# 5\_Experiment\_with\_more\_powerful\_regression\_models

September 5, 2021

## 1 Regression - Experimenting with additional models

In the previous notebook, we used simple regression models to look at the relationship between features of a bike rentals dataset. In this notebook, we'll experiment with more complex models to improve our regression performance.

Let's start by loading the bicycle sharing data as a **Pandas** DataFrame and viewing the first few rows. We'll also split our data into training and test datasets.

```
[1]: # Import modeules we'll need for this notebook
  import pandas as pd
  from sklearn.linear_model import LinearRegression
  from sklearn.metrics import mean_squared_error, r2_score
  from sklearn.model_selection import train_test_split
  import numpy as np
  import matplotlib.pyplot as plt
  %matplotlib inline
```

```
[2]: # load the training dataset
bike_data = pd.read_csv('daily-bike-share.csv')
bike_data['day'] = pd.DatetimeIndex(bike_data['dteday']).day
numeric_features = ['temp', 'atemp', 'hum', 'windspeed']
categorical_features =

→['season','mnth','holiday','weekday','workingday','weathersit', 'day']
```

	instant	dteday	season	уr	$\mathtt{mnth}$	holiday	weekday	workingday	\
0	1	1/1/2011	1	0	1	0	6	0	
1	2	1/2/2011	1	0	1	0	0	0	
2	3	1/3/2011	1	0	1	0	1	1	
3	4	1/4/2011	1	0	1	0	2	1	
4	5	1/5/2011	1	0	1	0	3	1	

	weathersit	${\tt temp}$	${\tt atemp}$	hum	windspeed	rentals	day	
0	2	0.344167	0.363625	0.805833	0.160446	331	1	
1	2	0.363478	0.353739	0.696087	0.248539	131	2	
2	1	0.196364	0.189405	0.437273	0.248309	120	3	
3	1	0.200000	0.212122	0.590435	0.160296	108	4	
4	1	0.226957	0.229270	0.436957	0.186900	82	5	

```
[3]: bike_data[numeric_features + ['rentals']].describe()
[3]:
                                                   windspeed
                  temp
                              atemp
                                            hum
                                                                  rentals
     count
            731.000000
                        731.000000
                                     731.000000
                                                 731.000000
                                                               731.000000
              0.495385
                           0.474354
                                       0.627894
                                                    0.190486
                                                               848.176471
     mean
     std
              0.183051
                           0.162961
                                       0.142429
                                                    0.077498
                                                               686.622488
    min
              0.059130
                           0.079070
                                       0.000000
                                                    0.022392
                                                                 2.000000
     25%
              0.337083
                                                    0.134950
                                       0.520000
                                                               315.500000
                           0.337842
     50%
              0.498333
                           0.486733
                                       0.626667
                                                    0.180975
                                                               713.000000
     75%
              0.655417
                           0.608602
                                       0.730209
                                                    0.233214
                                                              1096.000000
              0.861667
     max
                           0.840896
                                       0.972500
                                                    0.507463
                                                              3410.000000
[4]: bike_data.head()
[4]:
                                              holiday
                                                        weekday
        instant
                   dteday
                           season
                                    yr
                                        mnth
                                                                 workingday
     0
              1 1/1/2011
                                 1
                                     0
                                           1
                                                     0
                                                              6
                                                                           0
     1
              2 1/2/2011
                                     0
                                           1
                                                     0
                                                              0
                                                                           0
                                 1
     2
              3 1/3/2011
                                 1
                                           1
                                                     0
                                                              1
                                                                           1
     3
              4 1/4/2011
                                     0
                                           1
                                                     0
                                                              2
                                                                           1
                                 1
     4
              5 1/5/2011
                                 1
                                     0
                                           1
                                                     0
                                                              3
                                                                           1
        weathersit
                         temp
                                  atemp
                                              hum
                                                    windspeed rentals
     0
                    0.344167 0.363625
                                         0.805833
                                                     0.160446
                                                                   331
                                                                           1
     1
                 2 0.363478 0.353739
                                         0.696087
                                                     0.248539
                                                                   131
                                                                           2
                 1 0.196364 0.189405
                                         0.437273
                                                                   120
                                                                           3
                                                     0.248309
                                         0.590435
     3
                    0.200000 0.212122
                                                     0.160296
                                                                   108
                                                                           4
     4
                 1 0.226957 0.229270 0.436957
                                                     0.186900
                                                                    82
                                                                           5
[5]: # Separate features and labels
     # After separating the dataset, we now have numpy arrays named **X** containing
     → the features, and **y** containing the labels.
     X, y = bike_data[['season', 'mnth', __
      → 'holiday', 'weekday', 'workingday', 'weathersit', 'temp', 'atemp', 'hum', ⊔
      →'windspeed']].values, bike_data['rentals'].values
[6]: # Split data 70%-30% into training set and test set
     X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.30, u)
     →random_state=0)
     # Split data 70%-30% into training set and test set
     X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.30, __
      →random_state=0)
     print ('Training Set: %d rows\nTest Set: %d rows\" % (X_train.shape[0], X_test.
      \rightarrowshape[0]))
    Training Set: 511 rows
```

Test Set: 220 rows

Now we have the following four datasets:

- X train: The feature values we'll use to train the model
- y\_train: The corresponding labels we'll use to train the model
- $X_{test}$ : The feature values we'll use to validate the model
- **y\_test**: The corresponding labels we'll use to validate the model

Now we're ready to train a model by fitting a suitable regression algorithm to the training data.

### 1.1 Experiment with Algorithms

The linear regression algorithm we used last time to train the model has some predictive capability, but there are many kinds of regression algorithm we could try, including:

- Linear algorithms: Not just the Linear Regression algorithm we used above (which is technically an *Ordinary Least Squares* algorithm), but other variants such as *Lasso* and *Ridge*.
- Tree-based algorithms: Algorithms that build a decision tree to reach a prediction.
- Ensemble algorithms: Algorithms that combine the outputs of multiple base algorithms to improve generalizability.

**Note**: For a full list of Scikit-Learn estimators that encapsulate algorithms for supervised machine learning, see the Scikit-Learn documentation. There are many algorithms to choose from, but for most real-world scenarios, the Scikit-Learn estimator cheat sheet can help you find a suitable starting point.

### 1.1.1 Try Another Linear Algorithm

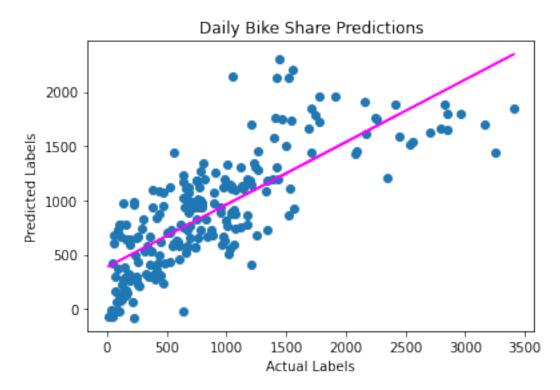
Let's try training our regression model by using a **Lasso** algorithm. We can do this by just changing the estimator in the training code.

```
[7]: from sklearn.linear_model import Lasso
     # Fit a lasso model on the training set
     model = Lasso().fit(X_train, y_train)
     print(model, "\n")
     # Evaluate the model using the test data
     predictions = model.predict(X_test)
     mse = mean_squared_error(y_test, predictions)
     print("MSE:", mse)
     rmse = np.sqrt(mse)
     print("RMSE:", rmse)
     r2 = r2_score(y_test, predictions)
     print("R2:", r2)
     # Plot predicted vs actual
     plt.scatter(y test, predictions)
     plt.xlabel('Actual Labels')
     plt.ylabel('Predicted Labels')
     plt.title('Daily Bike Share Predictions')
```

```
# overlay the regression line
z = np.polyfit(y_test, predictions, 1)
p = np.poly1d(z)
plt.plot(y_test,p(y_test), color='magenta')
plt.show()
```

### Lasso()

MSE: 201155.70593338402 RMSE: 448.5038527519959 R2: 0.605646863782449



## 1.1.2 Try a Decision Tree Algorithm

As an alternative to a linear model, there's a category of algorithms for machine learning that uses a tree-based approach in which the features in the dataset are examined in a series of evaluations, each of which results in a *branch* in a *decision tree* based on the feature value. At the end of each series of branches are leaf-nodes with the predicted label value based on the feature values.

It's easiest to see how this works with an example. Let's train a Decision Tree regression model using the bike rental data. After training the model, the code below will print the model definition and a text representation of the tree it uses to predict label values.

```
[9]: from sklearn.tree import DecisionTreeRegressor
from sklearn.tree import export_text

# Train the model
model = DecisionTreeRegressor().fit(X_train,y_train)
print(model, "\n")

# Visualize the model tree
tree = export_text(model)
print(tree)
```

#### DecisionTreeRegressor()

```
|--- feature_6 <= 0.45
    |--- feature_4 <= 0.50
        |--- feature_7 <= 0.32
            |--- feature_8 <= 0.41
                |--- feature_1 <= 2.50
                    |--- feature 7 <= 0.26
                        |--- value: [317.00]
                    |--- feature 7 > 0.26
                        |--- feature_8 <= 0.36
                            |--- value: [558.00]
                        |--- feature_8 > 0.36
                            |--- value: [515.00]
                |--- feature_1 > 2.50
                    |--- feature_9 <= 0.28
                        |--- feature_6 <= 0.28
                            |--- value: [981.00]
                        |--- feature_6 > 0.28
                          |--- value: [968.00]
                    |--- feature_9 > 0.28
                        |--- feature_1 <= 7.00
                            |--- value: [710.00]
                        |--- feature_1 > 7.00
                            |--- value: [532.00]
              -- feature_8 > 0.41
                |--- feature_7 <= 0.25
                    |--- feature_6 <= 0.18
                        |--- feature_8 <= 0.43
                            |--- value: [284.00]
                        |--- feature_8 > 0.43
                            |--- feature_7 <= 0.10
                                |--- value: [150.00]
                            |--- feature_7 > 0.10
                                |--- feature_7 <= 0.18
                                   |--- feature_9 <= 0.34
                                    |--- feature_7 <= 0.17
```

```
|--- value: [68.00]
                     |--- feature_7 > 0.17
                         |--- value: [67.00]
                 |--- feature_9 > 0.34
                     |--- value: [73.00]
             |--- feature_7 > 0.18
                 |--- value: [117.00]
    - feature_6 > 0.18
        - feature_9 <= 0.17
         |--- feature_9 <= 0.11
             |--- value: [140.00]
         |--- feature_9 > 0.11
             |--- value: [123.00]
     |--- feature_9 > 0.17
         |--- feature_6 <= 0.19
             |--- value: [333.00]
         |--- feature_6 > 0.19
             |--- feature_8 <= 0.53
                 |--- feature_9 <= 0.21
                     |--- value: [251.00]
                 |--- feature_9 > 0.21
                     |--- feature_6 <= 0.23
                        |--- value: [217.00]
                     |--- feature_6 > 0.23
                         |--- value: [205.00]
             |--- feature_8 > 0.53
                 |--- feature_8 <= 0.55
                     |--- value: [288.00]
                 |--- feature_8 > 0.55
                     |--- value: [275.00]
- feature_7 > 0.25
 |--- feature_9 <= 0.11
     |--- value: [706.00]
 |--- feature_9 > 0.11
     |--- feature_8 <= 0.54
         |--- feature_5 <= 1.50
             |--- feature_7 <= 0.26
                 |--- value: [309.00]
             |--- feature_7 > 0.26
                 |--- feature_0 <= 2.50
                     |--- feature_3 <= 0.50
                         |--- value: [408.00]
                     |--- feature_3 > 0.50
                         |--- truncated branch of depth 2
                 |--- feature_0 > 2.50
                     |--- feature_9 <= 0.27
                         |--- value: [502.00]
                     |--- feature_9 > 0.27
```

```
| | | |--- value: [440.00]
                   |--- feature_5 > 1.50
                       |--- value: [618.00]
               |--- feature_8 > 0.54
                   |--- feature_6 <= 0.29
                       |--- feature_5 <= 1.50
                           |--- value: [354.00]
                       |--- feature_5 > 1.50
                           |--- value: [318.00]
                   |--- feature_6 > 0.29
                       |--- feature_9 <= 0.25
                           |--- value: [155.00]
                       |--- feature_9 > 0.25
                          |--- value: [195.00]
|--- feature_7 > 0.32
   |--- feature_9 <= 0.25
       |--- feature_7 <= 0.38
           |--- feature_7 <= 0.36
                |--- feature_6 <= 0.36
                   |--- feature_1 <= 10.50
                       |--- feature_7 <= 0.33
                           |--- feature_9 <= 0.21
                               |--- feature_0 <= 1.50
                               | |--- value: [1047.00]
                               |--- feature_0 > 1.50
                                   |--- truncated branch of depth 2
                               |--- feature_9 > 0.21
                               |--- value: [724.00]
                       |--- feature_7 > 0.33
                           |--- feature_8 <= 0.83
                               |--- feature_7 <= 0.35
                                  |--- truncated branch of depth 2
                               |--- feature_7 > 0.35
                               | |--- value: [694.00]
                           |--- feature_8 > 0.83
                               |--- value: [879.00]
                     -- feature 1 > 10.50
                       |--- feature_8 <= 0.57
                           |--- feature_9 <= 0.22
                               |--- feature_8 <= 0.53
                               | |--- value: [1156.00]
                               |--- feature_8 > 0.53
                                   |--- truncated branch of depth 2
                           |--- feature_9 > 0.22
                           | |--- value: [943.00]
                       |--- feature_8 > 0.57
                           |--- feature_9 <= 0.10
                           | |--- feature_8 <= 0.66
```

```
|--- value: [955.00]
                     |--- feature_8 > 0.66
                         |--- truncated branch of depth 2
                 |--- feature_9 > 0.10
                     |--- feature 9 <= 0.17
                         |--- value: [767.00]
                     |--- feature_9 > 0.17
                         |--- value: [922.00]
       -- feature_6 > 0.36
         |--- value: [1658.00]
 |--- feature_7 > 0.36
     |--- feature_0 <= 2.50
         |--- value: [331.00]
     |--- feature_0 > 2.50
         |--- feature_6 <= 0.37
             |--- value: [538.00]
         |--- feature_6 > 0.37
            |--- value: [560.00]
- feature_7 > 0.38
 |--- feature_9 <= 0.24
     |--- feature_9 <= 0.15
         |--- feature_8 <= 0.67
             |--- feature_9 <= 0.14
                 |--- value: [2290.00]
             |--- feature_9 > 0.14
                 |--- value: [2252.00]
         |--- feature_8 > 0.67
             |--- feature_6 <= 0.40
                 |--- feature_9 <= 0.08
                     |--- value: [1249.00]
                 |--- feature_9 > 0.08
                     |--- value: [1153.00]
             |--- feature_6 > 0.40
                 |--- value: [1619.00]
        - feature 9 > 0.15
         |--- feature_8 <= 0.51
             |--- value: [1651.00]
         |--- feature_8 > 0.51
             |--- feature_9 <= 0.20
                 |--- feature_9 <= 0.15
                     |--- value: [1188.00]
                 |--- feature_9 > 0.15
                     |--- feature_8 <= 0.58
                         |--- value: [1070.00]
                     |--- feature_8 > 0.58
                         |--- truncated branch of depth 2
             |--- feature_9 > 0.20
                 |--- feature_1 <= 8.00
```

```
|--- value: [642.00]
                             |--- feature_1 > 8.00
                                 |--- value: [665.00]
             |--- feature_9 > 0.24
                 |--- value: [2301.00]
       -- feature_9 > 0.25
         |--- feature 8 <= 0.81
             |--- feature_6 <= 0.35
                 |--- value: [397.00]
             |--- feature_6 > 0.35
                 |--- feature_3 <= 3.00
                     |--- value: [982.00]
                 |--- feature_3 > 3.00
                     |--- feature_6 <= 0.40
                         |--- value: [640.00]
                     |--- feature_6 > 0.40
                     1
                         |--- value: [480.00]
         |--- feature_8 > 0.81
             |--- feature_7 <= 0.41
               |--- value: [120.00]
             |--- feature_7 > 0.41
                 |--- value: [121.00]
- feature_4 > 0.50
 |--- feature_6 <= 0.34
     |--- feature_1 <= 2.50
         |--- feature_7 <= 0.29
             |--- feature_7 <= 0.19
                 |--- feature_7 <= 0.14
                     |--- feature_5 <= 1.50
                         |--- feature_6 <= 0.12
                         | |--- value: [86.00]
                         |--- feature_6 > 0.12
                            |--- value: [89.00]
                         1
                     |--- feature_5 > 1.50
                         |--- value: [95.00]
                 |--- feature_7 > 0.14
                     |--- feature_8 <= 0.46
                         |--- feature_3 <= 4.50
                            |--- value: [61.00]
                         |--- feature_3 > 4.50
                             |--- value: [75.00]
                     |--- feature_8 > 0.46
                         |--- feature_9 <= 0.30
                             |--- feature_8 <= 0.49
                                 |--- feature_9 <= 0.26
                                     |--- value: [41.00]
                                 |--- feature_9 > 0.26
                                 | |--- value: [38.00]
```

```
|--- feature_8 > 0.49
                 |--- feature_6 <= 0.17
                     |--- truncated branch of depth 2
                 |--- feature_6 > 0.17
                     |--- value: [42.00]
                 1
           -- feature_9 > 0.30
             |--- value: [25.00]
- feature_7 > 0.19
    - feature_3 <= 4.50
     |--- feature_9 <= 0.26
        |--- feature_3 <= 2.50
             |--- feature_5 <= 1.50
                 |--- feature_9 <= 0.19
                     |--- truncated branch of depth 2
                 |--- feature_9 > 0.19
                    |--- truncated branch of depth 2
             |--- feature_5 > 1.50
                 |--- feature_7 <= 0.24
                     |--- value: [186.00]
                 |--- feature_7 > 0.24
                     |--- truncated branch of depth 2
            - feature 3 > 2.50
             |--- feature_8 <= 0.51
                 |--- feature_6 <= 0.22
                     |--- truncated branch of depth 2
                 |--- feature_6 > 0.22
                     |--- value: [82.00]
             |--- feature_8 > 0.51
                 |--- feature_6 <= 0.20
                     |--- value: [15.00]
                 |--- feature_6 > 0.20
                     |--- truncated branch of depth 4
     |--- feature_9 > 0.26
          -- feature_6 <= 0.22
             |--- value: [34.00]
         |--- feature_6 > 0.22
             |--- feature_9 <= 0.31
                |--- value: [72.00]
             |--- feature_9 > 0.31
                 |--- value: [64.00]
            - feature_3 > 4.50
     |--- feature_8 <= 0.47
        |--- value: [115.00]
    |--- feature_8 > 0.47
        |--- feature_6 <= 0.24
            |--- feature_1 <= 1.50
                |--- value: [148.00]
            |--- feature_1 > 1.50
```

```
| | |--- value: [149.00]
                  |--- feature_6 > 0.24
                     |--- value: [174.00]
   -- feature_7 > 0.29
     |--- feature 3 <= 4.50
         |--- feature_9 <= 0.15
              |--- feature 9 <= 0.12
                 |--- value: [74.00]
              |--- feature_9 > 0.12
                 |--- value: [135.00]
          |--- feature_9 > 0.15
              |--- feature_9 <= 0.23
                  |--- feature_6 <= 0.29
                      |--- value: [206.00]
                  |--- feature_6 > 0.29
                      |--- feature_1 <= 1.50
                     | |--- value: [173.00]
                      |--- feature_1 > 1.50
                         |--- value: [163.00]
              |--- feature_9 > 0.23
                 |--- value: [218.00]
         - feature 3 > 4.50
          --- feature_5 <= 1.50
              |--- feature_8 <= 0.53
                 |--- value: [310.00]
              |--- feature_8 > 0.53
                 |--- value: [307.00]
          |--- feature_5 > 1.50
             |--- value: [227.00]
-- feature_1 > 2.50
 |--- feature_9 <= 0.20
     |--- feature_9 <= 0.12
         |--- feature_9 <= 0.06
              |--- feature_3 <= 3.00
                 |--- value: [337.00]
              |--- feature_3 > 3.00
                 |--- value: [362.00]
            -- feature_9 > 0.06
              |--- feature_3 <= 3.50
                  |--- feature_5 <= 1.50
                     |--- value: [143.00]
                  |--- feature_5 > 1.50
                     |--- feature_6 <= 0.27
                         |--- value: [174.00]
                      |--- feature_6 > 0.27
                          |--- value: [178.00]
              |--- feature_3 > 3.50
                 |--- feature_8 <= 0.60
```

```
|--- feature_1 <= 11.50
                        |--- value: [243.00]
                    |--- feature_1 > 11.50
                        |--- value: [254.00]
                |--- feature_8 > 0.60
                    |--- feature_8 <= 0.66
                        |--- value: [268.00]
                    |--- feature_8 > 0.66
                        |--- value: [261.00]
    |--- feature_9 > 0.12
        |--- feature_8 <= 0.64
            |--- feature_8 <= 0.45
                |--- feature_8 <= 0.42
                    |--- value: [245.00]
                |--- feature_8 > 0.42
                    |--- value: [316.00]
            |--- feature_8 > 0.45
                |--- feature_8 <= 0.63
                    |--- feature_7 <= 0.30
                        |--- feature_9 <= 0.17
                            |--- truncated branch of depth 3
                        |--- feature_9 > 0.17
                            |--- truncated branch of depth 2
                    |--- feature_7 > 0.30
                        |--- feature_8 <= 0.52
                            |--- value: [359.00]
                        |--- feature_8 > 0.52
                            |--- truncated branch of depth 3
                |--- feature_8 > 0.63
                    |--- feature_0 <= 2.50
                        |--- value: [491.00]
                    |--- feature_0 > 2.50
                        |--- value: [429.00]
           - feature_8 > 0.64
            |--- feature 7 <= 0.31
                |--- value: [168.00]
            |--- feature_7 > 0.31
                |--- feature_8 <= 0.72
                    |--- feature_7 <= 0.33
                        |--- value: [289.00]
                    |--- feature_7 > 0.33
                        |--- value: [314.00]
                |--- feature_8 > 0.72
                    |--- value: [349.00]
|--- feature_9 > 0.20
    |--- feature_8 <= 0.78
        |--- feature_9 <= 0.23
          |--- feature_9 <= 0.21
        1
```

```
|--- feature_7 <= 0.27
        |--- feature_0 <= 1.50
            |--- value: [221.00]
        |--- feature_0 > 1.50
            |--- value: [222.00]
      -- feature_7 > 0.27
        |--- value: [198.00]
|--- feature_9 > 0.21
      - feature_6 <= 0.28
        |--- feature_9 <= 0.22
            |--- value: [137.00]
        |--- feature_9 > 0.22
            |--- value: [123.00]
      -- feature_6 > 0.28
        |--- feature_3 <= 4.00
            |--- value: [191.00]
        |--- feature_3 > 4.00
            |--- value: [177.00]
feature_9 > 0.23
|--- feature_3 <= 4.50
    |--- feature_8 <= 0.56
        |--- feature_0 <= 1.50
            |--- feature_6 <= 0.25
                |--- value: [203.00]
            |--- feature_6 > 0.25
                |--- truncated branch of depth 3
        |--- feature_0 > 1.50
            |--- feature_6 <= 0.30
                |--- value: [326.00]
            |--- feature_6 > 0.30
                |--- value: [317.00]
    |--- feature_8 > 0.56
        |--- feature_0 <= 3.00
            |--- feature_8 <= 0.71
                |--- value: [247.00]
            |--- feature_8 > 0.71
                |--- value: [195.00]
        |--- feature_0 > 3.00
            |--- feature_8 <= 0.58
                |--- value: [139.00]
            |--- feature_8 > 0.58
                |--- value: [150.00]
|--- feature_3 > 4.50
    |--- feature_9 <= 0.23
        |--- value: [456.00]
    |--- feature_9 > 0.23
        |--- feature_7 <= 0.29
           |--- feature_6 <= 0.28
```

```
|--- value: [300.00]
                             |--- feature_6 > 0.28
                                 |--- value: [307.00]
                         |--- feature_7 > 0.29
                             |--- value: [247.00]
            - feature 8 > 0.78
             |--- feature 1 <= 11.50
                 |--- feature_7 <= 0.28
                     |--- feature_5 <= 2.50
                         |--- value: [166.00]
                     |--- feature_5 > 2.50
                         |--- value: [179.00]
                 |--- feature_7 > 0.28
                     |--- feature_7 <= 0.30
                         |--- value: [123.00]
                     |--- feature_7 > 0.30
                     1
                       |--- value: [87.00]
             |--- feature_1 > 11.50
                 |--- value: [9.00]
- feature 6 > 0.34
 |--- feature_3 <= 4.50
     |--- feature_8 <= 0.48
         |--- feature_6 <= 0.42
             |--- feature_8 <= 0.44
                 |--- feature_3 <= 1.50
                     |--- value: [208.00]
                 |--- feature_3 > 1.50
                     |--- feature_9 <= 0.23
                         |--- value: [229.00]
                     |--- feature_9 > 0.23
                         |--- feature_6 <= 0.37
                             |--- value: [340.00]
                         |--- feature_6 > 0.37
                         |--- value: [324.00]
               -- feature 8 > 0.44
                 |--- feature_3 <= 3.50
                     |--- feature_8 <= 0.47
                         |--- feature_7 <= 0.37
                         | |--- value: [482.00]
                         |--- feature_7 > 0.37
                            |--- value: [518.00]
                     |--- feature_8 > 0.47
                         |--- value: [413.00]
                 |--- feature_3 > 3.50
                     |--- value: [663.00]
         |--- feature_6 > 0.42
             |--- feature_8 <= 0.40
                 |--- value: [1192.00]
```

```
|--- feature_8 > 0.40
        |--- feature_7 <= 0.44
            |--- feature_8 <= 0.45
               |--- value: [819.00]
            |--- feature_8 > 0.45
               |--- value: [834.00]
        |--- feature_7 > 0.44
            |--- value: [795.00]
feature_8 > 0.48
|--- feature_5 <= 1.50
   |--- feature_8 <= 0.55
        |--- feature_1 <= 2.50
            |--- feature_6 <= 0.36
                |--- feature_6 <= 0.35
                    |--- value: [141.00]
                |--- feature_6 > 0.35
                    |--- value: [199.00]
            |--- feature_6 > 0.36
                |--- feature_7 <= 0.39
                    |--- value: [253.00]
                |--- feature_7 > 0.39
                    |--- value: [259.00]
            feature_1 > 2.50
            |--- feature_0 <= 2.50
                |--- value: [432.00]
            |--- feature_0 > 2.50
               |--- value: [331.00]
      -- feature_8 > 0.55
        |--- feature_8 <= 0.65
            |--- feature_9 <= 0.19
                |--- feature_6 <= 0.40
                    |--- value: [615.00]
                |--- feature_6 > 0.40
                    |--- value: [571.00]
              -- feature_9 > 0.19
                |--- feature_7 <= 0.42
                    |--- value: [394.00]
                |--- feature_7 > 0.42
                    |--- value: [460.00]
        |--- feature_8 > 0.65
              -- feature_9 <= 0.10
                |--- feature_8 <= 0.74
                    |--- feature_3 <= 2.50
                        |--- value: [376.00]
                    |--- feature_3 > 2.50
                        |--- value: [370.00]
                |--- feature_8 > 0.74
                    |--- value: [305.00]
```

```
|--- feature_9 > 0.10
            |--- feature_7 <= 0.37
                |--- value: [439.00]
            |--- feature_7 > 0.37
                |--- feature_8 <= 0.67
                    |--- value: [433.00]
                |--- feature_8 > 0.67
                    |--- value: [410.00]
                feature_5 > 1.50
|--- feature_7 <= 0.39
   |--- feature_9 <= 0.17
        |--- feature_1 <= 10.50
           |--- value: [330.00]
        |--- feature_1 > 10.50
            |--- feature_6 <= 0.37
                |--- value: [466.00]
            |--- feature_6 > 0.37
                |--- value: [534.00]
   |--- feature_9 > 0.17
         -- feature_9 <= 0.35
            |--- feature_8 <= 0.82
                |--- feature_7 <= 0.37
                    |--- truncated branch of depth 3
                |--- feature_7 > 0.37
                    |--- value: [269.00]
            |--- feature_8 > 0.82
               |--- value: [203.00]
        |--- feature_9 > 0.35
            |--- value: [127.00]
  - feature_7 > 0.39
   |--- feature_9 <= 0.26
        |--- feature_1 <= 3.00
            |--- value: [190.00]
          - feature_1 > 3.00
            |--- feature_7 <= 0.40
                |--- value: [233.00]
            |--- feature_7 > 0.40
                |--- feature_7 <= 0.42
                   |--- truncated branch of depth 3
                |--- feature_7 > 0.42
                |--- truncated branch of depth 2
   |--- feature_9 > 0.26
       |--- feature_8 <= 0.75
            |--- feature_8 <= 0.69
                |--- feature_8 <= 0.64
                    |--- value: [181.00]
                |--- feature_8 > 0.64
               | |--- value: [167.00]
```

```
|--- feature_8 > 0.69
                         |--- value: [255.00]
                 |--- feature_8 > 0.75
                     |--- feature_8 <= 0.88
                         |--- feature_6 <= 0.42
                             |--- value: [81.00]
                         |--- feature_6 > 0.42
                             |--- value: [112.00]
                       -- feature_8 > 0.88
                         |--- feature_6 <= 0.42
                             |--- value: [50.00]
                         |--- feature_6 > 0.42
                             |--- value: [2.00]
- feature_3 > 4.50
 |--- feature_8 <= 0.39
     |--- value: [1807.00]
 --- feature_8 > 0.39
     |--- feature_5 <= 1.50
         |--- feature_7 <= 0.37
             |--- feature_6 <= 0.35
                 |--- value: [484.00]
             |--- feature_6 > 0.35
                 |--- feature_9 <= 0.24
                     |--- value: [709.00]
                 |--- feature_9 > 0.24
                     |--- value: [618.00]
                 -- feature_7 > 0.37
             |--- feature_9 <= 0.12
                 |--- value: [1095.00]
             |--- feature_9 > 0.12
                 |--- value: [1603.00]
     |--- feature_5 > 1.50
         |--- feature_7 <= 0.37
             |--- feature_6 <= 0.36
                 |--- value: [246.00]
             |--- feature_6 > 0.36
                 |--- value: [178.00]
           -- feature_7 > 0.37
             |--- feature_7 <= 0.39
                 |--- value: [796.00]
             |--- feature_7 > 0.39
                 |--- feature_6 <= 0.42
                     |--- feature_6 <= 0.41
                         |--- value: [470.00]
                     |--- feature_6 > 0.41
                         |--- value: [447.00]
                 |--- feature_6 > 0.42
                     |--- value: [548.00]
```

```
|--- feature_6 > 0.45
    |--- feature_4 <= 0.50
        |--- feature_8 <= 0.83
            |--- feature_1 <= 10.50
                |--- feature_9 <= 0.28
                    |--- feature_6 <= 0.81
                        |--- feature_8 <= 0.67
                            |--- feature_9 <= 0.09
                                |--- value: [3065.00]
                            |--- feature_9 > 0.09
                                |--- feature_8 <= 0.66
                                    |--- feature_9 <= 0.15
                                        |--- feature_9 <= 0.14
                                            |--- truncated branch of depth 8
                                        |--- feature_9 > 0.14
                                            |--- truncated branch of depth 3
                                    |--- feature_9 > 0.15
                                        |--- feature_9 <= 0.16
                                            |--- truncated branch of depth 4
                                        |--- feature_9 > 0.16
                                            |--- truncated branch of depth 10
                                   - feature_8 > 0.66
                                    |--- value: [3031.00]
                           - feature_8 > 0.67
                            |--- feature_7 <= 0.67
                                |--- feature_7 <= 0.50
                                    |--- feature_8 <= 0.79
                                        |--- feature_9 <= 0.14
                                            |--- value: [1138.00]
                                        |--- feature_9 > 0.14
                                            |--- truncated branch of depth 2
                                    |--- feature_8 > 0.79
                                        |--- value: [2207.00]
                                   - feature_7 > 0.50
                                    |--- feature_7 <= 0.51
                                        |--- value: [3155.00]
                                    |--- feature_7 > 0.51
                                        |--- feature_6 <= 0.69
                                            |--- truncated branch of depth 7
                                        |--- feature_6 > 0.69
                                            |--- truncated branch of depth 6
                            |--- feature_7 > 0.67
                                |--- feature_6 <= 0.74
                                    |--- feature_3 <= 0.50
                                        |--- feature_8 <= 0.76
                                            |--- value: [1298.00]
                                        |--- feature_8 > 0.76
                                        | |--- value: [1249.00]
```

```
|--- feature_3 > 0.50
                                 |--- feature_0 <= 2.50
                                   | |--- value: [1549.00]
                                   |--- feature_0 > 2.50
                                   | |--- value: [1521.00]
                           |--- feature_6 > 0.74
                           | |--- value: [1920.00]
               |--- feature_6 > 0.81
                   |--- feature_3 <= 3.00
                     |--- value: [1203.00]
                   |--- feature_3 > 3.00
                   | |--- value: [987.00]
           |--- feature_9 > 0.28
               |--- feature_7 <= 0.46
                   |--- value: [1558.00]
               |--- feature_7 > 0.46
                   |--- feature_1 <= 7.00
                   | |--- value: [1198.00]
                   |--- feature_1 > 7.00
                   | |--- value: [998.00]
       |--- feature_1 > 10.50
           |--- feature 8 <= 0.71
           | |--- value: [787.00]
           |--- feature 8 > 0.71
           | |--- value: [1097.00]
   |--- feature_8 > 0.83
       |--- feature_6 <= 0.67
           |--- feature_8 <= 0.88
               |--- feature_9 <= 0.19
               | |--- value: [1582.00]
               |--- feature_9 > 0.19
               | |--- value: [1483.00]
           |--- feature_8 > 0.88
               |--- feature_6 <= 0.48
                   |--- value: [1462.00]
               |--- feature_6 > 0.48
                   |--- feature_9 <= 0.16
                   | |--- value: [902.00]
                   |--- feature_9 > 0.16
                   | |--- value: [1033.00]
               1
       |--- feature_6 > 0.67
           |--- value: [226.00]
|--- feature_4 > 0.50
   |--- feature_8 <= 0.83
      |--- feature_3 <= 4.50
       | |--- feature_7 <= 0.53
       | | |--- feature_9 <= 0.10
           | | |--- feature_7 <= 0.47
```

```
|--- value: [1348.00]
 |--- feature_7 > 0.47
      |--- feature_1 <= 3.50
         |--- value: [1122.00]
     |--- feature 1 > 3.50
          |--- feature_9 <= 0.09
              |--- feature_6 <= 0.49
                  |--- value: [830.00]
              |--- feature_6 > 0.49
                  |--- value: [846.00]
          |--- feature_9 > 0.09
              |--- value: [763.00]
-- feature_9 > 0.10
 |--- feature_9 <= 0.23
      |--- feature_3 <= 2.50
          |--- feature_8 <= 0.64
              |--- feature_9 <= 0.18
                  |--- feature_0 <= 3.00
                      |--- truncated branch of depth 3
                  |--- feature_0 > 3.00
                      |--- truncated branch of depth 2
                 - feature_9 > 0.18
                  |--- feature_9 <= 0.19
                      |--- value: [922.00]
                  |--- feature_9 > 0.19
                      |--- value: [838.00]
            -- feature_8 > 0.64
              |--- feature_9 <= 0.14
                  |--- feature_3 <= 1.50
                      |--- value: [699.00]
                  |--- feature_3 > 1.50
                      |--- value: [637.00]
              |--- feature_9 > 0.14
                  |--- feature_9 <= 0.18
                      |--- value: [409.00]
                  |--- feature_9 > 0.18
                      |--- value: [486.00]
       -- feature_3 > 2.50
            -- feature_6 <= 0.51
              |--- feature_9 <= 0.13
                  |--- value: [655.00]
              |--- feature_9 > 0.13
                  |--- feature_7 <= 0.45
                      |--- value: [516.00]
                  |--- feature_7 > 0.45
                      |--- truncated branch of depth 4
          |--- feature_6 > 0.51
             |--- feature_6 <= 0.54
```

```
|--- feature_7 <= 0.52
                         |--- value: [735.00]
                      |--- feature_7 > 0.52
                          |--- value: [695.00]
                  |--- feature_6 > 0.54
                      |--- feature_0 <= 3.00
                          |--- value: [550.00]
                      |--- feature_0 > 3.00
                          |--- value: [559.00]
                      -- feature_9 > 0.23
         |--- feature_7 <= 0.47
              |--- feature_0 <= 3.00
                 |--- feature_7 <= 0.45
                      |--- value: [614.00]
                  |--- feature_7 > 0.45
                     |--- value: [745.00]
             |--- feature_0 > 3.00
                 |--- value: [471.00]
         |--- feature_7 > 0.47
             |--- feature 9 <= 0.28
                  |--- value: [1008.00]
             |--- feature_9 > 0.28
                  |--- feature_6 <= 0.49
                     |--- value: [905.00]
                 |--- feature_6 > 0.49
                     |--- value: [834.00]
-- feature_7 > 0.53
 |--- feature_9 <= 0.13
     |--- feature_7 <= 0.72
         |--- feature_6 <= 0.68
              |--- feature_8 <= 0.82
                 |--- feature_9 <= 0.09
                      |--- feature_9 <= 0.07
                         |--- truncated branch of depth 2
                      |--- feature_9 > 0.07
                          |--- truncated branch of depth 2
                    -- feature_9 > 0.09
                      |--- feature_6 <= 0.64
                         |--- truncated branch of depth 6
                      |--- feature_6 > 0.64
                         |--- truncated branch of depth 3
                      |--- feature_8 > 0.82
                 |--- value: [1334.00]
         |--- feature_6 > 0.68
             |--- feature_9 <= 0.12
                  |--- feature_8 <= 0.59
                     |--- value: [1177.00]
                 |--- feature_8 > 0.59
```

```
|--- feature_6 <= 0.72
                    | |--- value: [1363.00]
                    |--- feature_6 > 0.72
                        |--- truncated branch of depth 2
              -- feature 9 > 0.12
                |--- feature_9 <= 0.13
                    |--- feature 3 <= 1.50
                        |--- value: [989.00]
                    |--- feature_3 > 1.50
                        |--- truncated branch of depth 2
                |--- feature_9 > 0.13
                    |--- value: [1233.00]
   |--- feature_7 > 0.72
        |--- feature_9 <= 0.11
            |--- feature_0 <= 2.50
               |--- value: [673.00]
            |--- feature_0 > 2.50
               |--- value: [568.00]
        |--- feature_9 > 0.11
            |--- feature_9 <= 0.12
                |--- feature_1 <= 6.50
                   |--- value: [872.00]
                |--- feature_1 > 6.50
                | |--- value: [921.00]
            |--- feature_9 > 0.12
            I
                |--- value: [778.00]
|--- feature_9 > 0.13
    |--- feature_8 <= 0.53
        |--- feature_7 <= 0.73
            |--- feature_9 <= 0.15
                |--- value: [1281.00]
            |--- feature_9 > 0.15
                |--- feature_8 <= 0.51
                    |--- feature_1 <= 6.50
                        |--- truncated branch of depth 6
                    |--- feature_1 > 6.50
                        |--- truncated branch of depth 4
                |--- feature_8 > 0.51
                    |--- feature_6 <= 0.65
                        |--- value: [1242.00]
                    |--- feature_6 > 0.65
                        |--- value: [1032.00]
        |--- feature_7 > 0.73
            |--- value: [1405.00]
   |--- feature_8 > 0.53
        |--- feature_5 <= 1.50
            |--- feature_9 <= 0.17
           | |--- feature_9 <= 0.17
```

```
|--- feature_3 <= 3.50
                             |--- truncated branch of depth 7
                          |--- feature_3 > 3.50
                              |--- truncated branch of depth 2
                      |--- feature_9 > 0.17
                          |--- feature_3 <= 2.50
                              |--- value: [1128.00]
                          |--- feature_3 > 2.50
                              |--- value: [1198.00]
                    -- feature_9 > 0.17
                      |--- feature_7 <= 0.73
                          |--- feature_7 <= 0.66
                             |--- truncated branch of depth 7
                          |--- feature_7 > 0.66
                              |--- truncated branch of depth 5
                      |--- feature_7 > 0.73
                          |--- feature_9 <= 0.19
                              |--- value: [606.00]
                          |--- feature_9 > 0.19
                              |--- value: [662.00]
                          1
               --- feature_5 > 1.50
                  |--- feature 3 <= 1.50
                      |--- feature_8 <= 0.76
                          |--- feature_6 <= 0.57
                             |--- truncated branch of depth 2
                          |--- feature_6 > 0.57
                              |--- truncated branch of depth 4
                      |--- feature_8 > 0.76
                          |--- feature_1 <= 5.50
                              |--- value: [630.00]
                          |--- feature_1 > 5.50
                              |--- value: [653.00]
                    -- feature_3 > 1.50
                      |--- feature_9 <= 0.19
                          |--- feature_9 <= 0.15
                              |--- truncated branch of depth 5
                          |--- feature_9 > 0.15
                              |--- truncated branch of depth 3
                      |--- feature_9 > 0.19
                          |--- feature_1 <= 8.00
                              |--- truncated branch of depth 5
                          |--- feature_1 > 8.00
                             |--- value: [428.00]
-- feature_3 >
               4.50
  |--- feature_1 <= 4.00
      |--- value: [2469.00]
  |--- feature_1 > 4.00
     |--- feature_8 <= 0.72
```

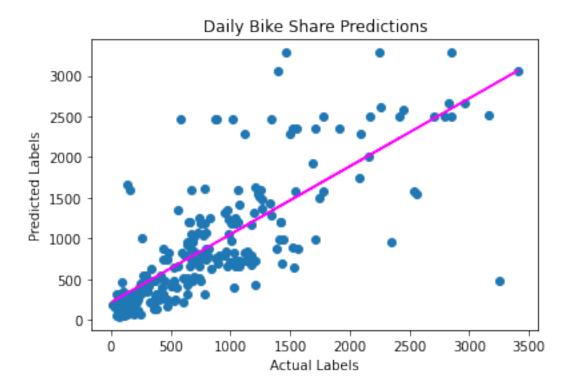
```
|--- feature_9 <= 0.12
    |--- feature_9 <= 0.08
        |--- value: [1325.00]
    |--- feature_9 > 0.08
        |--- feature_8 <= 0.65
           |--- feature_9 <= 0.09
                |--- value: [1511.00]
            |--- feature_9 > 0.09
                |--- value: [1516.00]
         -- feature_8 > 0.65
            |--- value: [1379.00]
    feature_9 > 0.12
    |--- feature_7 <= 0.77
        |--- feature_1 <= 6.50
            |--- feature_8 <= 0.52
                |--- feature_8 <= 0.36
                    |--- value: [898.00]
                |--- feature_8 > 0.36
                    |--- truncated branch of depth 2
              -- feature_8 > 0.52
                |--- feature_0 <= 2.50
                    |--- truncated branch of depth 3
                |--- feature_0 > 2.50
                    |--- truncated branch of depth 2
         -- feature_1 > 6.50
            |--- feature_6 <= 0.72
                |--- feature_6 <= 0.69
                    |--- truncated branch of depth 2
                |--- feature_6 > 0.69
                    |--- truncated branch of depth 3
            |--- feature_6 > 0.72
                |--- feature_9 <= 0.16
                    |--- value: [1366.00]
                |--- feature_9 > 0.16
                    |--- truncated branch of depth 2
    --- feature_7 > 0.77
        |--- feature_8 <= 0.52
            |--- value: [829.00]
        |--- feature_8 > 0.52
            |--- value: [670.00]
        1
feature_8 > 0.72
--- feature_9 <= 0.20
    |--- feature_1 <= 5.50
        |--- feature_9 <= 0.13
           |--- value: [909.00]
        |--- feature_9 > 0.13
           |--- value: [1417.00]
    |--- feature_1 > 5.50
```

```
|--- feature_6 <= 0.55
                           |--- value: [1182.00]
                        |--- feature_6 > 0.55
                           |--- feature_6 <= 0.70
                                |--- feature_8 <= 0.75
                                | |--- truncated branch of depth 2
                                |--- feature_8 > 0.75
                                    |--- truncated branch of depth 2
                            |--- feature_6 > 0.70
                                |--- value: [1045.00]
                |--- feature_9 > 0.20
                    |--- feature_1 <= 8.00
                        |--- value: [533.00]
                    |--- feature_1 > 8.00
                        |--- value: [529.00]
                   |--- feature_8 > 0.83
    |--- feature_5 <= 2.50
        |--- feature_9 <= 0.10
            |--- value: [258.00]
        |--- feature_9 > 0.10
            |--- feature_1 <= 5.50
                |--- feature 9 <= 0.19
                   |--- value: [692.00]
                |--- feature_9 > 0.19
                    |--- feature_3 <= 2.50
                        |--- value: [678.00]
                    |--- feature_3 > 2.50
                        |--- feature_7 <= 0.55
                           |--- value: [536.00]
                        |--- feature_7 > 0.55
                           |--- value: [547.00]
                        1
            |--- feature_1 > 5.50
                |--- feature_8 <= 0.89
                    |--- feature_6 <= 0.60
                        |--- value: [438.00]
                    |--- feature_6 > 0.60
                        |--- feature_3 <= 2.50
                          |--- value: [477.00]
                        |--- feature_3 > 2.50
                           |--- value: [480.00]
                        1
                |--- feature_8 > 0.89
                    |--- value: [555.00]
   |--- feature_5 > 2.50
        |--- feature_6 <= 0.50
            |--- value: [126.00]
        |--- feature_6 > 0.50
            |--- feature_8 <= 0.88
            | |--- value: [315.00]
```

So now we have a tree-based model; but is it any good? Let's evaluate it with the test data.

```
[10]: # Evaluate the model using the test data
      predictions = model.predict(X_test)
      mse = mean_squared_error(y_test, predictions)
      print("MSE:", mse)
      rmse = np.sqrt(mse)
      print("RMSE:", rmse)
      r2 = r2_score(y_test, predictions)
      print("R2:", r2)
      # Plot predicted vs actual
      plt.scatter(y_test, predictions)
      plt.xlabel('Actual Labels')
      plt.ylabel('Predicted Labels')
      plt.title('Daily Bike Share Predictions')
      # overlay the regression line
      z = np.polyfit(y_test, predictions, 1)
      p = np.poly1d(z)
      plt.plot(y_test,p(y_test), color='magenta')
     plt.show()
```

MSE: 259995.372727274 RMSE: 509.89741392487247 R2: 0.4902953900248517



The tree-based model doesn't seem to have improved over the linear model, so what else could we try?

#### 1.1.3 Try an Ensemble Algorithm

Ensemble algorithms work by combining multiple base estimators to produce an optimal model, either by applying an aggregate function to a collection of base models (sometimes referred to a *bagging*) or by building a sequence of models that build on one another to improve predictive performance (referred to as *boosting*).

For example, let's try a Random Forest model, which applies an averaging function to multiple Decision Tree models for a better overall model.

```
[11]: from sklearn.ensemble import RandomForestRegressor

# Train the model
model = RandomForestRegressor().fit(X_train, y_train)
print (model, "\n")

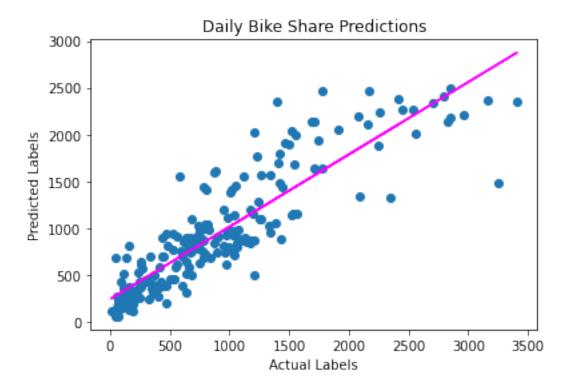
# Evaluate the model using the test data
predictions = model.predict(X_test)
mse = mean_squared_error(y_test, predictions)
print("MSE:", mse)
rmse = np.sqrt(mse)
print("RMSE:", rmse)
```

```
r2 = r2_score(y_test, predictions)
print("R2:", r2)

# Plot predicted vs actual
plt.scatter(y_test, predictions)
plt.xlabel('Actual Labels')
plt.ylabel('Predicted Labels')
plt.title('Daily Bike Share Predictions')
# overlay the regression line
z = np.polyfit(y_test, predictions, 1)
p = np.poly1d(z)
plt.plot(y_test,p(y_test), color='magenta')
plt.show()
```

#### RandomForestRegressor()

MSE: 111727.55500818181 RMSE: 334.25672021394246 R2: 0.7809651408347985

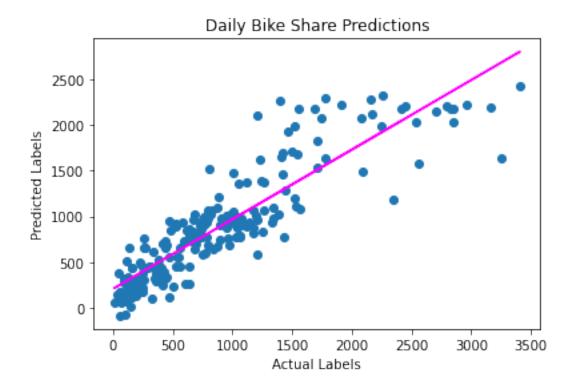


For good measure, let's also try a boosting ensemble algorithm. We'll use a Gradient Boosting estimator, which like a Random Forest algorithm builds multiple trees, but instead of building them all independently and taking the average result, each tree is built on the outputs of the previous one in an attempt to incrementally reduce the loss (error) in the model.

```
[12]: # Train the model
      from sklearn.ensemble import GradientBoostingRegressor
      # Fit a lasso model on the training set
      model = GradientBoostingRegressor().fit(X_train, y_train)
      print (model, "\n")
      # Evaluate the model using the test data
      predictions = model.predict(X_test)
      mse = mean_squared_error(y_test, predictions)
      print("MSE:", mse)
      rmse = np.sqrt(mse)
      print("RMSE:", rmse)
      r2 = r2_score(y_test, predictions)
      print("R2:", r2)
      # Plot predicted vs actual
      plt.scatter(y_test, predictions)
      plt.xlabel('Actual Labels')
      plt.ylabel('Predicted Labels')
      plt.title('Daily Bike Share Predictions')
      # overlay the regression line
      z = np.polyfit(y_test, predictions, 1)
      p = np.poly1d(z)
      plt.plot(y_test,p(y_test), color='magenta')
      plt.show()
```

GradientBoostingRegressor()

MSE: 103748.22054116831 RMSE: 322.0997059004685 R2: 0.7966081252452812



## 1.2 Summary

Here we've tried a number of new regression algorithms to improve performance. In the next notebook we'll look at 'tuning' these algorithms to improve performance.

## 1.3 Further Reading

To learn more about Scikit-Learn, see the Scikit-Learn documentation.