

CSI 3350: PROGRAMMING LANGUAGES

Department of Computer Science &
Engineering
Oakland University

What have we covered so far ?



- Described main quality criteria for high level programming languages such as readability, writability etc. (for example you can add new syntax to the language to facilitate the readability of your program using *define-syntax-rule*, *define-syntax* etc.)



- Described syntax of fundamental program components (*hw06 loop*, *block structure*, *scoping mechanism*, etc.,)



- Discussed fundamental concepts of operational semantics (*hw06*, coding the **value-of** function)

yet to cover



- Describe parameter passing and access to non-locals (hw07 – soon!)
- Described data types and type systems (*hw06*, *grammar*, *hw05*, *define-datatype*)



- Apply major features of functional programming languages (*hw01~hw04*, *map*, *foldl*, high order functions, *lambda* etc.)



- Described activation records (Sep 30 lecture notes, slides 43 ~ 66)

Road Ahead -

HW05 Due: Nov 12



HW06 Out Nov 13 (today), Due: Nov 24



Exam02 ← **Nov 27**



HW07



Final Exam : 7pm ~10pm : Dec 09, 2019

Road Ahead -

HW05 Due: Nov 12



HW06 Out Nov 13 (today), Due: Nov 24



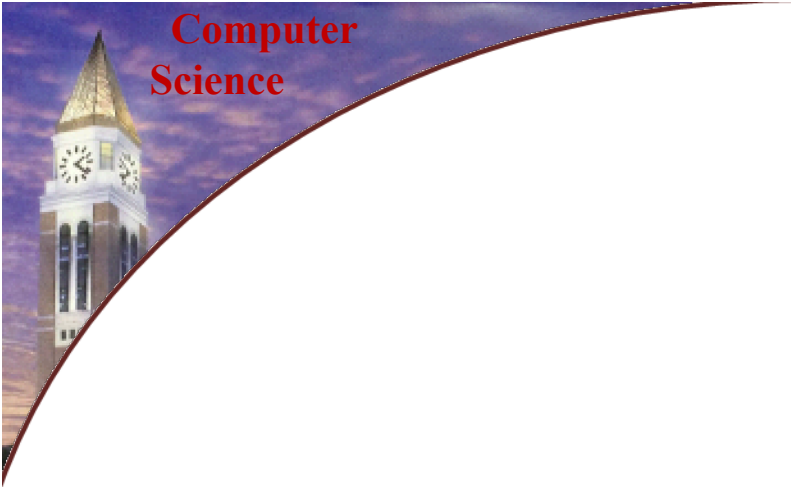
Exam02 ← **Nov 27**



HW07 adding procedure definition and
procedure call (parameter passing) into
the language implemented in hw06



Final Exam : 7pm ~10pm : Dec 09, 2019



closed book, closed notes, no electronic devices, but **1 page cheat-sheet allowed**

Exam 02

Time: 5:30pm ~ 7:17pm Wednesday, Nov 27th

Location: MSC 185

Coverage: HW05~06

Extend, and Modify the language implemented
in HW06 with new features.

CSI 3350
Fall 2019
Exam 2

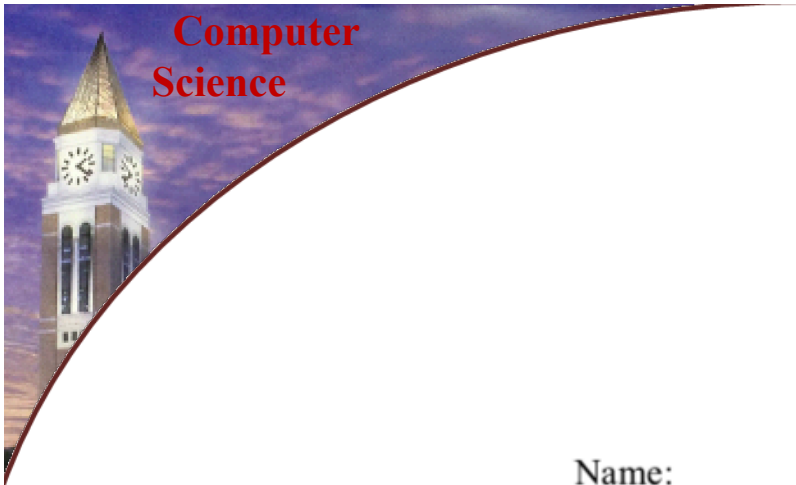
DO NOT OPEN THIS EXAM UNTIL INSTRUCTED TO DO SO

Name: _____

Student ID _____

- This exam is paper-based, closed book, no electronic devices, no headphones.
- Time limit: **110 minutes**.
- You are provided the following in a separate brochure:
 1. `hw06-solution.rkt`: the solution code for homework06
 2. `hw06-env-values.rkt`: which contains related data type definitions.
- Partial credit may be given for partially correct solutions.
- Use correct Scheme syntax; obvious syntax errors will cause deduction of points.
- Indentation is important to us for “clarity” reasons.
- You can use one (1) page (No bigger than 8.5 x 11 inch size, two (2) sides, no less than 9pt font) of notes, aka “cheat sheet”. Handwriting is okay. No photo-reduction is permitted. **These notes are to be handed in at the end of the test.** Have your name in the top right corner.
- You can use helping procedures whenever you like.
- Any questions please raise your hand and ask the exam proctor(s).

Good luck!



CSI 3350
Fall 2019

Exam 1 Make-up Questions

Name: _____

Student ID _____

- It is completely up to you if you would like to answer the following questions as a make-up for **exam 01**.
- Should you decide to complete them, you would receive up to 20 extra points, depending on the correctness of your answer. The summation of the earned **extra points** with your current score of exam 01 will be the **updated score of exam 01**.
- Any questions please raise your hand and ask the exam proctor(s).

Thank you!

Rule Of Thumb

Every expression will return a value!

For a program consisting of multiple expressions,
the **last** expression's value will be the value of
the overall expression!

a-program

- a-program consists of one or more expressions

```
(run "42")
```

```
(run "42  
    up(3)  
    #comment  
    down(4)  
    111")
```

HW06

(Problem 3)

```
<program> ::=
    <expr> <expr>* a-program

<expr> ::=
    number                "num-expr"
  | up(<expr>)             "up-expr"
  | down(<expr>)           "down-expr"
  | left(<expr>)           "left-expr"
  | right(<expr>)          "right-expr"

  | (<expr> <expr>)         "point-expr"
  | + <expr> <expr>        "add-expr"
  | origin? (<expr>)       "origin-expr"
  | if (<expr>)
    then <expr>
    else <expr>            "if-expr"

  | move (<expr> <expr> <expr>*) "move-expr"
```

HW06

(Problem 4)

<code><program> ::= <expr> <expr>*</code>	<code>"a-program"</code>
<code><expr> ::=</code>	
<code>number</code>	<code>"num-expr"</code>
<code> up(<expr>)</code>	<code>"up-expr"</code>
<code> down(<expr>)</code>	<code>"down-expr"</code>
<code> left(<expr>)</code>	<code>"left-expr"</code>
<code> right(<expr>)</code>	<code>"right-expr"</code>
<code> (<expr> <expr>)</code>	<code>"point-expr"</code>
<code> + <expr> <expr></code>	<code>"add-expr"</code>
<code> origin? (<expr>)</code>	<code>"origin-expr"</code>
<code> if (<expr>) then <expr> else <expr></code>	<code>"if-expr"</code>
<code> move (<expr> <expr> <expr>*)</code>	<code>"move-expr"</code>
<code> identifier</code>	<code>"iden-expr"</code>
<code> {<var-expr>* <expr>*}</code>	<code>"block-expr"</code>
 <code><var-expr> ::= val identifier = <expr></code>	<code>"val"</code>
<code> final val identifier = <expr></code>	<code>"final-val"</code>

A Block Expression Example (no nested blocks)

```
(check-equal?
  (run "{
    val x = up(3)
    val y = down(4)
    val z = + x y
    z
  }")
  (step-val (down-step 1))
  "you should be able to make use of previous variable definitions"
)
```

} Declaration List

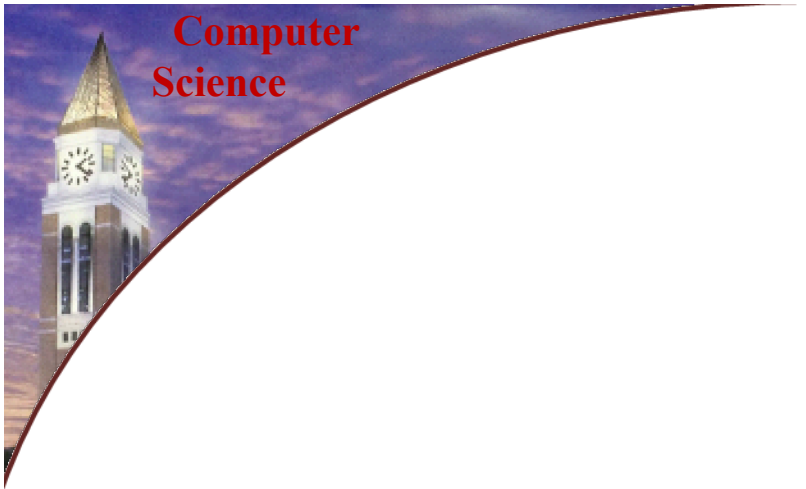
→ Value of the overall block expression

A Block Expression Example (with nested blocks)

```
(check-equal?  
  (run  
    "{  
      val x = 42  
      {  
        val y = 23  
        x  
      }  
    }")  
  (num-val 42)  
)
```

Nested Block Expression

Outer Block Expression



```
(run "{  
    val x = 42  
    x  
    val y = 33  
}")
```

<code><program> ::= <expr> <expr>*</code>	"a-program"
<code><expr> ::=</code>	
number	"num-expr"
up(<expr>)	"up-expr"
down(<expr>)	"down-expr"
left(<expr>)	"left-expr"
right(<expr>)	"right-expr"
(<expr> <expr>)	"point-expr"
+ <expr> <expr>	"add-expr"
origin? (<expr>)	"origin-expr"
if (<expr>) then <expr> else <expr>	"if-expr"
move (<expr> <expr> <expr>*)	"move-expr"
identifier	"iden-expr"
{<var-expr>* <expr>*}	"block-expr"
 <code><var-expr> ::= val identifier = <expr></code>	"val"
final val identifier = <expr>	"final-val"

```
(run "{
    val x = 42
    x
    val y = 33
}"))
```



`<program> ::= <expr> <expr>*`

"a-program"

`<expr> ::=`

number

"num-expr"

| up(<expr>)

"up-expr"

| down(<expr>)

"down-expr"

| left(<expr>)

"left-expr"

| right(<expr>)

"right-expr"

| (<expr> <expr>)

"point-expr"

| + <expr> <expr>

"add-expr"

| origin? (<expr>)

"origin-expr"

| if (<expr>) then <expr> else <expr>

"if-expr"

| move (<expr> <expr> <expr>*)

"move-expr"

| identifier

"iden-expr"

| {<var-expr>* <expr>*}

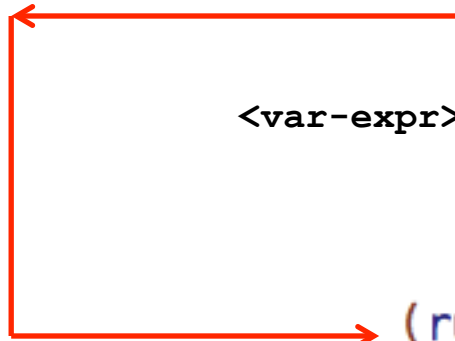
"block-expr"

`<var-expr> ::= val identifier = <expr>`

"val"

| final val identifier = <expr>

"final-val"



(run "{

val x = 42

x

val y = 33

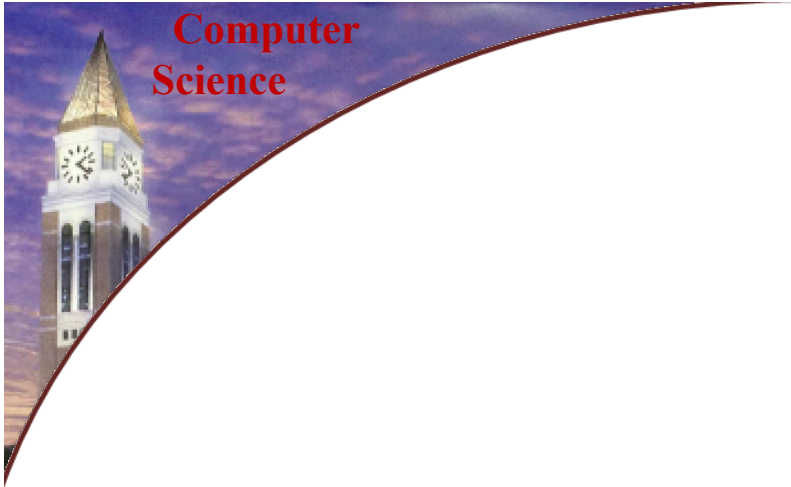
}

An <var-expr>
cannot follow an
<expr>

})

What is the Abstract Syntax Tree For the following?

```
"{  
  val x = 42  
  {  
    val x = 23  
  }  
  x  
}"
```



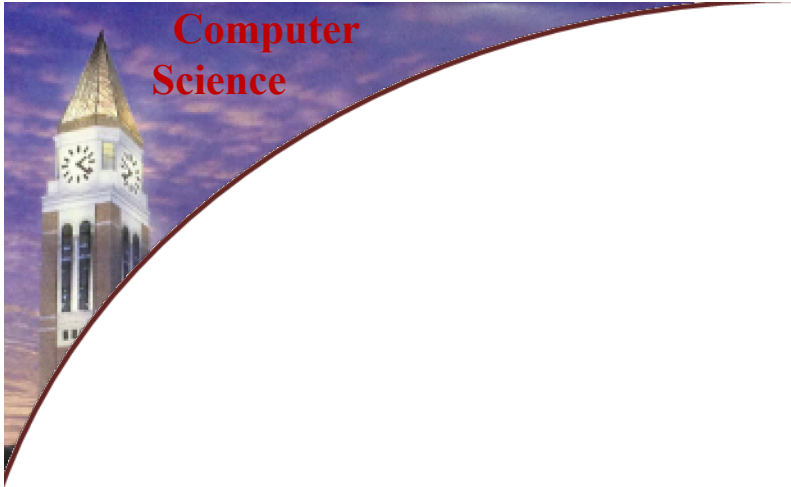
HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (raise (string-append "expected a program as string, got: " (~a program-string)))
      )
  )
```

; to kick off the interpreter here !

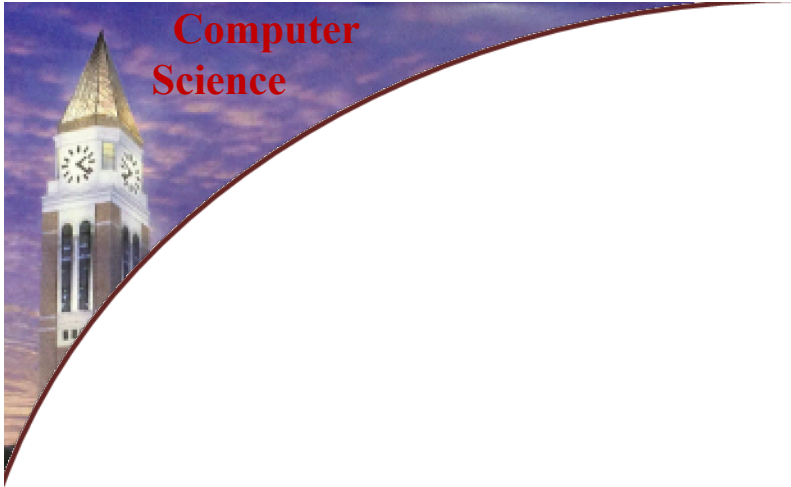


HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )
)
```



HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )
)
```

HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )
```

```
(define (value-of ast env)
```

```
)
```

HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )
```

```
(define (value-of ast env)
  (cond
    [(program? ast) (value-of-program ast env)]
    [(expr? ast) (value-of-expr ast env)]
    [(var-expr? ast) (value-of-var ast env)]
  )
)
```

HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )
```

```
(define (value-of ast env)
  (cond
    [(program? ast) (value-of-program ast env)]
    [(expr? ast) (value-of-expr ast env)]
    [(var-expr? ast) (value-of-var ast env)]
    [else (raise (~a "Unimplemented ast node: " ~a ast))]
  )
)
```

HW06

(Problem 4)

Further hints (code skeleton)

```
(define (run program-string)
  (if (string? program-string)
      (value-of (parser program-string) (empty-env)) ; to kick off the interpreter here !
      (raise (string-append "expected a program as string, got: " (~a program-string))))
  )

(define (value-of-program prog env)
  (cases program prog
    (a-program
     (expr rest-of-expressions)
     ;given a non-predicate function, andmap will apply the function
     ;to every element in the list and then return the value of
     ;applying the function on the last element.
     (andmap (lambda (ex) (value-of ex env))
              (flat-list expr rest-of-expressions)))
    )
  )
)
```


HW06

(Problem 3)

```
<program> ::=
    <expr> <expr>* a-program

<expr> ::=
    number                "num-expr"
  | up(<expr>)             "up-expr"
  | down(<expr>)           "down-expr"
  | left(<expr>)           "left-expr"
  | right(<expr>)          "right-expr"

  | (<expr> <expr>)         "point-expr"
  | + <expr> <expr>        "add-expr"
  | origin? (<expr>)       "origin-expr"
  | if (<expr>)
    then <expr>
    else <expr>            "if-expr"

  | move (<expr> <expr> <expr>*) "move-expr"
```

HW06

(Problem 3)

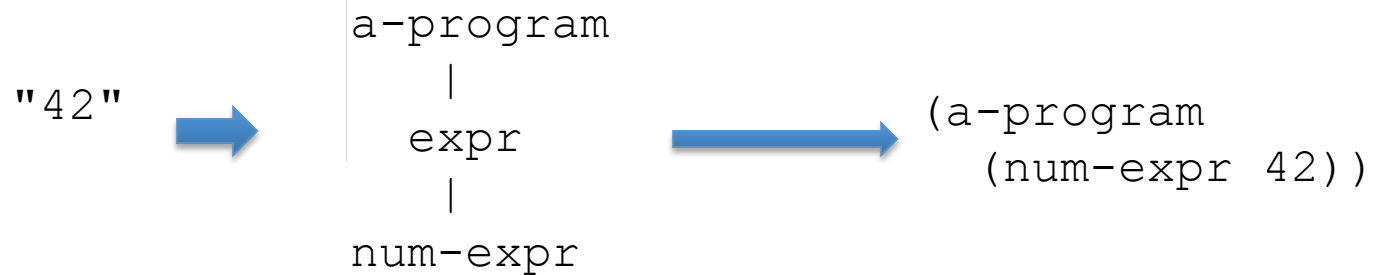
```
<program> ::=
    <expr> <expr>* a-program
<expr> ::=
    number                "num-expr"
  | up(<expr>)             "up-expr"
  | down(<expr>)           "down-expr"
  | left(<expr>)           "left-expr"
  | right(<expr>)          "right-expr"
```

```
(define-datatype program program?
  (a-program (first-exp expr?) (rest (list-of expr?))))
```

```
(define-datatype expr expr?
  (num-expr (n number?))
  (up-expr  (s expr?))
  (down-expr (s expr?))
  (left-expr (s expr?))
  (right-expr (s expr?)))
```

a-program

- What is the AST for "42" ?

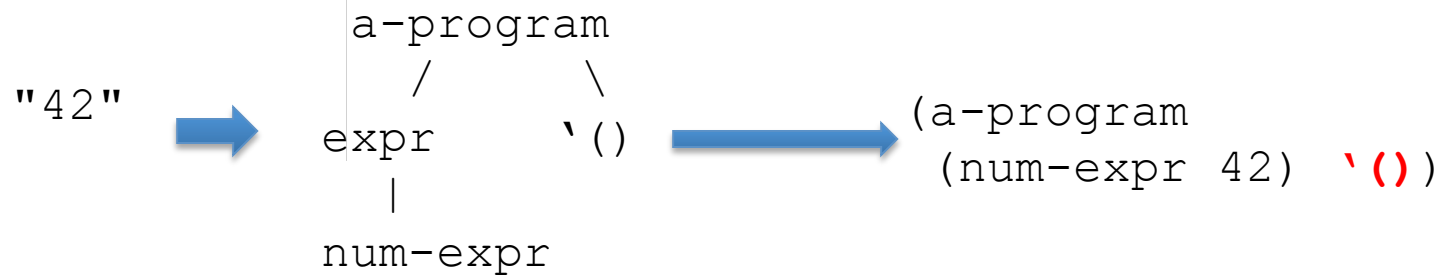


```

<program> ::=
    <expr> <expr>* a-program
<expr> ::=
    number                "num-expr"
  | up(<expr>)            "up-expr"
  | down(<expr>)          "down-expr"
  | left(<expr>)           "left-expr"
  | right(<expr>)          "right-expr"
  
```

a-program

- What is the AST for "42" ?



```

<program> ::=
    <expr> <expr>*  a-program

<expr> ::=
    number           "num-expr"
  | up(<expr>)       "up-expr"
  | down(<expr>)     "down-expr"
  | left(<expr>)     "left-expr"
  | right(<expr>)    "right-expr"
  
```

a-program

- What is the AST for "42"?



```
<program> ::=
    <expr> <expr>*  a-program
<expr> ::=
    number           "num-expr"
  | up(<expr>)       "up-expr"
  | down(<expr>)     "down-expr"
  | left(<expr>)     "left-expr"
  | right(<expr>)    "right-expr"
```

a-program

- What is the AST for "42"?



```
<program> ::=
    <expr> <expr>*    a-program
<expr> ::=
    number            "num-expr"
    | up(<expr>)       "up-expr"
    | down(<expr>)      "down-expr"
    | left(<expr>)      "left-expr"
    | right(<expr>)     "right-expr"
```

a-program

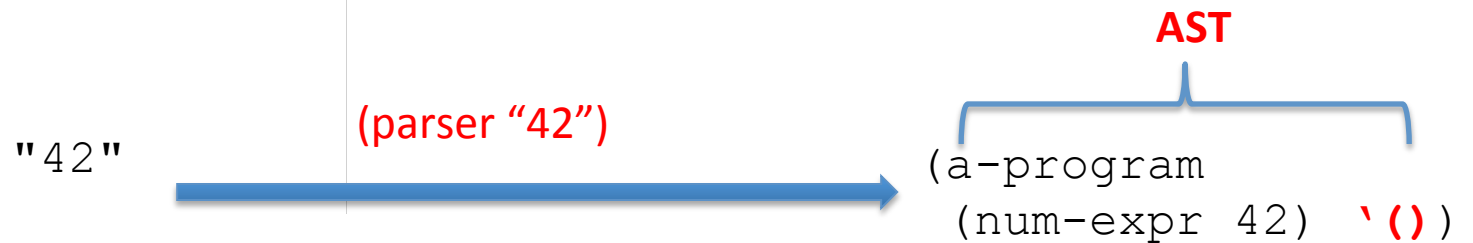
- What is the AST for "42"?



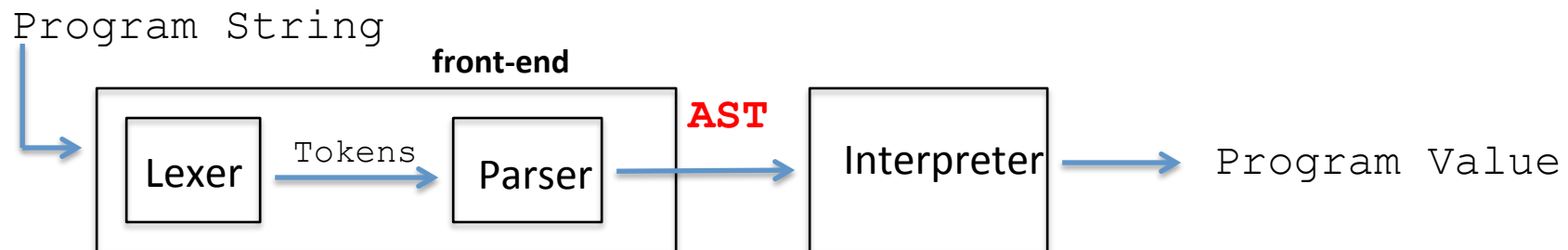
What should (run "42") return?

a-program

- What is the AST for "42"?



What should (run "42") return?

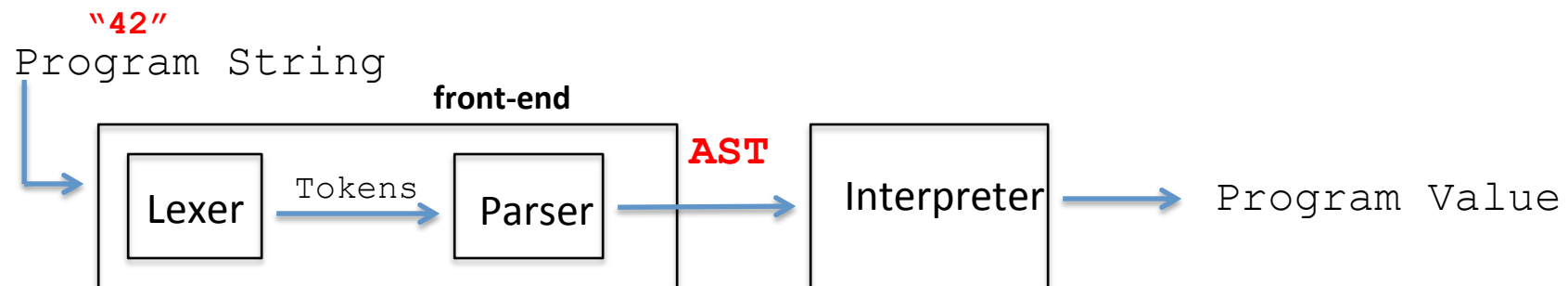


a-program

- What is the AST for "42"?



What should (run "42") return?

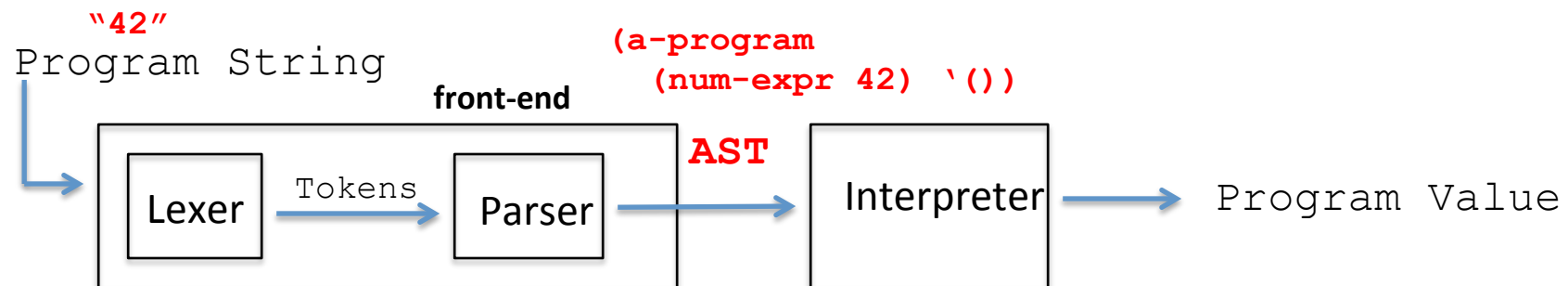


a-program

- What is the AST for "42"?

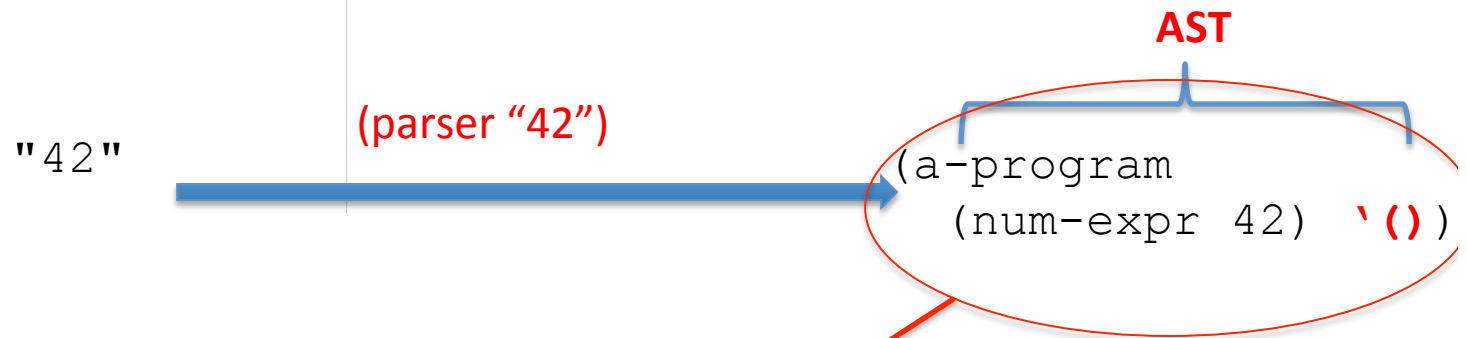


What should `(run "42")` return?

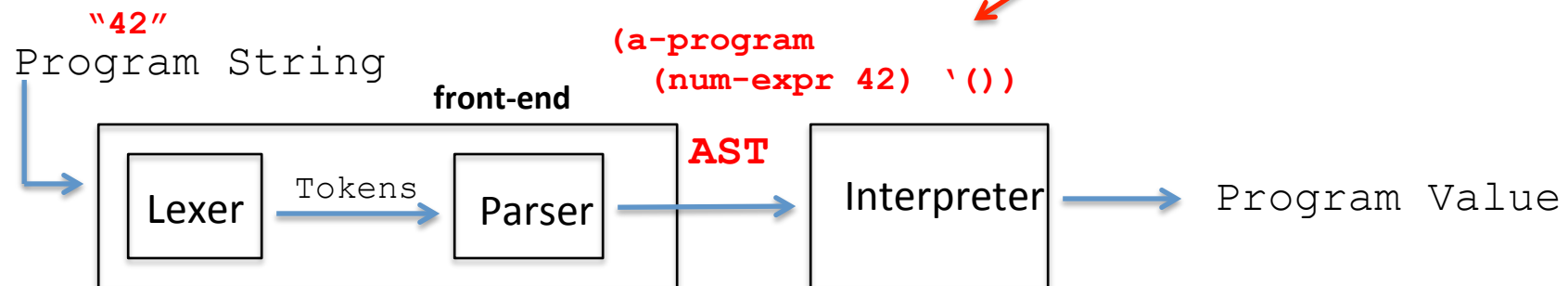


a-program

- What is the AST for "42"?



What should (run "42") return?

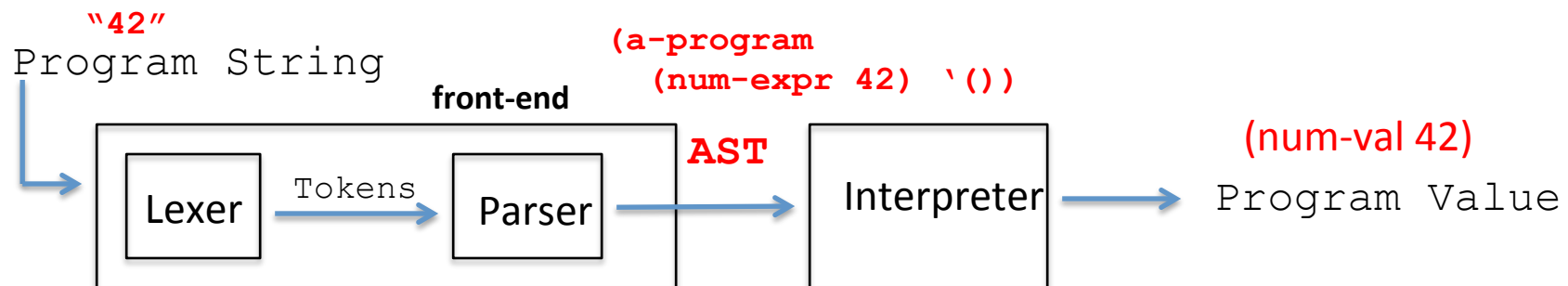


a-program

- What is the AST for "42"?



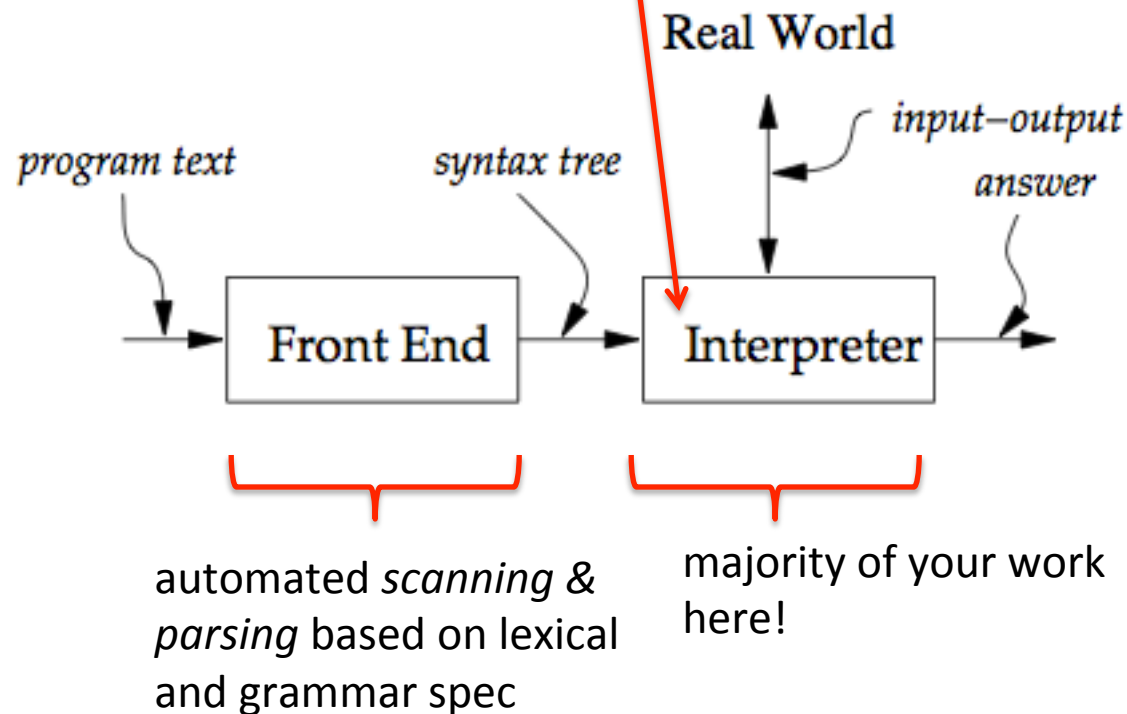
What should (run "42") return?



The Basic Form Of The Interpreter

problem 3

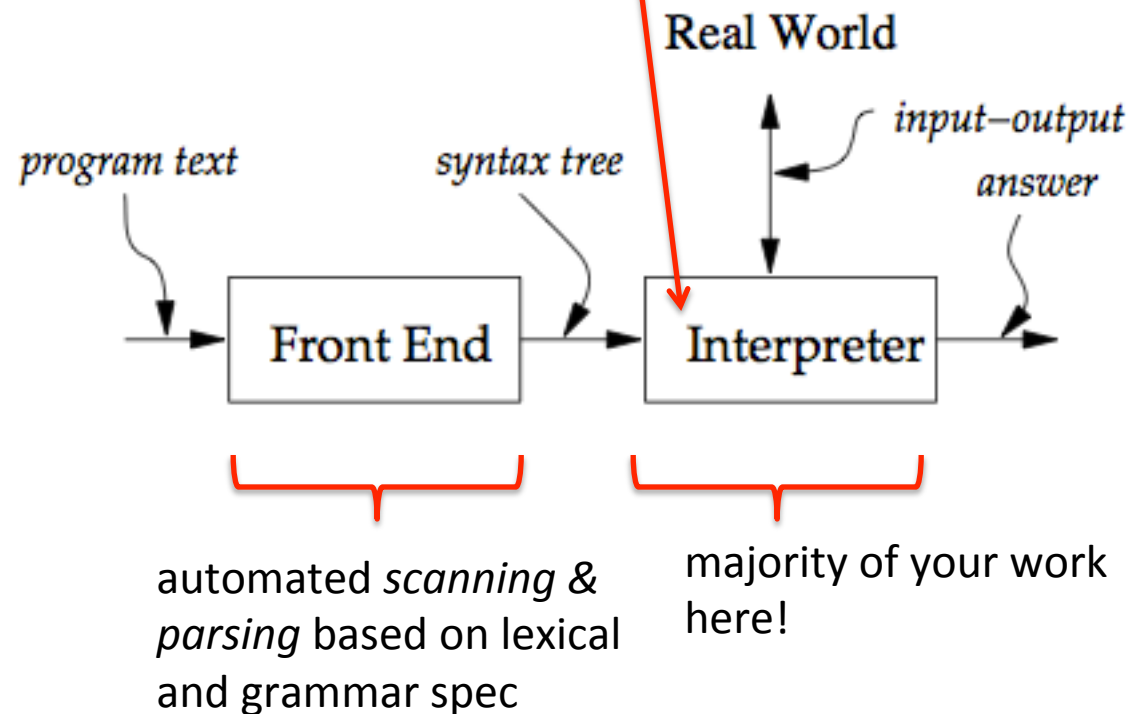
`(value-of-program ast) => expressed-val`



The Basic Form Of The Interpreter

problem 4

`(value-of-program ast env) => expressed-val`

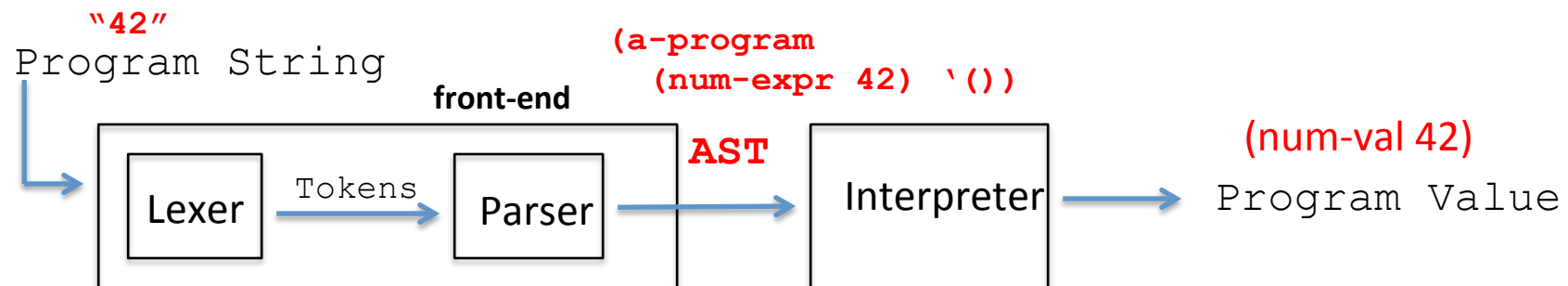


a-program

- What is the AST for "42"?



What should (run "42") return?



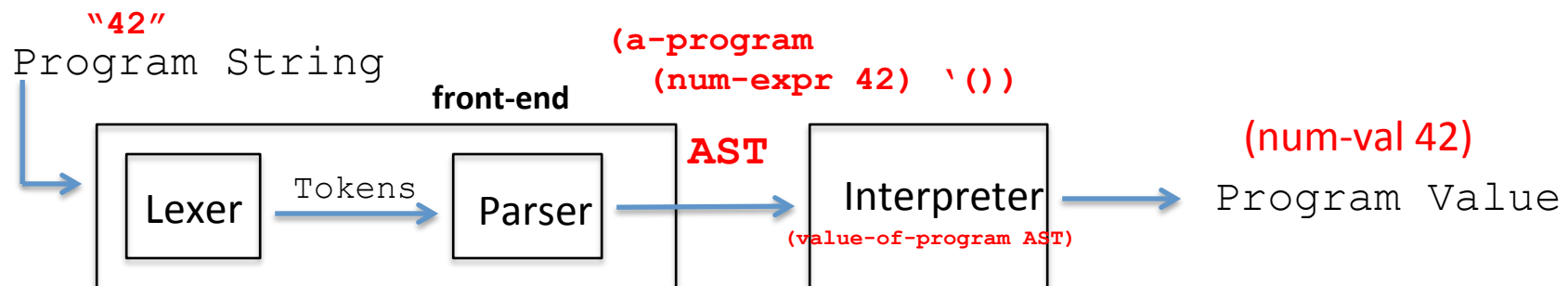
a-program

HW06
Problem 3

- What is the AST for "42"?



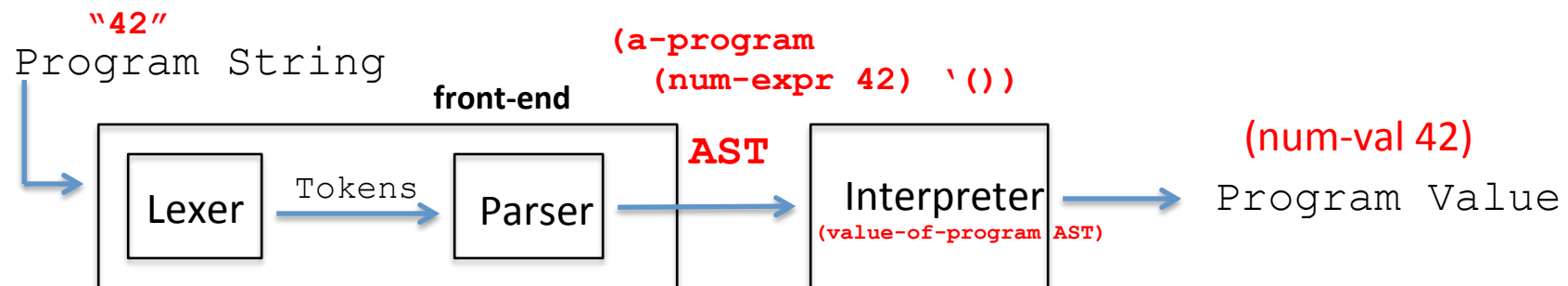
What should (run "42") return?



Intermediate steps

HW06
Problem 3

- (value-of-program ast)



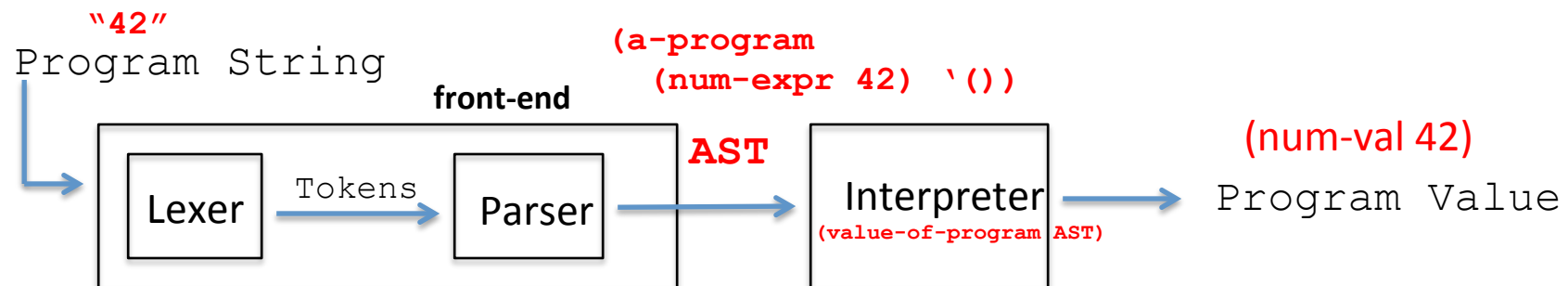
Intermediate steps

HW06
Problem 3

- (value-of-program ast)



replace ast with (a-program (num-expr 42) `())



Intermediate steps

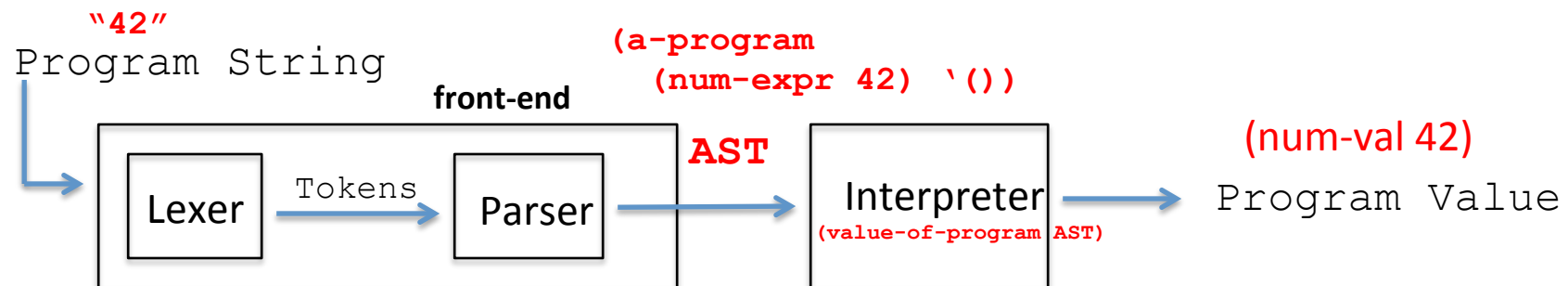
HW06
Problem 3

- (value-of-program ast)



automatically by (parser "42")

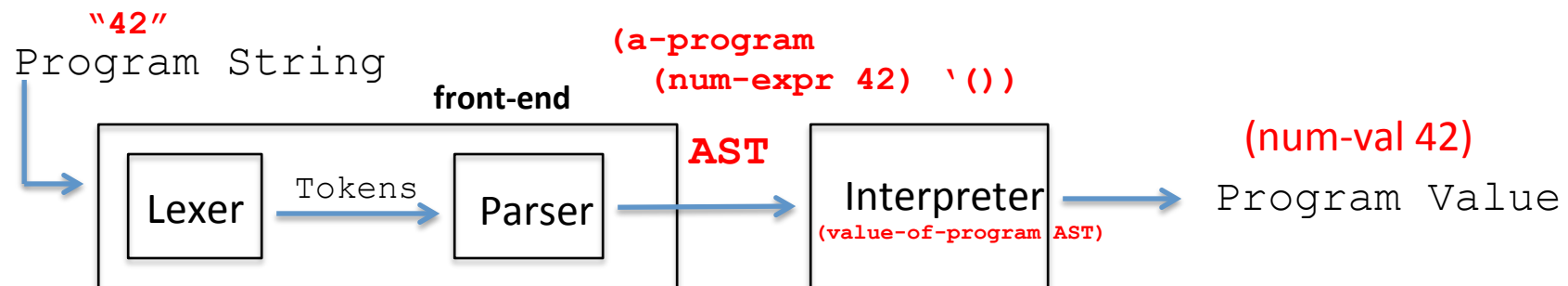
replace ast with (a-program (num-expr 42) `())



Intermediate steps

HW06
Problem 3

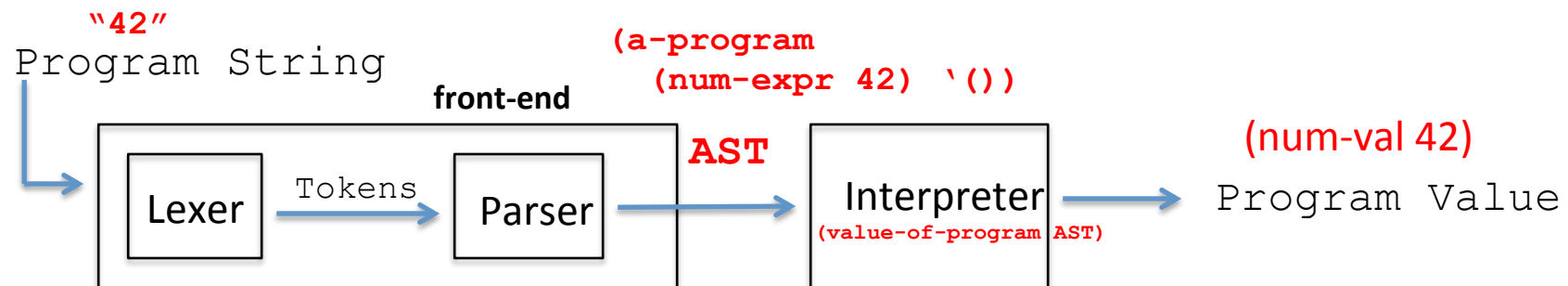
`(value-of-program (a-program (num-expr 42) `()))`



Intermediate steps

HW06
Problem 3

`(value-of-program (a-program (num-expr 42) `()))`



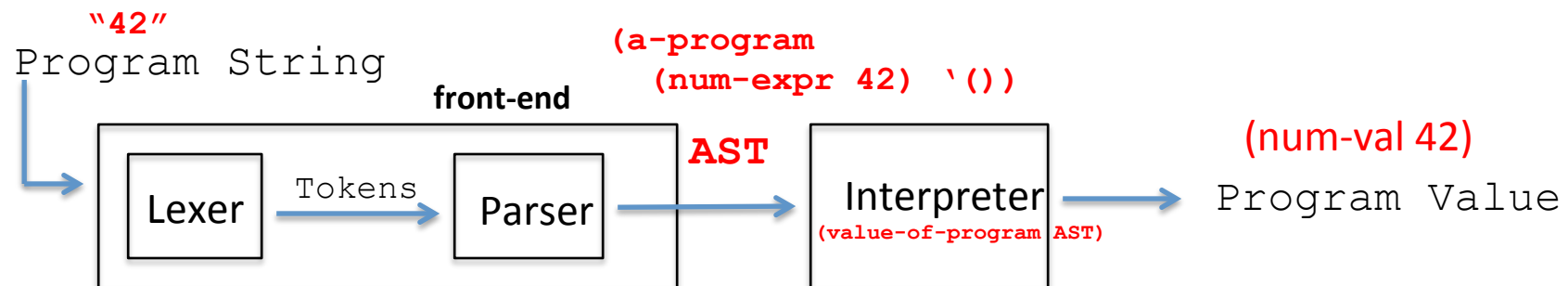
Intermediate steps

HW06
Problem 3

`(value-of-program (a-program (num-expr 42) `()))`



`(value-of-expr (num-expr 42))`



Intermediate steps

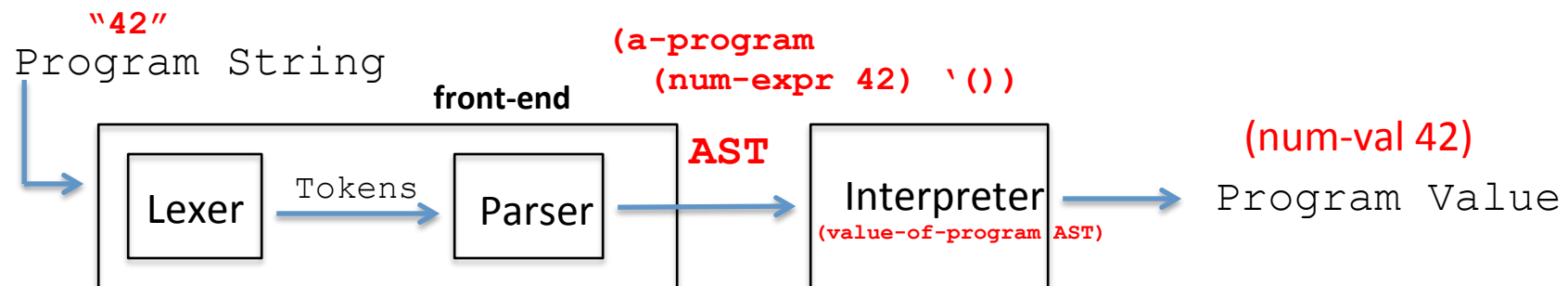
HW06
Problem 3

```
(value-of-program (a-program (num-expr 42) '()) )
```



```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (num-expr 42) '()) )
```

```
(value-of-expr (num-expr 42))
```



Intermediate steps

HW06
Problem 3

`(value-of-program (a-program (num-expr 42) '()))`

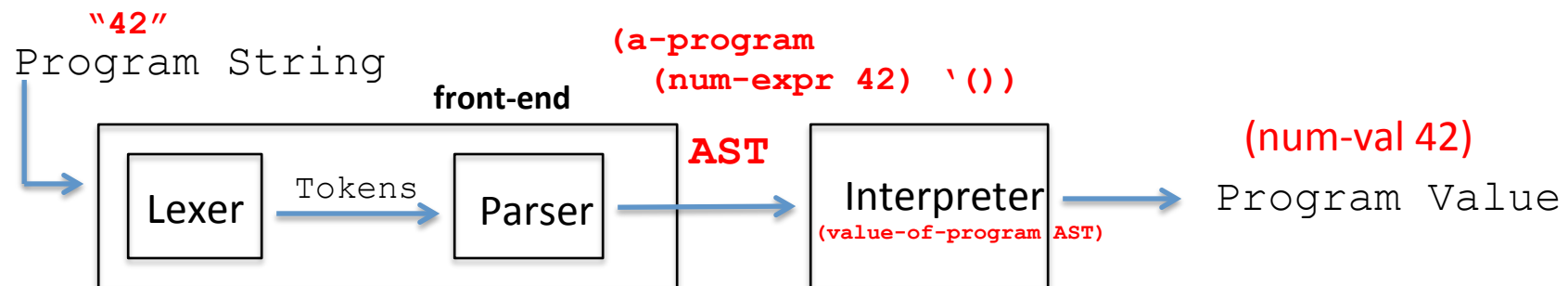


`(andmap (lambda(x) (value-of-expr x))
 (flat-list (num-expr 42) '()))`

`(value-of-expr (num-expr 42))`



How to generate `(num-val 42)`
from `(num-expr 42)` ?



Intermediate steps

HW06
Problem 3

`(value-of-program (a-program (num-expr 42) '()))`



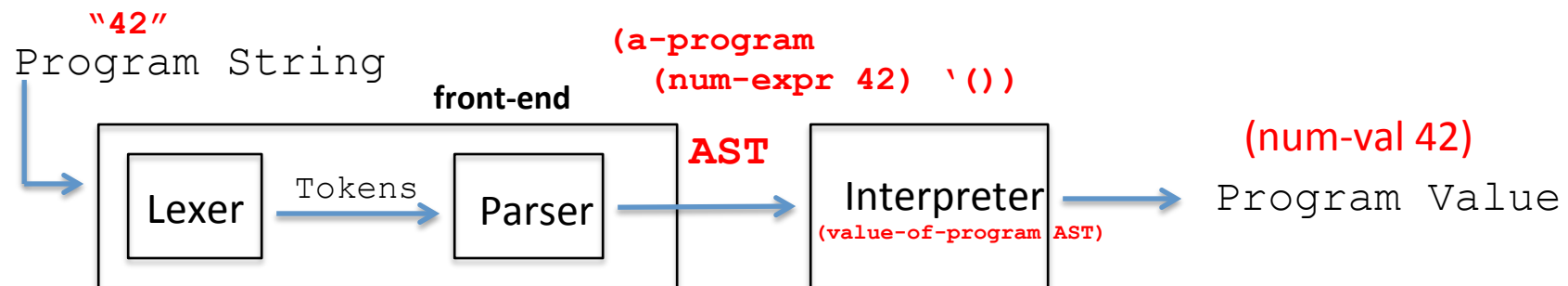
`(andmap (lambda(x) (value-of-expr x))
 (flat-list (num-expr 42) '()))`

`(value-of-expr (num-expr 42))`



How to generate `(num-val 42)`
from `(num-expr 42)` ?

Use **cases** !



Intermediate steps

HW06
Problem 3

```
(value-of-program (a-program (num-expr 42) '()) )
```

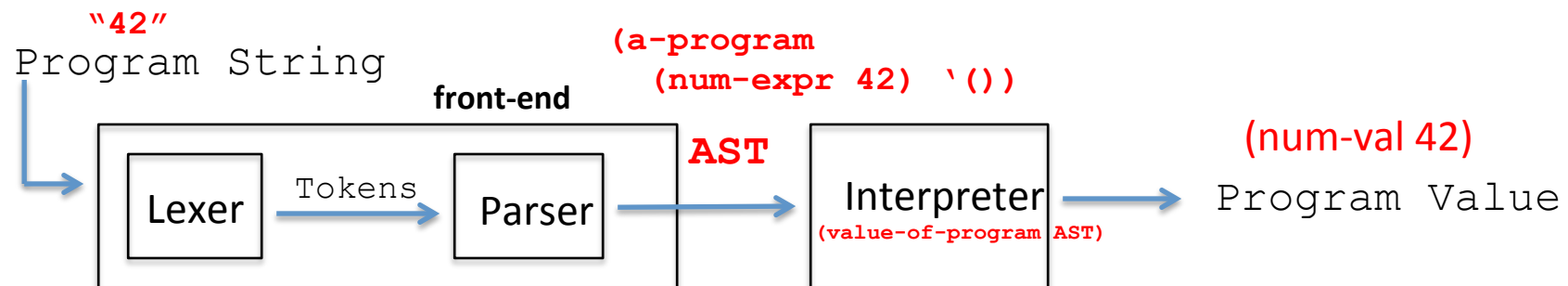


```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (num-expr 42) '()) )
```

```
(value-of-expr (num-expr 42))
```



```
(define (value-of-expr e)  
  (cases expr e  
    (num-expr (n) ... ) )
```



Intermediate steps

HW06
Problem 3

```
(value-of-program (a-program (num-expr 42) '()) )
```

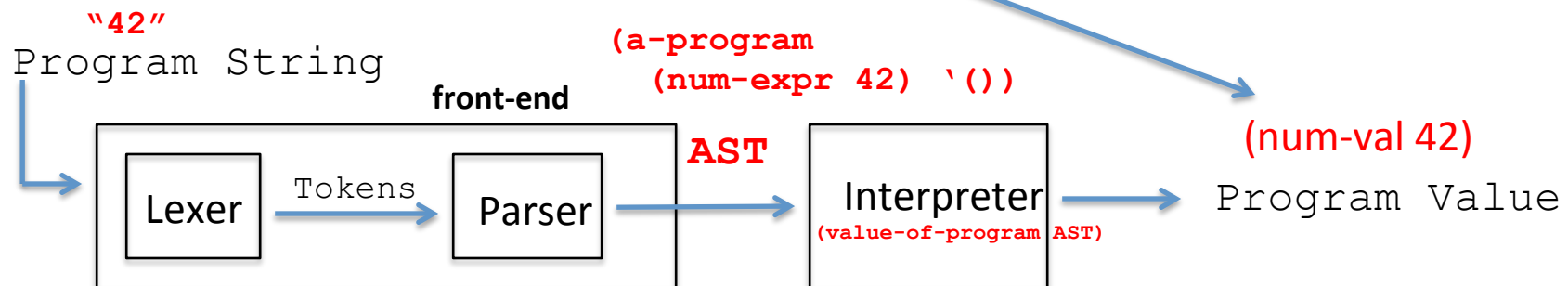
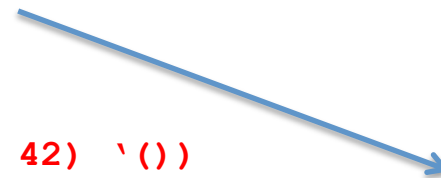


```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (num-expr 42) '()) )
```

```
(value-of-expr (num-expr 42))
```



```
(define (value-of-expr e)  
  (cases expr e  
    (num-expr (n) ... ) )
```



Intermediate steps

HW06
Problem 3

```
(value-of-program (a-program (num-expr 42) '()) )
```

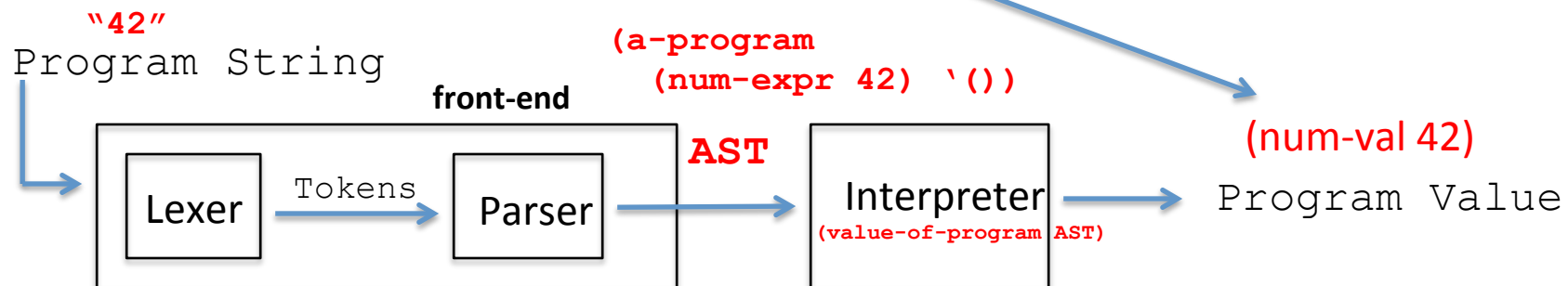


```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (num-expr 42) '()) )
```

```
(value-of-expr (num-expr 42))
```



```
(define (value-of-expr e)  
  (cases expr e  
    (num-expr (n) (num-val n) ) )
```



a-program

HW06
Problem 3

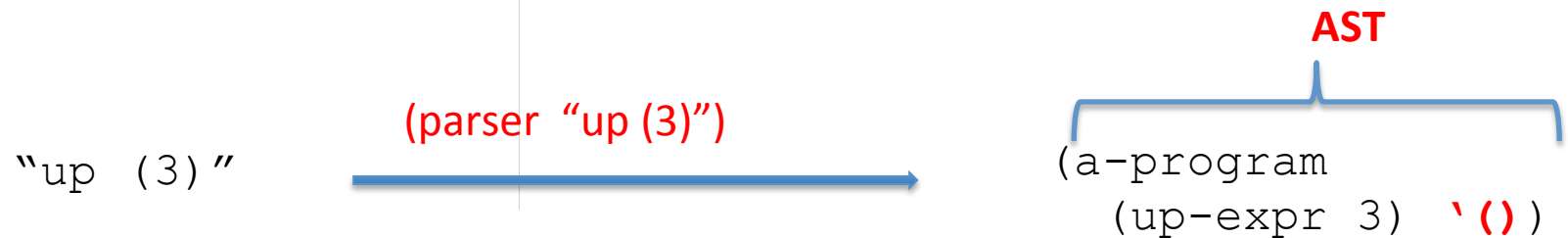
- How about this?

```
(run "up (3) ")
```

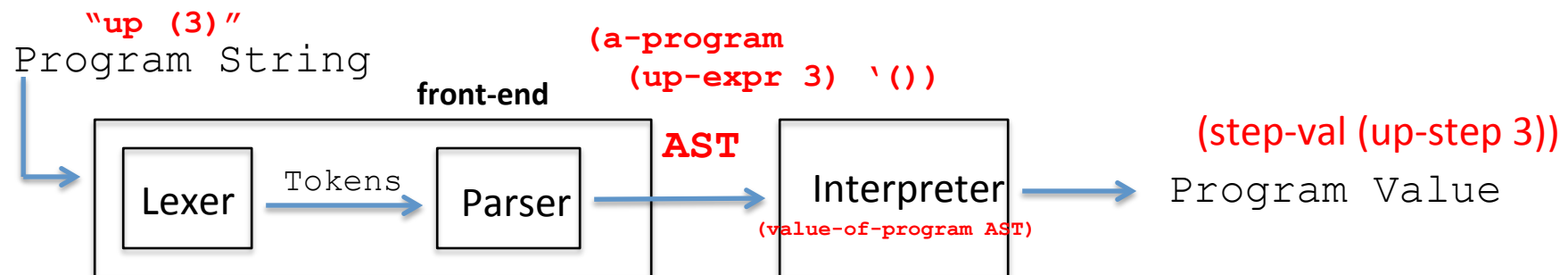
a-program

HW06 Problem 3

- What is the AST for "up (3)"?



What should (run "up (3)") return?



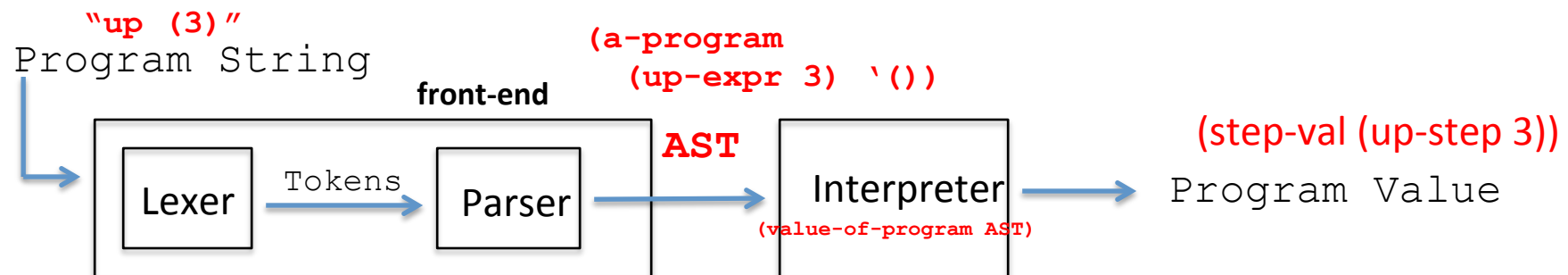
Intermediate steps

HW06
Problem 3

`(value-of-program (a-program (up-expr 3) '()))`



`(value-of-expr (up-expr 3))`



Intermediate steps

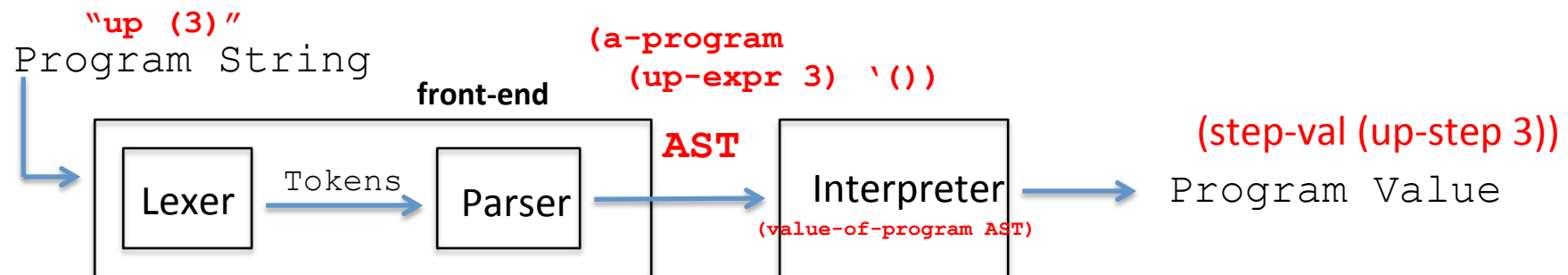
HW06
Problem 3

```
(value-of-program (a-program (up-expr 3) '()) )
```



```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (up-expr 3) '()) )
```

```
(value-of-expr (up-expr 3))
```



Intermediate steps

HW06
Problem 3

```
(value-of-program (a-program (up-expr 3) '()) )
```

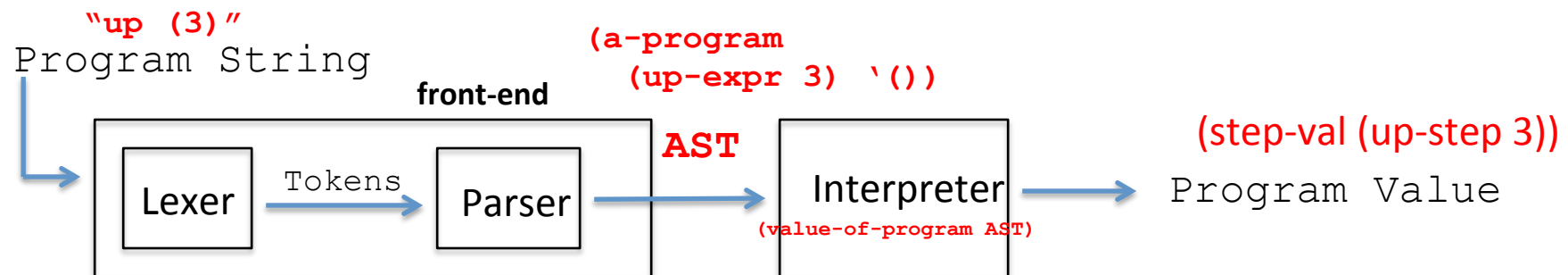


```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (up-expr 3) '()) )
```

```
(value-of-expr (up-expr 3))
```



```
(define (value-of-expr e)  
  (cases expr e  
    (up-expr (n) ... ) )
```



Intermediate steps

HW06
Problem 3

```
(value-of-program (a-program (up-expr 3) '()) )
```

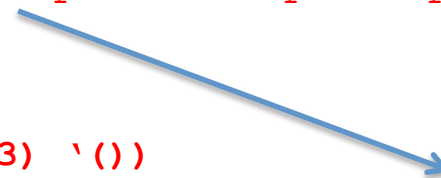


```
(andmap (lambda(x) (value-of-expr x))  
        (flat-list (up-expr 3) '()) )
```

```
(value-of-expr (up-expr 3))
```



```
(define (value-of-expr e)  
  (cases expr e  
    (up-expr (n) (step-val (up-step n)) ) )
```



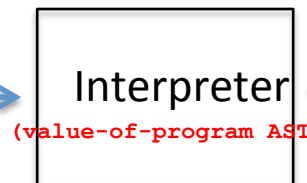
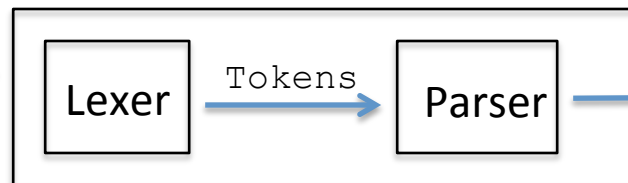
(step-val (up-step 3))

"up (3)"
Program String

front-end

(a-program
(up-expr 3) '())

AST

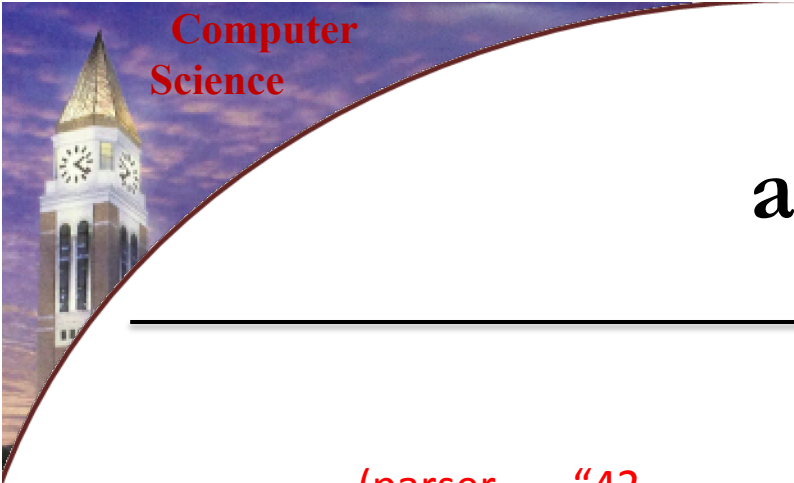


Program Value

a-program

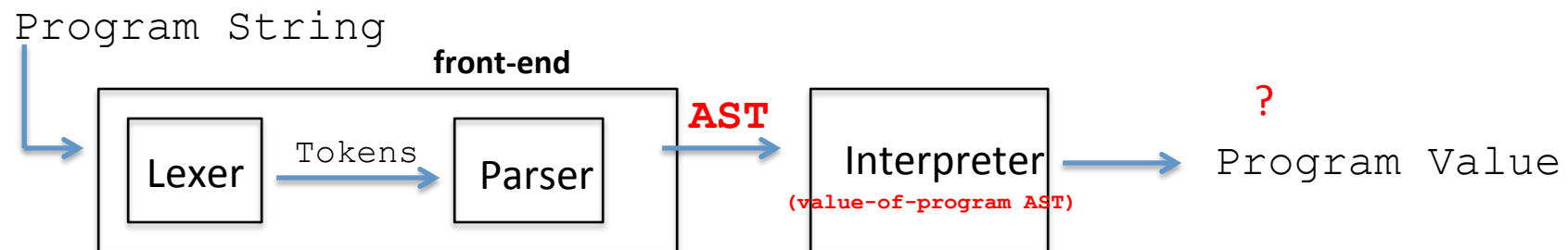
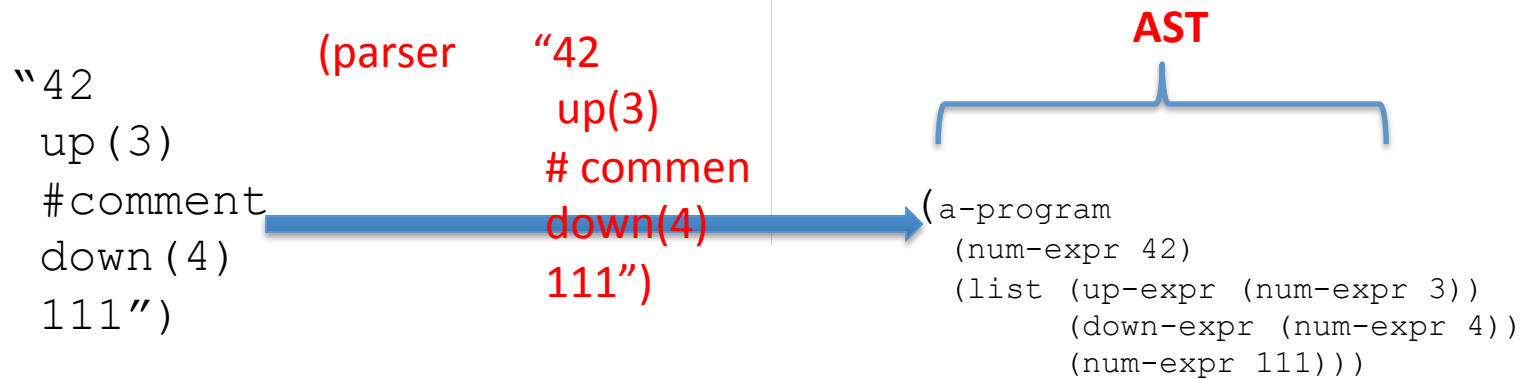
- How about this?

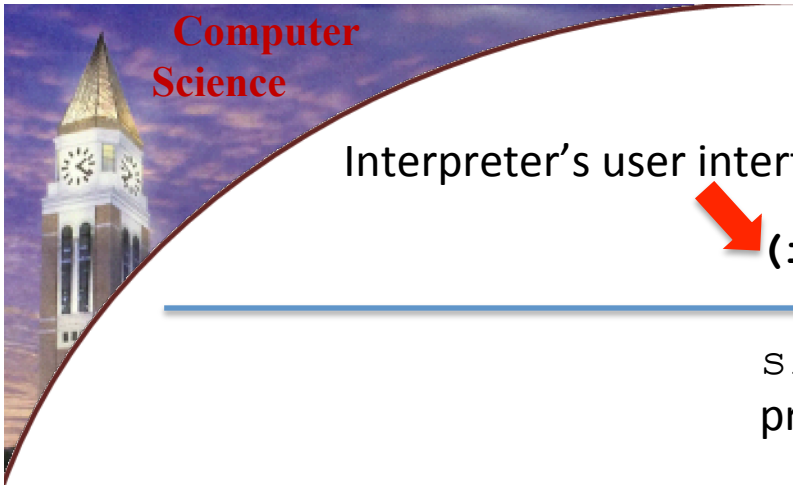
```
(run "42
    up(3)
    #comment
    down(4)
    111")
```



a-program

HW06 Problem 3





Interpreter's user interface



`(run program-string)`

HW06
Problem 4

`sllgen` generates parser that turns
program-string into ast



`(value-of ast env)`

- `(program? ast)`
- `(expr? ast)`
- `(var-expr? ast)`

`(value-of-program ast env)`



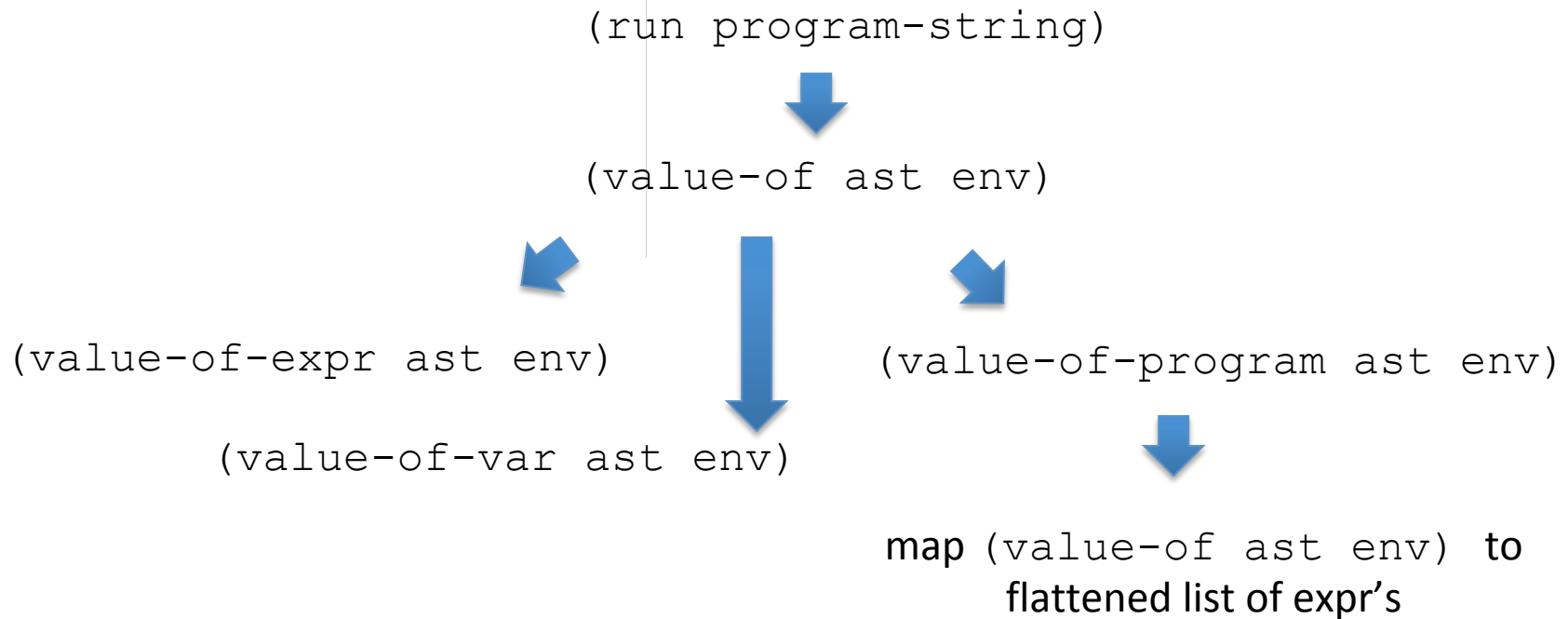
`(value-of-expr ast env)`



`(value-of-var ast env)`

a-program

HW06
Problem 4



```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
               lst-of-expr))
    ;...
  ))
```

```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
               lst-of-expr))
    ;...
  ))
```



```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
        lst-of-expr))
    ;...
  ))
```

```
;=====helpers for block-expr=====
(define (build-new-env lst-var-expr old-env)
  (if (null? lst-var-expr)
      old-env
      (build-new-env (cdr lst-var-expr) (one-at-a-time-add (car lst-var-expr) old-env))))
```

```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
        lst-of-expr))
    ;...
  ))
```

```
;=====helpers for block-expr=====
(define (build-new-env lst-var-expr old-env)
  (if (null? lst-var-expr)
      old-env
      (build-new-env (cdr lst-var-expr) (one-at-a-time-add (car lst-var-expr) old-env))))
```

```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
               lst-of-expr))
    ;...
  ))
```

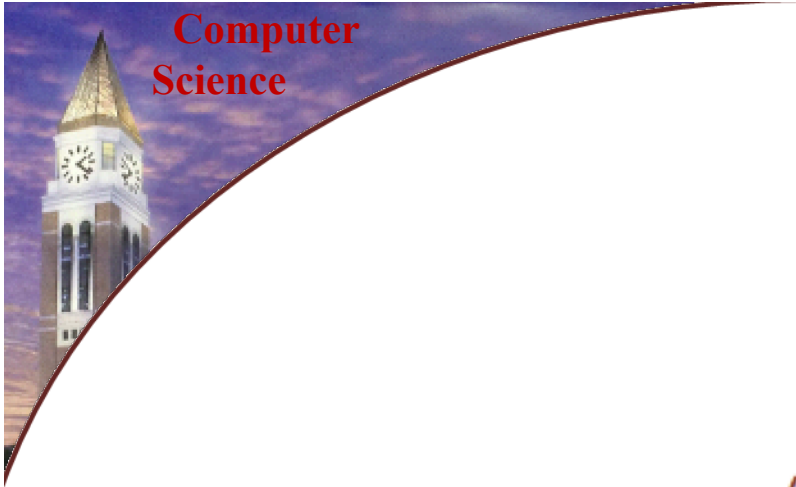
```
;=====helpers for block-expr=====
(define (build-new-env lst-var-expr old-env)
  (if (null? lst-var-expr)
      old-env
      (build-new-env (cdr lst-var-expr) (one-at-a-time-add (car lst-var-expr) old-env))))
```

```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
      (lst-of-var-expr lst-of-expr)
      (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
               lst-of-expr))
    ;...
  ))
```

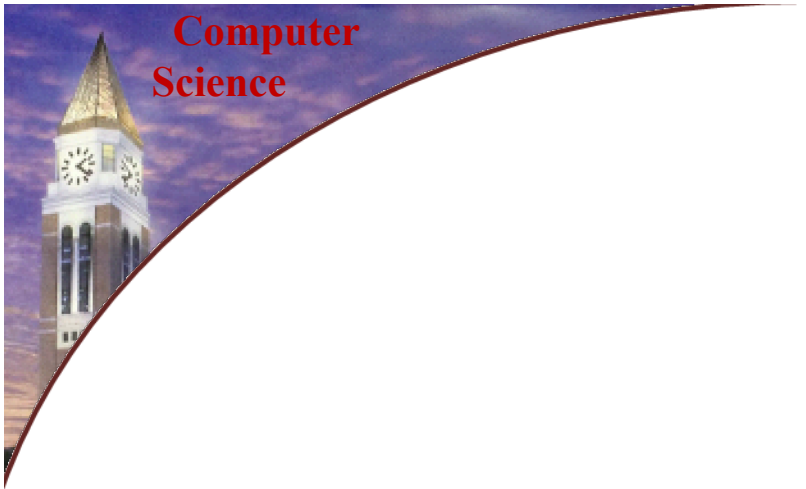
=====helpers for block-expr=====

```
(define (build-new-env lst-var-expr old-env)
  (if (null? lst-var-expr)
      old-env
      (build-new-env (cdr lst-var-expr) (one-at-a-time-add (car lst-var-expr) old-env))))

(define (one-at-a-time-add var old-env)
  (cases var-expr var
    (val (iden val-of-iden)
      (extend-env-wrapper iden (value-of val-of-iden old-env) old-env NON-FINAL))
    (final-val (iden val-of-iden)
      (extend-env-wrapper iden (value-of val-of-iden old-env) old-env FINAL))))
```



```
(run  
  "{  
    val x = 42  
    {  
      val x = 23  
    }  
    x  
  }")
```



```
(run "{  
    val x = 42  
    {val x = 23  
      x  
    }  
}" )
```

```
(run "{ val x = 3 }")
```

```
"{  
  val x = 42  
  {  
    val x = 23  
  }  
  x  
}"
```

val-expr

expr (block-expr is a
variant of expr)

expr (iden-expr is a
variant of expr)

expr (block-expr is a
variant of expr)


```
(define (value-of-expr ex env)
  (cases expr ex
    ;other variants of expr
    (iden-expr
     (var-name)
     (apply-env env var-name)))
```

```
"{
  val x = 42
  {
    val x = 23
  }
  x
}"
```

val-expr

expr (block-expr is a
variant of expr)

expr (iden-expr is a
variant of expr)

expr (block-expr is a
variant of expr)

```
(define (value-of-expr ex env)
  (cases expr ex
    ;other variants of expr
    (iden-expr
     (var-name)
     (apply-env env var-name)))
```

```
(define (value-of-expr ex env)
  (cases expr ex
    ; other kinds of expr's
    (block-expr
     (lst-of-var-expr lst-of-expr)
     (andmap (lambda (x) (value-of x (build-new-env lst-of-var-expr env)))
              lst-of-expr))
    ;...
    ))
```

```
"{
  val x = 42
  {
    val x = 23
  }
  x
}"
```

val-expr

expr (block-expr is a
variant of expr)

expr (iden-expr is a
variant of expr)

expr (block-expr is a
variant of expr)

The LET language

How to extend
LET with
procedure
handling
capabilities?

```
Program ::= Expression
         a-program (exp1)

Expression ::= Number
            const-exp (num)

Expression ::= -(Expression , Expression)
            diff-exp (exp1 exp2)

Expression ::= zero? (Expression)
            zero?-exp (exp1)

Expression ::= if Expression then Expression else Expression
            if-exp (exp1 exp2 exp3)

Expression ::= Identifier
            var-exp (var)

Expression ::= let Identifier = Expression in Expression
            let-exp (var exp1 body)
```

Figure 3.2 Syntax for the LET language

The Extended LET language

How to extend
LET with
procedure
handling
capabilities?

Expression ::= **proc** (*Identifier*) *Expression*
 proc-exp (var body)

Expression ::= (*Expression* *Expression*)
 call-exp (rator rand)

Program ::= *Expression*
 a-program (exp1)

Expression ::= *Number*
 const-exp (num)

Expression ::= - (*Expression* , *Expression*)
 diff-exp (exp1 exp2)

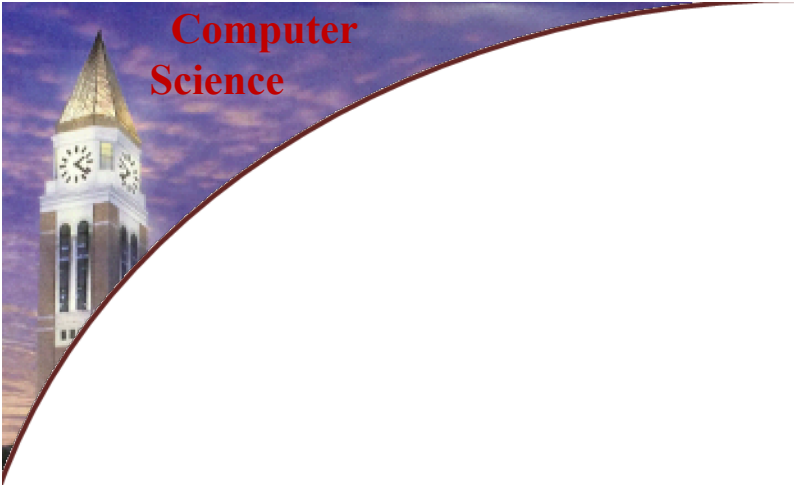
Expression ::= zero? (*Expression*)
 zero?-exp (exp1)

Expression ::= if *Expression* then *Expression* else *Expression*
 if-exp (exp1 exp2 exp3)

Expression ::= *Identifier*
 var-exp (var)

Expression ::= let *Identifier* = *Expression* in *Expression*
 let-exp (var exp1 body)

Figure 3.2 Syntax for the LET language



Suggested reading:

- EOPL: 3.1-3.2 (implementation of LET language)
- EOPL: 3.3 (Extend the LET language with Procedures p74- p82)

Extend the language with Procedures

- Concrete Syntax rules -

Expression ::= `proc` (Identifier) Expression
| (Expression Expression)

Procedure Definition

Procedure Call

Examples

```
let f = proc (x) -(x,11)
      in (f (f 77))
```

Examples

```
let f = proc (x) -(x,11)
      in (f (f 77))
```


Examples

```
let f = proc (x) -(x,11)
      in (f (f 77))
```

what should be the value of this
let expression ?

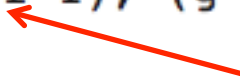
Examples

```
let f = proc (x) -(x,11)
      in (f (f 77))
```

←(num-val 55)

```
let x = 200
in let f = proc (z) -(z,x)
    in let x = 100
        in let g = proc (z) -(z,x)
            in -((f 1), (g 1))
```

```
let x = 200
in let f = proc (z) -(z,x)
  in let x = 100
    in let g = proc (z) -(z,x)
      in -((f 1), (g 1))
```



```
let x = 200
in let f ← proc (z) -(z,x)
    in let x = 100
        in let g = proc (z) -(z,x)
            in -((f 1), (g 1))
```

```
let x = 200
in let f = proc (z) -(z,x)
    in let x = 100
        in let g = proc (z) -(z,x)
            in -((f 1), (g 1))
```

creation-time
for procedure f

```
let x = 200
in let f = proc (z) -(z,x)
    in let x = 100
        in let g = proc (z) -(z,x)
            in -((f 1), (g 1))
```

creation-time
for procedure f

calling-time for
procedure f

```
let x = 200
in let f = proc (z) -(z,x)
    in let x = 100
        in let g = proc (z) -(z,x)
            in -((f 1), (g 1))
```

creation-time
for procedure f

calling-time for
procedure f



Static Scoping Vs. Dynamic Scoping

Examples

```
let f = proc (x) -(x,11)
      in f
```

← How about ?

- EOPL: 3.1-3.2 (implementation of LET language)
- EOPL: 3.3 (Extend the LET language with Procedures p74- p82)

- EOPL: 3.1-3.2 (implementation of LET language)
 - EOPL: 3.3 (Extend the LET language with Procedures p74- p82)
-

To Define a Procedure in Scheme –

```
(define a  
  (lambda (x) (+ x 1) ) )
```

- EOPL: 3.1-3.2 (implementation of LET language)
 - EOPL: 3.3 (Extend the LET language with Procedures p74- p82)
-

To Define a Procedure in Scheme –

```
(define a whole thing is one value, given to a  
  (lambda (x) (+ x 1) ) )
```

- EOPL: 3.1-3.2 (implementation of LET language)
- EOPL: 3.3 (Extend the LET language with Procedures p74- p82)

To Define a Procedure in Scheme –

```
(define a whole thing is one value, given to a  
  (lambda (x) (+ x 1) ) )
```

```
(define-datatype expval expval?  
  (num-val  
    (num number?) )  
  (bool-val  
    (bool boolean?))  
  (proc-val  
    (proc proc?))  
  )
```

- EOPL: 3.1-3.2 (implementation of LET language)
- EOPL: 3.3 (Extend the LET language with Procedures p74- p82)

To Define a Procedure in Scheme –

```
(define a whole thing is one value, given to a  
  (lambda (x) (+ x 1) ) )
```

```
(define-datatype expval expval?  
  (num-val  
    (num number?) )  
  (bool-val  
    (bool boolean?))  
  (proc-val  
    (proc proc?))  
  )
```


- EOPL: 3.1-3.2 (implementation of LET language)
- EOPL: 3.3 (Extend the LET language with Procedures p74- p82)

To Define a Procedure in Scheme –

```
(define a whole thing is one value, given to a  
  (lambda (x) (+ x 1) ) )
```

```
(define-datatype expval expval?  
  (num-val  
    (num number?) )  
  (bool-val  
    (bool boolean?))  
  (proc-val  
    (proc proc?))  
  )
```

```
(define-datatype proc proc?  
  (procedure  
    (var identifier?)  
    (body expression?)  
    (saved-env environment?)) )
```




Found at procedure
creation-time, **not**
procedure call-time !!

- EOPL: 3.1-3.2 (implementation of LET language)
 - EOPL: 3.3 (Extend the LET language with Procedures p74- p82)
-

```
(define-datatype expval expval?  
  (num-val  
    (num number?) )  
  (bool-val  
    (bool boolean?))  
  (proc-val  
    (proc proc?))  
  )
```

```
(define-datatype proc proc?  
  (procedure  
    (var identifier?)  
    (body expression?)  
    (saved-env environment?)))
```



The Extended LET language

Program ::= *Expression*

`a-program (exp1)`

Expression ::= *Number*

`const-exp (num)`

Expression ::= *-(Expression , Expression)*

`diff-exp (exp1 exp2)`

Expression ::= *zero? (Expression)*

`zero?-exp (exp1)`

Expression ::= *if Expression then Expression else Expression*

`if-exp (exp1 exp2 exp3)`

Expression ::= *Identifier*

`var-exp (var)`

Expression ::= *let Identifier = Expression in Expression*

`let-exp (var exp1 body)`

Expression ::= *proc (Identifier) Expression*

`proc-exp (var body)`

Expression ::= *(Expression Expression)*

`call-exp (rator rand)`

Figure 3.2 Syntax for the LET language

The **proc** language

Program ::= *Expression*

`a-program (exp1)`

Expression ::= *Number*

`const-exp (num)`

Expression ::= *-(Expression , Expression)*

`diff-exp (exp1 exp2)`

Expression ::= *zero? (Expression)*

`zero?-exp (exp1)`

Expression ::= *if Expression then Expression else Expression*

`if-exp (exp1 exp2 exp3)`

Expression ::= *Identifier*

`var-exp (var)`

Expression ::= *let Identifier = Expression in Expression*

`let-exp (var exp1 body)`

Expression ::= *proc (Identifier) Expression*

`proc-exp (var body)`

Expression ::= *(Expression Expression)*

`call-exp (rator rand)`

Figure 3.2 Syntax for the LET language