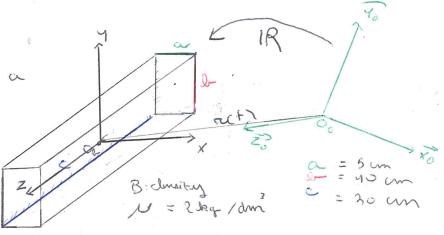
## (1)

## Tom Project for TEK4040 Mothematical Modelling of Dynamic systems

November 2022

Let us considerat a brick B with affire space



with center of mass & such that

B: For Obix, \$\overline{x}, \overline{y}, \overline{z} \gamma = \frac{1}{4}

Introducing inutial frome with affine space R

A: Fa= d 00, 180, MO, 72 4=104

introducing position vactor  $R(F) = \overline{O_0O_0}(F)$ and Rotation operator IR between  $y \circ y \to y \otimes y$ Auch  $E \cdot ho + IR = IR_{00} = IR_{00} = IR_{00} = R_{00}$ 

introducinos pusition vector  $\mathcal{P}_{\mathbf{c}} = \begin{bmatrix} P_1 \\ P_2 \\ P_3 \end{bmatrix} = \begin{bmatrix} \tilde{\gamma} \\ \tilde{\gamma} \\ \tilde{z} \end{bmatrix}$ 

such that  $z = \begin{bmatrix} \overline{Ouc}, \overline{x} \\ \overline{Ouc}, \overline{y} \end{bmatrix}$ 

 $\frac{1}{\sqrt{2}} = \iiint \left[ \frac{P_{2}^{2} + P_{3}^{2}}{-P_{2}P_{3}} \frac{-P_{4}P_{3}}{-P_{4}P_{3}^{2}} - P_{4}P_{3}^{2}} \right] \mathcal{N}(C) \, dr \, dr \, dr \, dz = \begin{bmatrix} J_{xx} \, J_{yy} \, J_{xz} \\ J_{xy} \, J_{yy} \, J_{yz} \\ J_{xy} \, J_{yz} \, J_{zz} \end{bmatrix}$   $CEB = \begin{bmatrix} J_{xx} \, J_{yy} \, J_{xz} \\ J_{xy} \, J_{yy} \, J_{yz} \\ J_{xz} \, J_{yz} \, J_{zz} \end{bmatrix}$ 

it con be shown that product of mention are mull become of symmetry:

Dif = - WSPiPs N OF OPD PR Li = Jopi = S[S[SP:PoN Opola]dpl = SSNPE[[Pazz] -Li/2] dpicple Jic = MN [Po + Po ] NOPE JOOPE = NL: VS [Pi2+Pi2] dph [ 3 + B2 P3] - Like OPh = NLid RLi + Li3 OPE

 $= \frac{1}{2} \left[ \frac{2}{3} + \frac{1}{2} \frac{1}{2} \frac{1}{2} \right]$   $= \frac{1}{2} \left[ \frac{2}{3} + \frac{1}{2} \frac{1}{2} \frac{1}{2} - \frac{1}{2} \frac{1}{2} \right]$   $= \frac{1}{2} \left[ \frac{1}{2} + \frac{1}{2} \frac{1}{2} \right]$   $= \frac{1}{2} \left[ \frac{1}{2} + \frac{1}{2} \frac{1}{2} \right]$ 

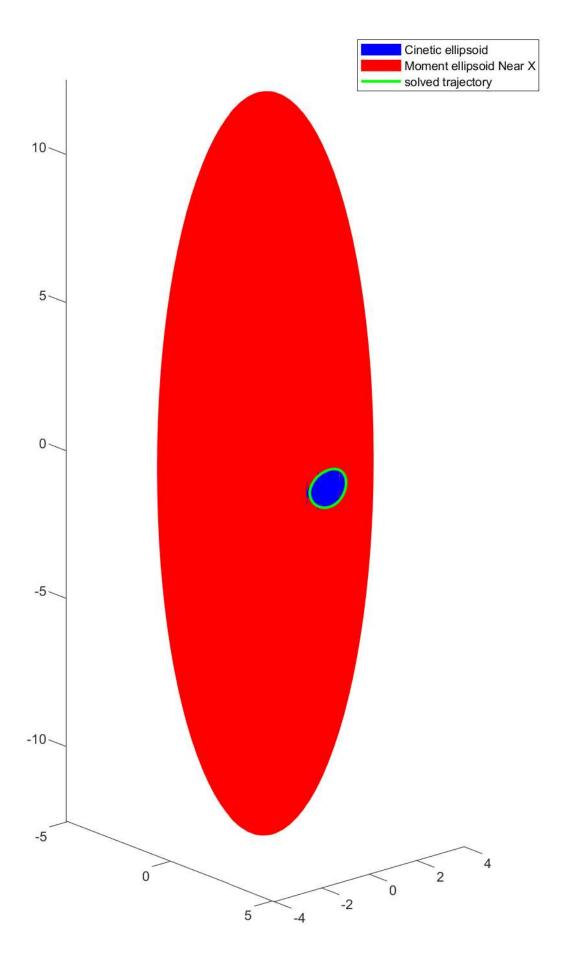
m = 2 e - 06 kg  $\int_{11}^{1} \approx 8,3 e - 09$  m.  $k_8 \cdot m^2$   $\int_{22}^{1} \approx 7,083 e - 09$   $kg \cdot m^2$   $\int_{33}^{6} \approx 2,083 e - 09$   $kg \cdot m^2$ 

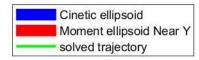
Dell'Given constant energy J, the inertice ellipseid ir defined wat to all It [ ?] J Xr Jb Xt = J  $(=) \frac{1}{2} \begin{bmatrix} P_1, P_2, P_3 \end{bmatrix} \begin{bmatrix} J_{77} & 0 & 0 \\ 0 & J_{22} & 0 \\ 0 & 0 & J_{33} \end{bmatrix} \begin{bmatrix} P_2 \\ P_3 \\ P_3 \end{bmatrix} = J$ needed Ju Pi + Jo2 2 + J33 P3 = J  $\frac{P_1^2}{25} + \frac{P_2^2}{25} + \frac{P_3^2}{25} = 4$ Jn 522 537 Co this is an ellipsuid with holy axis Given free torque metion the kinetic restation energy disposed from euler equations [ 500 mg] [ for all (iii), h), i x j x k, k = 0+1 [3] (using J = [ -0m 52 ] ] m: = 0 = J: W: + Wowk (Jak - Jin) 0 = Jic W. W. + W. W. W. (Jak - Ji)  $= \sum_{i=0}^{2} J_{ii} w_{i} w_{i}$   $= \sum_{i=0}^{2} J_{ii} w_{i} w_{i}$ => ) J. f. w. w. > S Si Wiwidt = K  $\frac{\omega^2}{2K} = I \Rightarrow \frac{\text{ellipsoid}}{\text{half axin}}$   $\alpha := \sqrt{2\pi}$   $\alpha := \sqrt{2\pi}$ a: = 125

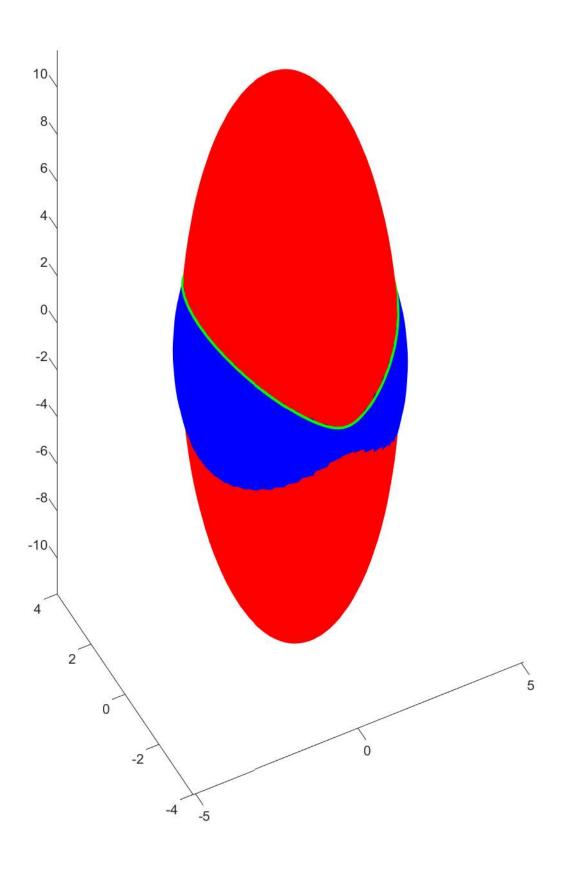
Given free torque metium: Else angular momentum Delipour is derived from => 11 he ! = ho ( wonstant length ( he = Jo Wo = [ Jan war ] (he) (he) = ho = Jxxwx + Jyy wy + Jzz wz We will perform retation along axis "new" \$ , is , \overline{\chi} ; with the some binetic energy ar a pure netation along Z of periode T = 1s. ( > K = 1 Wz Jzz ~ 4,44e=08 lkg.m².rad².j-2 N.m. + 1, rad² We can find  $W_x = \sqrt{2k} \approx 3.1446$  rad/s

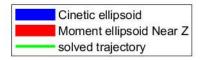
Similarly  $W_y = \sqrt{2k} \approx 3.9675$  and/s such that With = [wx] and Whey = [wy]
gives some kinetic energy or Whyz

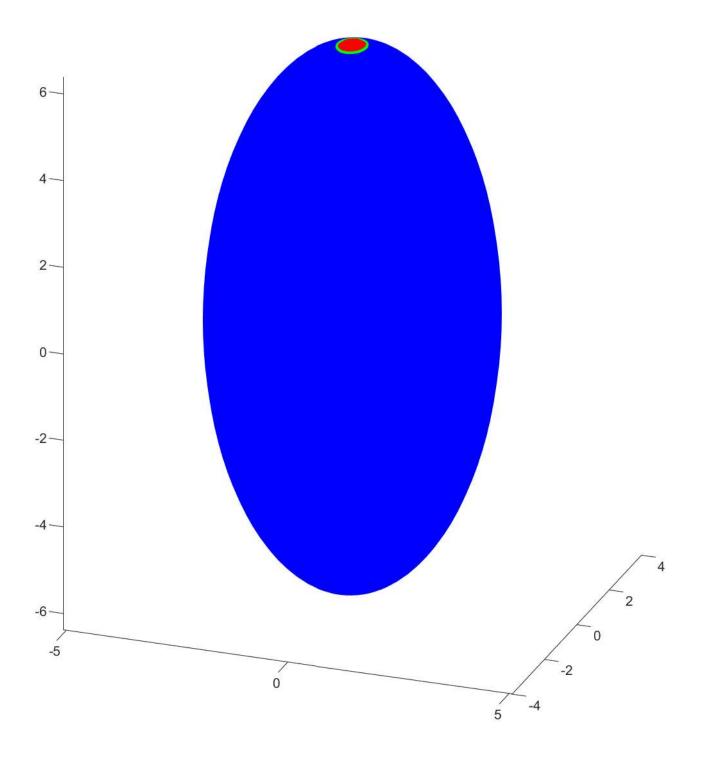
5 We will have WK Med z = WX Wer menz = [Wx.neorz] We meany = [ Wy ] = Wz meany = Wz meany = Wz Wit mean = [ Wx mean x] such that Emogy induced is equal to Ki it was also shown that  $W_2 = W_2 \sqrt{1 - \frac{W_r meorz}{W_x^2}}$   $W_1 = W_y \sqrt{1 - \frac{1}{100}}$   $W_x = W_x \sqrt{1 - \frac{1}{100}}$ S Wz = 6.8817 mod (s Wy = 3.3905 wd /s Wy = 3.125₽ wd / ~ ( Olipseid available after ) 3)  $W = \begin{bmatrix} \omega_{x} \\ \omega_{z} \end{bmatrix}$   $A(w) = \begin{bmatrix} \frac{1}{2\sqrt{1}}(\sqrt{1}) & \frac{1}{2\sqrt{$ it can be shown that with outer equotions (0) w= A(w) w the ellipsaids with selutions from (0) are printed below











We had  $\hat{w} = A(w) w (y)$ , we can find  $\hat{y} = \hat{y} = \hat{y$ 

Videos:

https://www.youtube.com/watch?v=pLlyY7RrBN0ab\_channel=Adrien

Source code:

https://github.com/Adrien9o2/TEK4040-A1