Machine Learning I (DATS 6202) Deep Neural Network

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Reference

- This set of slices was largely built on the following 8 wonderful books and a wide range of fabulous papers:
 - HML Hands-On Machine Learning with Scikit-Learn, Keras, and TensorFlow (2nd Edition)
 - PML Python Machine Learning (3rd Edition)
 - ESL The Elements of Statistical Learning (2nd Edition)
- PRML Pattern Recognition and Machine Learning
 - LFD Learning From Data
 - NND Neural Network Design (2nd Edition)
- NNDL Neural Network and Deep Learning
 - RL Reinforcement Learning: An Introduction
- For most materials covered in the slides, we will specify their corresponding books and papers for further reference

Code Example & Case Study

- See code example of topics discussed in this section in github repository: /p2_c2_s1_deep_neural_network/code_example
- See case study of Kaggle Competition related to this section in github repository: /p2_c2_s1_deep_neural_network/case_study

Overview

- Learning Objectives
- Designing Deep Neural Network
- Implementing Deep Neural Network
- Training Deep Neural Network
- 5 Fine-tuning Deep Neural Network
- 6 References

Learning Objectives

- It is expected to understand
 - the good practices for designing deep neural network
 - the good practices for training deep neural network
 - the good practices for fine-tuning deep neural network

Deep Neural Network (DNN)

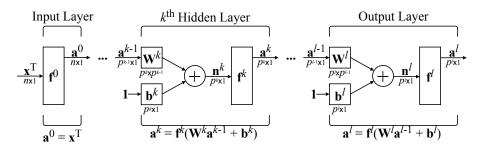


Figure 1: A fully-connected neural network.

The Architecture of DNN

- Some hyperparameters in the architecture of dnn are fixed:
 - the number of perceptrons on the input layer (p^0) = the number of features in the input (n)
 - the activation function on the input layer $(\mathbf{f}^0) = \text{linear}$
- Some hyperparameters in the architecture of dnn are not fixed:
 - the number of hidden layers
 - the number of perceptrons on the hidden layers and output layer $(p^k$ where k>0)
 - the activation functions on the hidden layers and output layer (\mathbf{f}^k where k>0)
 - ullet the objective function J

Regression

• Good Practice: Typical hyperparameter value in DNN regressors.

Hyperparameter	Typical value
# Input layer perceptrons	One per input feature
# Hidden layers	Depends on the problem
	but typically 1 to 5
# Perceptrons per hidden layer	Depends on the problem
	but typically 10 to 100
# Output layer perceptrons	1 per prediction dimension
Input layer activation	Linear
Hidden layer activation	ReLU (or SELU)
Output layer activation	Linear
	or ReLU/softplus (if positive outputs)
	or logistic/tanh (if bounded outputs)
Objective function	MSE
	or MAE/Huber (if outliers)

Table 1: Typical hyperparameter value in DNN regressors.

Binary Classification

Good Practice: Typical hyperparameter value in DNN binary classifiers. Here * indicates that the corresponding hyperparameter value is the same as that in DNN regressor (table 1).

Hyperparameter	Typical value	
# Input layer perceptrons * # Hidden layers *	One per input feature Depends on the problem but typically 1 to 5	
$\#$ Perceptrons per hidden layer \star	Depends on the problem but typically 10 to 100	
# Output layer perceptrons	1	
Input layer activation ★	Linear	
Hidden layer activation ★	ReLU (or SELU)	
Output layer activation	Logistic	
Objective function	Cross entropy	

Table 2: Typical hyperparameter value in DNN binary classifiers.

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Multilabel Binary Classification

Good Practice: Typical hyperparameter value in DNN multilabel binary classifiers.
Here * indicates that the corresponding hyperparameter value is the same as that
in DNN regressor (table 1).

Hyperparameter	Typical value	
# Input layer perceptrons * # Hidden layers *	One per input feature Depends on the problem but typically 1 to 5	
$\#$ Perceptrons per hidden layer \star	Depends on the problem but typically 10 to 100	
# Output layer perceptrons	1 per label	
Input layer activation ★	Linear	
Hidden layer activation ★	ReLU (or SELU)	
Output layer activation	Logistic	
Objective function	Cross entropy	

Table 3: Typical hyperparameter value in DNN multilabel binary classifiers.

Multiclass Classification

 Good Practice: Typical hyperparameter value in DNN multiclass classifiers. Here * indicates that the corresponding hyperparameter value is the same as that in DNN regressor (table 1).

Hyperparameter	Typical value	
$\#$ Input layer perceptrons \star	One per input feature	
# Hidden layers ⋆	Depends on the problem	
	but typically 1 to 5	
$\#$ Perceptrons per hidden layer \star	Depends on the problem	
	but typically 10 to 100	
# Output layer perceptrons	1 per class	
Input layer activation ★	Linear	
Hidden layer activation ★	ReLU (or SELU)	
Output layer activation	Softmax	
Objective function	Cross entropy	

Table 4: Typical hyperparameter value in DNN multiclass classifiers.

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The Most Popular Tools

- Below are the most popular tools for implementing DNN:
 - TensorFlow
 - Keras
 - PyTorch
- In this course we will be using tf.keras.

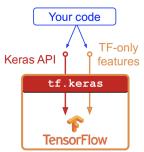


Figure 2: The tf.keras API. Picture courtesy of *Hands-On Machine Learning with Scikit-Learn, Keras, and TensorFlow (2nd Edition)*.

The Sequential API

 The sequential API allows us to create a DNN where the layers are fully connected in a sequential way (as shown in fig. 3).

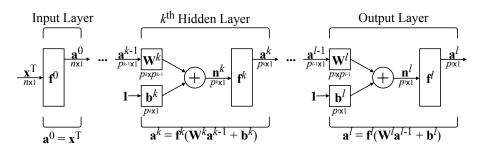


Figure 3: A fully-connected neural network.

The Sequential API

• The code below shows one way (by adding the layers one by one) to use the sequential API to create a dnn for the Fashion MNIST dataset (with 60,000 28×28 images):

```
# A sequential dnn
    model = keras.models.Sequential()
 3
4
    # Add the input layer
5
    model.add(keras.layers.Flatten(input_shape=[28, 28]))
6
    # Add two hidden layers
8
    model.add(keras.layers.Dense(50, activation="relu"))
9
    model.add(keras.layers.Dense(50, activation="relu"))
10
11
    # Add the output layer
12
    model.add(keras.layers.Dense(10, activation="softmax"))
```

- Line 5: It is recommended to specify the *input_shape* when adding the input layer to a Sequential model.
- Line 5: The flatten layer transforms the input data into a 1d array.

The Sequential API

• The code below shows another way (by passing the layers as a list) to use the sequential API to create a dnn:

```
# A sequential dnn with two hidden layers
model = keras.models.Sequential([
keras.layers.Flatten(input_shape=[28, 28]),
keras.layers.Dense(50, activation="relu"),
keras.layers.Dense(50, activation="relu"),
keras.layers.Dense(10, activation="softmax")])
```

Model Summary

Model: "sequential"

Layer (type)	Output	Shape	Param #
flatten (Flatten)	(None,	784)	0
dense (Dense)	(None,	50)	39250
dense_1 (Dense)	(None,	50)	2550
dense_2 (Dense)	(None,	10)	510

Total params: 42,310 Trainable params: 42,310 Non-trainable params: 0

Figure 4: A model summary.

Interpreting Model Summary

- In column *Layer (type)*: *Flatten* denotes a flatten layer and Dense denotes a dense (fully-connected) layer.
- In column *Output Shape*: *None* means the batch size can take any value.
- In column Param: the number of parameters on layer k is

$$p^k p^{k-1} + p^k, (1)$$

where p^k is the number of perceptrons on layer k (also the number of bias on the layer), p^kp^{k-1} the number of connecting weights between layer k-1 and k. For example:

- on layer dense: $39250 = 50 \times 784 + 50$
- on layer dense_1: $2550 = 50 \times 50 + 50$
- on layer dense_2: $510 = 10 \times 50 + 10$
- Training/Non-trainable params are the parameters that will/will not be updated by backpropagation.

Compiling DNN

- After creating a dnn, we need to compile it to specify hyperparameters such as loss function, optimizer and evaluation metrics.
- The code below shows how to compile a dnn using the compile() function:

```
# Compile the model
model.compile(optimizer=keras.optimizers.SGD(),
loss='sparse_categorical_crossentropy',
metrics=['accuracy'])
```

Training DNN

- After compiling a dnn, we can train the model on the training data and evaluate it on the validation data.
- The code below shows how to train and evaluate a dnn using the fit() function:

```
# Train and evaluate the model
history = model.fit(data_train,
epochs=10,
validation_data=data_valid)
```

History

```
Epoch 1/10
Epoch 2/10
Epoch 3/10
2625/2625 [============] - 16s 6ms/step - loss: 0.4515 - accuracy: 0.8407 - val loss: 0.4361 - val accuracy: 0.8469
Epoch 4/10
2625/2625 [=============] - 15s 6ms/step - loss: 0.4231 - accuracy: 0.8514 - val loss: 0.4149 - val accuracy: 0.8533
Epoch 5/10
2625/2625 [============] - 16s 6ms/step - loss: 0.4001 - accuracy: 0.8588 - val loss: 0.3933 - val accuracy: 0.8574
Epoch 6/10
Epoch 7/10
2625/2625 [==============] - 16s 6ms/step - loss: 0.3710 - accuracy: 0.8680 - val loss: 0.3808 - val accuracy: 0.8601
Epoch 8/10
Epoch 9/10
Epoch 10/10
2625/2625 [============= ] - 16s 6ms/step - loss: 0.3409 - accuracy: 0.8773 - val loss: 0.3558 - val accuracy: 0.8724
```

Figure 5: The training and validation history across 10 epochs.

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History

- In each epoch, the history displays:
 - column 1: the number of sample processed so far, with the corresponding progress bar
 - column 2: the mean training time per sample
 - remaining columns: the metrics (e.g., loss and accuracy) specified when compiling the model, on the training data and validation data (if specified when training the model)

The Learning Curve

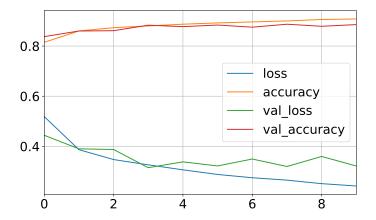


Figure 6: The learning curve of training and validation across 10 epochs.

The Learning Curve

- Fig. 6 shows that, when training progresses (generally)
 - the training and validation loss (the blue and green curve) decrease
 - the training and validation accuracy (the orange and red curve) increase
- A closer look at the figure shows that the validation loss/accuracy is lower/higher than the training loss/accuracy.
- However, this is not the case since the validation metrics are computed at the end of each epoch, whereas the training metrics are computed using a running mean during each epoch.
- In other words, the validation metrics are half an epoch (due to the running mean) ahead of the training metrics.
- Good Practice: When comparing the learning curve on the training and validation data, we should shift the curve on the training data by half an epoch to the left.

Saving and Loading DNN

- It took us several minutes to train the four layer sequential dnn (with 50 perceptrons on each hidden layer) on the Fashion MNIST dataset (with 60,000 28×28 images).
- In reality, both the dnn and the dataset can be much more complex, resulting in even higher training time.
- If the server crushed, the memory would be erased. As a result, the model, which resides in the memory during training, would be lost.
- For this reason we should periodically save the model on the disk when training processes. We can then load the saved model from disk.

The Checkpoint Callback

 The code below shows how to save a dnn using the checkpoint callback on the disk and load the saved dnn from disk.

```
# ModelCheckpoint callback
    model_checkpoint_cb = keras.callbacks.ModelCheckpoint(
        abspath + "/model/model.h5")
 4
5
    # Train, evaluate and save the model
    history = model.fit(data_train,
6
                         epochs=10,
8
                         validation_data=data_valid,
9
                         callbacks=[model_checkpoint_cb])
10
    # Load the saved model
11
12
    model = keras.models.load_model(abspath + "/model/model.h5")
```

• Line 2 and 12: abspath is the absolute path of the working directory.

Continuing Training DNN

- Both fig. 5 and 6 suggest that, the validation metrics would have been better had we trained the model longer.
- Luckily we can simply use the *fit()* function again to continue the training from where we left off.
- The code below shows how to do so.

```
# Train and save the model after each epoch
history = model.fit(data_train,
epochs=5,
validation_data=data_valid,
callbacks=[checkpoint_cb])
```

History

```
Epoch 1/5
2625/2625 [=======] - 168 6ms/step - loss: 0.4009 - accuracy: 0.8562 - val_loss: 0.4124 - val_accuracy: 0.8497
Epoch 2/5
2625/2625 [=======] - 168 6ms/step - loss: 0.3933 - accuracy: 0.8580 - val_loss: 0.4039 - val_accuracy: 0.8557
Epoch 3/5
2625/2625 [=======] - 178 6ms/step - loss: 0.3863 - accuracy: 0.8601 - val_loss: 0.3883 - val_accuracy: 0.8588
Epoch 4/5
2625/2625 [=============] - 178 7ms/step - loss: 0.3797 - accuracy: 0.8630 - val_loss: 0.3986 - val_accuracy: 0.8572
Epoch 5/5
2625/2625 [===============] - 178 6ms/step - loss: 0.3746 - accuracy: 0.8651 - val loss: 0.4131 - val accuracy: 0.8476
```

Figure 7: The training and validation history across the continued 5 epochs.

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The Learning Curve

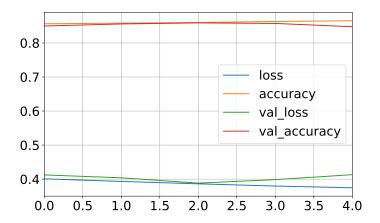


Figure 8: The learning curve of training and validation across the continued 5 epochs.

Overriding the Best Model

- Both the history (fig. 7) and learning curve (fig. 8) show that, while the metrics on the training data keep getting better, the ones on the validation first get better (from epoch 1 to 3) then get worse (from epoch 3 to 5).
- The variance above suggests that we could be overfitting the data after epoch 3. In other words, the model obtained in epoch 3 could be the best one.
- Unfortunately, the checkpoint callback will override the best model with the one obtained in the last epoch.
- Would not it be great if we only save the best model?

Checkpoint Callback

• Fortunately, we can tweak the checkpoint callback to do so:

```
1
    # ModelCheckpoint callback
 2
    model_checkpoint_cb = keras.callbacks.ModelCheckpoint(
        abspath + "/model/model.h5",
        save_best_only=True)
4
 5
6
    # Train, evaluate and save the best model
    history = model.fit(data_train,
8
                         epochs=20,
9
                         validation_data=data_valid,
10
                         callbacks=[model_checkpoint_cb])
```

- Line 4: save_best_only=True allows us to only save the best model.
- Line 8: As a result, we can use a large epoch number without worrying about training the model too short (underfitting) or too long (overfitting).

Tradeoff between Accuracy and Speed

- In terms of accuracy, we would like the epoch number to be as large
 as possible, since the larger the number the better the model (when
 using checkpoint callback).
- In terms of speed, we would like the epoch number to be as small as possible, since the smaller the number the faster the training.
- Intuitively we want to have a good tradeoff between accuracy and speed. One approach for doing so is Early Stopping.
- The idea is that, we monitor the validation metrics (e.g., loss or accuracy) and terminate the training as soon as the accuracy stops improving for some consecutive epochs.

EarlyStopping Callback

 The code below shows how to combine the checkpoint and earlystopping callback to strike a good balance between accuracy and speed:

```
# ModelCheckpoint callback
    model_checkpoint_cb = keras.callbacks.ModelCheckpoint(
        abspath + "/model/model.h5",
        save_best_only=True)
4
 5
    # EarlyStopping callback
6
    early_stopping_cb = keras.callbacks.EarlyStopping(
        patience=5,
8
        restore_best_weights=True)
9
10
    # Train, evaluate and save the best model
    history = model.fit(
11
12
        data train.
13
        epochs=20,
14
        validation_data=data_valid,
15
        callbacks=[model_checkpoint_cb, early_stopping_cb])
```

- Line 6: By default, EarlyStopping monitors validation loss.
- Line 7: patience is the number of consecutive epochs used in EarlyStopping.

Architecture and Hyperparameters

- Fine-tuning dnn involves fine-tuning both the architecture and the hyperparameters.
- Architecture:
 - number of hidden layers and perceptrons per hidden layer
 - · activation function of hidden layers
- Hyperparameters:
 - learning rate (very important)
 - optimizer
 - batch size

Hidden Layers and Perceptrons per Hidden Layer

- Good Practice: If there are SOTA dnns pretrained on similar data:
 - use Transfer Learning (more on this later)
- Good Practice: Otherwise:
 - # hidden layers: typically 1 to 5 (see tables 1 to 4)
 - # perceptrons per hidden layer:
 - usually same for each hidden layer (except for some dnns, e.g., auto-encoder)
 - typically 10 to 100 (see tables 1 to 4)
 - # hidden layers and perceptrons per hidden layer:
 - use larger number of hidden layers and perceptrons
 - use regularization (e.g., early stopping and drop-out, more on this later) to prevent overfitting
 - 1 this is as known as the "stretch pants" approach

Activation Function of Hidden Layers

- Good Practice:
 - typically ReLU (or SELU, see tables 1 to 4)
 - not essential to fine-tune

Learning Rate

- Good Practice: Instead of using hyperparameter tuning to find a constant learning rate, it is better to use *Learning Scheduling* to adjust learning rate during training.
- Here are some most widely used learning scheduling approaches:
 - Power scheduling
 - Exponential scheduling
 - Performance scheduling

Power Scheduling

- In *Power Scheduling*, learning rate decreases as training progresses.
- Concretely, learning rate is a function of the iteration number:

$$\eta(t) = \frac{\eta_0}{\left(1 + \frac{t}{s}\right)^c}. (2)$$

- Here:
 - ullet $\eta(t)$ is the learning rate at iteration t
 - η_0 is the initial learning rate
 - ullet s is the step size
- Based on eq. (2), we have the following relationship between learning rate at step ks, $\eta(ks)$, and that at step (k+1)s, $\eta((k+1)s)$:

$$\frac{\eta((k+1)s)}{\eta(ks)} = \frac{(k+1)^c}{(k+2)^c} = \left(1 - \frac{1}{k+2}\right)^c.$$
 (3)

• The relationship suggests that the decrease of learning rate gets smaller when training progresses.

Power Scheduling

 The code below shows how to use power scheduling by setting the decay hyperparameter of an optimizer:

```
# Compile the model
model.compile(optimizer=keras.optimizers.SGD(decay=0.001),
loss='sparse_categorical_crossentropy',
metrics=['accuracy'])
```

- Line 2: *decay* is the multiplicative inverse of the step size (s) in power scheduling.
- Line 2: The power (c) in power scheduling is set to 1.

Exponential Scheduling

- Similar to power scheduling, in Exponential Scheduling learning rate also decreases as training progresses.
- Concretely, learning rate is a function of the iteration number:

$$\eta(t) = \eta_0 0.1^{\frac{t}{s}}.$$
(4)

- Here:
 - $\eta(t)$ is the learning rate at iteration t
 - η_0 is the initial learning rate
 - s is the step size
- Based on eq. (4), we have the following relationship between learning rate at step ks, $\eta(ks)$, and that at step (k+1)s, $\eta((k+1)s)$:

$$\frac{\eta((k+1)s)}{\eta(ks)} = \frac{0.1^{\frac{k+1}{s}}}{0.1^{\frac{k}{s}}} = 0.1.$$
 (5)

• The relationship suggests that, unlike power scheduling where the decrease of learning rate gets smaller when training progresses, the decrease in exponential scheduling remains the same (by a factor of 10 every s step).

Exponential Scheduling

 The code below shows how to use exponential scheduling by setting the learning_rate hyperparameter of an optimizer:

```
# Get the number of samples in the training data
    m = tf.data.experimental.cardinality(data_train).numpy()
 3
4
    # Set the decay_steps
5
    s = 20 * m / batch_size
6
    # Get the learning rate
8
    learning_rate = keras.optimizers.schedules.ExponentialDecay(
9
        initial_learning_rate=0.01,
10
        decay_steps=s,
        decay_rate=0.1)
11
12
13
    # Compile the model
14
    model.compile(optimizer=keras.optimizers.SGD(learning_rate),
15
                  loss='sparse_categorical_crossentropy',
16
                  metrics=['accuracy'])
```

• Line 8: The learning_rate is set by keras.optimizers.schedules.ExponentialDecay.

Performance Scheduling

• In *Performance Scheduling*, learning rate is decreased by a factor of λ as soon as the validation metrics (e.g., validation loss) have not improved for some consecutive steps.

Performance Scheduling

 The code below shows how to use exponential scheduling by setting the learning_rate hyperparameter of an optimizer:

```
# ReduceLROnPlateau callback
    reduce_lr_on_plateau_cb = keras.callbacks.ReduceLROnPlateau(
        factor=0.1,
4
        patience=5)
 5
6
    # Train, evaluate and save the best model
    history = model.fit(
8
        data_train,
9
        epochs=20,
10
        validation_data=data_valid,
        callbacks=[model_checkpoint_cb,
11
12
                   early_stopping_cb,
13
                   reduce_lr_on_plateau_cb])
```

- Line 3: factor is the factor by which we decrease the learning rate.
- Line 4: *patience* is the number of consecutive steps for which the validation metrics stop improving.

Further Reading

• See HML Chapter 11 for more learning scheduling approaches.

References

