quantities used in the fit will be indicated as hcd, and are computed in a dedicated script of the analysis program, called *Calculation.cc*

$$\delta x = \frac{(x_{up,1} + x_{up,2})}{2} - \frac{(x_{down,1} + x_{down,2})}{2} \quad (5)$$

Where with 1,2 we are referring to the two sub-events with the same polarization. What is important to remember is that we are measuring the asymmetry about the number of counts of the spectrometer for different polarized scattered electrons. So the quantity that are more important for the analysis are the correlated-differences (hcd) defined as the average of the difference between the values measured for up-polarized electrons and down-polarized electrons.

Current asymmetry One the false asymmetry that needs to be included in the fit is the current asymmetry. It's the simplest false asymmetry to be corrected for the data. This is quite clear starting from the cross section definition:

$$\frac{dN}{dt} = I_0 n_t \frac{\sigma}{S} \quad (6)$$

where I_0 is the beam current, n_t is the density of the target, and S is the surface of the beam. With this we can directly compute the asymmetry:

$$Asym = \frac{\frac{dN_\uparrow}{dt} - \frac{dN_\downarrow}{dt}}{\frac{dN_\uparrow}{dt} + \frac{dN_\downarrow}{dt}} = \frac{\sigma_\uparrow I_0 \uparrow - \sigma_\downarrow I_0 \downarrow}{\sigma_\uparrow I_0 \uparrow + \sigma_\downarrow I_0 \downarrow} \quad (7)$$

Considering that the cross section slightly change for up/down polarization, to correct the current asymmetry we need:

$$Asym = \frac{I_{0\uparrow} - I_{0\downarrow}}{I_{0\uparrow} + I_{0\downarrow}}$$

this is a consequence of the fact that the luminosity is proportional to the beam current, so we don't need to add a new parameter to the model.

Energy correlated-difference The energy of the Beam directly change the cross-section, so the number of counts of the detectors. If there is a systematic change in energy from up to down polarized electrons, the asymmetry measured for each event can be different from what we expect.

Position The position of the beam on the target is computed considering that the particle are following a linear motion toward the target, so we describe the particles with the simply equation: $y = mx + q$. By imposing the passage of the particles at the y26, y25 and x26,x25 coordinates, we can obtain the hitting positions on the target. In our convention, the origin of the coordinate system overlap with the position of the target, so we need to compute the offset q . It's quite simple to show that the formula are:

$$q_x = \frac{X25Z21 - X21Z25}{Z21 - Z25} \quad (8)$$

$$q_y = \frac{Y25Z21 - Y21Z25}{Z21 - Z25} \quad (9)$$

Those data are stored in the data-tree. For each sub-events the position q_x e q_y is calculated, and it's stored in an array. An interesting details about the position of the beam on the target is that it will change during the data acquisition with lead, to prevent the target from melting.

Angle The angle useful for the analysis are the Θ_x and Θ_y angles on the target. These quantities are calculated with the following formula:

$$\Theta_{x,y} = \frac{(X/Y)_{25} + (X/Y)_{21}}{Z_{25} - Z_{21}} \quad (10)$$

with Z_{25} and Z_{21} the position of the two monitors in the beam line. This formula is obtained, also in this case, considering a linear motion and using the fact that the angles are supposed to be very small (so we can approximate the tangent to the first order).

pmts Counts The pmts counts are analyzed separately, using two different trees for handling the data: spekA and spekB. Because the two spectrometers (where our detectors will be placed) are allocated in different direction respect to the beam line, they will measure asymmetries with different signs. For each pmt that composes the spectrometer, there will be 4 different thresholds, selected with the Data acquisition board. The rawCounts are loaded from from the data files and stored in the data tree. As for the other monitors, in *Calculation.cc* a function calculates the offsetCorrectedCounts, loading from the file *standard.conf* the offsets of each pmt and then subtracting it from the rawCounts. Other values that are defined and computed are the Asymmetry, which doesn't need ad explanation, and the PolarityCorrelatedDifference and the rawIntraEventDifference, that are defined as:

$$pcd = \frac{Counts_{1,\uparrow} + Counts_{2,\uparrow} - Counts_{1,\downarrow} - Counts_{2,\downarrow}}{2}$$

$$ied = \max(Counts_{\uparrow}) - \min(Counts_{\downarrow})$$

These quantities are defined as the average of the difference between the counts of up and down polarized sub-events and the maximum intra event difference, and will be used to check if there are unexpected behaviors

in the data (neglecting the true and all the false asymmetries, we are supposed to see roughly the same number of counts for each of the sub-events) and cut out undesired events from the analysis). For the beam time four different threshold for each pmt will be selected and analyzed separately. This will lead, for dertcot B, to 12 different measure of the reconstructed asymmetry. The values will be averaged using the following formula:

$$\frac{\sum_{i=0}^{N_{detectorB/a}} \frac{A_i}{\sigma_i^2}}{\sum_{i=0}^{N_{spekb/a}} \frac{1}{\sigma_i^2}}$$

Now a scheme to summarize all the quantity that are computed and stored in the data tree, for the experiment:

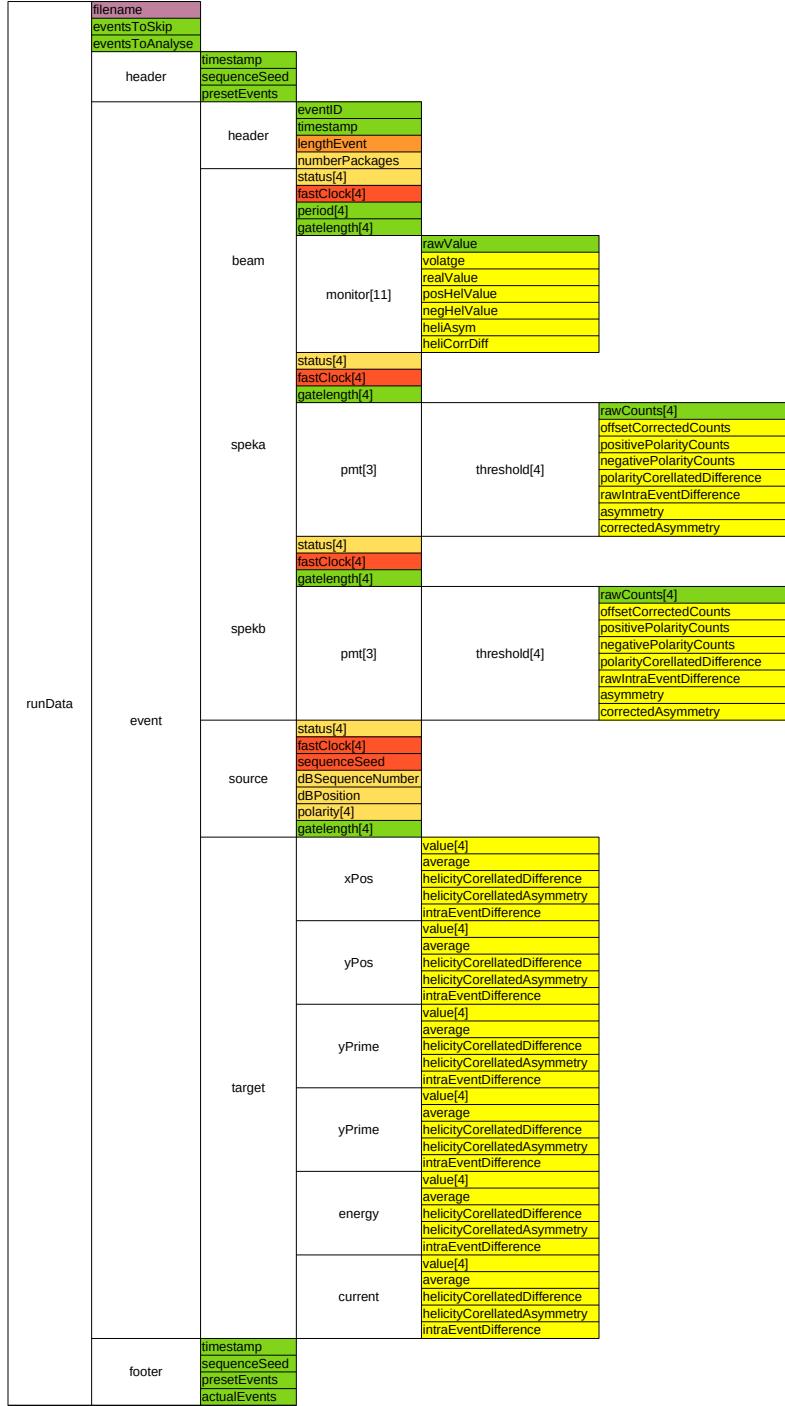


Figure 1: Scheme of the Data Tree

3 Electronic testing

For the next Beam time, the primary goal of the experiment is the evaluation of the electronics, that will be tested during the measure of the transverse asymmetry with carbon. The beam time is scheduled for the week (28/11 - 4/12) the electronics for the data acquisition needs to be tested, and also the correct settings for thresholds and voltage supply of the pmts needs to be set properly. At the beginning of the next beam time

some operations are needed, before taking data for the transverse asymmetry. It will be necessary to take pmts counts with different beam current, to check if the behaviour of the pmts is linear with the thresholds and the attenuation setted, and align the two spektrometers to the elastic scattering plane. Before the beam time, it is possible to study the counts of the pmts using cosmic rays, for selecting good values for thresholds, attenuation and power supply.

The number of events expected considering the size of the fused-silica coupled to the pmts (the detection part of the spektrometer B) is roughly $1 \text{ min}^{-1} \text{ cm}^{-1}$. So the expected number of Counts, considering $10 \text{ cm} \cdot 7 \text{ cm}$, is around 70 events, that produce Cherenkov light, collected by the dynodes of the pmts.

NINO board The Nino board is the device that is able to collect the number of pulses directly from the pmts. It's made by discriminators which compare the input signals (on the left side) to a signal that can be adjusted manually with the *pvDaq.py* scripts. For spekb the data acquisition is already available and is used to test the pmts, finding the good operation point. Here we display a photo of the Nino board (on the right side the connectors to the pmts of spekB):

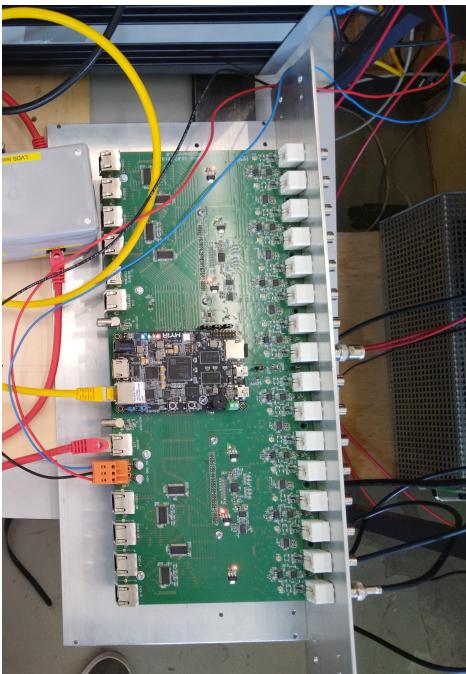


Figure 2: Nino board to read-out the input signals

For the Nino board there are two different parameters that can be adjusted: Threshold and Attenuation. The Threshold was set to a value equal to 600 for each of the three pmts of the spekb (following the instructions in the documentation), and we just changed the attenuation factor, to change the effective threshold of the pmts. It's important to notice that the Nino board is made in such a way that it doesn't compare to voltage signals, but read the total charge accumulated by the pulse and confront it with an internal threshold that can be changed. So it's not simple to identify a effective threshold in terms of voltage of the input signal. However the behaviour of the Nino board was studies before for the case of counting pulses from a scintillator detector, setting the threshold value at 750 (similar to our setting 600) and changing the attenuation. In this case a voltage threshold is shown, versus the attenuation:

It's important to remind that our conditions are slightly different: we are using a Cherenkov detector instead of a scintillator (different shape of the pulse) and a different value of the threshold. However this plot give us an indication of the trend of the threshold as a function of the attenuation. From the plot we see that around 500/600 there is a big variation in the NINO threshold, so the best working point for the pmts is around this values of the attenuation.

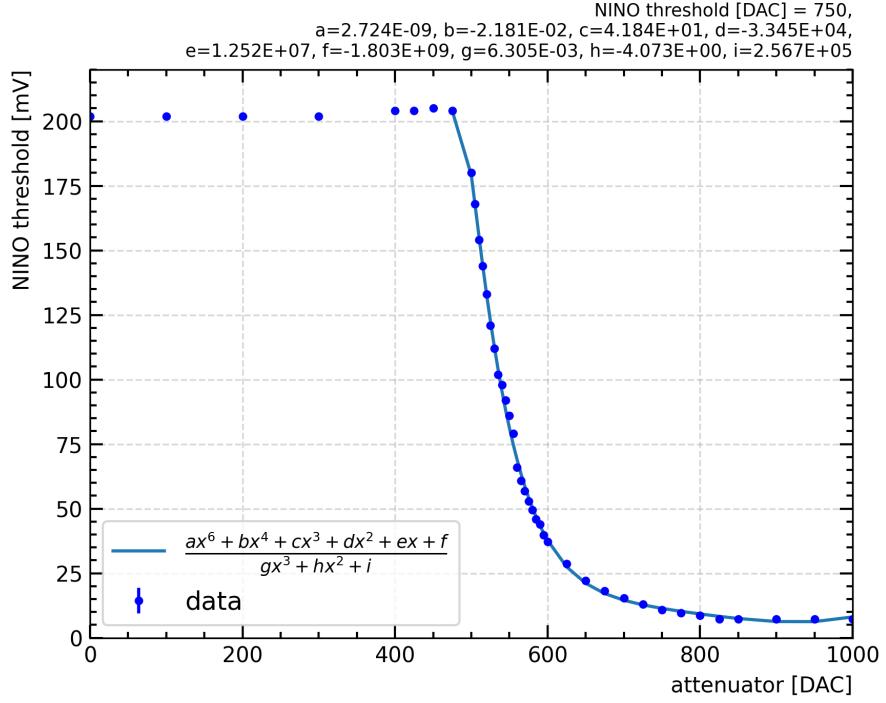


Figure 3: Calibration curve of the Nino board

Studying the pmts The pmts of the spekB are powered with a negative voltage around $\simeq -900$ V. Before taking the data we tried to observe some pulses at the oscilloscope, to check if the range of the power supply was correct :

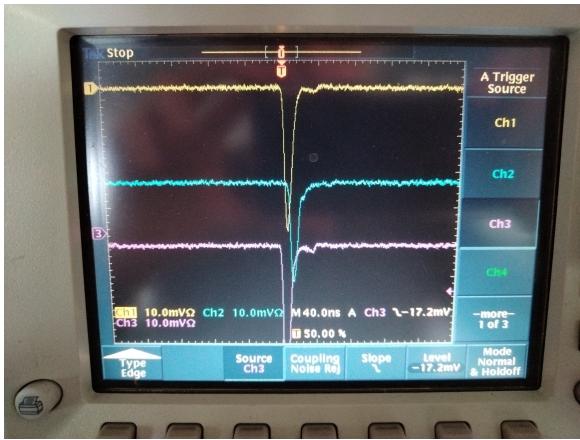


Figure 4: Signals of the three pmts of spekB observed at the oscilloscope, (threshold 10mV, CH1, CH2 CH3 are pmt 1,2,3)

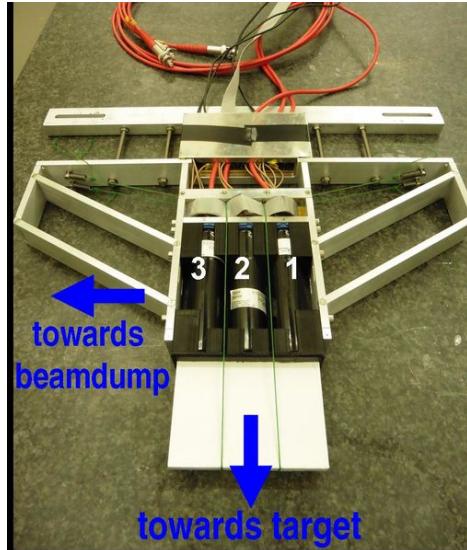


Figure 5: Spektrometer B

Then we started taking data varying the attenuation of the NINO board, with threshold fixed at 600. We decided to take a run on 1 min for some values of the attenuation, ranging from 300 to 3000 (maximum values is around 4000). Our interested is to select a region where the number of counts are scaling linearly with the attenuation and to identify the region where the behaviour for the pmts is no more linear (noise region). We observed a small knee in the plot, around the zone of 580 – 600 of attenuation, where the number of counts was almost constant, roughly equal to the number of expected events from muons hitting the detector. Reminding the figure (3), the threshold, around 500 – 600 of attenuation, has the correct value to let the NINO board to

collect the pulses produced by the muons.

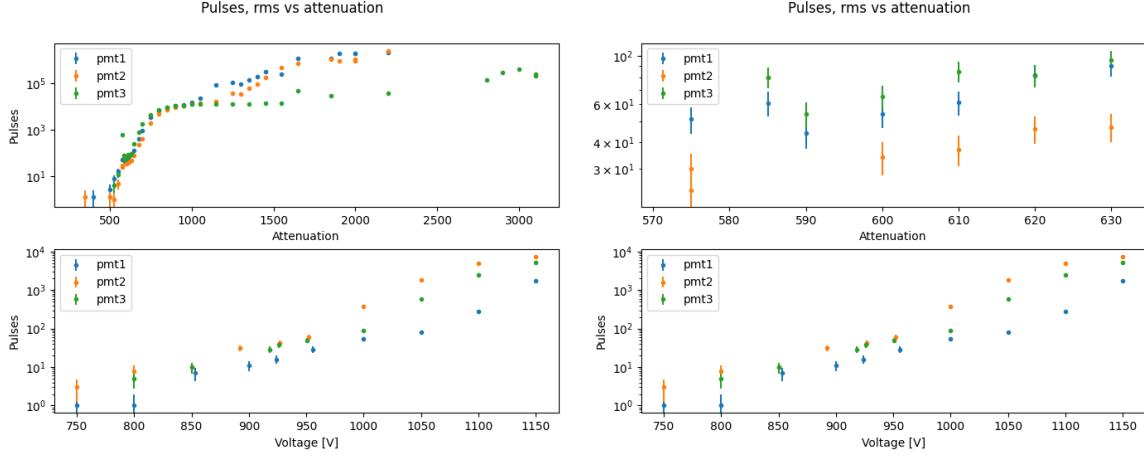


Figure 6: Counts of the NINO board versus attenuation (on the top) and voltage (below). On the left is possible to distinguish two different areas, one under $\simeq 750$ attenuation where there is linearity, and a zone on the left where the attenuation is too high and the noise is predominant.

Therefore, we decided to fix the attenuations of the pmt at 600. As we can observe from the plot on the right of figure 6 the pmt 1 and 3 have roughly the same number of counts. To equalize the behaviour of the three pmts, the power supply of the the second pmt was increased to have the same number of counts. At the end the power supply was fixed to -951 V, -925 V, -918 V.

At this point, we used a Pulser, that was able to produce signal with an high rate ($f = 13,17$ kHz). We plug the pulser directly in one of the input channenl of the NINO board, and took a run of 1 min log, to test how good the Daq is in counting the events. For a minute of run, considering that each sub-event last for 20 ms, we expect 750 events and 3000 sub-events. So the expected number of pulses for each event is:

$$\frac{60 \text{ s} \cdot f}{4 \cdot 750} = 263.4$$

The values that we obtained analyzing the run and taking the average counts, as shown in the following plot, is different, about the 75% of the number of counts expected. After some investigation we found that the problem was due to a wrong implementation on the fpga program in the Daq, that was resolved.

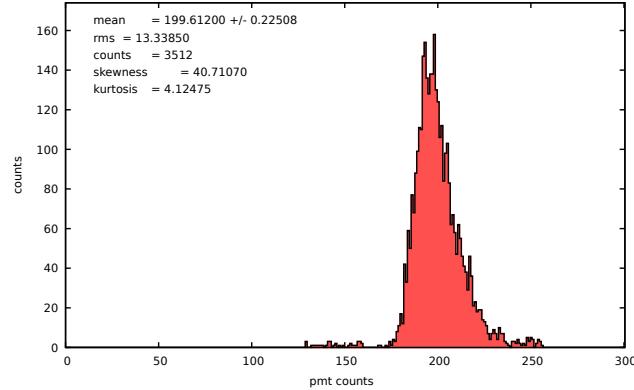


Figure 7: Counts of pmt 1 with the pulser

At this point we collected 10 runs, each of them 1 min long, to study the statistical fluctuation of the counts: we report here the obtained values:

Pmt:	1	2	3
1	58	60	62
2	62	55	59
3	61	59	70
4	73	66	70
5	68	66	56
6	59	52	64
7	69	74	77
8	48	49	57
9	70	54	58
10	60	61	66

This data are interesting to check if the counts are following the theoretical distribution of the events expected for cosmic rays at sea level. We know that the number of counts should be Poisson-distributed, following:

$$Pdf(\mu, k) = \frac{\mu^k}{k!} e^{-\mu} \quad (11)$$

The variance of the poisson distribution is equal to the mean of the counts, and we expect the same behaviour also for the sample mean and the sample variance:

$$\begin{aligned} \mu_1 &= 62.8 & \sigma_1^2 &= 54.40 & r_{12} &= 0.66 \\ \mu_2 &= 59.6 & \sigma_2^2 &= 57.15 & r_{23} &= 0.65 \\ \mu_3 &= 63.9 & \sigma_3^2 &= 46.98 & r_{13} &= 0.35 \end{aligned}$$

The third pmt has a variance lower than the expected, however the correlation between the nearby pmts is of quite high. Besides this, the correlation between the pmt 1 and 2, which are separated, is lower than the correlation between two adjacent pmts.

To check the correct operation of the detector, we exploited the possibility to observe coincidence using another pmt coupled to a plastic scintillator, placed above the detection area of the detector B:

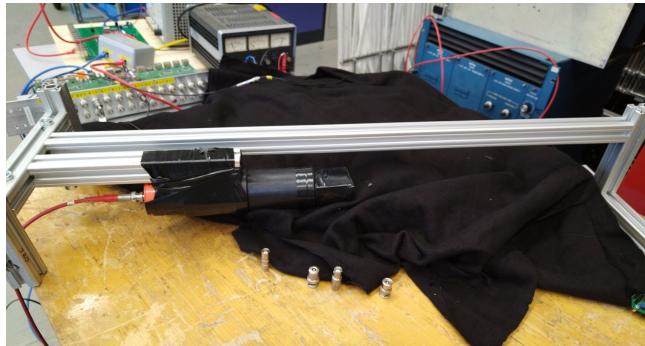


Figure 8: Setup to study the correlation between the pmts, the detector B was covered by a black blanket to shield the detector from optical photons.

	pmt0	pmt1	pmt2	pmt in coincidence
1	63	57	72	28
2	55	51	64	18
3	62	53	75	27
4	71	62	75	33
5	68	59	49	23
6	57	55	63	18
7	70	64	64	24
8	50	69	69	25
9	65	62	62	19
10	74	71	77	28

$$\begin{aligned}
 \mu_0 &= 63.5 & \sigma^2 &= 58.9 & r_3 &= 0.65 \\
 \mu_1 &= 60.3 & \sigma^2 &= 43.3 & r_2 &= 0.38 \\
 \mu_2 &= 67.0 & \sigma^2 &= 71.1 & r_1 &= 0.49
 \end{aligned}$$

The results are fine, we are able to see a positive correlation between the counts of the pmts in coincidence, and it is proof that the threshold, the voltage and attenuation were correctly set. The same procedures of calibration were performed on the Detector A, too. It is made by 9 pmts (but only 8 of them will be used for experiment). For the pmts 6,7,8,9 we finally selected a voltage of -1050 V , -1086 V , -950 V , -1050 V and an attenuation of 575 for all the four pmts:

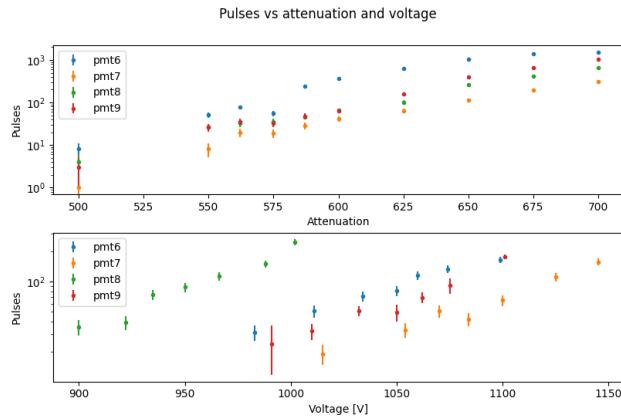


Figure 9: •

For the last 4 pmt used for the detector A, we raised the power of the pmt 4,3,2 down to -1450 V , and for 5 pmt to -1000 V in order to see some signals. Then we raised the threshold in the daq program up to 1000, and we tried to see some coincidence, with an attenuation of 750,725,775 for the pmt 4 3 2, (the pmt number 5 was not included, since we need one power supply for the pmt in coincidence).

pmt	4	3	2	pmt in coincidence
1	91	51	50	27
2	86	61	50	7
3	58	48	45	18
4	95	62	41	29
5	69	60	50	21
6	85	57	45	19
7	66	51	46	28
8	74	51	48	22
9	77	43	45	17
10	62	44	50	29

$$\begin{aligned}\mu_4 &= 76 & \sigma^2 &= 160 \\ \mu_3 &= 52.7 & \sigma^2 &= 49.8 \\ \mu_2 &= 47 & \sigma^2 &= 9.6\end{aligned}$$

This data are not what we expect, observing that for the other Detector we were able to see strong correlation with the single pmt in coincidence. Furthermore the variance of the counts is very different from the variance we expect from a poisson distribution. We decided to move the attenuation for the pmt 4,3,2 to the following values: 700 700 725 and take other 10 counts, one minute long, to see if the working point is better than before.

pmt	4	3	2	pmt in coincidence
1	43	36	30	13
2	56	30	46	17
3	49	42	35	23
4	34	27	33	16
5	60	38	49	19
6	54	44	38	20
7	54	42	36	17
8	47	44	51	16
9	48	41	43	14
10	49	39	31	16

$$\begin{aligned}\mu_4 &= 53.8 & \sigma^2 &= 49.4 & r_4 &= 0.41 \\ \mu_3 &= 33.6 & \sigma^2 &= 38.3 & r_3 &= 0.29 \\ \mu_2 &= 57.28 & \sigma^2 &= 39.2 & r_2 &= 0.09\end{aligned}$$

Now the pmt 4 and 3 seems to be in the correct values for threshold, attenuation and power. The last pmt has a variance less than the expected, and don't seem to be correlated with the other pmt. We decided to put the pmt in coincidence near to the second pmt, and raise the attenuation for the pmt number two, so now the attenuation is set to: 700,700,750 (725 coincidence, before 700).

pmt	4	3	2	pmt in coincidence
1	49	39	31	10
2	61	40	41	20
3	64	48	32	11
4	82	36	49	20
5	64	38	35	21
6	42	41	39	15
7	73	36	36	21
8	60	35	42	21
9	54	36	40	21
10	63	35	36	16

Now we report the mean count, the variance and the correlation between the pmt number two and the pmt in coincidence:

$$\mu_2 = 38.1 \quad \sigma^2 = 28.1 \quad r_2 = 0.63$$

The correlation is positive and high, so the behaviour of the pmt 2 seems correct, now. But for the pmt 4 and 3 we observed:

$$\begin{aligned}\mu_4 &= 61.2 & \sigma^2 &= 129 \\ \mu_3 &= 38.4 & \sigma^2 &= 15.8 \\ \mu_C &= 17.6 & \sigma^2 &= 18.7\end{aligned}$$

Here we see that the variance of the pmt 4 is roughly 2 times what we expect, while for the pmt 3 it is the half. This is quite surprising because all the values of the Detector A were fixed to the same values of the previous 10 runs, where the counts were in agreement with what we expect. Due to this strange behavior, we will focus our attention on calibrating the last four pmt, during the first day of the beam time, using directly the counts from the scattered electron.

Now we took some runs with pmt number 5

pmt 5	47	60	59	60	61	71	60	86	68	83
pmt in coincidence	16	17	17	16	21	14	17	19	12	23

The result are

$$\mu_5 = 65 \quad \sigma^2 = 128.6 \quad \mu_C = 17 \quad \sigma^2 = 7.2 \quad r = 0.29$$

For the last pmts of detectorA, we observe some differences from the expected behaviour. For the beam time, we will focus our attention on calibrating the last four pmt, carefully.

Now we report a table with all the final values of settings:

detector B	pmt 1	pmt 2	pmt 3
Voltage	-951 V	-925 V	-918 V
attenuation	600	600	600
threshold	600	600	600

Detector A	pmt 2	pmt 3	pmt 4	pmt 5	pmt 6	pmt 7	pmt 8	pmt9
Voltage	-1450 V	-1450 V	-1450 V	-1000 V	-1050 V	-1086 V	-950 V	-1050 V
attenuation	750	700	700	700	575	575	575	575
threshold	1000	1000	1000	1000	600	600	600	600

4 Analysis.cc

This is the main part of the Analysis program, where the data tree is filled and txt files with the data are produced for the fit.cc script, that will extract with the desired regression the parameters from the data. The program parses the RunData from the data acquisition board and start filling the *Data-tree*. With the script *HistosVoltage.cc* it's possible to create and fill some histograms, using the gnuplot library. At the beginning the program loads all the useful quantities stored in the *standard.conf* file, then it fills the data tree with the rawValues (VFC counts) for the monitors and the two detectors. After this, the program fills all the other values needed for the analysis, with the functions defined in the scripts *Calculation.cc*. Then the program calculates useful statistics for the *MomentumMethod.py* script, for a first estimation of the parameters.

following part still in italian, deprecated