

Exercício 2.7b

sexta-feira, 29 de setembro de 2023

10:00

b) Equações Reduzidas de Todas as Retas Tangentes à Curva $f(x) = 3x^3 + x + 4$, que Possam pelo Ponto $(1, 5)$

$$m = f'(x) = 9x^2 + 1$$

$$m = 9x^2 + 1$$

$$m = \frac{y_2 - y}{x_2 - x} = \frac{y_2 - 5}{x_2 - 1}$$

$$9x_2^2 + 1 = \frac{(3x_2^3 + x_2 + 4) - 5}{x_2 - 1}$$

$$(9x_2^2 + 1)(x_2 - 1) = 3x_2^3 + x_2 + 4 - 5$$

$$9x_2^3 - 9x_2^2 + x_2 - 1 = 3x_2^3 + x_2 - 1$$

$$9x_2^3 - 9x_2^2 + \cancel{x_2} - \cancel{1} - 3x_2^3 - \cancel{x_2} + \cancel{1} = 0$$

$$6x_2^3 - 9x_2^2 = 0$$

$$x^2(6x - 9) = 0$$

$$x^2 = 0$$

$$6x - 9 = 0$$

$$x = \frac{9}{6}$$

$$x = \frac{3}{2}$$

$$x = 0$$

$$m = 9(x)^2 + 1$$

$$= 9(0)^2 + 1$$

$$m = 1$$

$$f(0) = 3(0)^3 + 0 + 4$$

$$y = f(0) = 4$$

$$y = mx + b$$

$$4 = 1(0) + b$$

$$b = 4$$

$$y = x + 4$$

$$x = \frac{3}{2}$$

$$m = 9\left(\frac{3}{2}\right)^2 + 1$$

$$= 9\left(\frac{9}{4}\right) + 1$$

$$= \frac{81}{4} + 1$$

$$m = \frac{85}{4}$$

$$f\left(\frac{3}{2}\right) = 3\left(\frac{3}{2}\right)^3 + \frac{3}{2} + 4$$

$$= 3\left(\frac{27}{8}\right) + \frac{3}{2} + 4$$

$$= \frac{81}{8} + \frac{3}{2} + \frac{4}{1}$$

$$= \frac{81 + 12 + 32}{8}$$

$$y = f\left(\frac{3}{2}\right) = \frac{125}{8}$$

$$\frac{125}{8} = \frac{85}{4}\left(\frac{3}{2}\right) + b$$

$$\frac{125}{8} = \frac{255}{8} + b$$

$$\frac{125}{8} - \frac{255}{8} = b$$

$$\frac{125 - 255}{8} = b$$

$$b = -\frac{130}{8} = -\frac{65}{4}$$

$$y = \frac{85}{4}x - \frac{65}{4}$$

