

Empirical Review of Models used for Predicting Financial Market Crashes Using Market Data

Project: Literature Review

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Background and Introduction **Adrien (Goes with Background)**

We are not the first to approach this subject. Multiple papers have approached prediction of stock market crashes using Machine Learning. In a time series analysis approach, models used have traditionally included RNNs and Arima, and more recently Transformers [1] [2]. These models have been successfully and often used in Market Crash prediction [3].

Reviews and comparisons of these models, such as this project aims to do, have been made such as [3], but a comprehensive empirical review of Time-Series Analysis models on equal footing is lacking in literature. This project aims to address this lack, by providing an empirical comparison of the three aforementioned commonly used models in Time-Series Analysis (Arima models, RNNs and Transformers) to predict Market Crashes. [1] [2] We shall use data freely available on the Yahoo finance database, and tag historically factual Market Crashes by hand, as there are only few. We shall use the crashes as listed in this National Bureau of Economic Research's report. [4]

Methodology

When first looking at a time series, we need to know that whether there it is **stationary** or **non-stationary**, which means

- Justify why we chose those three models by finding similar work **Oscar ?** This might be good: <https://oarjst.com/sites/default/files/OARJST-2024-0095.pdf>

ARIMA on predicting market crash **Oscar**

Time series in stock market are mostly non-stationary. But except for differences in the local level or in trend, all parts of the series behave in a similar way [Box et al. 2015]. Box et al suggested a model called Autoregressive Integrated Moving Average (ARIMA) model which combines autoregression model and moving average model. It is a models that can be used in non-stationary time series to make prediction [M K Ho et al 2021 J. Phys.: Conf. Ser. 1988 012041]. The ARIMA model $ARIMA(p, d, q)$ has general form [Box et al. 2015]:

$$\varphi(B)z_t = \phi(B)\nabla^d z_t = \theta_0 + \theta(B)a_t$$

where

1. $\phi(B)$ is the autoregressive part with p degrees,
2. $\theta(B)$ is the moving average part with q degrees,
3. ∇ is the integrated (degree of differencing) part with d degrees,
4. and θ_0 is the constant term.

Using ACF (autocorrelation function) and PACF (partial ACF) can help us decide the hyperparameters p, d, q for building our model [Hyndman et al. 2018].

Recurrent Neural Networks **Adrien**

Recurrent Neural Networks are a class of neural network architectures designed to detect patterns in sequential data, such as handwriting, genomes, text, or numerical time series. [5] They have been used in multiple projects accounting to market Crashes, such as this project led by Tolo et al. [6]

Transformers **Inigo**

Transformers are neural network architectures that are based on "self-attention mechanisms" (allowing the model to weigh the importance of different elements in the input by computing attention scores between all positions) to model dependencies in sequential data. While Transformers were originally developed for natural language processing tasks like machine translation [Vaswani et al., "Attention is All You Need"], they have become popular for time series forecasting due to their ability to handle long-range dependencies.

Transformers can capture complex temporal patterns by assigning varying importance to different time steps, which is particularly useful in fluctuating/volatile financial markets. In fact, Zhou et al. demonstrated this with the Informer model, which efficiently handles long sequences and improves forecasting accuracy using self-attention [Zhou et al., "Informer: Beyond Efficient Transformer for Long Sequence Time-Series Forecasting"]. Moreover, Lim et al. were even able to outperform traditional methods by combining Transformer architecture with recurrent layers [Lim et al., "Temporal Fusion Transformers for Interpretable Multi-horizon Time Series Forecasting"].

Hence, the literature suggests that Transformers are a pertinent choice for identifying complex patterns in financial time series, as they can model dependencies across multiple time scales, potentially improving the precision of crash predictions compared to traditional methods like ARIMA and standard RNNs.

Criteria and Analysis **Oscar?**

- Summarize criteria and metrics in literature for comparing models.
- Justify the selection of those comparison methods based on sources

References

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