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B-Spline Approximation of $x(t)$

Problem 7.4

```
close all;
clear

for L = 1:4
```

Setup

```
N = 20;
W = [-pi:0.0001:pi];
t = [-100:0.0001:100];
h_L = zeros(1, 2*N+1);
h_L_half = zeros(1, N+1);
H_L = zeros(1, length(W));
x = @(t) 0.*(t<=0) + 0.5 .* ((t>0) .* (t<=10)) - sin(pi*t/10) .* ((t>10) .* (t<=20)) + 0.
*(t>20);
figure;
subplot(2, 2, 1);
plot(t, x(t));
title('Original Signal  $x(t)$ ', 'Interpreter', 'latex');
if L == 1
    b = @(t1) bspline1(t1);
elseif L == 2
    b = @(t1) bspline2(t1);
elseif L == 3
    b = @(t1) bspline3(t1);
elseif L == 4
    b = @(t1) bspline4(t1);
end
```

Computing h_L

Finding H_L

```
for i = 1:length(W)
    H_L(i) = 1 / G_L(W(i), L);
```

```

end

for i = 1:N
    h_L_half(i) = 0;
    % n = i - (N+1);
    h_L_half(i) = sum(H_L .* cos(W*(i-1)));
    h_L_half(i) = h_L_half(i);
end

h_L = [fliplr(h_L_half), h_L_half(2:end)];
h_L = h_L / (length(W));
% figure;
subplot(2, 2, 2);
plot([-N:N], h_L);
title('$h_L[n]$', 'Interpreter', 'latex')
xlabel('n');
ylabel('h_L[n]');

```

Finding $\alpha[n]$

```

prod_f = @(t1, n, l) (x(t1) .* b(t1-n-l));

n_r = 40;
l_r = 100;
al = zeros(1, 2*n_r+1);
for n = -n_r:n_r
    for l = 1:length(h_L)
        al(n+n_r+1) = al(n+n_r+1) + h_L(l) * integral(@(t1) (prod_f(t1, n, l - (N+1))), -
100, 100);
    end
end
% figure;
subplot(2,2,3);
stem([-n_r:n_r], al);
title('Basis coefficients $\alpha_n$', 'Interpreter', 'latex');
ylabel('\alpha_n');
xlabel('n');

```

Estimating with B-Splines and Dual Basis

```

y = zeros(1, length(t));
for n = -n_r:n_r
    y = y + al(n+n_r+1) * b(t-n);
end
%figure;
subplot(2,2,4)
hold on;
plot(t, y);
title('Original Signal: $x(t)$, Estimated Signal $y(t)$', 'Interpreter', 'latex');
plot(t, x(t));
ylabel('y(t), x(t)');
xlabel('t');

```

Computing Error

```
err = 0;
dt = (t(2)-t(1));
for i = 1:length(t)
    err = err + (abs(y(i) - x(t(i))) ^ 2) * dt;
end
disp(['Error for L = ' num2str(L) ' ' num2str(err)]);
```

```
end
```

Helper Function for Finding $G_L(e^{jw})$

Finding G_L

```
function Gw = G_L(w, L)
    Gw = 0;
    K = 50;
    for k = -K:K
        Gw = Gw + ((sin((w/2) + pi*k)) / ((w/2) + pi*k)) ^ (2*L + 2);
    end
end
```