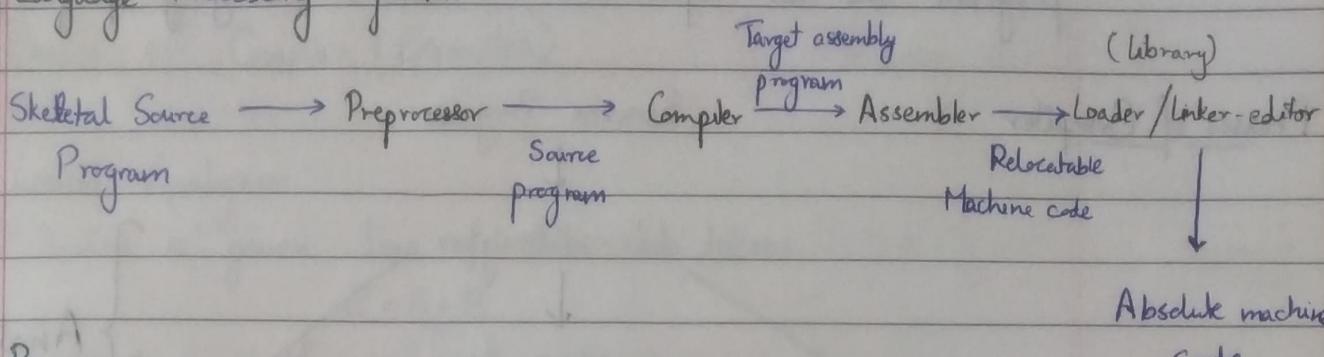


UNIT 1

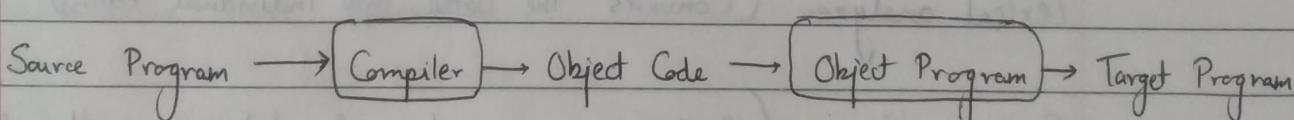
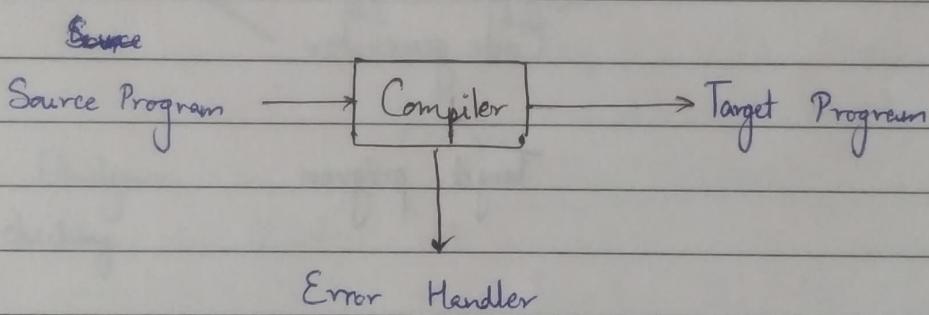
• Language Processing System.



1. Preprocessor

- Macro Preprocessing (work on macros #def)
- file inclusion Preprocessing (work on different file formats; image, video, link to others)
- Rational Preprocessing (synchronization of different older languages to modern control)
- Language extension (adding capabilities or functions to a language)

Compiler



* Interpreter

- Checks the program line by line.

- Easily to modify & identify errors

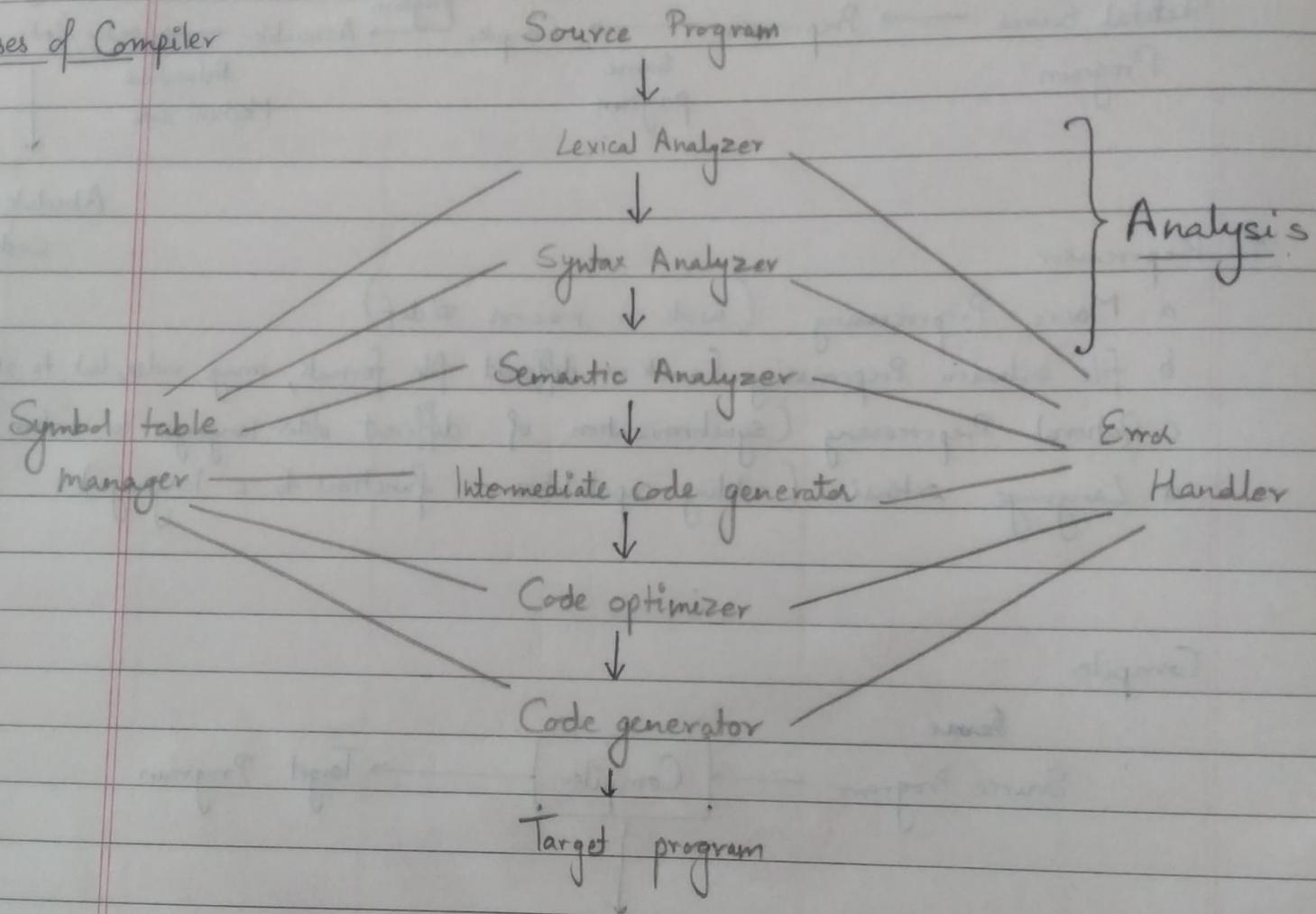
- Makes the code machine independent

- ↑ execution time

- ↑ memory consumption

Compiler

A translator program which converts a high-level language written program into an equivalent machine level language program.

Phases of Compiler

Lexical analyzer (Converts the code into individual tokens)

Syntax analyzer (Create a parser tree & determine the tokens to be grouped, to make a valid context)

~~Semantic analyzer~~ (relate syntactic structures to their language independent meanings)

Compilation process → Analysis → Synthesis

* Phases of Compiler (Examples)

1. Lexical Analyzer

↳ Divide a given line of codes into tokens.

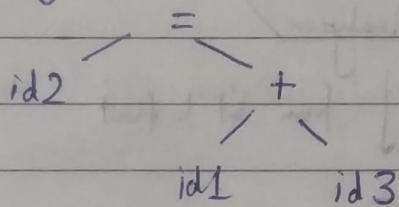
$$Z = A + B$$

$$\text{identifier } \alpha = \text{id1} + \text{id3}$$

2. Syntax Analyzer

↳ Combine the tokens to generate a valid expression.

↳ Create a parsing tree



3. Semantic Analyzer

↳ Type checking

4. Intermediate Code Generation

5. Code optimization

↳ Optional

↳ Techniques:

1. Local optimization

$\{ \begin{array}{l} A >= 6 \text{ goto L1} \\ \text{if } A >= 6 \text{ goto L3} \\ \text{L1: goto L3} \\ \text{L3: print(" ")} \end{array} \}$

2. Subsequence optimization

$\left. \begin{array}{l} A = B + C + D \\ E = B + C + F \end{array} \right\} \rightarrow \begin{array}{l} T_1 = B + C \\ A = T_1 + D \end{array}$

$$E = T_1 + F$$

(Saves time)

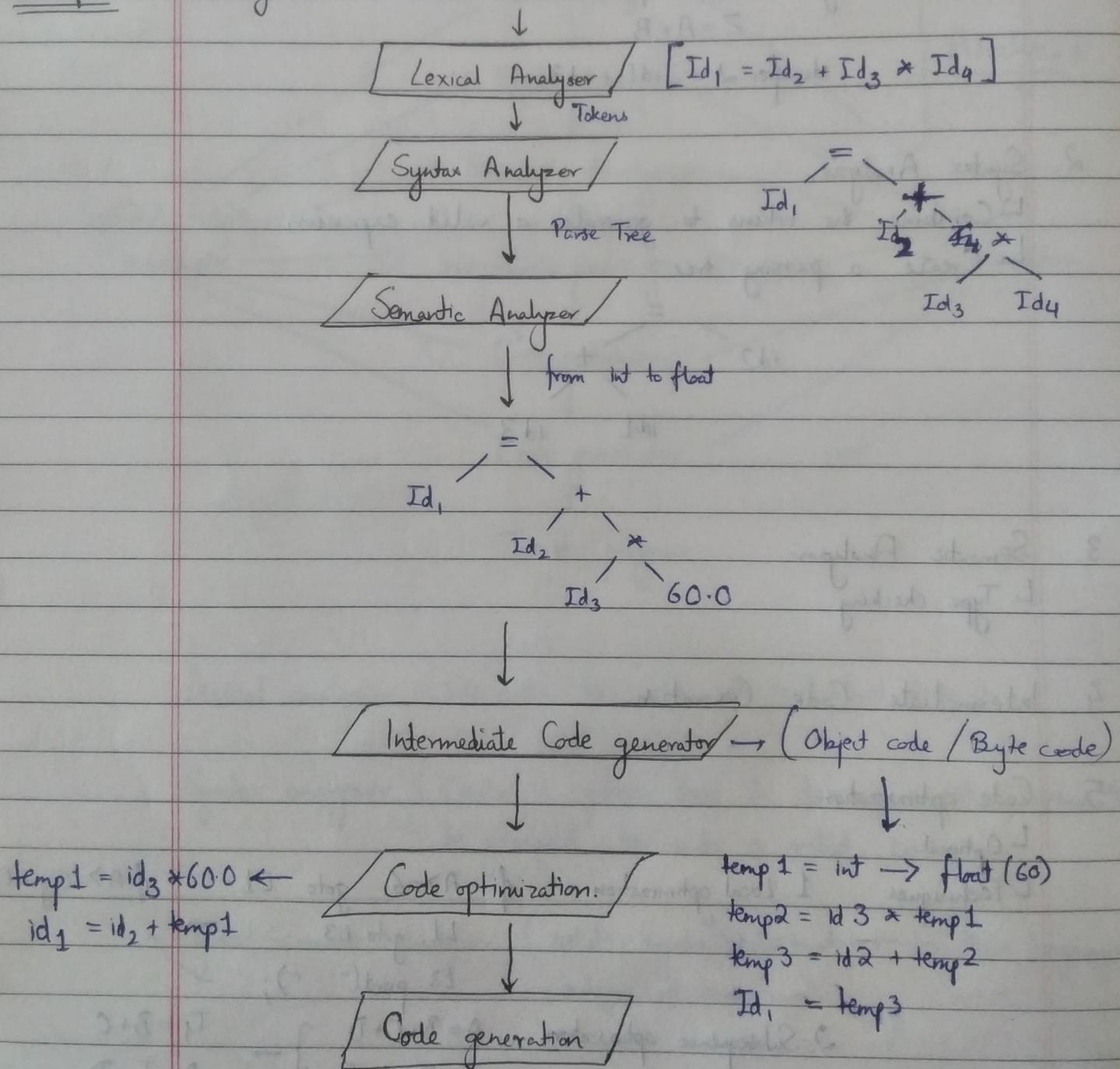
3. Loop optimization

// Remove any unnecessary calculations or operations from within the loop.

6. Code generation.

Example:

$$x = y + z * 60$$

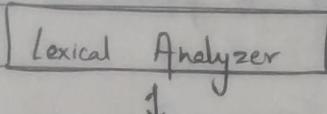


Ex2:

$$P = q + r / 100$$



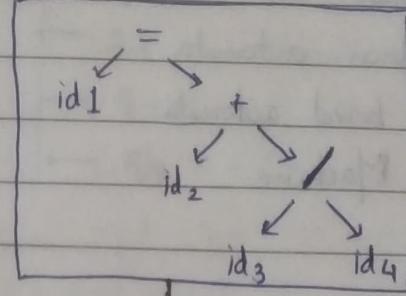
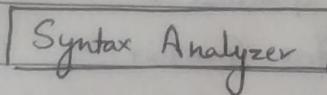
Step 1:-



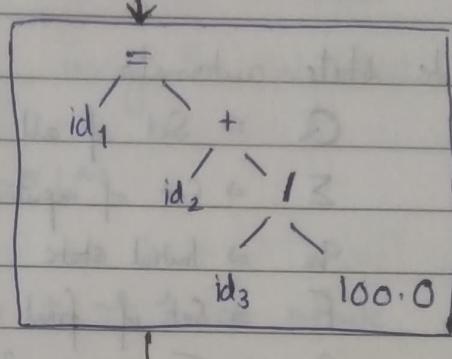
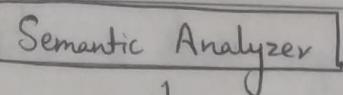
$$id_1 = id_2 + id_3 / id_4$$



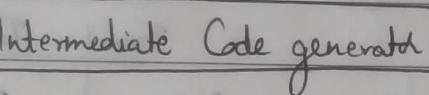
Step 2:-



Step 3:-



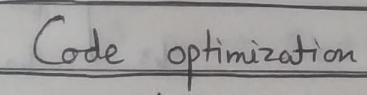
Step 4:-



$$\begin{aligned} \text{temp1} &= \text{int} \rightarrow \text{float} (\text{id}_4) \\ \text{temp2} &= \text{id}_3 / \text{temp1} \\ \text{temp3} &= \text{id}_2 + \text{temp2} \\ \text{id}_1 &= \text{temp3} \end{aligned}$$



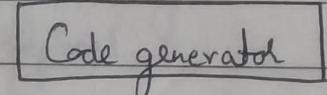
Step 5:-



$$\begin{aligned} \text{temp1} &= \text{id}_3 / 100.0 \\ \text{id}_1 &= \text{id}_2 + \text{temp1} \end{aligned}$$



Step 6:-



Corresponding machine language code

- * finite state automata
- * Grammar & its types
- * Ambiguous & unambiguous grammar

Automata

A machine which takes input from user to produce an output

finite state automata	\rightarrow	Regular Grammar
push down automata	\rightarrow	Context free Grammar
Linear bound automata	\rightarrow	Context sensitive Grammar
Turing Machine	\rightarrow	Type 0 Grammar.

finite state automata

DFA \Rightarrow

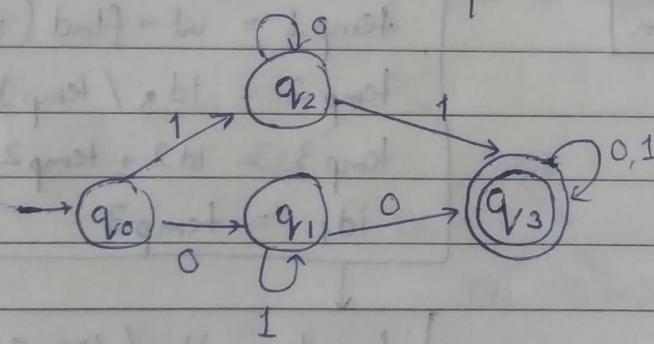
$Q \Rightarrow$ Set of all states

$\Sigma \Rightarrow$ Set of input alphabets/symbol

$q_0 \Rightarrow$ Initial state

$F \Rightarrow$ Set of final state(s)

$\delta \Rightarrow$ Transition function $(Q \times \Sigma \rightarrow Q)$



Transition Table

State	0	1
$\rightarrow q_0$	q_1	q_2
q_1	q_3	q_1
q_2	q_2	q_3
q_3	q_3	q_2

NFA \Rightarrow

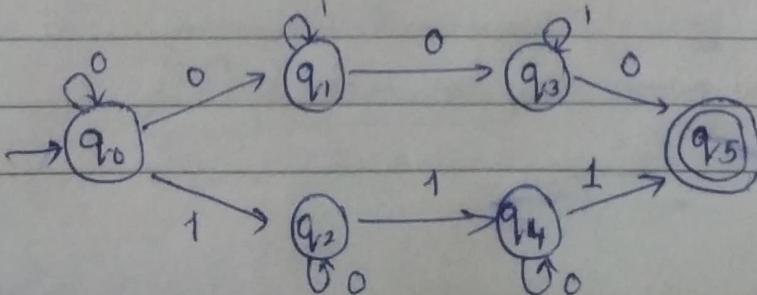
$Q \Rightarrow$ Set of all states

$\Sigma \Rightarrow$ Set of input symbols

$q_0 \Rightarrow$ Initial state

$F \Rightarrow$ Set of final state(s)

$\delta \Rightarrow$ Transition function $(\delta: Q \times \Sigma \rightarrow 2^Q)$



Date : ___ / ___ / ___

State	0	1
$\rightarrow q_0$	$\{q_0, q_1\}$	q_2
q_1	q_3	q_1
q_2	q_2	q_4
q_3	q_5	q_3
q_4	q_4	q_5
q_5	q_5	q_5

Regular Expression

Used to denote regular language, using the alphabets of the language.

$$abc \Rightarrow a^* bc, ab^+, a^* b^*$$

$*$ \rightarrow 0 or infinite $+\rightarrow$ 1 or infinite.

Grammar

N \rightarrow Non-terminal symbols (A, B, S, D, K, etc.)

T \rightarrow Terminal symbols {a, b, c, ...}

P \rightarrow Set of production rules

S \rightarrow Start symbol

- Terminal symbols can't be replaced but non-terminal symbols can be replaced.

$$\text{list} \rightarrow \text{list} + \text{digit} \mid \text{list} - \text{digit} \mid \text{digit}$$

$$\text{digit} \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

* Left-most derivation

$$\text{list} \rightarrow \text{list} + \text{digit}$$

$$\text{list} \rightarrow \text{list} - \text{digit} + \text{digit}$$

$$\text{list} \rightarrow \text{digit} - \text{digit} + \text{digit}$$

$$\text{list} \rightarrow$$

Parse Tree

$$\text{list} \rightarrow \text{list} + \text{digit} \mid \text{list} - \text{digit} \mid \text{digit}$$

$$\text{digit} \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

$$4 - 5 + 8$$

Left most derivation:

$$\text{list} \rightarrow \text{list} + \text{digit}$$

$$\rightarrow \text{list} - \text{digit} + \text{digit}$$

$$\rightarrow \text{digit} - \text{digit} + \text{digit}$$

$$\rightarrow 4 - \text{digit} + \text{digit}$$

$$\rightarrow 4 - 5 + \text{digit}$$

$$\rightarrow 4 - 5 + 8$$

$$\text{list}$$

$$/ \quad \backslash$$

$$\text{list} \quad + \quad \text{digit}$$

$$8$$

$$\text{list} - \text{digit}$$

$$5$$

$$4$$

Right most derivation

$$\text{list} \rightarrow \text{list} + \text{digit}$$

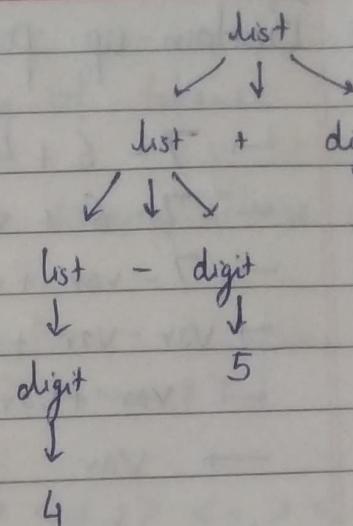
$$\rightarrow \text{list} + 8$$

$$\rightarrow \text{list} - \text{digit} + 8$$

$$\rightarrow \text{list} - 5 + 8$$

$$\rightarrow \text{digit} - 5 + 8$$

$$\rightarrow 4 - 5 + 8$$



* Ambigious Grammar \rightarrow More than 2 derivation / parse tree are present

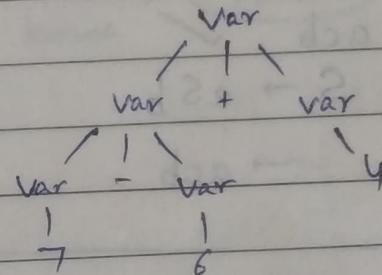
$$\star \text{Var} \rightarrow \text{Var} + \text{Var} \mid \text{var} - \text{var} \mid \text{Var} \quad | \quad 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9.$$

Left most \rightarrow

$$\text{Var} \rightarrow \text{Var} + \text{Var}$$

$$\rightarrow \text{Var} - \text{Var} + \text{Var}$$

$$\rightarrow 7 - 6 + 4$$



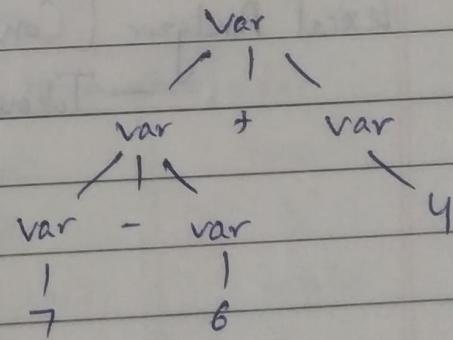
Right most \rightarrow

$$\text{Var} \rightarrow \text{var} + \text{var}$$

$$\rightarrow \text{var} + 4$$

$$\rightarrow \text{var} - \text{var} + \cancel{4}$$

$$\rightarrow 7 - 6 + 4$$



$$\text{Var} \rightarrow \text{var} - \text{var}$$

$$\rightarrow \cancel{\text{var}} \text{Var} \rightarrow \text{var} - \text{var}$$

$$\rightarrow \text{var} - \text{var} + \text{var}$$

$$\rightarrow 7 - 6 + 4$$

(Top-down parsing)

* Bottom-up Parsing

$\rightarrow 7 - 6 + 4$
 $\rightarrow 7 - 6 + \text{var}$
 $\rightarrow 7 - \text{var} + \text{var}$
 $\rightarrow \text{Var} - \text{var} + \text{var}$
 $\rightarrow \text{Var} + \text{var}$
 $\rightarrow \text{Var}$

Q $\Rightarrow S \rightarrow aSb \mid c \mid ab$

acb, abba

① acb ✓

$S \rightarrow aSb$

$\rightarrow acb$

② abba ✗

$S \rightarrow aSb$

$\rightarrow aabb$

Lexical Analyzer (Convert input into stream of tokens)

→ Tokens

1. Keywords
2. Identifiers
3. Operators
4. Punctuations
5. Constants
6. Literals
7. Strings

Lexeme

— A sequence of characters comprising of tokens.

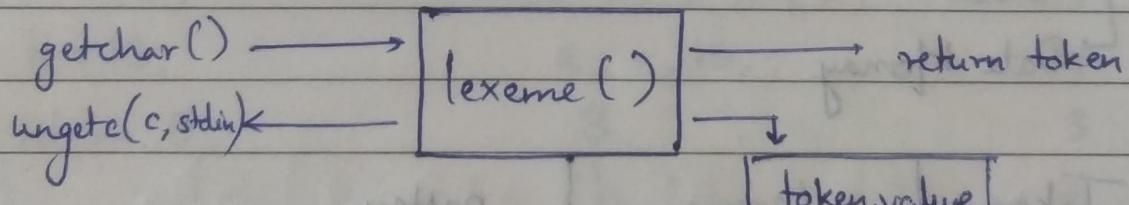
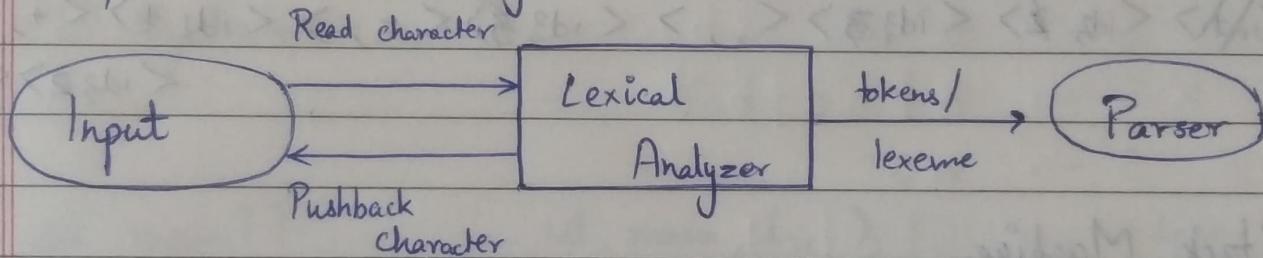
Input → Lexical Analyzer → Lexeme/Tokens

/ Removal of whitespaces & comments

① Constants :- $7+8 \rightarrow [\langle \text{num}, 7 \rangle \langle +, \rangle \langle \text{num}, 8 \rangle]$

② Identifiers :- $p\neq q+r \rightarrow [\langle \text{id}, 1 \rangle \langle =, \rangle \langle \text{id}, 2 \rangle \langle +, \rangle \langle \text{id}, 3 \rangle]$

* Interface of lexical Analyzer



Q).
 int x;
 x = 7;
 int y, z;
 z = x + y;

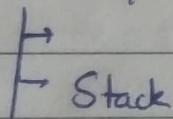
$\langle \text{id}, 1 \rangle \langle \text{=} \rangle \langle \text{num}, 7 \rangle$
 $\langle \text{id}, 3 \rangle \langle \text{=} \rangle \langle \text{id}, 1 \rangle \langle +, - \rangle$
 $\langle \text{id}, 2 \rangle$

- ~~int~~ ① int x ; $\langle \text{int} \rangle \langle \text{id}, 1 \rangle \langle ; \rangle$
 ② x = 7 ; $\langle \text{id}, 1 \rangle \langle \text{=} \rangle \langle \text{num}, 7 \rangle \langle ; \rangle$
 ③ int y, z ; $\langle \text{int} \rangle \langle \text{id}, 2 \rangle \langle \text{id}, 3 \rangle \langle ; \rangle$
 ④ z = x + y ; $\langle \text{id}, 3 \rangle \langle \text{=} \rangle \langle \text{id}, 1 \rangle \langle +, - \rangle$
 $\langle \text{id}, 2 \rangle \langle ; \rangle$

$\langle \text{int} \rangle$ will also be counted as a token.

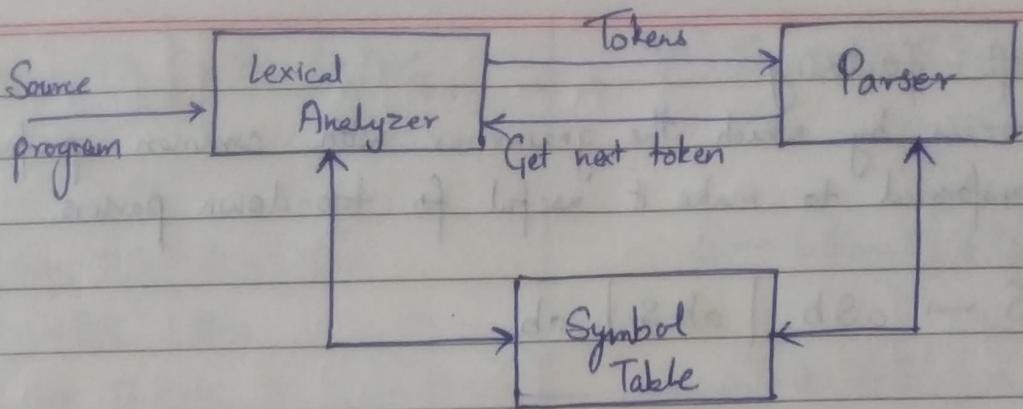
→ $\langle \text{int} \rangle \langle \text{id}_1, 1 \rangle \langle ; \rangle \langle \text{id}_1, 2 \rangle \langle \text{=} \rangle \langle \text{num}, 7 \rangle \langle ; \rangle$
 $\langle \text{int} \rangle \langle \text{id}_2, 1 \rangle \langle \text{id}_3, 2 \rangle \langle ; \rangle \langle \text{id}_3, 3 \rangle \langle \text{=} \rangle \langle \text{id}_1, 2 \rangle \langle +, - \rangle$
 $\langle \text{id}_2, 2 \rangle \langle ; \rangle$

Abstract Stack Machine



Data Memory

Token	Lexeme	pattern
const	const	const
if	if	If
relation	$\langle , \langle =, \rangle, \rangle =, =$	
i	pi	any numeric constant
num	3.14	any character b/w "and" except "
literal	"core"	pattern



- To identify the token
 - Regular Expression should define what tokens are possible/allowed in grammar
 - Recognize & categorize tokens
- * Errors generated by lexical analyzers (lexical errors)
- ① Not able to identify the token
 - ② Syntax error.

Q.

int main()

{

int a, b;

a = 10;

return 0;

}

int, main, (,)

{

int a, , b, ;

a, =, 10, ;

3

= 18

4

1

5

4

3

int main ()

{

int a = 10, b = 20;

printf ("sum is %d", a+b);

return 0;

}

4

1

9

8 9

3

1

= 27

Left factoring

Process by which the grammar with common prefixes is transformed to make it useful for top-down parsers.

$$\textcircled{1} \quad S \rightarrow asb \mid abs \mid ab$$

$$S \rightarrow as'$$

$$s' \rightarrow sb \mid bs \mid b$$

$$S \rightarrow as'$$

$$s' \rightarrow sb \mid s''s \mid$$

$$s'' \rightarrow b \# \&$$

$$\textcircled{2} \quad S \rightarrow ab \mid abc \mid abcd \mid b$$

$$S \rightarrow as' \mid b$$

$$x \quad s' \rightarrow b \mid bc \mid bcd$$

$$s' \rightarrow b s''$$

$$x \quad s'' \rightarrow \epsilon \mid c \mid cd$$

$$s'' \rightarrow \epsilon \mid cs'' \}$$

$$s''' \rightarrow \epsilon \mid d$$

$$\textcircled{3} \quad S \rightarrow aAb \mid aABC \mid aABcd \mid aAa$$

$$A \rightarrow a$$

$$B \rightarrow a$$

$$S \rightarrow as'$$

$$x \quad s' \rightarrow Ab \mid ABC \mid ABcd \mid Aa$$

$$s' \rightarrow AS''$$

$$x \quad s'' \rightarrow b \mid Bc \mid Bcd \mid a$$

$$s'' \rightarrow b \mid BS'' \mid a$$

$$x \quad s''' \rightarrow c \mid cd$$

$$s'''' \rightarrow cS''''$$

$$s'''' \rightarrow \epsilon \mid d$$

$$S \rightarrow as'$$

$$s' \rightarrow AS''$$

$$s'' \rightarrow b \mid BS'' \mid a$$

$$s''' \rightarrow CS'''$$

$$s'''' \rightarrow \epsilon \mid d$$

$$A \rightarrow a$$

$$B \rightarrow a$$

$$(4) A \rightarrow aAB \mid aBc \mid aAC$$

$$A \rightarrow aA'$$

$$\times A' \rightarrow AB \mid Bc \mid Ac$$

$$A' \rightarrow AA'' \mid Bc$$

$$A'' \rightarrow B \mid c$$

$$\rightarrow A \rightarrow aA'$$

$$A' \rightarrow AA'' \mid Bc$$

$$A'' \rightarrow B \mid c$$

$$(5) S \rightarrow bSSaas \mid bSSasb \mid bSb \mid a$$

$$S \rightarrow bSSaas \mid bSSasb \mid bSb \mid a$$

$$S \rightarrow bS' \mid a$$

$$\times S' \rightarrow SSaas \mid SSasb \mid Sb$$

$$S' \rightarrow SS''$$

$$\times S'' \rightarrow Saas \mid Sasb \mid b$$

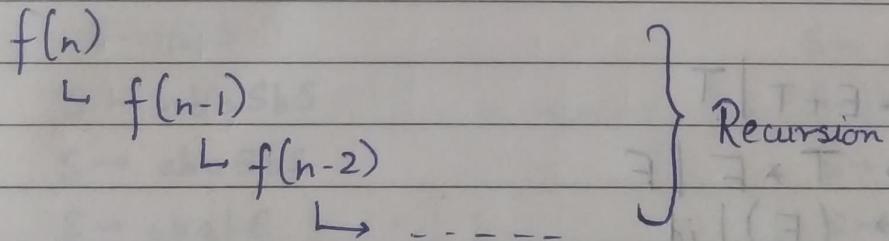
$$S'' \rightarrow SS''' \mid b$$

$$\times S''' \rightarrow aaS \mid aSb$$

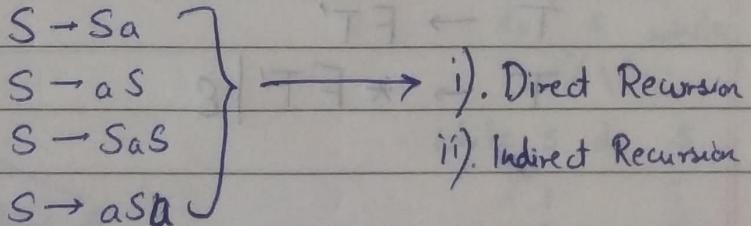
$$S''' \rightarrow aS'''$$

$$S'''' \rightarrow aS \mid Sb$$

* Left Recursion / Recursion



If a grammar is recursive, the non-terminals are present on both LHS & RHS.



$$\begin{array}{l} A \rightarrow aB/a \\ B \rightarrow aA \end{array} \quad \left. \begin{array}{l} \{ \\ \} \end{array} \right\} A \rightarrow aaA/a \quad] \text{Indirect Recursion.}$$

* Types of Direct Recursion

- i). Left Recursion [Non-terminal at extreme left] $S \rightarrow S\alpha$
- ii). Right Recursion [Non-terminal at extreme right] $S \rightarrow \alpha S$

Parser might lead to infinity operations in case of left recursion

Convert left recursion into right recursion

Q). $A \rightarrow \beta A' \quad A \rightarrow A\alpha / B$

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' / \epsilon$$

Q). $E \rightarrow E + T \quad | \quad T$

$$\left. \begin{array}{l} T \rightarrow T * F \quad | \quad F \\ F \rightarrow (E) \quad | \quad id \end{array} \right\}$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

Date: 04-feb-2022

Admet Dabral

190184010

B.T.CSE (AI-DS) Date: / /

Practice Assignment

CS304 - Compiler Design

- i). Consider the grammar $G = \langle \{S\}, \{\text{do, while}\}, P, S \rangle$ with productions P ,

$$S \rightarrow \text{do } S \text{ while } S \mid \text{while } S \text{ do } S \mid \epsilon$$

Show that this grammar is ambiguous.

$Sd \Rightarrow$ for simplicity,

Let $a = \text{do}$, $b = \text{while}$

$$S \rightarrow aSbS \mid bSaS \mid \epsilon$$

Considering string $w = abab$.

i). Left Parse Tree

$$S \rightarrow aSbS$$

$$S \rightarrow a \epsilon bS$$

$$S \rightarrow abS$$

$$S \rightarrow ab aSbS$$

$$S \rightarrow aba \epsilon bS$$

$$S \rightarrow abab \epsilon$$

$$S \rightarrow abab$$

$$S \rightarrow \text{do while do while}$$

ii). Right Parse Tree

$$S \rightarrow bSaSbS$$

$$S \rightarrow abSaSbS$$

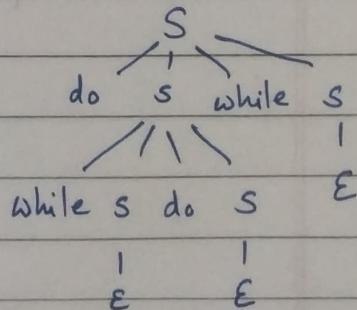
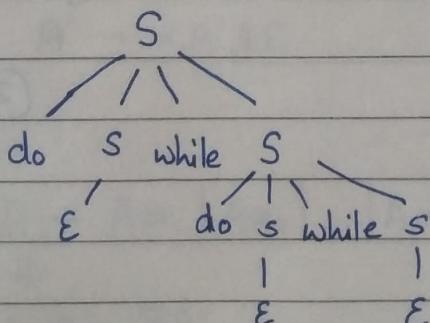
$$S \rightarrow abEaSbS$$

$$S \rightarrow aba \epsilon bS$$

$$S \rightarrow abab \epsilon$$

$$S \rightarrow abab$$

$$S \rightarrow \text{do while do while}$$



⇒ The given grammar is ambiguous.

①

2). Consider the grammar $G = \langle \{S\}, \{a, if, then\}, P, S \rangle$
 with productions P

$$S \rightarrow \text{if } S \text{ then } S \mid \text{if } S \mid a$$

Left factor the productions.

Sol = for simplicity,

$$\text{Let } a = a$$

$$\text{if } = b$$

$$\text{then} = c$$

Thus,

$$S \rightarrow bScS \mid bs \mid a$$

* Left factoring the production rules

$$S \rightarrow bS' \mid a$$

$$S' \rightarrow ScS \mid S$$

$$S' \rightarrow SS''$$

$$S'' \rightarrow cS \mid \epsilon$$

So, The left factored grammar is

$$S \rightarrow bS' \mid a$$

$$S' \rightarrow SS''$$

$$S'' \rightarrow cS \mid \epsilon$$

$$\Rightarrow \begin{cases} S \rightarrow \text{if } S' \mid a \\ S' \rightarrow \text{if } S \text{ then } S \mid \epsilon \end{cases}$$

Ans//

(2)

* for left recursion

- Try to find the terminating condition for the parser.

$$\textcircled{1} \quad A \rightarrow A\alpha | \beta$$

↓

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$\textcircled{6} \quad A \rightarrow A\alpha_1 | A\alpha_2 | \dots | A\alpha_n | \beta_1 | \beta_2 | \dots | \beta_r$$

↓

$$A \rightarrow \beta_1 A' | \beta_2 A' | \dots | \beta_r A'$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \dots | \alpha_n A' | \epsilon$$

$$\textcircled{2} \quad A \rightarrow A\alpha | \beta_1 | \beta_2$$

↓

$$A \rightarrow \beta_1 A' | \beta_2 A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$\textcircled{3} \quad A \rightarrow A\alpha_1 | A\alpha_2 | \beta$$

↓

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \epsilon$$

$$\textcircled{4} \quad A \rightarrow A\alpha | \beta_1 | \beta_2 | \dots | \beta_n$$

↓

$$A \rightarrow \beta_1 A' | \beta_2 A' | \dots | \beta_n A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$\textcircled{5} \quad A \rightarrow A\alpha_1 | A\alpha_2 | \dots | A\alpha_n | \beta$$

↓

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \dots | \alpha_n A'$$

Date: / /

Q) $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid id$
 \Downarrow

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow *FT' \mid \epsilon$
 $F \rightarrow (E) \mid id$

Q) $S \rightarrow Sab \mid c$
 \Downarrow
 $S \rightarrow cS'$
 $S' \rightarrow abs' \mid \epsilon$

Q) $S \rightarrow SSS \mid \alpha$

$S \rightarrow \alpha S'$
 $S' \rightarrow sss' \mid \epsilon$

Q) $A \rightarrow A \alpha A$
 $A \rightarrow A(A) \mid a$
 \Downarrow
 $A \rightarrow aA'$
 $A' \rightarrow (A) A' \mid \epsilon$

Q) $A \rightarrow AaA \mid b$

$A \rightarrow bA'$
 $A' \rightarrow aAA' \mid \epsilon$

Syntax Analyzer

Parsing techniques - Syntax Analysis

\rightarrow Top-down
 \rightarrow Bottom-up

① Top-down

- Root node to leaves
- Left most derivation
- Parse Tree decision based on production selected

Types

- i). Top-down with backtracking
(Recursive descent)
- ii). Top-down without backtracking
(Predictive parsing / LL1)

② Bottom-up

- Leaves \rightarrow root node
- Right most derivation
- Making a parsing tree is based on terminals (strings)

Types

- i). Operator precedence

ii). LR Parser

\rightarrow LR(0)
 \rightarrow SLR(1)
 \rightarrow LALR(1)
 \rightarrow CLR(1)

* Recursive Descent

$$\left. \begin{array}{l}
 E \rightarrow E + T \mid T \\
 T \rightarrow T * F \mid F \\
 F \rightarrow (E) \mid id
 \end{array} \right\} \quad \left. \begin{array}{l}
 E \rightarrow TE' \quad E' \rightarrow +TE' \mid \epsilon \\
 T \rightarrow FT' \quad T' \rightarrow *FT' \mid \epsilon \\
 F \rightarrow (E) \mid id
 \end{array} \right.$$

$\rightarrow id + id * id$

$E \rightarrow TE'$
 $E' \rightarrow +TE' | e$

① $id + id * id$
↑

$T \rightarrow FT'$

$T' \rightarrow *FT' | e$

$E \rightarrow TE'$

$F \rightarrow (E) | id$

$E \rightarrow FT'E'$
↑
 $\rightarrow (E)T'E'$) Backtrack

$E \rightarrow id T'E'$
↑

⑤ $id + id * id$
↑

② $id + id * id$
↑

$E \rightarrow id + id * (E)T'E'E'$
 $\rightarrow id + id * id T'E'E'$

$E \rightarrow id T'E'$
↑
 $\rightarrow id * FT'E'$) Backtrack

$E \rightarrow id EE'$

$E \rightarrow id E'$

$E \rightarrow id + TE'E'$
↑

⑥ $E \rightarrow id + id * id E E'E'$
 $\rightarrow id + id * id EE'$
 $\rightarrow id + id * id E$
 $\rightarrow id + id * id .$

③ $id + id * id$
↑

$E \rightarrow id + TE'E'$

$\rightarrow id + FT'E'E'$
↑
 $\rightarrow id + (E)T'E'E'$
 $\rightarrow id + id T'E'E'$

④ $id + id * id$
↑

$E \rightarrow id + id * FT'E'E'$

Q). $S \rightarrow p A y$ String = " play "
 $A \rightarrow a / \lambda a$

① play

$$S \rightarrow p \underset{\uparrow}{A} y$$

② play

$$S \rightarrow p \underset{\uparrow}{A} y$$

$$S \rightarrow p \underset{\uparrow}{a} y$$

$$S \rightarrow p \underset{\uparrow}{l} a y$$

③ play

$$S \rightarrow p \underset{\uparrow}{l} a y$$

④ play

$$S \rightarrow p l a y$$

* first & follow

$$S \rightarrow abc \mid d$$

String:- aabb
:- d

If the parser knows in advance, what comes in the string, then the possibility of backtracking is eliminated.

* first()

→ If α is any string of grammar, then $\text{First}(\alpha)$ is the set of terminals that are in first position in the string derived from α .

1. If the terminal symbol occurs in the $\text{First}()$, then $\text{First}(\alpha) = \{a\}$

2. If there is a rule $\alpha \rightarrow \epsilon$, then $\text{First}(\alpha) = \{\epsilon\}$

3. ~~for the rule,~~

$$\alpha \rightarrow x_1 x_2 x_3 \dots x_n \quad | \quad \alpha \rightarrow x_1 \mid x_2 \mid x_3 \mid \dots \mid x_n$$

$$\text{First}(\alpha) = \text{First}(x_1) \cup \text{First}(x_2) \cup \text{First}(x_3) \dots \cup \text{First}(x_n)$$

4. If $X \rightarrow Y a$, then $\text{first}(X) = \text{first}(Y)$, provided $\text{first}(Y)$ shouldn't contain ϵ .

① $S \rightarrow aAB$

$$\text{First}(S) = \{a\}$$

$$A \rightarrow bA \mid c$$

$$\text{First}(A) = \{b, c\}$$

$$B \rightarrow c \mid d \mid \epsilon$$

$$\text{First}(B) = \{c, d, \epsilon\}$$

② $S \rightarrow aAb$

$$\text{First}(S) = \{a\}$$

$$A \rightarrow bA \mid Bd$$

$$\text{First}(A) = \{b\} \cup \{c, d\} = \{b, c, d\}$$

$$B \rightarrow c \mid d$$

$$\text{First}(B) = \{c, d\}$$

$$\textcircled{3} \quad S \rightarrow (s) \mid \epsilon \quad \text{first}(s) = \{ _, \epsilon \}$$

$$\textcircled{4} \quad S \rightarrow (s) \mid a \quad \text{first}(s) = \{ _, a \}$$

$$\textcircled{5} \quad \begin{array}{l} S \rightarrow AB \\ A \rightarrow aA \mid b \\ B \rightarrow c \end{array} \quad \begin{array}{l} \text{first}(s) = \text{first}(A) = \{ a, b \} \\ \text{first}(A) = \{ a, b \} \\ \text{first}(B) = \{ c \} \end{array}$$

$$\textcircled{6} \quad \begin{array}{l} S \rightarrow AB \\ A \rightarrow a \mid \epsilon \\ B \rightarrow c \end{array} \quad \begin{array}{l} \text{first}(s) = \{ \text{first}(A) - \epsilon \} \cup \text{first}(B) = \{ a, c \} \\ \text{first}(A) = \{ a, \epsilon \} \\ \text{first}(B) = \{ c \} \end{array}$$

$$\textcircled{7} \quad \begin{array}{l} S \rightarrow ABCDE \\ A \rightarrow a \mid \epsilon \\ B \rightarrow b \mid \epsilon \\ C \rightarrow c \mid \epsilon \\ D \rightarrow d \mid \epsilon \\ E \rightarrow e \mid \epsilon \end{array} \quad \begin{array}{l} \text{first}(s) = \{ a, b, c, d, e, \epsilon \} \\ \text{first}(A) = \{ a, \epsilon \} \\ \text{first}(B) = \{ b, \epsilon \} \\ \text{first}(C) = \{ c, \epsilon \} \\ \text{first}(D) = \{ d, \epsilon \} \\ \text{first}(E) = \{ e, \epsilon \} \end{array}$$

x

If $X \rightarrow Y_1 Y_2 Y_3 \dots Y_n$

$$\textcircled{1} \quad \text{first}(X) = \text{first}(Y_i)$$

$$\textcircled{2} \quad \text{first}(Y_i) = \{ \epsilon \} \Rightarrow \text{first}(X) = \{ \text{first}\{Y_i\} - \epsilon \} \cup \text{first}\{Y_i\}$$

\textcircled{3} If $\text{first}(Y_i), i \in N$ contains ϵ

$\Leftrightarrow \text{first}(X)$ contains ϵ .