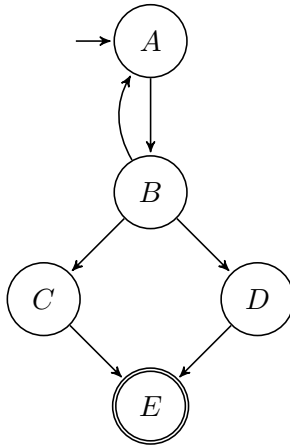


## Graph Coverage

We will discuss graph coverage in great detail. Many forms of software testing reduce to graph coverage, so once you understand how graph coverage works, you will have a good understanding of a key software testing topic.

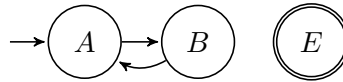
**Definition of Graphs.** (You should already be familiar with this material, but let's establish the terms we'll use in this class). Let's start with an example graph.



- $N$  : Set of nodes  $\{A, B, C, D, E\}$
- $N_0$  : Set of initial nodes  $\{A\}$
- $N_f$  : Set of final nodes  $\{E\}$
- $E \subseteq N \times N$  : Edges, e.g.  $(A, B)$  and  $(C, E)$ ;  
 $C$  is the predecessor and  
 $E$  is the successor in  $(C, E)$ .

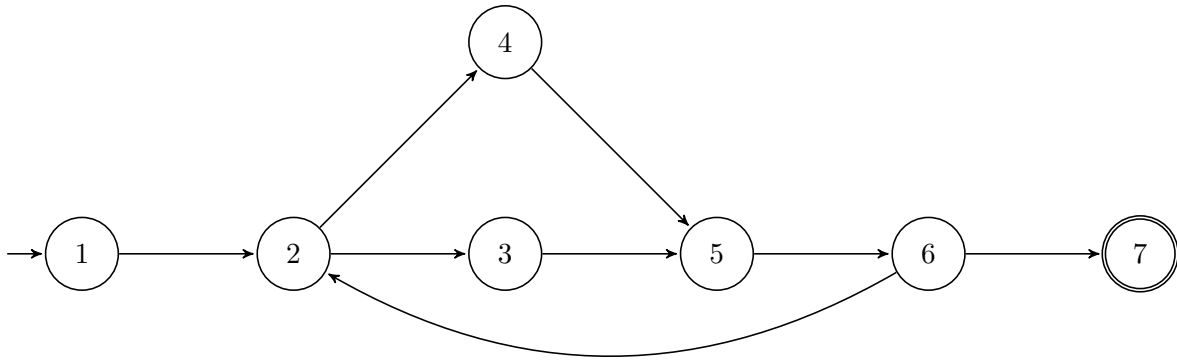
**Subgraph:** Let  $G'$  be a subgraph of  $G$ ; then the nodes of  $G'$  must be a subset  $N_{\text{sub}}$  of  $N$ . Then the initial nodes of  $G'$  are  $N_0 \cap N_{\text{sub}}$  and its final nodes are  $N_f \cap N_{\text{sub}}$ . The edges of  $G'$  are  $E \cap (N_{\text{sub}} \times N_{\text{sub}})$ .

For example, consider the case where we set  $N_{\text{sub}} = \{A, B, E\}$ . This induces the subgraph:



Note that graphs need not be connected.

**Paths.** The most important thing about a graph, for testing purposes, is the path through the graph. Here is a graph  $G_{\#}$  and some example paths through the graph.



- path 1:  $[2, 3, 5]$ , with length 2.
- path 2:  $[1, 2, 3, 5, 6, 2]$ , with length 5.
- not a path:  $[1, 2, 5]$ .

We say that path 1 is *from* node 2 *to* node 5. We can also say that path 1 is *from* edge  $(2, 3)$  *to*  $(3, 5)$ .

**Definition 1** A path is a sequence of nodes from a graph  $G$  whose adjacent pairs all belong to the set of edges  $E$  of  $G$ .

Note that length 0 paths are still paths.

**Definition 2** A subpath is a subsequence of a path.

This textbook definition is ambiguous: is  $[1, 2, 5]$  a subpath of  $[1, 2, 3, 5, 6, 2]$ ?

**Definition 3** A subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements.

Yes,  $[1, 2, 5]$  is a subsequence of  $[1, 2, 3, 5, 6, 2]$ . However,  $[1, 2, 5]$  is not a path, so we are going to say that it is not a subpath.

### Test cases and test paths.

Some paths are also test paths. Here is a test path from  $G_{\#}$ :

$[1, 2, 3, 5, 6, 7];$

here is another one:

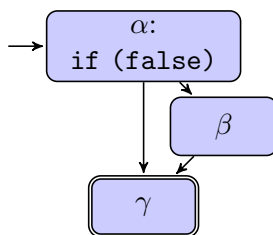
$[1, 2, 3, 5, 6, 2, 3, 5, 6, 7].$

You can easily come up with more paths. Now, test paths are linked to test cases. First, let's define the notion of a test path.

**Definition 4** A test path is a path  $p$  (possibly of length 0) that starts at some node in  $N_0$  and ends at some node in  $N_f$ .

Running the test case on the program or method yields one or more test paths. A test path may represent many test cases (for instance, if a program takes the same branches on all of those test cases); or a test path may represent no test cases (if it is infeasible).

**Paths and semantics.** When a graph is a program's control-flow graph, some of the paths in the graph may not correspond to program semantics. Consider the following graph.



Clearly  $\beta$  will never execute.

In this course, we will generally only talk about the *syntax* of a graph—its nodes and edges—and not its *semantics*.

However, in the following definition, we'll talk about both notions.

**Definition 5** A node  $n$  (or edge  $e$ ) is syntactically reachable from  $n_i$  if there exists a path from  $n_i$  to  $n$  (or  $e$ ). A node  $n$  (or edge  $e$ ) is semantically reachable if one of the paths from  $n_i$  to  $n$  can be reached on some input.

Standard graph algorithms, like breadth-first search and depth-first search, can compute syntactic reachability. (Semantic reachability is undecidable; no algorithm can precisely compute semantic reachability for all programs.)

We define  $\text{reach}_G(\chi)$  as the portion of the graph syntactically reachable from  $\chi$ . ( $\chi$  might be a node, an edge, a set of nodes, or a set of edges.) For example:

- $\text{reach}_G(N_0)$  is the set of nodes and edges reachable from the initial node(s);
- $\text{reach}_{G\#}(2)$  in the above graph  $G\#$  is  $\{2, 3, 4, 5, 6, 7\}$ ;
- $\text{reach}_{G\#}(7)$  is  $\{7\}$ .

Note that we include  $\chi$  in the set of nodes reachable from  $\chi$ , because paths of length 0 are paths.

When we talk about the nodes or edges in a graph  $G$  in a coverage criterion, we'll generally mean  $\text{reach}_G(N_0)$ ; the unreachable nodes tend to (1) be uninteresting; and (2) to frustrate coverage criteria.