### Lecture 11—Dependencies

January 28, 2015

#### Roadmap

Last Time: C++ atomics; C Compilers

This Time: Dependencies

#### Atomics when not using C++11

Not really.

gcc supports atomics via extensions:

https://gcc.gnu.org/onlinedocs/gcc/\_005f\_005fatomic-Builtins.html

OS X has atomics via OS calls:

 $\label{limits} $$ $$ $ \text{https://developer.apple.com/library/mac/documentation/Cocoa/Conceptual/Multithreading/ThreadSafety/ThreadSafety.html} $$$ 

etc...

#### Reference:

### Part I

# Dependencies

#### Next topic: Dependencies

Dependencies are the main limitation to parallelization.

Example: computation must be evaulated as XY and not YX.

### Not synchronization

Assume (for now) no synchronization problems.

Only trying to identify code that is safe to run in parallel.

#### Memory-carried Dependencies

Dependencies limit the amount of parallelization.

Can we execute these 2 lines in parallel?

```
\begin{array}{lll} x & = & 42 \\ x & = & x & + & 1 \end{array}
```

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x = 42 \\
x = x + 1
\end{array}$$

No.

• Assume x initially 1. What are possible outcomes?

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x = 42 \\
x = x + 1
\end{array}$$

No.

• Assume x initially 1. What are possible outcomes? x = 43 or x = 42

Next, we'll classify dependencies.

### Read After Read (RAR)

Can we execute these 2 lines in parallel? (initially x is 2)

$$\begin{vmatrix} y = x + 1 \\ z = x + 5 \end{vmatrix}$$

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#### Can we execute these 2 lines in parallel? (initially x is 2)

```
y = x + 1
z = x + 5
```

#### Yes.

- Variables y and z are independent.
- Variable x is only read.

RAR dependency allows parallelization.

### Read After Write (RAW)

#### What about these 2 lines? (again, initially x is 2):

```
\begin{array}{l}
x = 37 \\
z = x + 5
\end{array}
```

### Read After Write (RAW)

What about these 2 lines? (again, initially x is 2):

$$\begin{array}{rcl}
x &=& 37 \\
z &=& x &+& 5
\end{array}$$

No, z = 42 or z = 7.

RAW inhibits parallelization: can't change ordering. Also known as a true dependency.

### Write After Read (WAR)

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\begin{vmatrix} z = x + 5 \\ x = 37 \end{vmatrix}
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What if we change the order now? (again, initially x is 2)

$$z = x + 5$$

$$x = 37$$

No. Again, z = 42 or z = 7.

- WAR is also known as a anti-dependency.
- But, we can modify this code to enable parallelization.

### Removing Write After Read (WAR) Dependencies

#### Make a copy of the variable:

```
x_copy = x
z = x_copy + 5
x = 37
```

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#### We can now run the last 2 lines in parallel.

- Induced a true dependency (RAW) between first 2 lines.
- Isn't that bad?

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#### Not always:

```
z = very_long_function(x) + 5
x = very_long_calculation()
```

### Write After Write (WAW)

#### Can we run these lines in parallel? (initially x is 2)

```
z = x + 5
z = x + 40
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\begin{bmatrix} z = x + 5 \\ z = x + 40 \end{bmatrix}
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Nope, z = 42 or z = 7.

- WAW is also known as an output dependency.
- We can remove this dependency (like WAR):

### Write After Write (WAW)

#### Can we run these lines in parallel? (initially x is 2)

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Nope, z = 42 or z = 7.

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- We can remove this dependency (like WAR):

```
z_{\text{copy}} = x + 5

z = x + 40
```

## Summary of Memory-carried Dependencies

		Second Access	
		Read	Write
First Access	Read	No Dependency Read After Read (RAR)	Anti-dependency Write After Read (WAR)
	Write	True Dependency Read After Write (RAW)	Output Dependency Write After Write (WAW)