# **Weekly Summary Template**

# Advait Ashtikar

# Table of contents

Tuesday, Feb 14	1
Loading Libraries	2
Explanation of the Variables	3
Exploratory Data Analysis:	
Regression Model	7
Correlation Table	11
Variance Inflation Factors	14
Stepwise Regression	15
Thursday, Feb 16	22

# Tuesday, Feb 14

# ! TIL

Include a *very brief* summary of what you learnt in this class here. Today, I learnt the following concepts in class:

- 1. Multicollinearity
- 2. Variable Selection
- 3. Shrinkage Estimators

### **Loading Libraries**

```
library(tidyverse)
-- Attaching packages ----- tidyverse 1.3.2 --
v ggplot2 3.4.1 v purrr 1.0.1
v readr 2.1.4 v forcats 1.0.0
-- Conflicts ----- tidyverse conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag() masks stats::lag()
  library(ISLR2)
  library(dplyr)
  library(readr)
  library(purrr)
  library(glmnet)
Loading required package: Matrix
Attaching package: 'Matrix'
The following objects are masked from 'package:tidyr':
   expand, pack, unpack
Loaded glmnet 4.1-6
  library(caret)
Loading required package: lattice
Attaching package: 'caret'
The following object is masked from 'package:purrr':
   lift
```

# Loading required package: carData Attaching package: 'car' The following object is masked from 'package:dplyr': recode

The following object is masked from 'package:purrr':

some

library(car)

```
library(corrplot)
```

```
corrplot 0.92 loaded
```

In this class, we learnt about variable selection. For this, we will use **Boston housing dataset** which is described here:

```
library(ISLR2)
attach(Boston)

df <- Boston
head(df)</pre>
```

```
crim zn indus chas
                                           dis rad tax ptratio 1stat medv
                                rm age
1 0.00632 18
             2.31
                     0 0.538 6.575 65.2 4.0900
                                                 1 296
                                                          15.3
                                                               4.98 24.0
2 0.02731 0
             7.07
                     0 0.469 6.421 78.9 4.9671
                                                 2 242
                                                          17.8
                                                               9.14 21.6
3 0.02729
          0
             7.07
                     0 0.469 7.185 61.1 4.9671
                                                 2 242
                                                          17.8 4.03 34.7
4 0.03237
             2.18
                     0 0.458 6.998 45.8 6.0622
                                                 3 222
                                                               2.94 33.4
          0
                                                          18.7
5 0.06905
          0 2.18
                     0 0.458 7.147 54.2 6.0622
                                                 3 222
                                                          18.7 5.33 36.2
6 0.02985 0 2.18
                     0 0.458 6.430 58.7 6.0622
                                                 3 222
                                                          18.7 5.21 28.7
```

### **Explanation of the Variables**

The original data are 506 observations on 14 variables, medv being the target variable:

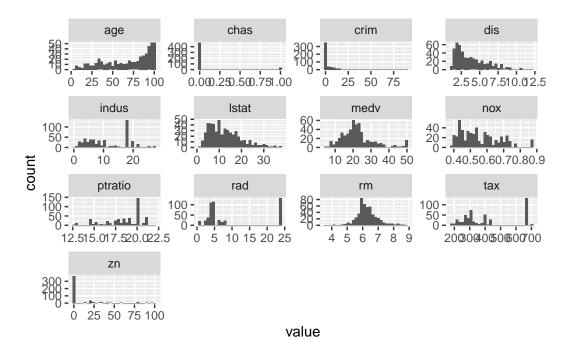
- crim per capita crime rate by town
- zn proportion of residential land zoned for lots over 25,000 sq.ft
- indus proportion of non-retail business acres per town
- chas Charles River dummy variable ( = 1 if tract bounds river; 0 otherwise)
- nox nitric oxides concentration (parts per 10 million)
- rm average number of rooms per dwelling
- age proportion of owner-occupied units built prior to 1940
- dis weighted distances to five Boston employment centres
- rad index of accessibility to radial highways
- tax full value property tax rate per USD 10,000
- ptratio pupil teacher ratio by town
- 1stat percentage of lower status of the population
- medv median value of owner occupied homes is USD 1000's

### **Exploratory Data Analysis:**

### Histogram:

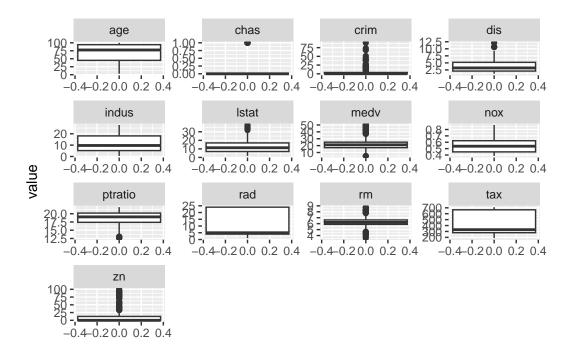
```
df %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  geom_histogram() +
  facet_wrap(~ key, scales = "free")
```

`stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



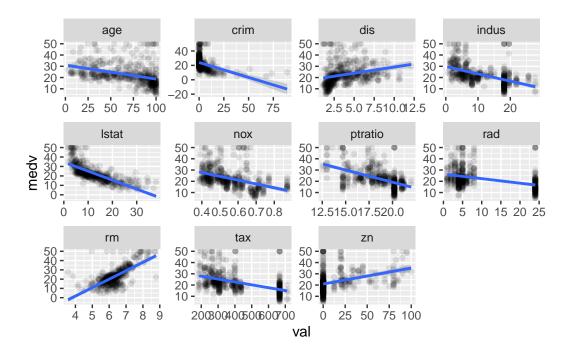
# Boxplot:

```
df %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(y = value)) +
  geom_boxplot() +
  facet_wrap(~ key, scales = "free")
```



Scatterplot: Used to get a better understanding of the data

```
df %>%
  select(-chas) %>%
  gather(key, val, -medv) %>%
  ggplot(aes(x = val, y = medv)) +
  geom_point(alpha = 0.1) +
  stat_smooth(formula = y ~ x, method = "lm") +
  facet_wrap(~ key, scales = "free")
```



# **Regression Model**

We begin by creating a regression model to predict  $\mathtt{medv}$ 

```
full_model <- lm(medv ~ ., df)
summary(full_model)</pre>
```

### Call:

lm(formula = medv ~ ., data = df)

### Residuals:

Min 1Q Median 3Q Max -15.1304 -2.7673 -0.5814 1.9414 26.2526

### Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	41.617270	4.936039	8.431	3.79e-16	***
crim	-0.121389	0.033000	-3.678	0.000261	***
zn	0.046963	0.013879	3.384	0.000772	***
indus	0.013468	0.062145	0.217	0.828520	
chas	2.839993	0.870007	3.264	0.001173	**

```
-18.758022
                        3.851355 -4.870 1.50e-06 ***
nox
             3.658119
                        0.420246 8.705 < 2e-16 ***
rm
             0.003611
                        0.013329 0.271 0.786595
age
            -1.490754
                        0.201623 -7.394 6.17e-13 ***
dis
                        0.066908 4.325 1.84e-05 ***
rad
            0.289405
            -0.012682
                        0.003801 -3.337 0.000912 ***
tax
ptratio
            -0.937533
                        0.132206 -7.091 4.63e-12 ***
lstat
            -0.552019
                        0.050659 -10.897 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 4.798 on 493 degrees of freedom Multiple R-squared: 0.7343, Adjusted R-squared: 0.7278 F-statistic: 113.5 on 12 and 493 DF, p-value: < 2.2e-16

broom::tidy(full\_model)

# A tibble: 13 x 5

	term	estimate	std.error	statistic	p.value
	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
1	(Intercept)	41.6	4.94	8.43	3.79e-16
2	crim	-0.121	0.0330	-3.68	2.61e- 4
3	zn	0.0470	0.0139	3.38	7.72e- 4
4	indus	0.0135	0.0621	0.217	8.29e- 1
5	chas	2.84	0.870	3.26	1.17e- 3
6	nox	-18.8	3.85	-4.87	1.50e- 6
7	rm	3.66	0.420	8.70	4.81e-17
8	age	0.00361	0.0133	0.271	7.87e- 1
9	dis	-1.49	0.202	-7.39	6.17e-13
10	rad	0.289	0.0669	4.33	1.84e- 5
11	tax	-0.0127	0.00380	-3.34	9.12e- 4
12	ptratio	-0.938	0.132	-7.09	4.63e-12
13	lstat	-0.552	0.0507	-10.9	6.39e-25

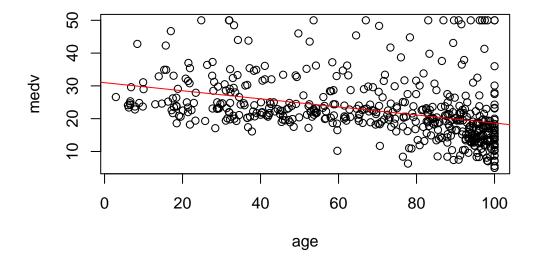
We can see that most of the variables are significant. However, notably

age and indus are not significant predictors of medv

Is this true?

### Plot and Regression Modelfor age

```
plot(medv ~ age, df)
abline(lm(medv ~ age), col = "red")
```



```
model_age <- lm(medv ~ age, df)
summary(model_age)</pre>
```

### Call:

lm(formula = medv ~ age, data = df)

### Residuals:

Min 1Q Median 3Q Max -15.097 -5.138 -1.958 2.397 31.338

### Coefficients:

---

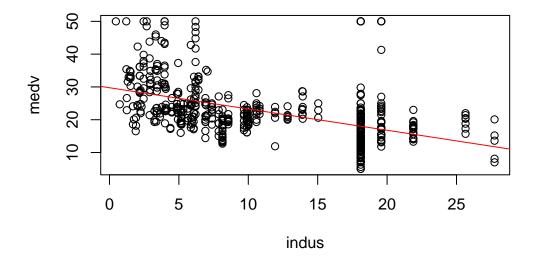
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.527 on 504 degrees of freedom

Multiple R-squared: 0.1421, Adjusted R-squared: 0.1404 F-statistic: 83.48 on 1 and 504 DF, p-value: < 2.2e-16

### Plot and Regression Model for indus

```
plot(medv ~ indus, df)
abline(lm(medv ~ indus), col = "red")
```



```
model_indus <- lm(medv ~ indus, df)
summary(model_indus)</pre>
```

### Call:

lm(formula = medv ~ indus, data = df)

### Residuals:

Min 1Q Median 3Q Max -13.017 -4.917 -1.457 3.180 32.943

### Coefficients:

Estimate Std. Error t value Pr(>|t|)

```
(Intercept) 29.75490    0.68345    43.54    <2e-16 ***
indus    -0.64849    0.05226    -12.41    <2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 8.057 on 504 degrees of freedom
Multiple R-squared: 0.234, Adjusted R-squared: 0.2325
```

154 on 1 and 504 DF, p-value: < 2.2e-16

### **Correlation Table**

F-statistic:

```
R <- df %>%
  keep(is.numeric) %>%
  cor()
R
```

```
indus
                                                 chas
              crim
                           7.n
                                                             nox
        1.00000000 -0.20046922
                               0.40658341 -0.055891582 0.42097171
crim
       -0.20046922 1.00000000 -0.53382819 -0.042696719 -0.51660371
zn
indus
        0.40658341 -0.53382819 1.00000000 0.062938027
                                                      0.76365145
chas
       -0.05589158 -0.04269672 0.06293803
                                          1.000000000
                                                      0.09120281
        0.42097171 -0.51660371 0.76365145 0.091202807
                                                      1.00000000
nox
       rm
age
        0.35273425 -0.56953734 0.64477851 0.086517774 0.73147010
dis
       rad
        0.62550515 -0.31194783 0.59512927 -0.007368241 0.61144056
tax
        0.58276431 - 0.31456332 \quad 0.72076018 - 0.035586518 \quad 0.66802320
ptratio 0.28994558 -0.39167855 0.38324756 -0.121515174 0.18893268
lstat
        0.45562148 -0.41299457
                               0.60379972 -0.053929298 0.59087892
medv
       -0.38830461 0.36044534 -0.48372516 0.175260177 -0.42732077
               rm
                                     dis
                                                  rad
                                                             tax
                                                                    ptratio
                          age
crim
       -0.21924670 0.35273425 -0.37967009 0.625505145
                                                      0.58276431
                                                                  0.2899456
zn
        0.31199059 -0.56953734 0.66440822 -0.311947826 -0.31456332 -0.3916785
       -0.39167585 0.64477851 -0.70802699 0.595129275
indus
                                                      0.72076018 0.3832476
chas
        0.09125123 0.08651777 -0.09917578 -0.007368241 -0.03558652 -0.1215152
       -0.30218819 0.73147010 -0.76923011 0.611440563
                                                      0.66802320
nox
                                                                  0.1889327
rm
        1.00000000 - 0.24026493 - 0.20524621 - 0.209846668 - 0.29204783 - 0.3555015
       -0.24026493 1.00000000 -0.74788054 0.456022452 0.50645559 0.2615150
age
dis
        0.20524621 - 0.74788054 1.00000000 - 0.494587930 - 0.53443158 - 0.2324705
rad
       -0.20984667 \quad 0.45602245 \quad -0.49458793 \quad 1.000000000 \quad 0.91022819 \quad 0.4647412
       -0.29204783 0.50645559 -0.53443158 0.910228189 1.00000000 0.4608530
tax
```

```
ptratio -0.35550149 0.26151501 -0.23247054 0.464741179
                                                          0.46085304
                                                                      1.0000000
                    0.60233853 -0.49699583 0.488676335 0.54399341
lstat
        -0.61380827
                                                                      0.3740443
medv
         0.69535995 -0.37695457
                                 0.24992873 -0.381626231 -0.46853593 -0.5077867
             lstat
                         medv
crim
         0.4556215 -0.3883046
        -0.4129946 0.3604453
indus
         0.6037997 -0.4837252
chas
        -0.0539293 0.1752602
nox
         0.5908789 -0.4273208
rm
        -0.6138083 0.6953599
         0.6023385 -0.3769546
age
dis
        -0.4969958 0.2499287
         0.4886763 -0.3816262
rad
         0.5439934 -0.4685359
tax
ptratio 0.3740443 -0.5077867
         1.0000000 -0.7376627
lstat
medv
        -0.7376627 1.0000000
```

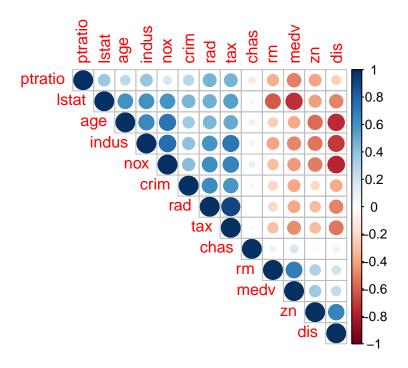
In a correlation table, we are selecting all the numeric values, where every single value is telling what the correlation with every other variable in data frame.

### **Q.** What is an admissible correlation value?

An admissible correlation value lies between -1 and 1.

A good way to visualize correlation is using corrplot()

```
library(corrplot)
corrplot(R, type = "upper", order = "hclust")
```



- From the plot we can see that, variables indus and age are fairly negatively correlated to the medv variable
- We can also see that, except chas variable, every other variable has some correlation with the other variables

### Call:

lm(formula = medv ~ ., data = df %>% select(-c(indus, nox, dis)))

### Residuals:

Min 1Q Median 3Q Max -16.9388 -3.0974 -0.7082 1.8472 28.3443

### Coefficients:

Estimate Std. Error t value Pr(>|t|)
(Intercept) 21.655695 4.215323 5.137 4.01e-07 \*\*\*
crim -0.091908 0.034722 -2.647 0.008380 \*\*
zn 0.008794 0.012670 0.694 0.487957

```
2.952830
                        0.913519
                                   3.232 0.001309 **
chas
rm
             4.100202
                       0.439135
                                   9.337 < 2e-16 ***
             0.020892
                      0.012195
                                  1.713 0.087315 .
age
                        0.067890
                                   3.710 0.000231 ***
             0.251852
rad
tax
            -0.012434
                        0.003469 -3.584 0.000371 ***
                        0.129206 -6.862 2.03e-11 ***
ptratio
            -0.886594
lstat
            -0.573951
                        0.053177 -10.793 < 2e-16 ***
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 5.084 on 496 degrees of freedom
Multiple R-squared: 0.6999,
                                Adjusted R-squared: 0.6944
```

F-statistic: 128.5 on 9 and 496 DF, p-value: < 2.2e-16

### **Variance Inflation Factors**

The variance inflation factor (VIF) is the ratio of the variance of estimating some parameter in a model that includes multiple other terms (parameters) by the variance of a model constructed using only one term.

If the standard error increases, then the significance of the variable decreases.

```
library(car)
vif_model <- lm(medv ~ ., df)
vif(vif_model) %>%
  knitr::kable()
```

	X
crim	1.767486
zn	2.298459
indus	3.987181
chas	1.071168
nox	4.369093
rm	1.912532
age	3.088232
dis	3.954037
rad	7.445301
tax	9.002158
ptratio	1.797060
İstat	2.870776

A high inflation factor is any factor that is greater than 2.

# Stepwise Regression

The process of selecting variables that are relatively more important than the other variables is known as **stepwise regression**.

```
null_model <- lm(medv ~ 1, df)
full_model <- lm(medv ~ ., df)</pre>
```

The null\_model does not contain any variable in a data frame.

The full\_model contains all the variables in a data frame.

```
library(caret)
  forward_model <- step(null_model,</pre>
                         direction = "forward",
                         scope = formula(full_model))
Start: AIC=2246.51
medv \sim 1
          Df Sum of Sq
                         RSS
                                 AIC
+ lstat
           1
               23243.9 19472 1851.0
               20654.4 22062 1914.2
+ rm
           1
               11014.3 31702 2097.6
+ ptratio 1
+ indus
           1
                9995.2 32721 2113.6
                9377.3 33339 2123.1
+ tax
+ nox
           1
               7800.1 34916 2146.5
                6440.8 36276 2165.8
+ crim
           1
                6221.1 36495 2168.9
+ rad
           1
+ age
           1
                6069.8 36647 2171.0
+ zn
           1
                5549.7 37167 2178.1
                2668.2 40048 2215.9
+ dis
           1
+ chas
           1
                1312.1 41404 2232.7
                       42716 2246.5
<none>
Step: AIC=1851.01
medv ~ lstat
          Df Sum of Sq
                         RSS
                                 AIC
           1
                4033.1 15439 1735.6
+ rm
```

```
2670.1 16802 1778.4
+ ptratio 1
+ chas
           1
                786.3 18686 1832.2
+ dis
                772.4 18700 1832.5
           1
           1 304.3 19168 1845.0
1 274.4 19198 1845.8
+ age
+ tax
           1
                160.3 19312 1848.8
+ zn
+ crim 1 146.9 19325 1849.2
+ indus 1 98.7 19374 1850.4
<none>
                        19472 1851.0
+ rad
         1 25.1 19447 1852.4
               4.8 19468 1852.9
+ nox
           1
```

Step: AIC=1735.58
medv ~ lstat + rm

		${\tt Df}$	Sum o	f Sq	RSS	AIC
+	ptratio	1	171	1.32	13728	1678.1
+	chas	1	54	8.53	14891	1719.3
+	tax	1	42	5.16	15014	1723.5
+	dis	1	35	1.15	15088	1725.9
+	crim	1	31	1.42	15128	1727.3
+	rad	1	18	0.45	15259	1731.6
+	indus	1	6	1.09	15378	1735.6
<1	none>				15439	1735.6
+	zn	1	5	6.56	15383	1735.7
+	age	1	2	0.18	15419	1736.9
+	nox	1	1	4.90	15424	1737.1

Step: AIC=1678.13
medv ~ lstat + rm + ptratio

```
Df Sum of Sq RSS
+ dis
            499.08 13229 1661.4
      1
+ chas 1
            377.96 13350 1666.0
+ crim 1 122.52 13606 1675.6
           66.24 13662 1677.7
+ age
<none>
                  13728 1678.1
+ tax 1 44.36 13684 1678.5
           24.81 13703 1679.2
+ nox 1
+ zn
      1 14.96 13713 1679.6
            6.07 13722 1679.9
+ rad 1
+ indus 1 0.83 13727 1680.1
```

```
Step: AIC=1661.39
medv ~ lstat + rm + ptratio + dis
       Df Sum of Sq RSS
                            AIC
        1
            759.56 12469 1633.5
+ nox
+ chas
             267.43 12962 1653.1
+ indus 1
            242.65 12986 1654.0
           240.34 12989 1654.1
+ tax
        1
+ crim 1 233.54 12995 1654.4
       1 144.81 13084 1657.8
+ zn
+ age
        1 61.36 13168 1661.0
                   13229 1661.4
<none>
            22.40 13206 1662.5
+ rad
Step: AIC=1633.47
medv ~ lstat + rm + ptratio + dis + nox
       Df Sum of Sq RSS
                            AIC
+ chas
       1
             328.27 12141 1622.0
             151.71 12318 1629.3
+ zn
       1
+ crim 1 141.43 12328 1629.7
+ rad
        1 53.48 12416 1633.3
<none>
                   12469 1633.5
+ indus 1 17.10 12452 1634.8
+ tax 1
            10.50 12459 1635.0
     1
             0.25 12469 1635.5
+ age
Step: AIC=1621.97
medv ~ lstat + rm + ptratio + dis + nox + chas
       Df Sum of Sq
                     RSS
                            AIC
+ zn
        1 164.406 11977 1617.1
       1 116.330 12025 1619.1
+ crim
+ rad 1 58.556 12082 1621.5
<none>
                   12141 1622.0
           26.274 12115 1622.9
+ indus 1
            4.187 12137 1623.8
+ tax
      1
+ age
        1
             2.331 12139 1623.9
Step: AIC=1617.07
medv ~ lstat + rm + ptratio + dis + nox + chas + zn
```

Df Sum of Sq

RSS

AIC

```
+ crim 1 170.902 11806 1611.8
                   11977 1617.1
<none>
        1 31.773 11945 1617.7
+ tax
+ rad
        1
            28.311 11948 1617.9
+ indus 1 27.377 11949 1617.9
            0.071 11977 1619.1
+ age
        1
Step: AIC=1611.8
medv ~ lstat + rm + ptratio + dis + nox + chas + zn + crim
       Df Sum of Sq RSS
                            AIC
       1 155.006 11651 1607.1
+ rad
                   11806 1611.8
<none>
+ indus 1 24.957 11781 1612.7
             1.418 11804 1613.7
+ tax
        1
+ age
        1
            0.178 11806 1613.8
Step: AIC=1607.11
medv ~ lstat + rm + ptratio + dis + nox + chas + zn + crim +
   rad
       Df Sum of Sq RSS
                            AIC
+ tax
            298.573 11352 1596.0
<none>
                    11651 1607.1
+ indus 1
            44.346 11606 1607.2
            0.581 11650 1609.1
+ age
      1
Step: AIC=1595.98
medv ~ lstat + rm + ptratio + dis + nox + chas + zn + crim +
   rad + tax
       Df Sum of Sq RSS
                          AIC
                    11352 1596.0
<none>
+ age
             1.6865 11350 1597.9
        1
+ indus 1
             1.0784 11351 1597.9
  summary(forward_model)
Call:
lm(formula = medv ~ lstat + rm + ptratio + dis + nox + chas +
    zn + crim + rad + tax, data = df
```

```
Residuals:
```

```
Min 1Q Median 3Q Max -15.1814 -2.7625 -0.6243 1.8448 26.3920
```

### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 41.451747
                         4.903283
                                    8.454 3.18e-16 ***
             -0.546509
lstat
                         0.047442 -11.519 < 2e-16 ***
rm
              3.672957
                         0.409127
                                    8.978 < 2e-16 ***
                         0.130423 -7.138 3.39e-12 ***
             -0.930961
ptratio
dis
             -1.515951
                         0.187675 -8.078 5.08e-15 ***
            -18.262427
                         3.565247 -5.122 4.33e-07 ***
nox
chas
              2.871873
                         0.862591
                                    3.329 0.000935 ***
zn
              0.046191
                         0.013673
                                    3.378 0.000787 ***
             -0.121665
                         0.032919 -3.696 0.000244 ***
crim
              0.283932
                         0.063945
                                    4.440 1.11e-05 ***
rad
             -0.012292
                         0.003407 -3.608 0.000340 ***
tax
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.789 on 495 degrees of freedom Multiple R-squared: 0.7342, Adjusted R-squared: 0.7289 F-statistic: 136.8 on 10 and 495 DF, p-value: < 2.2e-16

AIC is like a replacement for  $R^2$ 

Unlike  $R^2$ , where a higher value is better, we prefer to have a low AIC value

Based on lstat is the best model, as it has the lowest value

Forward Selection: In this form of stepwise regression we keep building our model from 0 (or a low value), and add variables, until we reach a stage where our AIC ends to be high.

```
- indus
          1 1.08 11350 1597.9
                1.69 11351 1597.9
- age
          1
<none>
                     11349 1599.8
- chas
              245.31 11595 1608.7
          1 256.28 11606 1609.2
- tax
            263.59 11613 1609.5
- crim
          1 311.49 11661 1611.6
          1 430.71 11780 1616.7
- rad
              546.10 11896 1621.6
- nox
          1
- ptratio 1 1157.70 12507 1647.0
          1 1258.52 12608 1651.1
- dis
          1 1744.36 13094 1670.2
- rm
          1 2733.54 14083 1707.0
- lstat
Step: AIC=1597.9
medv ~ crim + zn + chas + nox + rm + age + dis + rad + tax +
   ptratio + lstat
         Df Sum of Sq RSS
                             AIC
                1.69 11352 1596.0
- age
<none>
                     11350 1597.9
            251.21 11602 1607.0
- chas
          1
- zn
          1 262.99 11614 1607.5
          1 299.68 11650 1609.1
- tax
- crim
         1 313.07 11664 1609.7
         1 453.61 11804 1615.7
- rad
             574.23 11925 1620.9
- nox
          1
- ptratio 1 1168.01 12518 1645.5
          1 1333.19 12684 1652.1
- dis
- rm
          1 1750.50 13101 1668.5
          1 2743.21 14094 1705.4
- lstat
Step: AIC=1595.98
medv ~ crim + zn + chas + nox + rm + dis + rad + tax + ptratio +
   lstat
         Df Sum of Sq RSS
                              AIC
<none>
                     11352 1596.0
- chas
              254.21 11606 1605.2
          1
          1 261.75 11614 1605.5
- zn
          1 298.57 11651 1607.1
- tax
          1 313.27 11666 1607.8
- crim
```

1 452.16 11804 1613.7

- rad

```
601.74 11954 1620.1
- nox
           1
- ptratio
           1
               1168.51 12521 1643.5
- dis
               1496.35 12848 1656.6
           1
               1848.38 13201 1670.3
- rm
           1
- lstat
           1
               3043.23 14395 1714.2
  summary(backward model)
Call:
lm(formula = medv ~ crim + zn + chas + nox + rm + dis + rad +
    tax + ptratio + lstat, data = df)
Residuals:
     Min
               1Q
                    Median
                                 3Q
                                         Max
-15.1814 -2.7625
                   -0.6243
                             1.8448
                                     26.3920
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                         4.903283
(Intercept) 41.451747
                                    8.454 3.18e-16 ***
crim
             -0.121665
                         0.032919 -3.696 0.000244 ***
                                    3.378 0.000787 ***
              0.046191
                         0.013673
zn
              2.871873
                         0.862591
                                    3.329 0.000935 ***
chas
nox
            -18.262427
                         3.565247 -5.122 4.33e-07 ***
                                    8.978 < 2e-16 ***
              3.672957
                         0.409127
rm
dis
             -1.515951
                         0.187675 -8.078 5.08e-15 ***
                                    4.440 1.11e-05 ***
rad
              0.283932
                         0.063945
             -0.012292
                         0.003407 -3.608 0.000340 ***
tax
ptratio
             -0.930961
                         0.130423 -7.138 3.39e-12 ***
             -0.546509
                         0.047442 -11.519 < 2e-16 ***
lstat
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4.789 on 495 degrees of freedom
Multiple R-squared: 0.7342,
                                Adjusted R-squared: 0.7289
F-statistic: 136.8 on 10 and 495 DF, p-value: < 2.2e-16
```

Another way to do the same, is using **Backward Selection**. In this we start with the full\_model, and start removing variable, until we see a decrease in the AIC value. At this point, if we remove any more variables, the AIC value would increase.

In this case, both **forward** and **backward** models have given the same result. This may not always be the case.

• Another option for the direction in the step() function is both this is a hybrid of both forward and backward selection.

# Thursday, Feb 16

# ! TIL

Include a  $very\ brief$  summary of what you learnt in this class here. Today, I learnt the following concepts in class:

- 1. Item 1
- 2. Item 2
- 3. Item 3