

b) Given Transfer function,

$$TF = \frac{K(s+2)(s+4)}{(s+1)(s+3)}$$

Poles for given transfer function is  $s=-1$  and  $s=-3$  and zeroes of given transfer function is  $s=-2$  and  $s=-4$ .

No. of zeroes = No. of poles,

No. infinite zeroes (or) poles to be added, Hence, there is No. Need of asymptotes,

We can use, characteristic equation for break and break away points,

$$1 + \frac{K(s+2)(s+4)}{(s+1)(s+3)} = 0 \Rightarrow K = \frac{-(s+1)(s+3)}{(s+2)(s+4)}$$

Now by doing  $\frac{dK}{ds} = 0$ ;

$$(s+2)(s+4)[2s+4] - (s+1)(s+3)[2s+6] = 0$$

$$\Rightarrow \cancel{2}(s+2)(s+4)(s+2) = \cancel{2}(s+1)(s+3)(s+3)$$

$$\Rightarrow (s+2)^2(s+4) = (s+1)(s+3)^2$$

$$\Rightarrow (s^2+4s+4)(s+4) = (s+1)(s^2+6s+9)$$

$$\Rightarrow \cancel{s^3} + 4s^2 + 4s^2 + 16s + 4s + 16 = \cancel{s^3} + 6s^2 + 9s + s^2 + 6s + 9$$

$$\Rightarrow \boxed{s^2 + 5s + 7 = 0} \Rightarrow \underbrace{\text{No-roots which are real}}$$

No. Breakin or Break away point.

There is No. angle of Departure (a) Angle of Arrival because There are no. Complex roots (a) No. Complex zeroes.

Hence Rootlocus is:

