

⑤ Given Transfer function,

$$TF = \frac{K}{(s^2 + 2s + 5)}$$

Now This Equation does not have zeroes but it has complex poles,

The complex poles are roots of  $s^2 + 2s + 5$ ,

$$P = 2; Z = 0$$

$$\text{ie, } s^2 + 2s + 5 = 0 \Rightarrow (s+1)^2 = -4 \Rightarrow (s+1) = \pm 2i \\ \Rightarrow s = -1 + 2i \text{ (a) } s = -1 - 2i$$

Let us locate the poles and first let us find asymptote angle and centroid.

$$\text{Centroid} = \frac{-1 + 2i + (-1 - 2i)}{2 - 0} = \frac{-2}{2} = \underline{\underline{-1}}$$

$$\text{Angle made by Asymptotes} = \frac{(2q+1)\pi}{2} = \text{only ~~one~~ two possible value of angle}$$

hence, Asymptote is against -ve real axis.

$$= \frac{\pi}{2} \text{ and } \frac{3\pi}{2} \\ = 90^\circ \text{ and } 270^\circ$$

as both the poles are complex we can calculate

Angle of departure,

$$\text{Angle of departure } (\beta) = 180^\circ - (\text{angle made relative to other poles} \\ + (\text{angle made relative to other zeroes})) \\ = 180^\circ - 90^\circ = \underline{\underline{90^\circ}} \rightarrow \text{angle of departure}$$

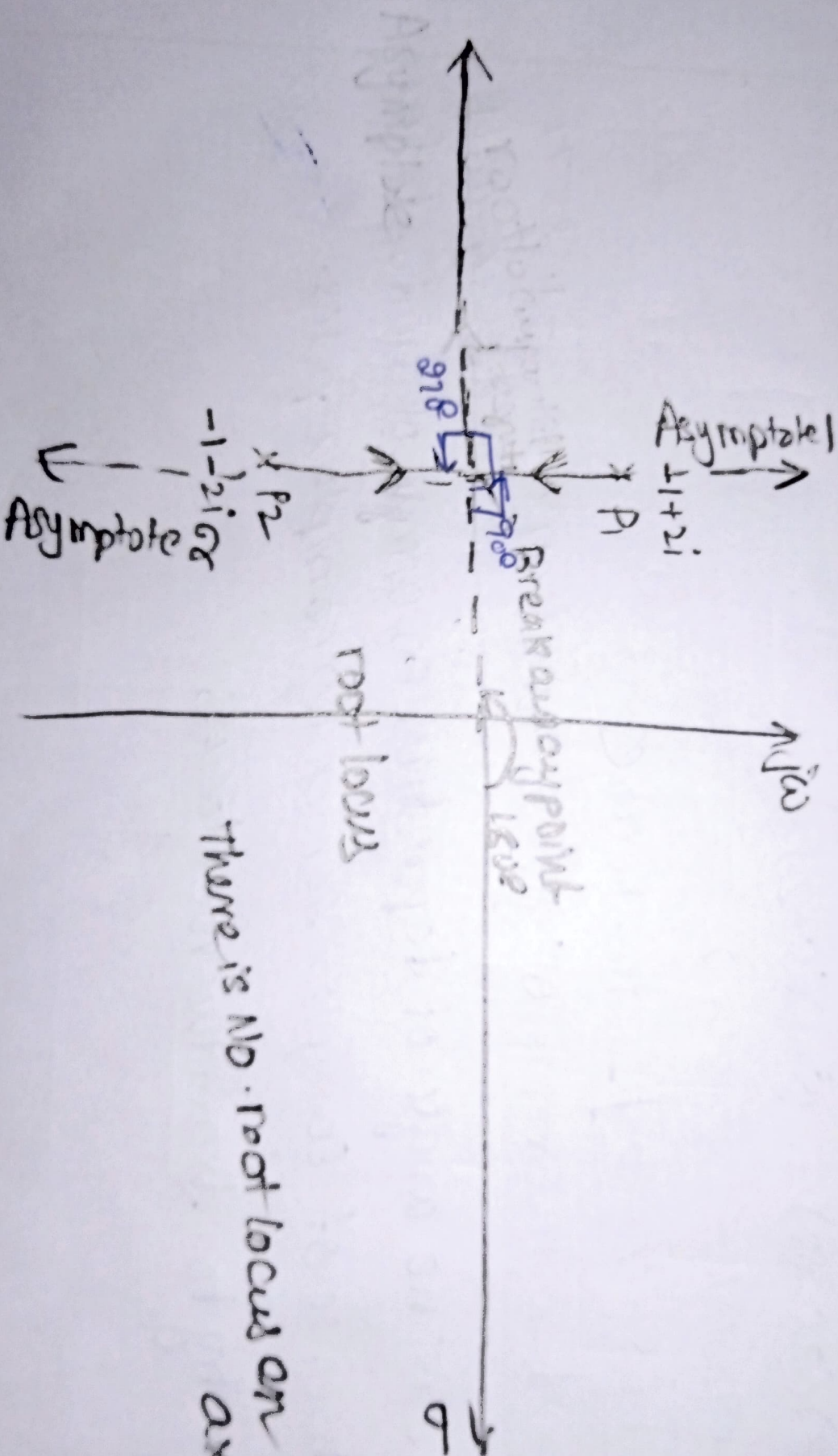
Which is  $270^\circ$  for other pole,

and if we use characteristic Equation, which is,

$$\frac{K}{s^2 + 2s + 5} = -1 \Rightarrow K = -(s^2 + 2s + 5)$$

$$\frac{dK}{ds} = 0 \Rightarrow -(2s + 2) = 0 \Rightarrow \boxed{s = -1}$$

And hence Break away point is same as Centroid, i.e.  
if we draw root locus,



there is no root locus on real axis at all